Dracarys

Team Referrence Library

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上海交通大学 Shanghai Jiao Tong University			Page 1
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多边形与圆面积交

```
1 double areaCT(Point pa, Point pb, double r) {
     if (pa.len() < pb.len()) {</pre>
       swap(pa, pb);
 3
 4
     if (sign(pb.len()) == 0) {
 5
 6
       return 0;
 7
 8
     double a = pb.len(), b = pa.len(), c = (pb - pa).len();
 9
     double sinB = fabs(det(pb, pb - pa) / a / c),
          cosB = dot(pb, pb - pa) / a / c,
10
11
           sinC = fabs(det(pa, pb) / a/ b),
          cosC = dot(pa, pb) / a / b;
12
     double B = atan2(sinB, cosB), C = atan2(sinC, cosC);
13
14
     if (a > r) {
       S = C / 2 * r * r;
15
       h = a * b * sinC / c;
16
17
       if (h < r && B < PI / 2) {
18
         S = (acos(h / r) * r * r - h * sqrt(r * r - h * h));
19
20
     } else if (b > r) {
       double theta = PI - B - asin(sinB / r * a);
21
       S = a * r * sin(theta) / 2 + (C - theta) / 2 * r * r;
22
23
     } else {
       S = sinC * a * b / 2;
24
25
26
     return S;
27
```

二维几何

```
1 | #include <iostream>
2 | #include <cmath>
   #include <vector>
   using namespace std;
5
6
   const double PI = acos(-1.0);
8
   const double EPS = 1e-8;
   int sign(double x)
10
11
12
     return x \leftarrow -EPS ? -1 : x > EPS;
13 | }
14
15 double newSqrt(double x)
```

```
16 {
17
     return x < 0 ? 0 : sqrt(x);
18 }
19
   struct Point {
20
     double x, y;
21
     Point(double x = 0, double y = 0) : x(x), y(y) {}
22
     Point operator + (const Point &that) const {
23
24
       return Point(x + that.x, y + that.y);
25
26
     Point operator - (const Point &that) const {
       return Point(x - that.x, y - that.y);
27
28
     Point operator * (const double &that) const {
29
       return Point(x * that, y * that);
30
     }
31
     Point operator / (const double &that) const {
32
       return Point(x / that, y / that);
33
34
     Point rotate(const double ang) { // 逆时针旋转 ang 弧度
35
36
       return Point(cos(ang) * x - sin(ang) * y, cos(ang) * y + sin(ang) * x);
37
38
     Point turn90() { // 逆时针旋转 90 度
       return Point(-y, x);
39
40
41
     double len2() const {
       return x * x + y * y;
42
43
     double len() const {
44
       return sqrt(x * x + y * y);
45
46
     Point unit() const {
47
       return *this / len();
48
49
     int operator < (const Point &that) const {</pre>
50
       int d = sign(x - that.x); if (d) return d < 0;</pre>
51
       return sign(y - that.y) < 0;</pre>
52
53
54
   double det(Point a, Point b)
55
56
     return a.x * b.y - b.x * a.y;
57
58
   double dot(Point a, Point b)
59
60 {
```

```
return a.x * b.x + a.v * b.v:
61
                                                                                            106
62 }
                                                                                            107
 63 double det(Point s, Point a, Point b)
                                                                                            108
                                                                                                  p1 = o + delta:
 64 | {
                                                                                            109
                                                                                                  p2 = o - delta;
 65
      return (a.x - s.x) * (b.y - s.y) - (b.x - s.x) * (a.y - s.y);
                                                                                                  return true;
                                                                                            110
 66 | }
                                                                                            111
 67
                                                                                            112
                                                                                            113 // 求圆与圆的交面积
 68 struct Line {
 69
      Point a, b;
 70
      Line(Point a, Point b) : a(a), b(b) {}
                                                                                            115
                                                                                            116
71 | };
                                                                                                    return 0;
 72
                                                                                            117
    Point isLL(const Line &11, const Line &12) {
                                                                                            118
      double s1 = det(12.b - 12.a, 11.a - 12.a),
                                                                                            119
 74
           s2 = -det(12.b - 12.a, 11.b - 12.a);
                                                                                            120
 75
 76
      return (l1.a * s2 + l1.b * s1) / (s1 + s2);
                                                                                                    return r * r * PI;
                                                                                            121
 77
                                                                                            122
    bool onSeg(const Line &1, const Point &p) { // 点在线段上
 78
                                                                                            123
      return sign(det(p - 1.a, 1.b - 1.a)) == 0 && sign(dot(p - 1.a, p - 1.b)) <= 0;
 79
                                                                                            124
 80
                                                                                            125
 81
    Point projection(const Line &l, const Point &p) { // 点到直线投影
                                                                                            126
 82
      return 1.a + (1.b - 1.a) * (dot(p - 1.a, 1.b - 1.a) / (1.b - 1.a).len2());
                                                                                            127
 83 | }
                                                                                            128
 84 | double disToLine(const Line &1, const Point &p) {
                                                                                            129
      return abs(det(p - 1.a, 1.b - 1.a) / (1.b - 1.a).len());
 85
                                                                                            130
 86 | }
                                                                                            131
 87
    double disToSeg(const Line &1, const Point &p) { // 点到线段距离
                                                                                            132
 88
      return sign(dot(p - 1.a, 1.b - 1.a)) * sign(dot(p - 1.b, 1.a - 1.b)) != 1 ?
                                                                                            133
 89
        disToLine(1, p) : min((p - 1.a).len(), (p - 1.b).len());
                                                                                            134
 90
                                                                                            135
    Point symmetryPoint(const Point a, const Point b) { // 点 b 关于点 a 的中心对称点
                                                                                            136
 91
      return a + a - b;
                                                                                            137
                                                                                                  return true;
 92
                                                                                            138
 93
    Point reflection(const Line &1, const Point &p) { // 点关于直线的对称点
                                                                                            139
 94
      return symmetryPoint(projection(l, p), p);
95
 96 | }
    struct Circle {
                                                                                            142 {
 97
      Point o;
 98
                                                                                            143
      double r;
                                                                                            144
 99
      Circle (Point o = Point(0, 0), double r = 0) : o(o), r(r) {}
100
                                                                                            145
101 };
                                                                                            146
102
                                                                                                  p1 = c.o + p + delta;
                                                                                            147
103 // 求圆与直线的交点
                                                                                            148
                                                                                                  p2 = c.o + p - delta;
104 bool isCL(Circle a, Line 1, Point &p1, Point &p2) {
                                                                                            149
                                                                                                  return true;
     if (sign(det(l.a - a.o, l.b - a.o) / (l.a - l.b).len()) > 0) return false;
                                                                                            150 }
```

```
Point o = isLL(Line(a.o. a.o + (1.b - 1.a).turn90()), 1);
  Point delta = (1.b - 1.a).unit() * newSqrt(a.r * a.r - (o - a.o).len2()):
double areaCC(const Circle &c1, const Circle &c2) {
  double d = (c1.o - c2.o).len();
 if (sign(d - (c1.r + c2.r)) >= 0) {
  if (sign(d - abs(c1.r - c2.r)) \leftarrow 0)
    double r = min(c1.r, c2.r);
  double x = (d * d + c1.r * c1.r - c2.r * c2.r) / (2 * d),
       t1 = acos(x / c1.r), t2 = acos((d - x) / c2.r);
  return c1.r * c1.r * t1 + c2.r * c2.r * t2 - d * c1.r * sin(t1);
// 求圆与圆的交点,注意调用前要先判定重圆
bool isCC(Circle a, Circle b, Point &p1, Point &p2) {
  double s1 = (a.o - b.o).len();
  if (sign(s1 - a.r - b.r)) > 0 \mid | sign(s1 - abs(a.r - b.r)) < 0) return false;
  double s2 = (a.r * a.r - b.r * b.r) / s1;
  double aa = (s1 + s2) * 0.5, bb = (s1 - s2) * 0.5;
  Point o = (b.o - a.o) * (aa + bb)) + a.o;
  Point delta = (b.o - a.o).unit().turn90() * newSqrt(a.r * a.r - aa * aa);
  p1 = o + delta, p2 = o - delta;
// 求点到圆的切点,按关于点的左手方向返回两个点
bool tanCP(const Circle &c, const Point &p0, Point &p1, Point &p2)
  double x = (p0 - c.o).len2(), d = x - c.r * c.r;
 if (d < EPS) return false;</pre>
  Point p = (p0 - c.o) * (c.r * c.r / x);
  Point delta = ((p0 - c.o) * (-c.r * sqrt(d) / x)).turn90();
```

```
151
    // 求圆到圆的外共切线,按关于 c1.o 的左手方向返回两条线
152
    vector<Line> extanCC(const Circle &c1, const Circle &c2)
154 | {
      vector<Line> ret;
155
156
      if (sign(c1.r - c2.r) == 0) {
        Point dir = c2.o - c1.o;
157
158
        dir = (dir * (c1.r / dir.len())).turn90();
        ret.push_back(Line(c1.o + dir, c2.o + dir));
159
160
        ret.push_back(Line(c1.o - dir, c2.o - dir));
161
      } else {
162
        Point p = (c1.0 * -c2.r + c2.o * c1.r) / (c1.r - c2.r);
163
        Point p1, p2, q1, q2;
        if (tanCP(c1, p, p1, p2) && tanCP(c2, p, q1, q2)) {
164
165
         if (c1.r < c2.r) swap(p1, p2), swap(q1, q2);
166
          ret.push_back(Line(p1, q1));
167
          ret.push_back(Line(p2, q2));
168
        }
169
170
      return ret;
171
172
    // 求圆到圆的内共切线,按关于 c1.o 的左手方向返回两条线
    vector<Line> intanCC(const Circle &c1, const Circle &c2)
175 | {
176
      vector<Line> ret;
      Point p = (c1.0 * c2.r + c2.o * c1.r) / (c1.r + c2.r);
177
178
      Point p1, p2, q1, q2;
      if (tanCP(c1, p, p1, p2) && tanCP(c2, p, q1, q2)) {
179
180
        ret.push_back(Line(p1, q1));
181
        ret.push_back(Line(p2, q2));
182
     }
183
      return ret;
184 }
185
186 | bool contain(vector<Point> polygon, Point p) { // 判断点 p
      → 是否被多边形包含,包括落在边界上
      int ret = 0, n = polygon.size();
187
188
      for(int i = 0; i < n; ++ i) {
189
        Point u = polygon[i], v = polygon[(i + 1) % n];
190
        if (onSeg(Line(u, v), p)) return true;
        if (sign(u.y - v.y) \leftarrow 0) swap(u, v);
191
        if (sign(p.y - u.y) > 0 \mid | sign(p.y - v.y) <= 0) continue;
192
        ret += sign(det(p, v, u)) > 0;
193
194
```

```
return ret & 1:
195
196 }
197
    |vector<Point> convexCut(const vector<Point>&ps, Line 1) { // 用半平面 (q1,q2)
       → 的逆时针方向去切凸多边形
      vector<Point> qs;
199
200
      int n = ps.size();
201
      for (int i = 0; i < n; ++i) {
202
        Point p1 = ps[i], p2 = ps[(i + 1) \% n];
203
        int d1 = sign(det(l.a, l.b, p1)), d2 = sign(det(l.a, l.b, p2));
        if (d1 >= 0) qs.push_back(p1);
204
        if (d1 * d2 < 0) qs.push_back(isLL(Line(p1, p2), 1));</pre>
205
206
207
      return qs;
208
     vector<Point> convexHull(vector<Point> ps) { // 求点集 ps 组成的凸包
209
      int n = ps.size(); if (n <= 1) return ps;</pre>
210
      sort(ps.begin(), ps.end());
211
      vector<Point> qs;
212
      for (int i = 0; i < n; qs.push back(ps[i++]))
213
214
        while (qs.size() > 1 \&\& sign(det(qs[qs.size()-2],qs.back(),ps[i])) <= 0)

    qs.pop_back();
      for (int i = n - 2, t = qs.size(); i >= 0; qs.push back(ps[i--]))
215
216
        while ((int)qs.size() > t && sign(det(qs[(int)qs.size()-2],qs.back(),ps[i])) <=</pre>
           → 0) qs.pop back();
      qs.pop back(); return qs;
217
218 }
219
    int main()
220
221
      Circle c1, c2;
222
223
      c1.0 = Point(0, 0); c1.r = 10;
      c2.o = Point(10, 10); c1.r = 10;
224
225
      Point p1, p2;
226
      return 0;
227
```

$n \log n$ 半平面交

```
struct Point {
   Point norm() const {
    double 1 = len();
   return Point(x / 1, y / 1);
}

int quad() const {
```

```
return sign(y) == 1 \mid \mid (sign(y) == 0 \&\& sign(x) >= 0);
 9
     }
10 };
11
   struct Line {
12
     bool include(const Point &p) const {
13
       return sign(det(b - a, p - a)) > 0;
14
     }
15
16
      Line push() const{ // 将半平面向外推 eps
17
18
       const double eps = 1e-6;
       Point delta = (b - a).turn90().norm() * eps;
19
       return Line(a - delta, b - delta);
20
^{21}
   };
22
23
   bool sameDir(const Line &10, const Line &11) {
24
     return parallel(10, 11) && sign(dot(10.b - 10.a, 11.b - 11.a)) == 1;
25
26
27
28
   bool operator < (const Point &a, const Point &b) {</pre>
     if (a.quad() != b.quad()) {
29
       return a.quad() < b.quad();</pre>
30
     } else {
31
       return sign(det(a, b)) > 0;
32
33
34
35
   bool operator < (const Line &10, const Line &11) {
     if (sameDir(10, 11)) {
37
38
       return l1.include(10.a);
     } else {
39
       return (10.b - 10.a) < (11.b - 11.a);
40
41
42
43
   bool check(const Line &u, const Line &v, const Line &w) {
44
     return w.include(intersect(u, v));
45
46
47
   vector<Point> intersection(vector<Line> &1) {
     sort(1.begin(), 1.end());
49
     deque<Line> q;
50
     for (int i = 0; i < (int)l.size(); ++i) {</pre>
51
52
       if (i && sameDir(l[i], l[i - 1])) {
```

```
continue;
53
       }
54
       while (q.size() > 1 && !check(q[q.size() - 2], q[q.size() - 1], l[i])) {
55
56
         q.pop back();
57
58
       while (q.size() > 1 \&\& !check(q[1], q[0], l[i])) {
         q.pop_front();
59
60
       }
61
       q.push_back(l[i]);
62
63
     while (q.size() > 2 \& !check(q[q.size() - 2], q[q.size() - 1], q[0])) {
64
       q.pop_back();
65
66
     while (q.size() > 2 \&\& !check(q[1], q[0], q[q.size() - 1])) {
67
       q.pop_front();
68
     }
69
     vector<Point> ret;
     for (int i = 0; i < (int)q.size(); ++i) {</pre>
70
       ret.push back(intersect(q[i], q[(i + 1) % q.size()]));
71
72
     }
73
     return ret;
74 }
```

