# Lecture 24: Logic II

Brian Hou August 2, 2016

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- Scheme Recursive Art Contest is open! Submissions due 8/9

Introduction

Functions

Data

Mutability

Objects

Interpretation

Paradigms

Applications

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**Applications** 

This week (Paradigms), the goals are:

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- This week (Paradigms), the goals are:
  - To study examples of paradigms that are very different from what we have seen so far

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**Applications** 

- This week (Paradigms), the goals are:
  - To study examples of paradigms that are very different from what we have seen so far
  - To expand our definition of what counts as programming

Did you mean: nag a ram?

cat

cat at

at

cat at

cat

at

cat at

cat

at act

cat at

cat

at act

atc

cat at

cat

at act

atc

cat at

cta

cat

at act atc

cat at

ta tca

cat at act atc cat at cta ta tca

tac

```
def anagram(s):
```

```
def anagram(s):
   if len(s) == 0:
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def anagram(s):
    if len(s) == 0:
        return [[]]
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    anagrams = anagram(s[1:])
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    for x in anagrams:
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        for i in range(0, len(x) + 1):
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        for i in range(0, len(x) + 1):
            new_anagram = x[:i] + [s[0]] + x[i:]
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            result.append(new_anagram)
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    return result
```

```
logic> (fact (insert ?a ?r (?a . ?r)))
```

```
logic> (fact (insert ?a ?r (?a . ?r)))
logic> (fact (insert ?a (?b . ?r) (?b . ?s))
```

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  - Examples: "racecar"

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```
logic> (fact (palindrome ?s)
```

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Palindromes (demo)

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- If we describe a solution in two different ways, will the computer take the same amount of time to compute a solution?

- In declarative programming, we tell the computer what a solution looks like, rather than how to get the solution
- If we describe a solution in two different ways, will the computer take the same amount of time to compute a solution?
  - Probably not...

Reverse (demo)

# Break!

# Arithmetic

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  - 0, (+ 1 0), (+ 1 (+ 1 0)), (+ 1 (+ 1 (+ 1 0))), ...

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- Let's create our own number representation!
  - We'll limit ourselves to non-negative integers
- We can represent the numbers
  - 0, 1, 2, 3, ... as
  - $\cdot$  0, (+ 1 0), (+ 1 (+ 1 0)), (+ 1 (+ 1 (+ 1 0))), ...
- This is still a symbolic representation! Logic doesn't know that these are Scheme expressions that would evaluate to that number

Mathematical facts:

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  - 0 + n = n

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```
logic> (fact (+ 0 ?n ?n))
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- Mathematical facts:
  - 0 + n = n
  - In order for (x + 1) + y = (z + 1) to be true, x + y = z

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logic> (fact (+ (+ 1 ?x) ?y (+ 1 ?z))
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logic> (fact (* 0 ?n 0))
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  - 0 \* n = 0
  - In order for (x + 1) \* y = z to be true, x \* y + y = z

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# Subtraction and Division

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  - Subtraction is the inverse of addition

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    - In order for x y = z, y + z = x

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```
logic> (fact (- ?x ?y ?z)
```

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- However, just because the computer is the one solving the problem doesn't mean that we can write any declarative program and it will "just work"
- As declarative programmers, we (eventually) should understand how the underlying problem solver works
- This semester, just focus on writing declarative programs;
   no need to worry about the underlying solver yet!