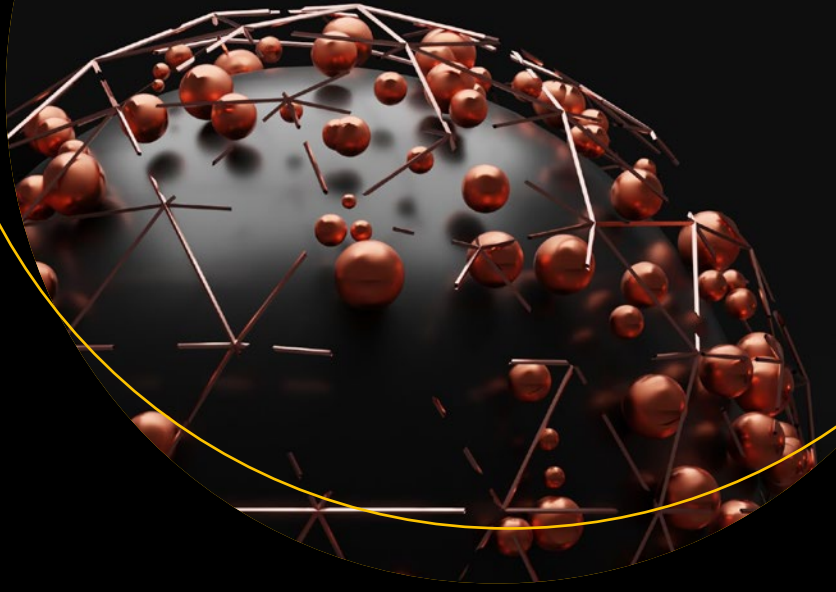

Adaptive Machine Learning Algorithms with Python

Solve Data Analytics and Machine Learning Problems on Edge Devices

Chanchal Chatterjee

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I dedicate this book to my father, Basudev Chatterjee, and all my teachers and mentors who have guided and inspired me.

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