Delaunay 三角剖分

```
2 Delaunay Triangulation 随机增量算法:
3 节点数至少为点数的 6 倍,空间消耗较大注意计算内存使用
  建图的过程在 build 中,注意初始化内存池和初始三角形的坐标范围 (Triangulation::LOTS)
5 Triangulation::find 返回包含某点的三角形
6 Triangulation::add_point 将某点加入三角剖分
  |某个 Triangle 在三角剖分中当且仅当它的 has_children 为 0
8 | 如果要找到三角形 u 的邻域,则枚举它的所有 u.edge[i].tri, 该条边的两个点为 u.p[(i+1)%3],
     \hookrightarrow u.p[(i+2)\%3]
9 */
  const int N = 100000 + 5;
10
  const int MAX TRIS = N * 6;
12 const double EPSILON = 1e-6;
  const double PI = acos(-1.0);
  using namespace std;
14
15
16 struct Point {
17
    double x,v;
18
    Point(): x(0), y(0) {}
    Point(double x, double y) : x(x), y(y) {}
    inline bool operator == (Point const& that) const {
```

```
return x == that.x && y == that.y;
                                                                                            64
                                                                                                  bool has children() const {
                                                                                            65
22
    }
                                                                                                    return children[0] != 0;
                                                                                             66
23 | };
24
                                                                                            67
                                                                                                  int num children() const {
   inline double sqr(double x) { return x*x; }
                                                                                            68
                                                                                                    return children[0] == 0 ? 0
25
   double dist sqr(Point const& a, Point const& b) {
                                                                                            69
                                                                                                      : children[1] == 0 ? 1
26
     return sqr(a.x-b.x) + sqr(a.y-b.y);
                                                                                             70
                                                                                                      : children[2] == 0 ? 2 : 3;
27
28
   }
                                                                                             71
                                                                                                  }
   bool in_circumcircle(Point const& p1, Point const& p2, Point const& p3, Point const&
                                                                                                  bool contains(Point const& q) const {
                                                                                             72
      → p4) {
                                                                                             73
                                                                                                    double a = side(p[0],p[1],q);
     double u11 = p1.x - p4.x;
                                                                                                    double b = side(p[1],p[2],q);
30
                                                                                             74
                                                                                                    double c = side(p[2], p[0], q);
     double u21 = p2.x - p4.x;
                                                                                             75
31
                                                                                             76
                                                                                                    return a >= -EPSILON && b >= -EPSILON && c >= -EPSILON;
     double u31 = p3.x - p4.x;
32
33
     double u12 = p1.y - p4.y;
                                                                                             77
     double u22 = p2.y - p4.y;
                                                                                             78
                                                                                                } triange_pool[MAX_TRIS], *tot_triangles;
34
     double u32 = p3.y - p4.y;
                                                                                                void set_edge(Edge a, Edge b) {
35
                                                                                             79
36
     double u13 = sqr(p1.x) - sqr(p4.x) + sqr(p1.y) - sqr(p4.y);
                                                                                            80
                                                                                                  if (a.tri) a.tri->edge[a.side] = b;
     double u23 = sqr(p2.x) - sqr(p4.x) + sqr(p2.y) - sqr(p4.y);
                                                                                            81
                                                                                                  if (b.tri) b.tri->edge[b.side] = a;
37
     double u33 = sqr(p3.x) - sqr(p4.x) + sqr(p3.y) - sqr(p4.y);
                                                                                                  if (a.tri && b.tri) {
38
                                                                                            82
     double det = -u13*u22*u31 + u12*u23*u31 + u13*u21*u32 - u11*u23*u32 - u12*u21*u33
                                                                                                    assert(a.tri->p[(a.side+1)%3] == b.tri->p[(b.side+2)%3]);
39
                                                                                            83

→ + u11*u22*u33:

                                                                                            84
                                                                                                    assert(a.tri->p[(a.side+2)%3] == b.tri->p[(b.side+1)%3]);
     return det > EPSILON;
                                                                                            85
40
                                                                                            86
41
42 | double side(Point const& a, Point const& b, Point const& p) {
                                                                                            87
                                                                                                class Triangulation {
     return (b.x-a.x)*(p.y-a.y) - (b.y-a.y)*(p.x-a.x);
                                                                                            88
                                                                                                  public:
43
                                                                                            89
                                                                                                    Triangulation() {
44
                                                                                                      const double LOTS = 1e6;
                                                                                            90
45
   typedef int SideRef;
46
                                                                                             91
                                                                                                      the_root = new(tot_triangles++)
   struct Triangle;
                                                                                                        typedef Triangle* TriangleRef;
48
                                                                                            92
   struct Edge {
                                                                                                    ~Triangulation() {}
                                                                                            93
     TriangleRef tri;
                                                                                                    TriangleRef find(Point p) const {
                                                                                            94
50
     SideRef
                 side;
                                                                                            95
                                                                                                      return find(the_root,p);
51
     Edge() : tri(0), side(0) {}
                                                                                                    }
                                                                                            96
52
     Edge(TriangleRef tri, SideRef side) : tri(tri), side(side) {}
                                                                                                    void add_point(Point const& p) {
53
                                                                                            97
54 | };
                                                                                            98
                                                                                                      add point(find(the root,p),p);
   struct Triangle {
                                                                                                    }
                                                                                            99
55
56
     Point p[3];
                                                                                                  private:
                                                                                           100
     Edge edge[3];
                                                                                                    TriangleRef the root;
                                                                                           101
57
     TriangleRef children[3];
                                                                                                    static TriangleRef find(TriangleRef root, Point const& p) {
58
                                                                                           102
                                                                                                      for(;;) {
59
     Triangle() {}
                                                                                           103
60
     Triangle(Point const& p0, Point const& p1, Point const& p2) {
                                                                                           104
                                                                                                        assert(root->contains(p));
61
       p[0] = p0; p[1] = p1; p[2] = p2;
                                                                                                        if (!root->has children()) {
                                                                                           105
62
       children[0] = children[1] = children[2] = 0;
                                                                                           106
                                                                                                          return root;
63
                                                                                                        } else {
                                                                                           107
```

```
108
              int flag = true:
              for (int i = 0; i < 3 && root->children[i]; ++i) {
109
                if (root->children[i]->contains(p)) {
110
111
                  root = root->children[i];
                  break;
112
                }
113
114
115
              assert(flag&&"point not found");
116
117
          }
118
        void add_point(TriangleRef root, Point const& p) {
119
          TriangleRef tab,tbc,tca;
120
          /* split it into three triangles */
121
          tab = new(tot_triangles++) Triangle(root->p[0], root->p[1], p);
122
          tbc = new(tot_triangles++) Triangle(root->p[1], root->p[2], p);
123
          tca = new(tot_triangles++) Triangle(root->p[2], root->p[0], p);
124
          set edge(Edge(tab,0), Edge(tbc,1));
125
126
          set_edge(Edge(tbc,0), Edge(tca,1));
127
          set_edge(Edge(tca,0), Edge(tab,1));
128
          set_edge(Edge(tab,2), root->edge[2]);
129
          set_edge(Edge(tbc,2), root->edge[0]);
          set edge(Edge(tca,2), root->edge[1]);
130
          root->children[0] = tab;
131
          root->children[1] = tbc;
132
          root->children[2] = tca;
133
          flip(tab,2);
134
          flip(tbc,2);
135
136
          flip(tca,2);
137
138
        void flip(TriangleRef tri, SideRef pi) {
          TriangleRef trj = tri->edge[pi].tri;
139
140
          int pj = tri->edge[pi].side;
141
          if (!trj) return;
          if (!in_circumcircle(tri->p[0],tri->p[1],tri->p[2],trj->p[pj])) return;
142
143
          assert(tri->p[(pi+2)%3] == trj->p[(pj+1)%3]);
          assert(tri->p[(pi+1)%3] == trj->p[(pj+2)%3]);
144
          /* flip edge between tri,trj */
145
          TriangleRef trk = new(tot triangles++) Triangle(tri->p[(pi+1)%3], trj->p[pj],
146

    tri->p[pi]);
147
          TriangleRef trl = new(tot_triangles++) Triangle(trj->p[(pj+1)%3], tri->p[pi],
            set edge(Edge(trk,0), Edge(trl,0));
148
          set_edge(Edge(trk,1), tri->edge[(pi+2)%3]);
149
          set_edge(Edge(trk,2), trj->edge[(pj+1)%3]);
150
```

```
set edge(Edge(trl,1), trj->edge[(pj+2)%3]);
151
152
          set edge(Edge(trl,2), tri->edge[(pi+1)%3]);
          tri->children[0] = trk; tri->children[1] = trl; tri->children[2] = 0;
153
154
          trj->children[0] = trk; trj->children[1] = trl; trj->children[2] = 0;
          flip(trk,1);
155
          flip(trk,2);
156
          flip(trl,1);
157
158
          flip(trl,2);
159
160 };
161
162 int n;
163 Point ps[N];
164
165
    void build()
166
167
      tot_triangles = triange_pool;
168
      cin >> n;
      for(int i = 0; i < n; ++ i) {
169
170
        int x, y;
171
        scanf("%d%d", &x, &y);
172
        ps[i].x = x; ps[i].y = y;
173
      random shuffle(ps, ps + n);
174
175
      Triangulation tri;
176
      for(int i = 0; i < n; ++ i) {
        tri.add_point(ps[i]);
177
178
179 }
180
181
    int main()
182 {
183
      build();
184
      return 0;
185 }
```

三维几何操作合并

```
8 // 平面法向量 : 平面上两个向量叉积
  9 // 点共平面 : 平面上一点与之的向量点积法向量为 0
10 // 点在线段 ( 直线 ) 上 : 共线且两边点积非正
11 // 点在三角形内 ( 不包含边界, 需再判断是与某条边共线 )
12 bool pointInTri(const Point3D &a, const Point3D &b, const Point3D &c, const Point3D
           → &p) {
          return sign(det(a - b, a - c).len() - det(p - a, p - b).len() - det(p - b, p -
13
               \rightarrow c).len() - det(p - c, p - a).len()) == 0;
14 | }
15 // 共平面的两点是否在这平面上一条直线的同侧
16 bool sameSide(const Point3D &a, const Point3D &b, const Point3D &p0, const Point3D
           → &p1) {
          return sign(dot(det(a - b, p0 - b), det(a - b, p1 - b))) > 0;
17
18 }
19 // 两点在平面同侧 : 点积法向量符号相同
20 // 两直线平行 / 垂直 : 同二维
21 // 平面平行 / 垂直 : 判断法向量
22 // 线面垂直 : 法向量和直线平行
23 // 判断空间线段是否相交 : 四点共面两线段不平行相互在异侧
24 // 线段和三角形是否相交 : 线段在三角形平面不同侧
           → 三角形任意两点在线段和第三点组成的平面的不同侧
25 // 求空间直线交点
26 Point3D intersection(const Point3D &a0, const Point3D &b0, const Point3D &a1, const
           → Point3D &b1) {
          double t = ((a0.x - a1.x) * (a1.y - b1.y) - (a0.y - a1.y) * (a1.x - b1.x)) /
               \hookrightarrow ((a0.x - b0.x) * (a1.y - b1.y) - (a0.y - b0.y) * (a1.x - b1.x));
28
          return a0 + (b0 - a0) * t;
29 | }
      // 求平面和直线的交点
31 Point3D intersection(const Point3D &a, const Point3D &b, const Point3D &c, const
           → Point3D &10, const Point3D &11) {
          Point3D p = pVec(a, b, c); // 平面法向量
          double t = (p.x * (a.x - 10.x) + p.y * (a.y - 10.y) + p.z * (a.z - 10.z)) / (p.x * (a.z - 10.z)) / (p.z - 10.z)) / (p.z - 10.z) / (p.z
33
               \rightarrow (11.x - 10.x) + p.y * (11.y - 10.y) + p.z * (11.z - 10.z));
          return 10 + (11 - 10) * t;
34
35 | }
36 | // 求平面交线 : 取不平行的一条直线的一个交点,以及法向量叉积得到直线方向
      // 点到直线距离 : 叉积得到三角形的面积除以底边
38 // 点到平面距离 : 点积法向量
39 // 直线间距离 : 平行时随便取一点求距离,否则又积方向向量得到方向点积计算长度
40 // 直线夹角 : 点积 平面夹角 : 法向量点积
41 // 三维向量旋转操作(绕向量 s 旋转 ang 角度),对于右手系 s 指向观察者时逆时针
42 // 矩阵版
43 | void rotate(const Point3D &s, double ang) {
          double 1 = s.len(), x = s.x / 1, y = s.y / 1, z = s.z / 1, sinA = sin(ang), cosA = sin(ang)

    cos(ang);
```

三维凸包

```
#define SIZE(X) (int(X.size()))
2 #define PI 3.14159265358979323846264338327950288
3 struct Point {
    Point cross(const Point &p) const
    { return Point(y * p.z - z * p.y, z * p.x - x * p.z, x * p.y - y * p.x); }
6 | \rinfo[1005]:
7 int mark[1005][1005],n, cnt;;
8 double mix(const Point &a, const Point &b, const Point &c)
g { return a.dot(b.cross(c)); }
10 double area(int a, int b, int c)
11 | { return ((info[b] - info[a]).cross(info[c] - info[a])).length(); }
12 double volume(int a, int b, int c, int d)
13 | { return mix(info[b] - info[a], info[c] - info[a], info[d] - info[a]); }
14 | struct Face {
    int a, b, c; Face() {}
15
    Face(int a, int b, int c): a(a), b(b), c(c) {}
16
17
     int &operator [](int k)
18
     { if (k == 0) return a; if (k == 1) return b; return c; }
19
   vector <Face> face;
   inline void insert(int a, int b, int c) { face.push back(Face(a, b, c)); }
   void add(int v) {
22
     vector <Face> tmp; int a, b, c; cnt++;
23
24
     for (int i = 0; i < SIZE(face); i++) {</pre>
25
       a = face[i][0]; b = face[i][1]; c = face[i][2];
26
       if (Sign(volume(v, a, b, c)) < 0)</pre>
       mark[a][b] = mark[b][a] = mark[b][c] = mark[c][b] = mark[c][a] = mark[a][c] =
27

    cnt;

28
       else tmp.push back(face[i]);
     } face = tmp;
20
     for (int i = 0; i < SIZE(tmp); i++) {</pre>
30
       a = face[i][0]; b = face[i][1]; c = face[i][2];
31
       if (mark[a][b] == cnt) insert(b, a, v);
32
```

```
if (mark[b][c] == cnt) insert(c, b, v);
33
       if (mark[c][a] == cnt) insert(a, c, v);
34
35 | }}
36 \mid int Find() {
     for (int i = 2; i < n; i++) {
37
38
       Point ndir = (info[0] - info[i]).cross(info[1] - info[i]);
       if (ndir == Point()) continue; swap(info[i], info[2]);
39
       for (int j = i + 1; j < n; j++) if (Sign(volume(0, 1, 2, j)) != 0) {
40
41
         swap(info[j], info[3]); insert(0, 1, 2); insert(0, 2, 1); return 1;
42 | } return 0; }
43 | int main() {
     for (; scanf("%d", &n) == 1; ) {
44
       for (int i = 0; i < n; i++) info[i].Input();</pre>
45
       sort(info, info + n); n = unique(info, info + n) - info;
46
       face.clear(); random_shuffle(info, info + n);
47
48
       if (Find()) { memset(mark, 0, sizeof(mark)); cnt = 0;
         for (int i = 3; i < n; i++) add(i); vector<Point> Ndir;
49
         for (int i = 0; i < SIZE(face); ++i) {</pre>
50
           Point p = (info[face[i][0]] - info[face[i][1]]).cross(
51
52
               info[face[i][2]] - info[face[i][1]]);
           p = p / p.length(); Ndir.push back(p);
53
         } sort(Ndir.begin(), Ndir.end());
54
         int ans = unique(Ndir.begin(), Ndir.end()) - Ndir.begin();
55
56
         printf("%d\n", ans);
       } else printf("1\n");
57
58 } }
59 // 求重心
60 double calcDist(const Point &p, int a, int b, int c)
61 | { return fabs(mix(info[a] - p, info[b] - p, info[c] - p) / area(a, b, c)); }
62 //compute the minimal distance of center of any faces
63 double findDist() { //compute center of mass
     double totalWeight = 0; Point center(.0, .0, .0);
64
     Point first = info[face[0][0]];
65
66
     for (int i = 0; i < SIZE(face); ++i) {</pre>
67
       Point p = (info[face[i][0]]+info[face[i][1]]+info[face[i][2]]+first)*.25;
68
       double weight = mix(info[face[i][0]] - first, info[face[i][1]]
69
           - first, info[face[i][2]] - first);
       totalWeight += weight; center = center + p * weight;
70
     } center = center / totalWeight;
71
72
     double res = 1e100; //compute distance
73
     for (int i = 0; i < SIZE(face); ++i)</pre>
       res = min(res, calcDist(center, face[i][0], face[i][1], face[i][2]));
74
       return res; }
75
```

