

Lecture 6

STA 371G

Making Better Decisions



Decision making is the only way that individuals can purposely exercise any control over their lives, careers, or their surroundings.

- Ralph Keeney, Making Better Decision Makers, Decision Analysis, vol. 1 No:4, 2004



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- Larger ones require software

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- How a decision-maker can quantify the value of information
- How attitudes toward risk and uncertainty can affect the analysis

Elements of a Decision Analysis

All problems have three common elements:

- The decisions available to the decision maker.
- The possible outcomes and the probabilities of these outcomes.
- A value model that provides monetary values for the various outcomes.

Once these elements are defined, the decision maker can find an optimal decision.

Payoff Tables

A payoff table lists the payoff for each decision outcome pair; positive values are gains and negative values are losses.

	01	O2	О3
D1	\$10	\$10	\$10
D2	- \$10	\$20	\$30
D3	- \$30	\$30	\$80

- This table shows three possible decisions (D1, D2, and D3) and three possible outcomes (O1, O2, and O3) for each.
- Which decision do you prefer?



Payoff Tables

We need to know the probability of each outcome to make a good decision!

	01	O2	О3
D1	\$10	\$10	\$10
D2	- \$10	\$20	\$30
D3	- \$30	\$30	\$80

- Suppose P(O1) = 0.3, P(O2) = 0.5, P(O3) = 0.2
- Now which decision do you prefer?

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- E(D3) = ?



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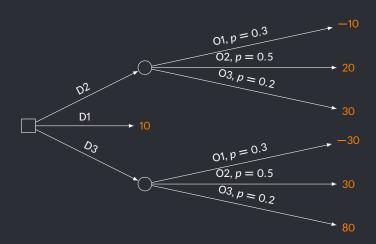
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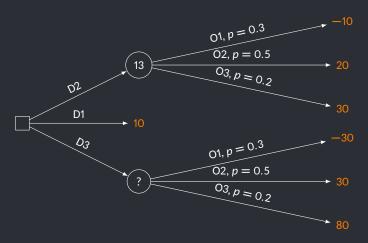
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- EVs are calculated through a "rolling-back" process.

Example



Rolling back: Step 1

Calculate the expected value at each probability node:

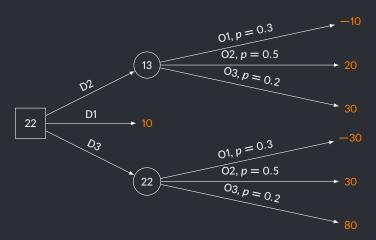




$$E(D1) = .3(-10) + .5(20) + .2(30) = 13$$

Rolling back: Step 2

Calculate the maximum at each decision node:



Take decision D3 since 22 = max(10, 13, 22).

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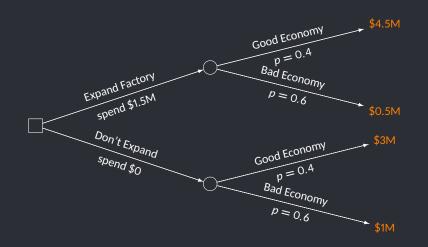
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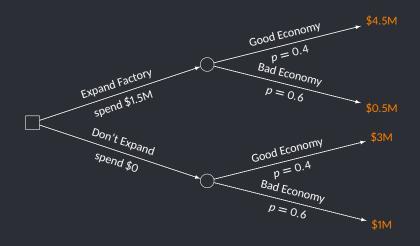
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- If she expands the factory, she expects to earn \$6M if the economy is good and \$2M if it is bad.
- She estimates that there is a 40 percent chance of a good economy and a 60 percent chance of a bad economy.

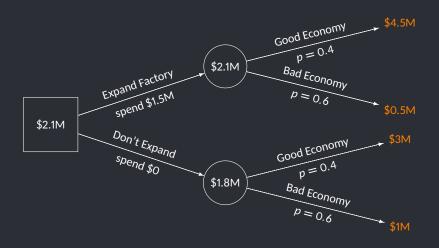
Should she expand?





$$E(\text{expand}) = (.4(6) + .6(2)) - 1.5 = 2.1$$

 $E(\text{don't expand}) = (.4(3) + .6(1)) = 1.8$



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Since \$2.1 > \$1.8, she should expand!

Sequential decisions

She later learns if she expands, she can opt to either:

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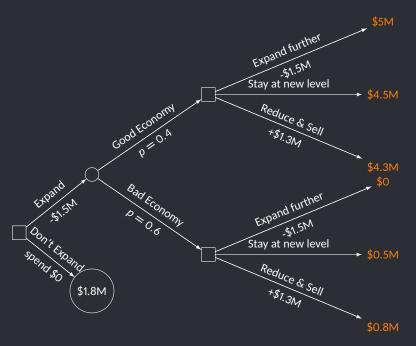
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- (c) do nothing.

How has the decision changed?



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Therefore the value of the option is

$$E(\text{new}) - E(\text{old}) = 2.48 - 2.1 = 0.38,$$

or \$380,000.

Does this look familiar?

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- A further refinement is to take time value of money into account and present value everything.