凸包上快速询问

```
1
      给定凸包, \log n 内完成各种询问, 具体操作有:
      1. 判定一个点是否在凸包内
3
      2. 询问凸包外的点到凸包的两个切点
      3. 询问一个向量关于凸包的切点
      4. 询问一条直线和凸包的交点
      INF 为坐标范围,需要定义点类大于号
7
      改成实数只需修改 sign 函数,以及把 long long 改为 double 即可
      构造函数时传入凸包要求无重点,面积非空,以及 pair(x,v) 的最小点放在第一个
9
10
   #include <vector>
11
   #include <functional>
   using namespace std;
13
14
   const int INF = 1000000000;
15
16
17
   struct Convex
18
19
     int n;
     vector<Point> a;
20
     vector<Point> upper, lower;
21
22
     Convex(vector<Point> _a) : a(_a) {
23
      n = a.size();
24
      int ptr = 0;
25
      for(int i = 1; i < n; ++ i) if (a[ptr] < a[i]) ptr = i;
26
       for(int i = 0; i <= ptr; ++ i) lower.push_back(a[i]);</pre>
       for(int i = ptr; i < n; ++ i) upper.push_back(a[i]);</pre>
27
28
       upper.push_back(a[0]);
29
30
     int sign(long long x) {
       return x < 0 ? -1 : x > 0;
31
32
     pair<long long, int> get tangent(vector<Point> &convex, Point vec) {
33
       int l = 0, r = (int)convex.size() - 2;
34
      for(; l + 1 < r; ) {
35
36
        int mid = (1 + r) / 2;
        if (sign((convex[mid + 1] - convex[mid]).det(vec)) > 0) r = mid;
37
38
        else 1 = mid;
39
       return max(make pair(vec.det(convex[r]), r), make pair(vec.det(convex[0]), 0));
40
41
42
     void update_tangent(const Point &p, int id, int &i0, int &i1) {
       if ((a[i0] - p).det(a[id] - p) > 0) i0 = id;
       if ((a[i1] - p).det(a[id] - p) < 0) i1 = id;</pre>
```

```
45
46
     void binary search(int 1, int r, Point p, int &i0, int &i1) {
       if (1 == r) return;
47
48
       update tangent(p, 1 % n, i0, i1);
       int sl = sign((a[1 \% n] - p).det(a[(1 + 1) \% n] - p));
49
       for(; l + 1 < r; ) {
50
         int mid = (1 + r) / 2;
51
52
         int smid = sign((a[mid % n] - p).det(a[(mid + 1) % n] - p));
53
         if (smid == sl) l = mid;
         else r = mid;
54
       }
55
56
       update tangent(p, r % n, i0, i1);
57
58
     int binary_search(Point u, Point v, int l, int r) {
       int sl = sign((v - u).det(a[1 % n] - u));
59
60
       for(; l + 1 < r; ) {
61
         int mid = (1 + r) / 2;
62
         int smid = sign((v - u).det(a[mid % n] - u));
         if (smid == sl) l = mid;
63
         else r = mid;
64
65
66
       return 1 % n;
67
68
     // 判定点是否在凸包内,在边界返回 true
     bool contain(Point p) {
69
       if (p.x < lower[0].x || p.x > lower.back().x) return false;
70
       int id = lower_bound(lower.begin(), lower.end(), Point(p.x, -INF)) -
71
          → lower.begin();
       if (lower[id].x == p.x) {
72
         if (lower[id].y > p.y) return false;
73
       } else if ((lower[id - 1] - p).det(lower[id] - p) < 0) return false;</pre>
74
       id = lower_bound(upper.begin(), upper.end(), Point(p.x, INF), greater<Point>())
75
          → - upper.begin();
       if (upper[id].x == p.x) {
76
         if (upper[id].y < p.y) return false;</pre>
77
       } else if ((upper[id - 1] - p).det(upper[id] - p) < 0) return false;</pre>
78
       return true;
79
80
81
     // 求点 p 关于凸包的两个切点,如果在凸包外则有序返回编号,多解返回任意一个図否则返回
        \hookrightarrow false
     bool get tangent(Point p, int &i0, int &i1) {
82
83
       if (contain(p)) return false;
84
85
       int id = lower_bound(lower.begin(), lower.end(), p) - lower.begin();
86
       binary search(0, id, p, i0, i1);
```

```
87
        binary search(id, (int)lower.size(), p, i0, i1);
 88
        id = lower bound(upper.begin(), upper.end(), p, greater<Point>()) -
          → upper.begin():
 89
        binary search((int)lower.size() - 1, (int)lower.size() - 1 + id, p, i0, i1);
       binary search((int)lower.size() - 1 + id, (int)lower.size() - 1 +
 90
          91
       return true:
 92
      }
      // 求凸包上和向量 vec 叉积最大的点,返回编号,有多个返回任意一个
 93
      int get_tangent(Point vec) {
 94
       pair<long long, int> ret = get_tangent(upper, vec);
 95
 96
       ret.second = (ret.second + (int)lower.size() - 1) % n;
       ret = max(ret, get_tangent(lower, vec));
 97
 98
       return ret.second;
 99
100
     // 求凸包和直线 u,v 的交点,如果无严格相交返回 false 。如果有则是和(i,next(i))
        → 的交点,两个点无序,交在点上不确定返回两条线段之一。
      bool get intersection(Point u, Point v, int &i0, int &i1) {
101
       int p0 = get tangent(u - v), p1 = get tangent(v - u);
102
       if (sign((v - u).det(a[p0] - u)) * sign((v - u).det(a[p1] - u)) < 0) {
103
104
         if (p0 > p1) swap(p0, p1);
105
         i0 = binary search(u, v, p0, p1);
106
         i1 = binary search(u, v, p1, p0 + n);
         return true;
107
108
       } else {
109
         return false:
       }
110
     }
111
112 };
```

圆的面积模板 $(n^2 \log n)$

```
dRatio = ((a.r - b.r) * (a.r + b.r) / d2 + 1) / 2
14
15
           pRatio = sqr(-(d2 - sqr(a.r - b.r)) * (d2 - sqr(a.r + b.r)) / (d2 * d2 *
             \hookrightarrow 4));
16
     Point d = b.o - a.o, p = d.rotate(PI / 2),
         q0 = a.o + d * dRatio + p * pRatio,
17
18
         q1 = a.o + d * dRatio - p * pRatio;
     double ang0 = (q0 - a.o).ang(),
19
20
          ang1 = (q1 - a.o).ang();
21
     evt.push_back(Event(q1, ang1, 1));
     evt.push_back(Event(q0, ang0, -1));
22
     cnt += ang1 > ang0;
23
24
25
   bool issame(const Circle &a, const Circle &b) {
26
     return sign((a.o - b.o).len()) == 0 && sign(a.r - b.r) == 0;
27
28
29
   bool overlap(const Circle &a, const Circle &b) {
30
     return sign(a.r - b.r - (a.o - b.o).len()) >= 0;
31
32
33
   bool intersect(const Circle &a, const Circle &b) {
34
     return sign((a.o - b.o).len() - a.r - b.r) < 0;
35
36
   }
37
38 int C;
39 | Circle c[N];
   double area[N];
41
42
   void solve() {
     memset(area, 0, sizeof(double) * (C + 1));
43
     for (int i = 0; i < C; ++i) {
44
       int cnt = 1;
45
46
       vector<Event> evt;
       for (int j = 0; j < i; ++j) {
47
48
         if (issame(c[i], c[j])) {
           ++cnt;
49
         }
50
51
52
       for (int j = 0; j < C; ++j) {
         if (j != i && !issame(c[i], c[j]) && overlap(c[j], c[i])) {
53
           ++cnt;
54
55
56
       for (int j = 0; j < C; ++j) {
57
```

```
58 :
         if (j != i && !overlap(c[j], c[i]) && !overlap(c[i], c[j]) && intersect(c[i],
            addEvent(c[i], c[j], evt, cnt);
59
60
         }
61
       }
62
        if (evt.size() == 0) {
          area[cnt] += PI * c[i].r * c[i].r;
63
64
        } else {
65
         sort(evt.begin(), evt.end());
66
         evt.push_back(evt.front());
67
          for (int j = 0; j + 1 < (int)evt.size(); ++j) {</pre>
68
            cnt += evt[j].delta;
69
            area[cnt] += det(evt[j].p, evt[j + 1].p) / 2;
70
            double ang = evt[j + 1].ang - evt[j].ang;
71
           if (ang < 0) {
              ang += PI * 2;
72
73
            area[cnt] += ang * c[i].r * c[i].r / 2 - sin(ang) * c[i].r * c[i].r / 2;
74
75
76
       }
77
78
```

三角形的心

```
1 | Point inCenter(const Point &A, const Point &B, const Point &C) { // 内心
     double a = (B - C).len(), b = (C - A).len(), c = (A - B).len(),
       s = fabs(det(B - A, C - A)),
 3
       r = s / p;
     return (A * a + B * b + C * c) / (a + b + c);
 6
   |Point circumCenter(const Point &a, const Point &b, const Point &c) { // 外心
     Point bb = b - a, cc = c - a;
     double db = bb.len2(), dc = cc.len2(), d = 2 * det(bb, cc);
11
     return a + Point(bb.y * dc - cc.y * db, cc.x * db - bb.x * dc) / d;
12
13
   Point othroCenter(const Point &a, const Point &b, const Point &c) { // 垂心
     Point ba = b - a, ca = c - a, bc = b - c;
15
16
     double Y = ba.y * ca.y * bc.y,
          A = ca.x * ba.y - ba.x * ca.y,
17
18
          x0 = (Y + ca.x * ba.y * b.x - ba.x * ca.y * c.x) / A,
          y0 = -ba.x * (x0 - c.x) / ba.y + ca.y;
19
     return Point(x0, y0);
20
21
```

最小覆盖球

```
int npoint, nouter; Tpoint pt[200000], outer[4],res; double radius,tmp;
2 void ball() {
     Tpoint q[3]; double m[3][3], sol[3], L[3], det;
     int i,j; res.x = res.y = res.z = radius = 0;
     switch ( nouter ) {
5
     case 1: res=outer[0]; break;
     case 2: res=(outer[0]+outer[1])/2; radius=dist2(res, outer[0]); break;
7
     case 3:
9
       for (i=0; i<2; ++i) q[i]=outer[i+1]-outer[0];</pre>
10
       for (i=0; i<2; ++i) for(j=0; j<2; ++j) m[i][j]=dot(q[i], q[j])*2;
       for (i=0; i<2; ++i) sol[i]=dot(q[i], q[i]);</pre>
11
       if (fabs(det=m[0][0]*m[1][1]-m[0][1]*m[1][0])<eps) return;</pre>
12
       L[0]=(sol[0]*m[1][1]-sol[1]*m[0][1])/det;
13
14
       L[1]=(sol[1]*m[0][0]-sol[0]*m[1][0])/det;
       res=outer[0]+q[0]*L[0]+q[1]*L[1];
15
16
       radius=dist2(res, outer[0]);
17
       break:
18
     case 4:
19
       for (i=0; i<3; ++i) q[i]=outer[i+1]-outer[0], sol[i]=dot(q[i], q[i]);</pre>
       for (i=0;i<3;++i) for(j=0;j<3;++j) m[i][j]=dot(q[i],q[j])*2;
20
       det= m[0][0]*m[1][1]*m[2][2]
21
22
       + m[0][1]*m[1][2]*m[2][0]
       + m[0][2]*m[2][1]*m[1][0]
23
24
       - m[0][2]*m[1][1]*m[2][0]
       - m[0][1]*m[1][0]*m[2][2]
25
26
       - m[0][0]*m[1][2]*m[2][1];
27
       if ( fabs(det)<eps ) return;</pre>
28
       for (j=0; j<3; ++j) {
29
         for (i=0; i<3; ++i) m[i][j]=sol[i];
30
         L[j]=(m[0][0]*m[1][1]*m[2][2]
         + m[0][1]*m[1][2]*m[2][0]
31
32
         + m[0][2]*m[2][1]*m[1][0]
         - m[0][2]*m[1][1]*m[2][0]
33
         - m[0][1]*m[1][0]*m[2][2]
34
35
         - m[0][0]*m[1][2]*m[2][1]
36
         ) / det:
         for (i=0; i<3; ++i) m[i][j]=dot(q[i], q[j])*2;
37
38
       } res=outer[0];
       for (i=0; i<3; ++i ) res = res + q[i] * L[i];</pre>
39
       radius=dist2(res, outer[0]);
40
41 | }}
42 | void minball(int n) { ball();
     if ( nouter<4 ) for (int i=0; i<n; ++i)</pre>
     if (dist2(res, pt[i])-radius>eps) {
```

```
outer[nouter++]=pt[i]; minball(i); --nouter;
45
46
       if (i>0) { Tpoint Tt = pt[i];
47
         memmove(&pt[1], &pt[0], sizeof(Tpoint)*i); pt[0]=Tt;
48 }}}
   int main0(){
49
     scanf("%d", &npoint);
50
     for (int i=0;i<npoint;i++) scanf("%1f%1f%1f",&pt[i].x,&pt[i].y,&pt[i].z);</pre>
51
52
     random_shuffle(pt,pt+npoint); radius=-1;
53
     for (int i=0;i<npoint;i++) if (dist2(res,pt[i])-radius>eps)
       nouter=1, outer[0]=pt[i], minball(i);
54
     printf("%.5f\n",sqrt(radius));
55
56
```

经纬度求球面最短距离

```
1 //lati 为纬度 longi 为经度 R 为半径
2 double Dist(double lati1,double longi1,double lati2,double longi2,double R) {
3 double pi=acos(-1.0); lati1*=pi/180,longi1*=pi/180,lati2*=pi/180,longi2*=pi/180;
4 double x1=cos(lati1)*sin(longi1),y1=cos(lati1)*cos(longi1),z1=sin(lati1);
5 double x2=cos(lati2)*sin(longi2),y2=cos(lati2)*cos(longi2),z2=sin(lati2);
6 double theta=acos(x1*x2+y1*y2+z1*z2); return(R*theta);
7 }
```

长方体表面两点最短距离

```
1 int r;
 2 | void turn(int i, int j, int x, int y, int z, int x0, int y0, int L, int W, int H) {
    if (z==0) { int R = x*x+y*y; if (R< r) r=R;
     } else {
 4
       if(i)=0 \& i < 2) turn(i+1, j, x0+L+z, y, x0+L-x, x0+L, y0, H, W, L);
       if(j \ge 0 \&\& j < 2) turn(i, j+1, x, y0+W+z, y0+W-y, x0, y0+W, L, H, W);
       if(i <= 0 \&\& i >- 2) turn(i-1, j, x0-z, y, x-x0, x0-H, y0, H, W, L);
       if(j<=0 && j>-2) turn(i, j-1, x, y0-z, y-y0, x0, y0-H, L, H, W);
9 | }}
10 int main(){
     int L, H, W, x1, y1, z1, x2, y2, z2;
     cin >> L >> W >> H >> x1 >> y1 >> z1 >> x2 >> y2 >> z2;
     if (z1!=0 \&\& z1!=H) if (y1==0 || y1==W)
13
14
           swap(y1,z1), std::swap(y2,z2), std::swap(W,H);
15
     else swap(x1,z1), std::swap(x2,z2), std::swap(L,H);
16
     if (z1==H) z1=0, z2=H-z2;
     r=0x3fffffff; turn(0,0,x2-x1,y2-y1,z2,-x1,-y1,L,W,H);
17
18
     cout<<r<<endl; return 0;</pre>
19 }
```

最大团

```
1 // Super Fast Maximum Clique
 2 // To Build Graph: Maxclique(Edges, Number of Nodes)
 3 // To Get Answer: mcqdyn(AnswerNodes Index Array, AnswserLength)
   typedef bool BB[N];
   struct Maxclique {
     const BB* e; int pk, level; const float Tlimit;
     struct Vertex{ int i, d; Vertex(int i):i(i),d(0){} };
 8
     typedef vector<Vertex> Vertices; typedef vector<int> ColorClass;
     Vertices V; vector<ColorClass> C; ColorClass QMAX, Q;
 9
     static bool desc_degree(const Vertex &vi, const Vertex &vj){
10
       return vi.d > vj.d;
11
12
13
     void init colors(Vertices &v){
       const int max degree = v[0].d;
14
       for(int i = 0; i < (int)v.size(); i++) v[i].d = min(i, max degree) + 1;
15
16
     void set_degrees(Vertices &v){
17
18
       for(int i = 0, j; i < (int)v.size(); i++)</pre>
19
         for(v[i].d = j = 0; j < int(v.size()); j++)
           v[i].d += e[v[i].i][v[j].i];
20
21
22
     struct StepCount{ int i1, i2; StepCount():i1(0),i2(0){} };
      vector<StepCount> S;
23
24
      bool cut1(const int pi, const ColorClass &A){
       for(int i = 0; i < (int)A.size(); i++) if (e[pi][A[i]]) return true;</pre>
25
26
       return false;
27
28
     void cut2(const Vertices &A, Vertices &B){
29
       for(int i = 0; i < (int)A.size() - 1; i++)
         if(e[A.back().i][A[i].i])
30
           B.push_back(A[i].i);
31
32
     void color sort(Vertices &R){
33
       int j = 0, maxno = 1, min_k = max((int)QMAX.size() - (int)Q.size() + 1, 1);
34
       C[1].clear(), C[2].clear();
35
36
       for(int i = 0; i < (int)R.size(); i++) {</pre>
         int pi = R[i].i, k = 1;
37
38
         while(cut1(pi, C[k])) k++;
         if(k > maxno) maxno = k, C[maxno + 1].clear();
39
40
         C[k].push back(pi);
         if(k < min_k) R[j++].i = pi;</pre>
41
42
       if(j > 0) R[j - 1].d = 0;
43
       for(int k = min_k; k <= maxno; k++)</pre>
44
```

```
for(int i = 0; i < (int)C[k].size(); i++)</pre>
45
46
           R[j].i = C[k][i], R[j++].d = k;
47
48
     void expand dyn(Vertices &R){// diff -> diff with no dyn
       S[level].i1 = S[level].i1 + S[level - 1].i1 - S[level].i2;//diff
49
       S[level].i2 = S[level - 1].i1;//diff
50
       while((int)R.size()) {
51
         if((int)Q.size() + R.back().d > (int)QMAX.size()){
52
           Q.push_back(R.back().i); Vertices Rp; cut2(R, Rp);
53
           if((int)Rp.size()){
54
             if((float)S[level].i1 / ++pk < Tlimit) degree_sort(Rp);//diff</pre>
55
56
              color_sort(Rp);
             S[level].i1++, level++;//diff
57
58
             expand_dyn(Rp);
             level--;//diff
59
60
           }
61
           else if((int)Q.size() > (int)QMAX.size()) QMAX = Q;
62
           Q.pop back();
63
         }
64
         else return;
65
         R.pop_back();
66
       }
67
68
     void mcqdyn(int* maxclique, int &sz){
69
        set degrees(V); sort(V.begin(), V.end(), desc degree); init colors(V);
       for(int i = 0; i < (int)V.size() + 1; i++)S[i].i1 = S[i].i2 = 0;
70
71
       expand_dyn(V); sz = (int)QMAX.size();
72
       for(int i = 0; i < (int)QMAX.size(); i++) maxclique[i] = QMAX[i];</pre>
73
     void degree_sort(Vertices &R){
74
       set_degrees(R); sort(R.begin(), R.end(), desc_degree);
75
76
     Maxclique(const BB* conn, const int sz, const float tt = 0.025) \
77
78
      : pk(0), level(1), Tlimit(tt){
       for(int i = 0; i < sz; i++) V.push_back(Vertex(i));</pre>
79
80
       e = conn, C.resize(sz + 1), S.resize(sz + 1);
81
82 };
```

极大团计数

```
1 //Bool g[][] 为图的邻接矩阵,图点的标号由 1 至 n
2 void dfs(int size){
3    int i, j, k, t, cnt, best = 0;
4    if (ne[size]==ce[size]){    if (ce[size]==0) ++ans; return; }
5    for (t=0, i=1; i<=ne[size]; ++i) {
```

```
for (cnt=0, j=ne[size]+1; j<=ce[size]; ++j)</pre>
        if (!g[list[size][i]][list[size][j]]) ++cnt;
 8
        if (t==0 || cnt<best) t=i, best=cnt;</pre>
 9
      } if (t && best<=0) return;</pre>
      for (k=ne[size]+1; k<=ce[size]; ++k) {</pre>
10
        if (t>0){ for (i=k; i<=ce[size]; ++i)
11
12
            if (!g[list[size][t]][list[size][i]]) break;
          swap(list[size][k], list[size][i]);
13
        } i=list[size][k]; ne[size+1]=ce[size+1]=0;
14
        for (j=1; j<k; ++j)if (g[i][list[size][j]])</pre>
15
16
            list[size+1][++ne[size+1]]=list[size][j];
        for (ce[size+1]=ne[size+1], j=k+1; j<=ce[size]; ++j)</pre>
17
18
        if (g[i][list[size][j]]) list[size+1][++ce[size+1]]=list[size][j];
19
        dfs(size+1); ++ne[size]; --best;
        for (j=k+1, cnt=0; j<=ce[size]; ++j) if (!g[i][list[size][j]]) ++cnt;</pre>
20
        if (t==0 || cnt<best) t=k, best=cnt;</pre>
^{21}
        if (t && best<=0) break;
22
23 | }}
   void work(){
24
25
      ne[0]=0; ce[0]=0;
26
     for (int i=1; i<=n; ++i) list[0][++ce[0]]=i;
27
      ans=0; dfs(0);
28 }
```

KM

```
// 最小匹配, 自带初始化 n <= m 方案存在 p[] 中
2
   const int N = 105;
   const int INF = 10000000000; // 严格大于最大边权
6
   int n, m, a[N][N];
   int u[N], v[N], p[N], fa[N];
10
11
   int minv[N];
12
   bool used[N];
13
14
   int km() {
15
16
     for (int i = 0; i < n; ++i) {
       u[i] = 0;
17
18
     for (int i = 0; i <= m; ++i) {
19
       v[i] = 0;
20
```

```
p[i] = n;
21
22
     for (int i = 0; i < n; ++i) {
23
24
       p[m] = i;
       int j0 = m;
25
26
       for (int j = 0; j <= m; ++j) {
27
         minv[j] = INF;
28
         used[j] = false;
29
30
       do {
         used[j0] = true;
31
         int i0 = p[j0], delta = INF, j1;
32
         for (int j = 0; j < m; ++j) {
33
34
           if (!used[j]) {
              int cur = a[i0][j] - u[i0] - v[j];
35
36
              if (cur < minv[j]) {</pre>
                minv[j] = cur;
37
38
                fa[j] = j0;
39
40
              if (minv[j] < delta) {</pre>
                delta = minv[j];
41
                j1 = j;
42
43
           }
44
45
46
         for (int j = 0; j <= m; ++j) {
           if (used[j]) {
47
48
              u[p[j]] += delta;
              v[j] -= delta;
49
50
           } else {
              minv[j] -= delta;
51
           }
52
         }
53
         j0 = j1;
54
       } while (p[j0] != n);
55
56
       do {
         int j1 = fa[j0];
57
58
         p[j0] = p[j1];
         j0 = j1;
59
60
       } while (j0 != m);
61
62
     return -v[m];
63
```

最小树形图

```
namespace LIUZHU{
     const int MAXN;
     int from [MAXN + 10][MAXN * 2 + 10];
     int edge[MAXN + 10][MAXN * 2 + 10];
     int sel[MAXN * 2 + 10], fa[MAXN * 2 + 10];
      int vis[MAXN * 2 + 10];
     const int INF;// INF >= sum( W_ij )
     int getfa(int x){
       if(x == fa[x]) return x;
10
       return fa[x] = getfa(fa[x]);
11
12
13
     void liuzhu(){ // 1-base: root is 1, answer = (sel[i], i) for i in [2..n]
       fa[1] = 1;
14
15
       for(int i = 2; i <= n; ++i){
16
         sel[i] = 1;
         fa[i] = i;
17
18
         for(int j = 1; j <= n; ++j) if(fa[j] != i){
19
           from[j][i] = i;
           if(edge[sel[i]][i] > edge[j][i]) sel[i] = j;
20
21
22
       int limit = n;
23
24
       while(1){
         int prelimit = limit;
25
26
         memset(vis, 0, sizeof(vis));
         vis[1] = 1;
27
28
         for(int i = 2; i <= prelimit; ++i) if(fa[i] == i && !vis[i]){</pre>
29
           int j = i;
           while(!vis[j]){
30
              vis[j] = i;
31
             j = getfa(sel[j]);
32
33
           if(j == 1 || vis[j] != i) continue;
34
35
           vector<int> C;
36
           int k = j;
37
38
              C.push_back(k);
              k = getfa(sel[k]);
39
40
           }while(k != j);
           ++limit;
41
           for(int i = 1; i <= n; ++i){
42
              edge[i][limit] = INF;
43
              from[i][limit] = limit;
44
```

```
45
46
            fa[limit] = vis[limit] = limit;
            for(int i = 0; i < int(C.size()); ++i){</pre>
47
48
              int x = C[i];
              fa[x] = limit;
49
50
              for(int j = 1; j <= n; ++j){
                if(edge[j][x] != INF && edge[j][limit] > edge[j][x] - edge[sel[x]][x]){
51
                  edge[j][limit] = edge[j][x] - edge[sel[x]][x];
52
                  from[j][limit] = x;
53
                }
54
              }
55
56
            for(int j = 1; j <= n; ++j) if(getfa(j) == limit){</pre>
57
58
              edge[j][limit] = INF;
59
60
            sel[limit] = 1;
61
            for(int j = 1; j <= n; ++j){
62
              if(edge[sel[limit]][limit] > edge[j][limit]){
63
                sel[limit] = j;
64
             }
65
66
         if(prelimit == limit) break;
67
68
69
       for(int i = limit; i > 1; --i){
         sel[from[sel[i]][i]] = sel[i];
70
71
7^2
73 | }
```

无向图最小割

```
int cost[maxn][maxn],seq[maxn],len[maxn],n,m,pop,ans;
bool used[maxn];
void Init(){
   int i,j,a,b,c;
   for(i=0;i<n;i++) for(j=0;j<n;j++) cost[i][j]=0;
   for(i=0;i<m;i++){
      scanf("%d %d %d",&a,&b,&c); cost[a][b]+=c; cost[b][a]+=c;
   }
   pop=n; for(i=0;i<n;i++) seq[i]=i;
}
void Work(){
   ans=inf; int i,j,k,l,mm,sum,pk;
   while(pop > 1){
      for(i=1;i<pop;i++) used[seq[i]]=0; used[seq[0]]=1;</pre>
```

```
for(i=1;i<pop;i++) len[seq[i]]=cost[seq[0]][seq[i]];</pre>
15
16
        pk=0: mm=-inf: k=-1:
17
        for(i=1;i<pop;i++) if(len[seq[i]] > mm){ mm=len[seq[i]]; k=i; }
18
        for(i=1;i<pop;i++){</pre>
          used[seq[l=k]]=1;
19
          if(i==pop-2) pk=k;
20
          if(i==pop-1) break;
21
22
          mm=-inf:
23
          for(j=1;j<pop;j++) if(!used[seq[j]])</pre>
            if((len[seq[j]]+=cost[seq[1]][seq[j]]) > mm)
24
              mm=len[seq[j]], k=j;
25
26
       }
27
       sum=0;
28
        for(i=0;i<pop;i++) if(i != k) sum+=cost[seq[k]][seq[i]];</pre>
       ans=min(ans,sum);
29
        for(i=0;i<pop;i++)</pre>
30
          cost[seq[k]][seq[i]]=cost[seq[i]][seq[k]]+=cost[seq[pk]][seq[i]];
31
32
       seq[pk]=seq[--pop];
33
34
     printf("%d\n",ans);
35 | }
```

带花树

```
1 vector<int> link[maxn];
   int n,match[maxn],Queue[maxn],head,tail;
3 int pred[maxn],base[maxn],start,finish,newbase;
   bool InQueue[maxn],InBlossom[maxn];
   void push(int u){ Queue[tail++]=u;InQueue[u]=true; }
   int pop(){ return Queue[head++]; }
   int FindCommonAncestor(int u,int v){
8
     bool InPath[maxn];
     for(int i=0;i<n;i++) InPath[i]=0;</pre>
     while(true){ u=base[u];InPath[u]=true;if(u==start) break;u=pred[match[u]]; }
10
     while(true){ v=base[v];if(InPath[v]) break;v=pred[match[v]]; }
11
     return v;
12
13
   void ResetTrace(int u){
14
     int v:
15
16
     while(base[u]!=newbase){
       v=match[u];
17
18
       InBlossom[base[u]]=InBlossom[base[v]]=true;
19
       u=pred[v];
       if(base[u]!=newbase) pred[u]=v;
20
^{21}
22 }
```

```
void BlossomContract(int u,int v){
      newbase=FindCommonAncestor(u,v);
24
25
     for (int i=0;i<n;i++)</pre>
26
     InBlossom[i]=0;
     ResetTrace(u);ResetTrace(v);
27
28
     if(base[u]!=newbase) pred[u]=v;
29
     if(base[v]!=newbase) pred[v]=u;
30
     for(int i=0;i<n;++i)</pre>
31
     if(InBlossom[base[i]]){
32
       base[i]=newbase;
       if(!InQueue[i]) push(i);
33
34
35
   bool FindAugmentingPath(int u){
36
     bool found=false;
37
38
     for(int i=0;i<n;++i) pred[i]=-1,base[i]=i;</pre>
     for (int i=0;i<n;i++) InQueue[i]=0;</pre>
39
     start=u;finish=-1; head=tail=0; push(start);
40
      while(head<tail){</pre>
41
42
       int u=pop();
       for(int i=link[u].size()-1;i>=0;i--){
43
         int v=link[u][i];
44
         if(base[u]!=base[v]&&match[u]!=v)
45
46
           if(v==start||(match[v]>=0&&pred[match[v]]>=0))
              BlossomContract(u,v);
47
48
            else if(pred[v]==-1){
              pred[v]=u;
49
              if(match[v]>=0) push(match[v]);
50
              else{ finish=v; return true; }
51
           }
52
       }
53
54
55
     return found;
56
    void AugmentPath(){
57
58
     int u=finish,v,w;
     while(u>=0){ v=pred[u];w=match[v];match[v]=u;match[u]=v;u=w; }
59
60
   void FindMaxMatching(){
     for(int i=0;i<n;++i) match[i]=-1;</pre>
62
     for(int i=0;i<n;++i) if(match[i]==-1) if(FindAugmentingPath(i)) AugmentPath();</pre>
64 }
```

动态最小生成树

```
/* 动态最小生成树 Q(logQ)^2
     (qx[i],qy[i]) 表示将编号为 qx[i] 的边的权值改为 qy[i]
     删除一条边相当于将其权值改为 ∞
 3
     加入一条边相当于将其权值从 ∞ 变成某个值 */
   const int qsize=maxm+3*maxq;
 5
   int x[qsize],y[qsize],z[qsize], qx[maxq],qy[maxq],n,m,Q;
   void init(){
 8
     scanf("%d%d",&n,&m);
     for(int i=0;i<m;i++) scanf("%d%d%d",x+i,y+i,z+i);</pre>
 9
     scanf("%d",&Q);
10
     for(int i=0;i<Q;i++){ scanf("%d%d",qx+i,qy+i); qx[i]--; }</pre>
11
12 }
13 | int a[maxn], *tz;
14 int find(int x){
15
     int root=x; while(a[root]) root=a[root];
16
     int next; while(next=a[x]){ a[x]=root; x=next; }
     return root;
17
18 }
   inline bool cmp(const int &a,const int &b){ return tz[a]<tz[b]; }
   int kx[maxn],ky[maxn],kt, vd[maxn],id[maxm], app[maxm];
20
   bool extra[maxm];
21
   void solve(int *qx,int *qy,int Q,int n,int *x,int *y,int *z,int m,long long ans){
22
     if(Q==1){
23
24
       for(int i=1;i<=n;i++) a[i]=0;
       z[qx[0]]=qy[0];
25
26
       for(int i=0;i<m;i++) id[i]=i;tz=z;</pre>
       sort(id,id+m,cmp); int ri,rj;
27
28
       for(int i=0;i<m;i++){</pre>
29
         ri=find(x[id[i]]); rj=find(y[id[i]]);
         if(ri!=rj){ ans+=z[id[i]]; a[ri]=rj; }
30
31
       printf("%I64d\n",ans);
32
33
       return;
34
     int ri,rj;
35
36
     //contract
     kt=0;
37
38
     for(int i=1;i<=n;i++) a[i]=0;</pre>
     for(int i=0;i<Q;i++){</pre>
39
40
       ri=find(x[qx[i]]); rj=find(y[qx[i]]); if(ri!=rj) a[ri]=rj;
41
     int tm=0;
42
     for(int i=0;i<m;i++) extra[i]=true;</pre>
43
     for(int i=0;i<Q;i++) extra[ qx[i] ]=false;</pre>
44
```

```
for(int i=0;i<m;i++) if(extra[i]) id[tm++]=i;</pre>
45
46
     tz=z; sort(id,id+tm,cmp);
     for(int i=0;i<tm;i++){</pre>
47
48
       ri=find(x[id[i]]); rj=find(y[id[i]]);
       if(ri!=rj){
49
         a[ri]=rj; ans += z[id[i]];
50
         kx[kt]=x[id[i]]; ky[kt]=y[id[i]]; kt++;
51
       }
52
53
     for(int i=1;i<=n;i++) a[i]=0;
54
     for(int i=0;i<kt;i++) a[ find(kx[i]) ]=find(ky[i]);</pre>
55
56
     int n2=0;
     for(int i=1;i<=n;i++) if(a[i]==0)
57
58
     vd[i]=++n2;
     for(int i=1;i<=n;i++) if(a[i])</pre>
59
60
     vd[i]=vd[find(i)];
61
     int m2=0, *Nx=x+m, *Ny=y+m, *Nz=z+m;
     for(int i=0;i<m;i++) app[i]=-1;</pre>
62
63
     for(int i=0;i<Q;i++) if(app[qx[i]]==-1){</pre>
64
       Nx[m2]=vd[x[qx[i]];Ny[m2]=vd[y[qx[i]];Nz[m2]=z[qx[i]];
65
       app[qx[i]]=m2; m2++;
66
67
     for(int i=0;i<0;i++){ z[qx[i]]=qy[i]; qx[i]=app[qx[i]]; }
68
     for(int i=1;i<=n2;i++) a[i]=0;</pre>
69
     for(int i=0;i<tm;i++){</pre>
       ri=find(vd[ x[id[i]] ]); rj=find(vd[ y[id[i]] ]);
70
71
       if(ri!=rj){
72
         a[ri]=rj; Nx[m2]=vd[ x[id[i]] ];
         Ny[m2]=vd[ y[id[i]] ]; Nz[m2]=z[id[i]]; m2++;
73
       }
74
75
76
     int mid=0/2;
     solve(qx,qy,mid,n2,Nx,Ny,Nz,m2,ans);
77
78
     solve(qx+mid,qy+mid,Q-mid,n2,Nx,Ny,Nz,m2,ans);
79
   void work(){ if(Q) solve(qx,qy,Q,n,x,y,z,m,0); }
81 | int main(){init(); work(); return 0; }
```

Hopcroft

```
int from[1010],wh[1010],g[1010];
int num[100010],nxt[100010],tot;
int n,m,ans,h,t,q[1010],dx[1010],dy[1010];
bool bfs(){
bool ret=false;
h=0;t=0;
```

```
for(int i=0;i<n;i++) if(wh[i]==-1) t++, q[t]=i;</pre>
8
     memset(dx,0,sizeof(dx)), memset(dy,0,sizeof(dy));
     while(h++<t){</pre>
10
        for(int i=g[q[h]];i!=0;i=nxt[i])
         if(dy[num[i]]==0){
11
            dy[num[i]]=dx[q[h]]+1;
12
           if(from[num[i]]==-1) ret=true;
13
            else{
14
15
              dx[from[num[i]]]=dx[q[h]]+2;
16
              q[++t]=from[num[i]];
17
18
         }
19
20
     return ret;
^{21}
   bool dfs(int x){
^{22}
      for(int i=g[x];i!=0;i=nxt[i]){
23
       if(dy[num[i]]==dx[x]+1){
24
         dy[num[i]]=0;
25
         if(from[num[i]]==-1||dfs(from[num[i]])){
26
            wh[x]=num[i];from[num[i]]=x;return true;
27
         }
28
29
30
31
     return false;
32
   void hopcroft(){
33
     memset(from,-1,sizeof(from)), memset(wh,-1,sizeof(wh));
34
     while(bfs())
35
36
       for(int i=0;i<n;i++)</pre>
         if(wh[i]==-1&&dfs(i)) ans++;
37
38 }
   void insert(int x,int y){ tot++;num[tot]=y;nxt[tot]=g[x];g[x]=tot; }
   int main(){
40
     while(scanf("%d %d",&n,&m)==2){
41
42
        tot=0; memset(g,0,sizeof(g));
        for(int i=0;i<n;i++){</pre>
43
         int x; scanf("%d",&x);
44
         for(int j=0;j<x;j++){</pre>
45
46
           int y; scanf("%d",&y);
           y--; insert(i,y);
47
48
         }
49
        ans=0; hopcroft(); printf("%d\n",ans);
50
51
```

```
52 }
```

素数判定

```
int strong_pseudo_primetest(long long n,int base) {
        long long n2=n-1,res;
3
       int s=0;
4
       while(n2\%2==0) n2>>=1,s++;
5
       res=powmod(base,n2,n);
6
       if((res==1)||(res==n-1)) return 1;
       s--;
8
       while(s \ge 0) {
9
           res=mulmod(res,res,n);
           if(res==n-1) return 1;
10
11
           s--;
12
13
       return 0; // n is not a strong pseudo prime
14 }
   int isprime(long long n) {
15
16
     static LL testNum[]={2,3,5,7,11,13,17,19,23,29,31,37};
     static LL lim[]={4,0,1373653LL,25326001LL,25000000000LL,2152302898747LL, \
17
     3474749660383LL,341550071728321LL,0,0,0,0);
18
     if(n<2||n==3215031751LL) return 0;
19
     for(int i=0;i<12;++i){
20
       if(n<lim[i]) return 1;</pre>
21
       if(strong_pseudo_primetest(n,testNum[i])==0) return 0;
22
23
24
     return 1;
25
```

启发式分解

```
1 int ansn; LL ans[1000];
   LL func(LL x,LL n){ return(mod_mul(x,x,n)+1)%n; }
3 LL Pollard(LL n){
     LL i,x,y,p;
     if(Rabin_Miller(n)) return n;
     if(!(n&1)) return 2;
     for(i=1;i<20;i++){
8
       x=i; y=func(x,n); p=gcd(y-x,n);
       while(p==1) {x=func(x,n); y=func(func(y,n),n); p=gcd((y-x+n)%n,n)%n;}
       if(p==0||p==n) continue;
10
11
       return p;
12
13
   void factor(LL n){
     LL x;
15
```

二次剩余

```
void calcH(int &t, int &h, const int p) {
     int tmp = p - 1; for (t = 0; (tmp & 1) == 0; tmp /= 2) t++; h = tmp;
 3 | }
   // solve equation x^2 \mod p = a
   bool solve(int a, int p, int &x, int &y) {
     srand(19920225);
     if (p == 2) \{ x = y = 1; return true; \}
     int p2 = p / 2, tmp = power(a, p2, p);
     if (tmp == p - 1) return false;
     if ((p + 1) \% 4 == 0) {
10
       x = power(a, (p + 1) / 4, p); y = p - x; return true;
11
     } else {
12
       int t, h, b, pb; calcH(t, h, p);
13
       if (t >= 2) {
14
         do \{b = rand() \% (p - 2) + 2;
15
16
         } while (power(b, p / 2, p) != p - 1);
         pb = power(b, h, p);
17
18
       } int s = power(a, h / 2, p);
       for (int step = 2; step <= t; step++) {</pre>
19
         int ss = (((long long)(s * s) % p) * a) % p;
20
         for (int i = 0; i < t - step; i++) ss = ((long long)ss * ss) % p;
21
22
         if (ss + 1 == p) s = (s * pb) % p; pb = ((long long)pb * pb) % p;
       x = ((long long)s * a) % p; y = p - x;
23
     } return true;
24
25 | }
```

Pell 方程

```
1 ULL A,B,p[maxn],q[maxn],a[maxn],g[maxn],h[maxn];
2 | int main() {
     for (int test=1, n;scanf("%d",&n) && n;++test) {
       printf("Case %d: ",test);
4
       if (fabs(sqrt(n)-floor(sqrt(n)+1e-7))<=1e-7) {</pre>
6
         int a=(int)(floor(sqrt(n)+1e-7)); printf("%d %d\n",a,1);
       } else {
         // 求 x^2 - ny^2 = 1 的最小正整数根, n 不是完全平方数
8
9
         p[1]=q[0]=h[1]=1;p[0]=q[1]=g[1]=0;
10
         a[2]=(int)(floor(sqrt(n)+1e-7));
         for (int i=2;i;++i) {
11
           g[i]=-g[i-1]+a[i]*h[i-1]; h[i]=(n-sqr(g[i]))/h[i-1];
12
```

蔡勒公式

```
int zeller(int y,int m,int d) {
   if (m<=2) y--,m+=12; int c=y/100; y%=100;
   int w=((c>>2)-(c<<1)+y+(y>>2)+(13*(m+1)/5)+d-1)%7;
   if (w<0) w+=7; return(w);
}</pre>
```

Schreier-Sims

```
namespace Schreier_Sims_Algorithm{
     struct Permutation{
       vector<int> P;
3
       Permutation(){}
       Permutation(int n){
         P.resize(n);
       Permutation inv()const{
         Permutation ret(P.size());
10
         for(int i = 0; i < int(P.size()); ++i) ret.P[P[i]] = i;</pre>
11
         return ret;
12
       int &operator [](const int &dn){
13
14
         return P[dn];
15
16
       void resize(const size_t &sz){
         P.resize(sz);
17
18
       size_t size()const{
19
20
         return P.size();
21
       const int &operator [](const int &dn)const{
22
         return P[dn];
23
24
25
26
     Permutation operator *(const Permutation &a, const Permutation &b){
27
       Permutation ret(a.size());
28
       for(int i = 0; i < (int)a.size(); ++i){
         ret[i] = b[a[i]];
29
```

```
vector<Bucket> buckets(n);
30
                                                                                               75
                                                                                               76
                                                                                                         swap(buckets, buckets);
31
       return ret;
     }
                                                                                                         vector<Bucket> _bucketsInv(n);
32
                                                                                               77
33
                                                                                               78
                                                                                                         swap(bucketsInv, bucketsInv);
     typedef vector<Permutation> Bucket;
                                                                                                         vector<Table> lookupTable(n);
                                                                                               79
34
                                                                                                         swap(lookupTable, lookupTable);
     typedef vector<int> Table;
                                                                                               80
35
                                                                                               81
36
     typedef pair<int,int> pii;
                                                                                               82
     int n, m;
                                                                                                       for(int i = 0; i < n; ++i){
37
     vector<Bucket> buckets, bucketsInv;
                                                                                               83
38
                                                                                                         lookupTable[i].resize(n);
     vector<Table> lookupTable;
                                                                                               84
                                                                                                         fill(lookupTable[i].begin(), lookupTable[i].end(), -1);
39
                                                                                               85
40
                                                                                               86
     int fastFilter(const Permutation &g, bool addToGroup = true){
                                                                                                       Permutation id(n);
41
       int n = buckets.size();
                                                                                               87
                                                                                                       for(int i = 0; i < n; ++i){
42
                                                                                               88
43
       Permutation p;
                                                                                                         id[i] = i;
       for(int i = 0; i < n; ++i){
                                                                                               89
44
         int res = lookupTable[i][p[i]];
                                                                                                       for(int i = 0; i < n; ++i){
45
                                                                                               90
46
         if(res == -1){
                                                                                                         buckets[i].push_back(id);
                                                                                               91
           if(addToGroup){
                                                                                                         bucketsInv[i].push back(id);
                                                                                               92
47
             buckets[i].push back(p);
48
                                                                                                         lookupTable[i][i] = 0;
                                                                                               93
             bucketsInv[i].push_back(p.inv());
                                                                                                       }
49
                                                                                               94
50
             lookupTable[i][p[i]] = (int)buckets[i].size() - 1;
                                                                                                       for(int i = 0; i < m; ++i){
                                                                                               95
           }
                                                                                               96
                                                                                                         fastFilter(gen[i]);
51
           return i;
52
                                                                                               97
         }
                                                                                               98
                                                                                                       queue<pair<point,point> > toUpdate;
53
         p = p * bucketsInv[i][res];
                                                                                                       for(int i = 0; i < n; ++i){
                                                                                               99
54
                                                                                                         for(int j = i; j < n; ++j){}
         swap(i1,i2);
                                                                                              100
55
56
                                                                                                           for(int k = 0; k < (int)buckets[i].size(); ++k){</pre>
       }
                                                                                              101
                                                                                                             for(int 1 = 0; 1 < (int)buckets[j].size(); ++1){</pre>
57
       return -1;
                                                                                              102
58
                                                                                                               toUpdate.push(make_pair(pii(i,k), pii(j,l)));
                                                                                              103
                                                                                                             }
59
                                                                                              104
60
     long long calcTotalSize(){
                                                                                              105
61
       long long ret = 1;
                                                                                              106
                                                                                                         }
62
       for(int i = 0; i < n; ++i){
                                                                                                       }
                                                                                              107
63
                                                                                              108
                                                                                                       while(!toUpdate.empty()){
         ret *= buckets[i].size();
64
                                                                                                         pii a = toUpdate.front().first;
                                                                                              109
65
       return ret;
                                                                                              110
                                                                                                         pii b = toUpdate.front().second;
66
                                                                                                         toUpdate.pop();
                                                                                              111
67
                                                                                                         int res = fastFilter(buckets[a.first][a.second] * buckets[b.first][b.second]);
                                                                                              112
68
     bool inGroup(const Permutation &g){
                                                                                                         if(res==-1) continue;
                                                                                              113
       return fastFilter(g, false) == -1;
                                                                                                         pii newPair(res, (int)buckets[res].size() - 1);
69
                                                                                              114
                                                                                                         for(int i = 0; i < n; ++i){
70
                                                                                              115
                                                                                              116
                                                                                                           for(int j = 0; j < (int)buckets[i].size(); ++j){</pre>
71
     void solve(const Bucket &gen,int n){// m perm[0..n - 1]s
                                                                                                             if(i <= res){</pre>
72
                                                                                              117
                                                                                              118
                                                                                                               toUpdate.push(make pair(pii(i , j), newPair));
       n = _n, m = gen.size();
73
       {//clear all
                                                                                                             }
74
                                                                                              119
```

Romberg

```
1 template<class T>
 2 double romberg(const T&f,double a,double b,double eps=1e-8){
     std::vector<double>t; double h=b-a,last,curr; int k=1,i=1;
     t.push_back(h*(f(a)+f(b))/2); // 梯形
     do{ last=t.back(); curr=0; double x=a+h/2;
 5
       for(int j=0;j<k;++j) curr+=f(x),x+=h;</pre>
 7
       curr=(t[0]+h*curr)/2; double k1=4.0/3.0, k2=1.0/3.0;
 8
       for(int j=0;j<i;j++){ double temp=k1*curr-k2*t[j];</pre>
         t[j]=curr; curr=temp; k2/=4*k1-k2; k1=k2+1; // 防止溢出
 9
       } t.push_back(curr); k*=2; h/=2; i++;
10
     } while(std::fabs(last-curr)>eps);
11
     return t.back();
12
13 | }
```

线性规划

```
1 // 求\max\{cx \mid Ax \le b, x \ge 0\}的解
2 typedef vector<double> VD;
3 | VD simplex(vector<VD> A, VD b, VD c) {
     int n = A.size(), m = A[0].size() + 1, r = n, s = m - 1;
     vector\langle VD \rangle D(n + 2, VD(m + 1, 0)); vector\langle int \rangle ix(n + m);
6
     for (int i = 0; i < n + m; ++ i) ix[i] = i;
     for (int i = 0; i < n; ++ i) {
8
       for (int j = 0; j < m - 1; ++ j) D[i][j] = -A[i][j];
       D[i][m - 1] = 1; D[i][m] = b[i];
       if (D[r][m] > D[i][m]) r = i;
10
11
      for (int j = 0; j < m - 1; ++ j) D[n][j] = c[j];
12
     D[n + 1][m - 1] = -1;
13
      for (double d; ; ) {
14
15
       if (r < n) {
16
         int t = ix[s]; ix[s] = ix[r + m]; ix[r + m] = t;
         D[r][s] = 1.0 / D[r][s]; vector<int> speedUp;
17
18
         for (int j = 0; j <= m; ++ j) if (j != s) {
           D[r][j] *= -D[r][s];
19
           if(D[r][j]) speedUp.push_back(j);
20
```

```
21
         }
22
         for (int i = 0; i <= n + 1; ++ i) if (i != r) {
23
           for(int j = 0; j < speedUp.size(); ++ j)</pre>
24
           D[i][speedUp[j]] += D[r][speedUp[j]] * D[i][s];
           D[i][s] *= D[r][s];
25
26
       } r = -1; s = -1;
       for (int j = 0; j < m; ++ j) if (s < 0 || ix[s] > ix[j])
27
28
         if (D[n + 1][j] > EPS || (D[n + 1][j] > -EPS && D[n][j] > EPS)) s = j;
29
       if (s < 0) break;
       for (int i = 0; i < n; ++ i) if (D[i][s] < -EPS)
30
         if (r < 0 \mid | (d = D[r][m] / D[r][s] - D[i][m] / D[i][s]) < -EPS
31
             || (d < EPS \&\& ix[r + m] > ix[i + m])) r = i;
32
       if (r < 0) return VD(); // 无边界
33
34
     if (D[n + 1][m] < -EPS) return VD(); // 无解
35
36
     VD x(m - 1);
     for (int i = m; i < n + m; ++ i) if (ix[i] < m - 1) x[ix[i]] = D[i - m][m];
37
38
     return x; // 最优值在 D[n][m]
39 }
```

FFT

```
// double 精度对10^9 + 7 取模最多可以做到2^20
   const int MOD = 1000003;
   const double PI = acos(-1);
   typedef complex<double> Complex;
   const int N = 65536, L = 15, MASK = (1 << L) - 1;
10
11 | Complex w[N];
12
   void FFTInit() {
13
     for (int i = 0; i < N; ++i) {
14
       w[i] = Complex(cos(2 * i * PI / N), sin(2 * i * PI / N));
15
16
17
18
   void FFT(Complex p[], int n) {
19
     for (int i = 1, j = 0; i < n - 1; ++i) {
20
       for (int s = n; j ^= s >>= 1, ~j & s;);
21
       if (i < j) {
22
         swap(p[i], p[j]);
23
```

```
24
25
26
     for (int d = 0; (1 << d) < n; ++d) {
27
       int m = 1 << d, m2 = m * 2, rm = n >> (d + 1);
28
       for (int i = 0; i < n; i += m2) {
29
         for (int j = 0; j < m; ++j) {
30
           Complex &p1 = p[i + j + m], &p2 = p[i + j];
31
           Complex t = w[rm * j] * p1;
32
           p1 = p2 - t;
33
           p2 = p2 + t;
34
       }
35
36
37
38
   Complex A[N], B[N], C[N], D[N];
39
40
   void mul(int a[N], int b[N]) {
41
     for (int i = 0; i < N; ++i) {
42
       A[i] = Complex(a[i] >> L, a[i] & MASK);
43
       B[i] = Complex(b[i] >> L, b[i] & MASK);
44
45
46
     FFT(A, N);
     FFT(B, N);
47
48
     for (int i = 0; i < N; ++i) {
       int j = (N - i) \% N;
49
       Complex da = (A[i] - conj(A[j])) * Complex(0, -0.5),
50
           db = (A[i] + conj(A[j])) * Complex(0.5, 0),
51
           dc = (B[i] - conj(B[j])) * Complex(0, -0.5),
52
           dd = (B[i] + conj(B[j])) * Complex(0.5, 0);
53
       C[j] = da * dd + da * dc * Complex(0, 1);
54
       D[i] = db * dd + db * dc * Complex(0, 1);
55
56
     FFT(C, N);
57
58
     FFT(D, N);
59
     for (int i = 0; i < N; ++i) {
60
       long long da = (long long)(C[i].imag() / N + 0.5) % MOD,
61
             db = (long long)(C[i].real() / N + 0.5) % MOD,
62
             dc = (long long)(D[i].imag() / N + 0.5) % MOD,
63
             dd = (long long)(D[i].real() / N + 0.5) % MOD;
64
       a[i] = ((dd << (L * 2)) + ((db + dc) << L) + da) % MOD;
65
66 }
```

NTT

```
1 //R 是 2^n*a+1 形质数 p 的原根
   void NFT(int P[], int n, int oper) {
     for (int i = 1, j = 0; i < n - 1; ++i) {
 4
       for (int s = n; j ^= s >>= 1, ~j \& s;);
       if (i < j) {
 5
         swap(P[i], P[j]);
 9
     for (int d = 0; (1 << d) < n; ++d) {
       int m = 1 << d, m2 = m * 2;
10
       int unit p0 = powmod(R, (MOD - 1) / m2);
11
12
       if (oper < 0) {
13
         unit_p0 = inverse(unit_p0);
14
15
       for (int i = 0; i < n; i += m2) {
16
         int unit = 1;
17
         for (int j = 0; j < m; ++j) {
18
           int &P1 = P[i + j + m],
19
             &P2 = P[i + j];
20
           int t = (long long)unit * P1 % MOD;
21
           P1 = (P2 - t + MOD) \% MOD;
22
           P2 = (P2 + t) \% MOD;
           unit = (long long)unit * unit p0 % MOD;
23
24
25
26
27
```

FWT

```
void FWT(int a[N], int N) {
     for (int d = 1; d < N; d <<= 1) {
3
       int d2 = d \ll 1;
       for (int i = 0; i < N; i += d2) {
         int *x = a + i, *y = a + i + d;
         for (int j = 0; j < d; ++j, ++x, ++y) {
          if ((*x += *y) >= MOD) {
             *x -= MOD;
10
           if ((*y = *x - (*y << 1)) < 0) {
11
             if ((*y += MOD) < 0) {
12
               *v += MOD;
             }
13
14
15
```

```
16
17
18
19
   void xorPow(int a[N], int n, int b[N]) {
20
     memset(b, 0, sizeof(int) * N);
21
     b[0] = 1;
22
     FWT(a, N);
23
     FWT(b, N);
24
     while(n) {
25
26
      if (n & 1) {
         dot(b, a, N);
27
28
       }
29
       dot(a, a, N);
30
       n >>= 1;
31
     FWT(b, N);
32
     norm(b, N);
33
34
```

回文串 manacher

```
for(int i=1,j=0;i!=(n<<1)-1;++i){
  int p=i>>1,q=i-p,r=((j+1)>>1)+l[j]-1;
  l[i]=r<q?0:min(r-q+1,l[(j<<1)-i]);
  while(p-l[i]!=-1&&q+l[i]!=n&&s[p-l[i]]==s[q+l[i]]) l[i]++;
  if(q+l[i]-1>r) j=i;
  a+=l[i];
}
```

后缀数组 (倍增)

```
int rank[MAX_N],height[MAX_N];
   int cmp(int *x,int a,int b,int d){
     return x[a]==x[b]&&x[a+d]==x[b+d];
3
4
   void doubling(int *a,int N,int M){
     static int sRank[MAX N],tmpA[MAX N],tmpB[MAX N];
     int *x=tmpA,*y=tmpB;
8
     for(int i=0;i<M;++i) sRank[i]=0;</pre>
     for(int i=0;i<N;++i) ++sRank[x[i]=a[i]];</pre>
     for(int i=1;i<M;++i) sRank[i]+=sRank[i-1];</pre>
10
11
      for(int i=N-1;i>=0;--i) sa[--sRank[x[i]]]=i;
      for(int d=1,p=0;p<N;M=p,d<<=1){</pre>
12
       p=0; for(int i=N-d;i<N;++i) y[p++]=i;</pre>
13
       for(int i=0;i<N;++i) if(sa[i]>=d) y[p++]=sa[i]-d;
14
15
        for(int i=0;i<M;++i) sRank[i]=0;</pre>
```

```
16
        for(int i=0;i<N;++i) ++sRank[x[i]];</pre>
17
        for(int i=1;i<M;++i) sRank[i]+=sRank[i-1];</pre>
18
       for(int i=N-1;i>=0;--i) sa[--sRank[x[y[i]]]]=y[i];
19
        swap(x,y); x[sa[0]]=0; p=1;
       for(int i=1;i<N;++i) x[sa[i]]=cmp(y,sa[i],sa[i-1],d)?p-1:p++;
20
21
22
   void calcHeight(){
23
24
     for(int i=0;i<N;++i) rank[sa[i]]=i;</pre>
25
     int cur=0; for(int i=0;i<N;++i)</pre>
26
     if(rank[i]){
       if(cur) cur--;
27
28
       for(;a[i+cur]==a[sa[rank[i]-1]+cur];++cur);
29
       height[rank[i]]=cur;
30
31
```

后缀数组 (DC3)

```
1 // 待排序的字符串放在 r 数组中, 从 r[0] 到 r[n-1], 长度为 n, 且最大值小于 m
2 // 约定除 r[n-1] 外所有的 r[i] 都大于 0, r[n-1]=0
3 // 函数结束后, 结果放在 sa 数组中, 从 sa[0] 到 sa[n-1]
   #define maxn 10000
   #define F(x) ((x)/3+((x)%3==1?0:tb))
  #define G(x) ((x)<tb?(x)*3+1:((x)-tb)*3+2)
7 int wa[maxn],wb[maxn],wv[maxn],wss[maxn]; // 必须这么大
8 int s[maxn*3],sa[maxn*3];
   int c0(int *r,int a,int b){return r[a]==r[b]&&r[a+1]==r[b+1]&&r[a+2]==r[b+2];}
   int c12(int k,int *r,int a,int b){
10
    if(k==2) return r[a] < r[b] | | r[a] == r[b] & c12(1,r,a+1,b+1);
11
12
     else return r[a] < r[b] | | r[a] == r[b] & wv[a+1] < wv[b+1];
13
   void sort(int *r,int *a,int *b,int n,int m){
14
     int i; for(i=0;i<n;i++) wv[i]=r[a[i]];</pre>
15
16
     for(i=0;i<m;i++) wss[i]=0; for(i=0;i<n;i++) wss[wv[i]]++;</pre>
17
     for(i=1;i<m;i++) wss[i]+=wss[i-1];</pre>
18
     for(i=n-1;i>=0;i--) b[--wss[wv[i]]]=a[i];
19
   void dc3(int *r,int *sa,int n,int m){
20
     int i,j,*rn=r+n,*san=sa+n,ta=0,tb=(n+1)/3,tbc=0,p;
21
22
     r[n]=r[n+1]=0;
     for(i=0;i<n;i++) if(i%3!=0) wa[tbc++]=i;
23
24
     sort(r+2,wa,wb,tbc,m); sort(r+1,wb,wa,tbc,m); sort(r,wa,wb,tbc,m);
     for(p=1,rn[F(wb[0])]=0,i=1;i<tbc;i++)
25
26
       rn[F(wb[i])]=c0(r,wb[i-1],wb[i])?p-1:p++;
```

```
if(p<tbc) dc3(rn,san,tbc,p);</pre>
27
28
      else for(i=0;i<tbc;i++) san[rn[i]]=i;</pre>
      for (i=0;i<tbc;i++) if(san[i]<tb) wb[ta++]=san[i]*3;</pre>
29
30
      if(n\%3==1) wb[ta++]=n-1;
      sort(r,wb,wa,ta,m); for(i=0;i<tbc;i++) wv[wb[i]=G(san[i])]=i;</pre>
31
      for(i=0,j=0,p=0;i<ta && j<tbc;p++)</pre>
32
       sa[p]=c12(wb[j]%3,r,wa[i],wb[j])?wa[i++]:wb[j++];
33
      for(;i<ta;p++) sa[p]=wa[i++]; for(;j<tbc;p++) sa[p]=wb[j++];}</pre>
34
   int main(){
35
36
     int n, m=0; scanf("%d",&n);
      for (int i=0;i<n;i++) scanf("%d",&s[i]),s[i]++,m=max(s[i]+1,m);</pre>
37
38
      printf("%d\n",m); s[n++]=0; dc3(s,sa,n,m);
      for (int i=0;i<n;i++) printf("%d ",sa[i]);printf("\n");</pre>
39
40 | }
```

后缀自动机

```
struct State {
     int length;
     State *parent,*go[C];
 3
     State(int length):length(length),parent(NULL){
       memset(go,0,sizeof(go));
 5
 6
 7
     State* extend(State *start,int token){
 8
       State *p=this;
       State *np=new State(this->length+1);
 9
       while(p!=NULL&&p->go[token]==NULL)
10
         p->go[token]=np, p=p->parent;
11
12
       if(p==NULL) np->parent=start;
       else{
13
         State *q=p->go[token];
14
         if(p->length+1==q->length) np->parent=q;
15
16
         else{
17
           State *nq=new State(p->length+1);
18
           memcpy(nq->go,q->go,sizeof(q->go));
           nq->parent=q->parent;
19
           np->parent=q->parent=nq;
20
           while(p!=NULL&&p->go[token]==q)
21
              p->go[token]=nq, p=p->parent;
22
23
       }
24
25
       return np;
26
27 };
```

后缀树 (With Walk)

```
int pos;
2
   struct Node {
     int 1, r;
     Node *suf, *ch[C];
     Node (int l = -1, int r = INF) : l(l), r(r) {
9
       suf = 0;
       memset(ch, 0, sizeof(ch));
10
11
12
13
     int len() {
       return min(r, pos + 1) - 1;
14
15
16
   };
17
18 int top;
19
   Node pool[N << 1];</pre>
20
21
   Node *root, *nxtSuf, *cur;
22
23
24
   int text[N];
25
26
   int remCnt, curP, curLen;
27
28
   void init() {
     top = 0, pos = -1, remCnt = 0, curP = 0, curLen = 0;
29
30
     nxtSuf = NULL;
     root = cur = new(pool + (top++)) Node(-1, -1);
31
32
33
   void link(Node *u) {
34
     if (nxtSuf) {
35
36
       nxtSuf->suf = u;
37
38
     nxtSuf = u;
39
40
   bool walk(Node *u) {
     int len = u->len();
42
     if (curLen >= len) {
43
       curP += len;
```

```
curLen -= len;
                                                                                                     nxtSuf = NULL:
45
                                                                                               90
                                                                                                     for (int i = 0; i < top; ++i) {
46
       cur = u;
                                                                                               91
       return true;
                                                                                               92
                                                                                                      if (pool[i].r == INF) {
47
48
                                                                                               93
                                                                                                        link(pool + i);
     return false;
                                                                                                      }
49
                                                                                               94
50
                                                                                               95
                                                                                                    while (remCnt > 0) {
                                                                                               96
51
   void extend(int c) {
                                                                                                      if (curLen) {
                                                                                               97
52
     text[++pos] = c;
                                                                                                        int curE = text[curP];
53
                                                                                               98
     nxtSuf = NULL;
                                                                                               99
                                                                                                        Node *nxt = cur->ch[curE];
54
     ++remCnt;
                                                                                                        if (walk(nxt)) {
                                                                                              100
55
56
     while (remCnt) {
                                                                                                          continue;
                                                                                              101
       curP = curLen ? curP : pos;
                                                                                              102
                                                                                                        }
57
58
                                                                                                        Node *split = new(pool + (top++)) Node(nxt->1, nxt->1 + curLen);
       int curE = text[curP];
                                                                                              103
       if (!cur->ch[curE]) {
                                                                                              104
                                                                                                        cur->ch[curE] = split;
59
60
         cur->ch[curE] = new(pool + (top++)) Node(pos);
                                                                                                        nxt->1 += curLen;
                                                                                              105
61
         link(cur);
                                                                                                        split->ch[text[nxt->1]] = nxt;
                                                                                              106
62
       } else {
                                                                                                        link(split);
                                                                                              107
63
         Node *nxt = cur->ch[curE];
                                                                                                      } else {
                                                                                              108
         if (walk(nxt)) {
                                                                                                        link(cur);
64
                                                                                              109
65
           continue;
                                                                                                      }
                                                                                             110
66
                                                                                              111
                                                                                                       --remCnt;
         if (text[nxt->l + curLen] == c) {
                                                                                                      if (cur == root && curLen > 0) {
67
                                                                                             112
68
           ++curLen;
                                                                                              113
                                                                                                         --curLen;
           link(cur);
                                                                                                        curP = pos - remCnt + 1;
69
                                                                                              114
           break;
70
                                                                                              115
                                                                                                      } else {
                                                                                             116
                                                                                                         cur = cur->suf ? cur->suf : root;
71
         Node *split = new(pool + (top++)) Node(nxt->1, nxt->1 + curLen);
                                                                                                      }
72
                                                                                              117
         cur->ch[curE] = split;
                                                                                             118
73
         split->ch[c] = new(pool + (top++)) Node(pos);
                                                                                                    if (nxtSuf != root) {
74
                                                                                              119
         nxt->1 += curLen;
                                                                                                      link(root);
75
                                                                                              120
76
         split->ch[text[nxt->1]] = nxt;
                                                                                              121
         link(split);
77
                                                                                              122
78
       }
                                                                                              123
       --remCnt;
                                                                                                  int buf[N];
79
                                                                                              124
       if (cur == root && curLen > 0) {
80
                                                                                              125
81
         --curLen;
                                                                                              126
                                                                                                  struct Walker {
82
         curP = pos - remCnt + 1;
                                                                                                    Node *cur, *root;
                                                                                              127
83
                                                                                                    int curP, curLen, pos, totLen;
       } else {
                                                                                              128
84
          cur = cur->suf ? cur->suf : root;
                                                                                              129
                                                                                                    Walker(Node* root) : root(root) {
85
                                                                                              130
86
                                                                                             131
                                                                                                      cur = root;
87
                                                                                              132
                                                                                                      curP = -1;
88
                                                                                                       curLen = 0;
                                                                                              133
8g | void finish() {
                                                                                                      totLen = 0;
                                                                                              134
```

```
pos = -1;
135
136
      }
137
138
      void descend() {
        while (curLen > 0) {
139
          Node *nxt = cur->ch[buf[curP]];
140
          int len = nxt->len();
141
          if (curLen >= len) {
142
            curP += len;
143
            curLen -= len;
144
            cur = nxt;
145
146
          } else {
            break;
147
148
          }
149
150
151
      void walk(int c) {
152
        buf[++pos] = c;
153
        while (curLen) {
154
          Node *nxt = cur->ch[buf[curP]];
155
          if (nxt->l + curLen <= ::pos && text[nxt->l + curLen] == c) {
156
            ++totLen;
157
158
            ++curLen;
            break;
159
160
          } else {
161
            --totLen;
            if (cur == root && curLen > 0) {
162
163
              --curLen;
164
              curP = pos - curLen;
165
            } else {
166
              cur = cur->suf;
167
            }
168
            descend();
169
170
        if (curLen == 0) {
171
          curP = pos;
172
          int curE = buf[curP];
173
          while (cur && !cur->ch[curE]) {
174
175
            --totLen;
176
            cur = cur->suf;
          }
177
178
          if (cur) {
            ++totLen;
179
```

后缀树 (With Pop Front)

```
1 int pos;
   int text[N];
   struct Node {
     int 1, r;
     Node *suf, *ch[C];
10
     int dgr;
11
     Node *fa;
12
13
     Node (int l = -1, int r = INF) : l(1), r(r) {
14
15
       suf = fa = NULL;
16
       memset(ch, 0, sizeof(ch));
       dgr = 0;
17
18
19
20
     Node* addEdge(Node *t) {
       int c = text[t->1];
21
22
       dgr += !ch[c];
       ch[c] = t;
23
       t->fa = this;
24
       return t;
25
26
27
28
     int len() {
       return min(r, pos + 1) - 1;
29
30
31
   };
32
   int top;
33
34
```

```
35 \mid Node pool[N << 1];
36
   Node *root, *nxtSuf, *cur;
37
38
   int remCnt, curP, curLen;
39
40
   long long size;
41
42
43
   queue<Node*> leaves;
44
   void init() {
45
      top = 0, pos = -1;
46
      remCnt = 0, curP = 0, curLen = 0;
47
48
      nxtSuf = NULL;
      root = cur = new(pool + (top++)) Node(-1, -1);
49
      size = 0;
50
      while (leaves.size()) {
51
       leaves.pop();
52
53
54
55
   void link(Node *u) {
56
     if (nxtSuf) {
57
58
        nxtSuf->suf = u;
59
60
      nxtSuf = u;
61
62
63
   bool walk(Node *u) {
64
      int len = u->len();
65
     if (curLen >= len) {
66
        curP += len;
67
        curLen -= len;
68
        cur = u;
69
        return true;
70
     return false;
71
72
73
   void extend(int c) {
74
      text[++pos] = c;
75
76
      nxtSuf = NULL;
      ++remCnt;
77
78
      while (remCnt) {
        curP = curLen ? curP : pos;
79
```

```
80
         int curE = text[curP];
 81
         if (!cur->ch[curE]) {
 82
          leaves.push(cur->addEdge(new(pool + (top++)) Node(pos)));
 83
          link(cur);
 84
        } else {
 85
          Node *nxt = cur->ch[curE];
 86
          if (walk(nxt)) {
 87
             continue;
 88
          }
 89
          if (text[nxt->l + curLen] == c) {
            ++curLen;
 90
            link(cur);
 91
            break;
 92
 93
          Node *split = new(pool + (top++)) Node(nxt->1, nxt->1 + curLen);
 94
          cur->addEdge(split);
 95
 96
          leaves.push(split->addEdge(new(pool + (top++)) Node(pos)));
          nxt->1 += curLen;
 97
          split->addEdge(nxt);
 98
          link(split);
 99
100
        }
101
         --remCnt;
        if (cur == root && curLen > 0) {
102
          curP = pos - (--curLen);
103
104
        } else {
           cur = cur->suf ? cur->suf : root;
105
        }
106
107
108
       size += leaves.size();
109
110
    void finish() {
111
       nxtSuf = NULL;
112
113
       for (int i = 0; i < top; ++i) {
        if (pool[i].r == INF) {
114
115
          link(pool + i);
116
        }
117
       while (remCnt > 0) {
118
        if (curLen) {
119
          int curE = text[curP];
120
          Node *nxt = cur->ch[curE];
121
          if (walk(nxt)) {
122
             continue;
123
124
          }
```

```
Node *split = new(pool + (top++)) Node(nxt->1, nxt->1 + curlen);
                                                                                                          int curE = text[curP];
125
                                                                                               170
126
          leaves.push(cur->addEdge(split));
                                                                                                          if (!cur->ch[curE]) {
                                                                                               171
                                                                                                            Node *leaf = new(pool + (top++)) Node(pos - curlen + 1);
          nxt->1 += curLen;
127
                                                                                               172
128
          split->addEdge(nxt);
                                                                                               173
                                                                                                            leaves.push(cur->addEdge(leaf));
          link(split);
                                                                                                            size += leaf->len();
129
                                                                                               174
                                                                                                            --remCnt;
        } else {
                                                                                               175
130
          leaves.push(cur);
                                                                                                            if (cur == root && curLen > 0) {
131
                                                                                               176
132
          link(cur);
                                                                                               177
                                                                                                              curP = pos - (--curLen) + 1;
133
        }
                                                                                               178
                                                                                                           } else {
134
        --remCnt;
                                                                                               179
                                                                                                              cur = cur->suf ? cur->suf : root;
        if (cur == root && curLen > 0) {
                                                                                               180
135
136
          --curLen;
                                                                                               181
                                                                                                            while (curLen && walk(cur->ch[text[curP]])) {
          curP = pos - remCnt + 1;
                                                                                               182
                                                                                                              continue:
137
138
                                                                                               183
                                                                                                           }
        } else {
139
          cur = cur->suf ? cur->suf : root;
                                                                                               184
                                                                                                         }
        }
                                                                                               185
                                                                                                        }
140
                                                                                               186
141
      if (nxtSuf != root) {
                                                                                               187
142
        link(root);
                                                                                               188
143
                                                                                               189 int n;
144
145
                                                                                               190
146
                                                                                               191
                                                                                                   char s[N], buf[N];
    void eraseUp(Node *&u) {
                                                                                               192
147
148
      size -= u->len();
                                                                                                   int ord[N], stop, sord[N << 1];</pre>
                                                                                               193
      int ch = text[u->1];
149
                                                                                               194
      u = u \rightarrow fa;
                                                                                                    void dfs(Node *u) {
150
                                                                                               195
      u->ch[ch] = NULL;
                                                                                                      sord[u - pool] = stop++;
151
                                                                                               196
                                                                                                      for (int i = 0; i < C; ++i) {
152
      --(u->dgr);
                                                                                               197
                                                                                               198
                                                                                                       if (u->ch[i]) {
153 }
                                                                                                          dfs(u->ch[i]);
154
                                                                                               199
    void erase() {
                                                                                               200
                                                                                                        }
155
156
      Node *u = leaves.front();
                                                                                               201
      leaves.pop();
                                                                                               202
157
158
      while (u-)dgr == 0 \&\& u != cur) {
                                                                                               203
        eraseUp(u);
                                                                                                    void getOrd() {
159
                                                                                               204
      }
160
                                                                                               205
                                                                                                      init();
161
      if (u == cur) {
                                                                                               206
                                                                                                      for (int i = 0; i < n; ++i) {
162
        if (cur->dgr == 0 && curLen == 0) {
                                                                                                        extend(s[i] - 'a');
                                                                                               207
          int len = u->len();
163
                                                                                               208
          curLen = len:
164
                                                                                               209
                                                                                                      finish();
          curP = pos - len + 1;
165
                                                                                                      stop = 0;
166
          cur = cur->fa;
                                                                                               211
                                                                                                      dfs(root);
167
          eraseUp(u);
                                                                                                      int i = 0;
                                                                                               212
168
                                                                                               213
                                                                                                      while (leaves.size()) {
        if (curLen) {
                                                                                                        ord[i++] = sord[leaves.front() - pool];
169
                                                                                               214
```

```
215 leaves.pop();
216 }
217 }
```

字符串最小表示

```
std::string find(std::string s) {
   int i,j,k,l,N=s.length(); s+=s;
   for(i=0,j=1;j<N;){
      for(k=0;k<N&&s[i+k]==s[j+k];k++);
      if(k>=N) break;
      if(s[i+k]<s[j+k]) j+=k+1;
      else l=i+k,i=j,j=max(l,j)+1;
   }
   return s.substr(i,N);
}</pre>
```

轻重链剖分

```
1 | struct Tree(){}*root[N];
2 int father[N],size[N],depth[N];
3 int bfsOrd[N],pathId[N],ordInPath[N],sqn[N];
   void doBfs(int s){
     int qh=0,qt=0,*que=bfsOrd; father[s]=-1; depth[s]=0;
     for(que[qt++]=s;qh<qt;){</pre>
7
       int u=que[qh++];
8
       foreach(iter,adj[u]){
9
         int v=*iter; if(v==father[u]) continue;
         father[v]=u; depth[v]=depth[u]+1; que[qt++]=v;
10
11
       }
12
13
   void doSplit(){
14
     for(int i=N-1;i>=0;--i){
15
16
       int u=bfsOrd[i]; size[u]=1;
       foreach(iter,adj[u]){
17
18
         int v=*iter; if(v==father[u]) continue; size[u]+=size[v];
       }
19
20
     memset(pathId,-1,sizeof pathId);
21
     for(int i=0;i<N;++i){</pre>
22
       int top=bfsOrd[i],cnt=0;
23
24
       if(pathId[top]!=-1) continue;
       for(int next,u=top;u!=-1;u=next){
25
26
         sqn[cnt]=val[u]; ordInPath[u]=cnt; pathId[u]=top; ++cnt;
27
         next=-1;
28
         foreach(iter,adj[u]){
```

```
int v=*iter; if(v==father[u]) continue;
if(next<0||size[next]<size[v]) next=v;
}

root[top]=new Tree(0,cnt,sqn);
}

void prepare(){ doBfs(0); doSplit(); }</pre>
```

KD Tree

```
#include <cstdio>
  #include <vector>
   #include <iostream>
   #include <algorithm>
   using namespace std;
7 \mid // 带插入版本 ,没有写内存回收 ,空间复杂度 n \log n ,如果不需要插入可以大大简化
8 // N 为最大点数, D 为每个点的最大维度, d 为实际维度
  │// 以查找最近点为例 ret 为当前最近点的距离的平方 , 用来剪枝 , 查询 k 近或 k 远的方法类似
   // 使用时注意先 initNull
10
  const long long INF = (int)1e9 + 10;
12
  const int N = 2000000 + 10;
   const int D = 5;
13
14
   const double SCALE = 0.75;
   struct Point { int x[D]; } buf[N];
15
16 int d;
   struct Node {
17
18
    int depth, size;
19
     Node *ch[2], *p;
     Point val, maxv, minv;
20
     void set(Node *t, int d) { ch[d] = t; t->p = this; }
21
     bool dir() { return this == p->ch[1]; }
22
     bool balanced() {
23
      return (double)max(ch[0]->size, ch[1]->size) <= (double)size * SCALE;
24
25
26
     void update() {
       size = ch[0] -> size + ch[1] -> size + 1;
27
28
       for(int i = 0; i < d; ++ i) {
        \max v.x[i] = \max(val.x[i], \max(ch[0]->\max v.x[i], ch[1]->\max v.x[i]));
29
30
        minv.x[i] = min(val.x[i], min(ch[0]->minv.x[i], ch[1]->minv.x[i]));
31
32
   } nodePool[N], *totNode, *null;
34 | Node* newNode(Point p, int depth) {
```

```
Node *t = totNode ++:
                                                                                                80
                                                                                                        int dir = 0:
35
                                                                                                81
                                                                                                        for( ; cur != null; ) {
36
     t - ch[0] = t - ch[1] = t - p = null;
     t->depth = depth;
                                                                                                82
                                                                                                          last = cur:
37
38
     t-val = t-maxv = t-minv = p;
                                                                                                 83
                                                                                                          dir = (p.x[cur->depth] > cur->val.x[cur->depth]);
     t \rightarrow size = 1;
                                                                                                84
                                                                                                          cur = cur->ch[dir];
39
     return t;
                                                                                                85
40
41 | }
                                                                                                86
                                                                                                        Node *t = newNode(p, (last->depth + 1) % d), *bad = null;
42 long long ret;
                                                                                                87
                                                                                                        last->set(t, dir);
                                                                                                 88
43
   int ctr;
                                                                                                        for( ; t != null; t = t->p) {
   int cmp(const Point &a, const Point &b) { return a.x[ctr] < b.x[ctr]; }</pre>
                                                                                                89
                                                                                                          t->update();
   struct KDTree {
                                                                                                          if (!t->balanced()) bad = t;
                                                                                                90
     Node *root;
                                                                                                        }
46
                                                                                                91
     KDTree() { root = null; }
                                                                                                        if (bad != null) rebuild(bad);
                                                                                                92
47
     KDTree(Point *a, int n) {
48
                                                                                                93
       root = build(a, 0, n - 1, 0);
                                                                                                      long long calcEval(Point u, Node *t, int d) {
49
                                                                                                94
     }
                                                                                                        long long l = t \rightarrow minv.x[d], r = t \rightarrow maxv.x[d], x = u.x[d];
                                                                                                95
50
     Node *build(Point *a, int l, int r, int depth) {
                                                                                                        if (x >= 1 && x <= r) return 0LL;
                                                                                                 96
51
       if (1 > r) return null;
                                                                                                        long long ret = min(abs(x - 1), abs(x - r));
52
                                                                                                97
       ctr = depth;
                                                                                                98
                                                                                                        return ret * ret;
53
       sort(a + 1, a + r + 1, cmp);
                                                                                                99
54
       int mid = (1 + r) >> 1;
                                                                                               100
                                                                                                      void updateAns(Point u, Point p) {
55
                                                                                                        // 在这里更新答案
56
       Node *t = newNode(a[mid], depth);
                                                                                               101
       t->set(build(a, 1, mid - 1, (depth + 1) % d), 0);
                                                                                               102
57
58
       t->set(build(a, mid + 1, r, (depth + 1) % d), 1);
                                                                                                      void query(Node *t, Point p) {
                                                                                               103
                                                                                                        if (t == null) return;
59
       t->update();
                                                                                               104
60
       return t;
                                                                                                        updateAns(t->val, p);
                                                                                               105
61
                                                                                                        long long evalLeft = calcEval(p, t->ch[0], t->depth);
                                                                                               106
62
      void tranverse(Node *t, Point *vec, int &tot) {
                                                                                                        long long evalRight = calcEval(p, t->ch[1], t->depth);
                                                                                               107
63
       if (t == null) return;
                                                                                               108
                                                                                                        if (evalLeft <= evalRight) {</pre>
64
       vec[tot ++] = t->val;
                                                                                                          query(t->ch[0], p);
                                                                                               109
65
       tranverse(t->ch[0], vec, tot);
                                                                                                          if (ret > evalRight) query(t->ch[1], p);
                                                                                               110
66
       tranverse(t->ch[1], vec, tot);
                                                                                               111
                                                                                                        } else {
67
                                                                                               112
                                                                                                          query(t->ch[1], p);
68
                                                                                                          if (ret > evalLeft) query(t->ch[0], p);
      void rebuild(Node *t) {
                                                                                               113
69
       Node *p = t \rightarrow p;
                                                                                                        }
                                                                                               114
70
       int tot = 0;
                                                                                               115
       tranverse(t, buf, tot);
                                                                                                      void query(Point p) {
71
                                                                                               116
       Node *u = build(buf, 0, tot - 1, t->depth);
                                                                                                        query(root, p);
7^2
                                                                                               117
       p->set(u, t->dir());
                                                                                               118
73
       for( ; p != null; p = p->p) p->update();
                                                                                               119 };
74
75
       if (t == root) root = u;
                                                                                                    void initNull() {
76
                                                                                                      totNode = nodePool;
                                                                                                      null = totNode ++;
      void insert(Point p) {
77
78
                                                                                                      null->size = 0;
       if (root == null) { root = newNode(p, 0); return; }
                                                                                               123
       Node *cur = root, *last = null;
                                                                                                      for(int i = 0; i < d; ++ i) {
79
                                                                                               124
```

```
125     null->maxv.x[i] = -INF;
126     null->minv.x[i] = INF;
127     }
128 }
```

Splay Tree

```
1 // 注意初始化内存池和 null 节点
   struct Node{
     int rev, size; Node *ch[2], *p;
 3
     void set(Node*,int); int dir(); void update(); void relax(); void appRev();
   } nodePool[MAX_NODE],*curNode,*null;
 6 | Node *newNode(){
     Node *t=curNode++; t->rev=0, t->size=1;
     t->ch[0]=t->ch[1]=t->p=null; return t;
 9
10 struct Splay{
     Node *root;
11
     Splay(){ root=newNode(); root->set(newNode(),0); root->update(); }
12
     void rot(Node *t){
13
       Node *p=t->p; int d=t->dir();
14
       p->relax(); t->relax();
15
16
       if(p==root) root=t;
       p->set(t->ch[!d],d); p->p->set(t,p->dir()); t->set(p,!d);
17
18
       p->update();
19
     void splay(Node *t,Node *f=null){
20
       for(t->relax();t->p!=f;)
21
22
         if(t->p->p==f) rot(t);
         else t->dir()==t->p->dir()?(rot(t->p),rot(t)):(rot(t),rot(t));
23
       t->update();
24
25
26
   void initNull(){ curNode=nodePool;null=curNode++;null->size=0; }
   void Node::set(Node *t,int _d){ ch[_d]=t; t->p=this; }
   int Node::dir(){ return this==p->ch[1]; }
29
   void Node::update(){ size=ch[0]->size+ch[1]->size+1;}
   void Node::relax(){ if(rev) ch[0]->appRev(), ch[1]->appRev(), rev=false; }
31
   void Node::appRev(){ if(this==null) return; rev^=true; swap(ch[0],ch[1]); }
```

Link Cut Tree

```
1 // 注意初始化 null 节点,单点的 is_root 初始为 true
2 struct Node{
3 Node *ch[2], *p;
4 int is_root, rev;
5 bool dir();
```

```
void set(Node*, bool);
     void update();
     void relax();
     void app rev();
     *null;
10
   void rot(Node *t){
11
     Node *p=t->p; bool d=t->dir();
12
     p->relax(); t->relax(); p->set(t->ch[!d],d);
13
14
     if(p->is_root) t->p=p->p,swap(p->is_root,t->is_root);
     else p->p->set(t,p->dir());
15
16
     t->set(p,!d); p->update();
17
   void splay(Node *t){
18
19
     for(t->relax();!t->is_root;)
       if(t->p->is_root) rot(t);
20
       else t->dir()==t->p->dir() ?(rot(t->p),rot(t)) :(rot(t),rot(t));
^{21}
     t->update();
22
23
   void access(Node *t){
24
25
     for(Node *s=null; t!=null; s=t,t=t->p){
26
       splay(t);
       if (t->p == null) { /*TODO*/ }
27
28
       t->ch[1]->is root=true; s->is root=false;
       t->ch[1]=s; t->update();
29
30
31
   bool Node::dir(){ return this==p->ch[1]; }
   void Node::set(Node *t,bool _d){ ch[_d]=t; t->p=this; }
   void Node::update(){ }
   void Node::app_rev(){ if (this == null) return; rev ^= true; swap(ch[0], ch[1]); }
35
   void Node::relax() { if(this==null) return; if (rev) { ch[0]->app_rev();
     37 | void make_root(Node *u) { access(u); splay(u); u->app_rev(); }
```

Dominator Tree

```
vector<int> prec[N], succ[N];

vector<int> ord;

int stamp, vis[N];

int num[N];

int fa[N];
```

```
10
   void dfs(int u) {
11
      vis[u] = stamp;
12
13
      num[u] = ord.size();
      ord.push_back(u);
14
      for (int i = 0; i < (int)succ[u].size(); ++i) {</pre>
15
16
        int v = succ[u][i];
        if (vis[v] != stamp) {
17
18
         fa[v] = u;
          dfs(v);
19
20
^{21}
22
23
   int fs[N], mins[N];
24
25
26
   int dom[N], sem[N];
27
28
   int find(int u) {
29
      if (u != fs[u]) {
        int v = fs[u];
30
        fs[u] = find(fs[u]);
31
        if (mins[v] != -1 && num[sem[mins[v]]] < num[sem[mins[u]]]) {</pre>
32
          mins[u] = mins[v];
33
34
35
36
      return fs[u];
37
38
39
   void merge(int u, int v) {
      fs[u] = v;
40
41
   }
4^2
   vector<int> buf[N];
43
44
   int buf2[N];
45
46
   void mark(int source) {
47
48
      ord.clear();
      ++stamp;
49
      dfs(source);
50
      for (int i = 0; i < (int)ord.size(); ++i) {</pre>
51
        int u = ord[i];
52
        fs[u] = u;
53
        mins[u] = -1;
54
```

```
buf2[u] = -1;
55
56
     for (int i = (int)ord.size() - 1; i > 0; --i) {
57
58
       int u = ord[i], p = fa[u];
       sem[u] = p;
59
60
        for (int j = 0; j < (int)prec[u].size(); ++j) {</pre>
61
         int v = prec[u][j];
62
         if (use[v] != stamp) {
63
            continue;
64
65
         if (num[v] > num[u]) {
66
            find(v);
            v = sem[mins[v]];
67
68
69
         if (num[v] < num[sem[u]]) {</pre>
            sem[u] = v;
70
         }
7^{1}
72
        buf[sem[u]].push_back(u);
73
        mins[u] = u;
74
75
        merge(u, p);
76
        while (buf[p].size()) {
         int v = buf[p].back();
77
78
         buf[p].pop_back();
79
          find(v);
80
         if (sem[v] == sem[mins[v]]) {
            dom[v] = sem[v];
81
82
         } else {
83
            buf2[v] = mins[v];
84
85
       }
86
87
      dom[ord[0]] = ord[0];
88
      for (int i = 0; i < (int)ord.size(); ++i) {</pre>
       int u = ord[i];
89
       if (~buf2[u]) {
90
          dom[u] = dom[buf2[u]];
91
92
93
94
```

DancingLinks

```
struct node{
node *left,*right,*up,*down,*col; int row,cnt;
}*head,*col[MAXC],Node[MAXNODE],*ans[MAXNODE];
```

```
4 | int totNode:
   void insert(const std::vector<int> &V,int rownum){
     std::vector<node*> N:
      for(int i=0;i<int(V.size());++i){</pre>
 8
       node* now=Node+(totNode++); now->row=rownum;
       now->col=now->up=col[V[i]], now->down=col[V[i]]->down;
 9
10
       now->up->down=now, now->down->up=now;
       now->col->cnt++; N.push back(now);
11
12
      for(int i=0;i<int(V.size());++i)</pre>
13
       N[i]->right=N[(i+1)%V.size()], N[i]->left=N[(i-1+V.size())%V.size()];
14
15 | }
16
   void Remove(node *x){
     x->left->right=x->right, x->right->left=x->left;
17
18
     for(node *i=x->down;i!=x;i=i->down)
        for(node *j=i->right;j!=i;j=j->right)
19
         j->up->down=j->down, j->down->up=j->up, --(j->col->cnt);
20
21
   void Resume(node *x){
22
      for(node *i=x->up;i!=x;i=i->up)
23
       for(node *j=i->left;j!=i;j=j->left)
24
         j->up->down=j->down->up=j, ++(j->col->cnt);
25
26
     x->left->right=x, x->right->left=x;
27
   bool search(int tot){
28
     if(head->right==head) return true;
29
     node *choose=NULL;
30
      for(node *i=head->right;i!=head;i=i->right){
31
       if(choose==NULL||choose->cnt>i->cnt) choose=i;
32
       if(choose->cnt<2) break;</pre>
33
34
     Remove(choose);
35
      for(node *i=choose->down;i!=choose;i=i->down){
36
        for(node *j=i->right;j!=i;j=j->right) Remove(j->col);
37
38
        ans[tot]=i;
39
       if(search(tot+1)) return true;
       ans[tot]=NULL;
40
       for(node *j=i->left;j!=i;j=j->left) Resume(j->col);
41
42
     Resume(choose):
43
     return false;
44
45
   void prepare(int totC){
     head=Node+totC;
47
     for(int i=0;i<totC;++i) col[i]=Node+i;</pre>
48
```

```
49     totNode=totC+1;
50     for(int i=0;i<=totC;++i){
51         (Node+i)->right=Node+(i+1)%(totC+1);
52         (Node+i)->left=Node+(i+totC)%(totC+1);
53         (Node+i)->up=(Node+i)->down=Node+i;
54     }
55 }
```

弦图相关

- 1. 团数 < 色数, 弦图团数 = 色数
- 2. 设 next(v) 表示 N(v) 中最前的点 . 令 w* 表示所有满足 $A\in B$ 的 w 中最后的一个点,判断 $v\cup N(v)$ 是否为极大团 ,只需判断是否存在一个 w,满足 Next(w)=v 且 $|N(v)|+1\le |N(w)|$ 即可 .
- 3. 最小染色: 完美消除序列从后往前依次给每个点染色,给每个点染上可以染的最小的颜色
- 4. 最大独立集: 完美消除序列从前往后能选就选
- 5. 弦图最大独立集数 = 最小团覆盖数 , 最小团覆盖 : 设最大独立集为 $\{p_1, p_2, \dots, p_t\}$, 则 $\{p_1 \cup N(p_1), \dots, p_t \cup N(p_t)\}$ 为最小团覆盖

图同构 Hash

$$F_t(i) = (F_{t-1}(i) \times A + \sum_{i \to j} F_{t-1}(j) \times B + \sum_{j \to i} F_{t-1}(j) \times C + D \times (i = a)) \mod P$$

枚举点 a 迭代 K 次后求得的就是 a 点所对应的 hash 值 其中 K , A , B , C , D , P 为 hash 参数 , 可自选

直线下有多少个格点

```
1 LL solve(LL n,LL a,LL b,LL m){
2    // 计算 for (int i=0;i<n;++i) s+=floor((a+b*i)/m)
3    //n,m,a,b>0
4    if(b==0) return n*(a/m);
5    if(a>=m) return n*(a/m)+solve(n,a%m,b,m);
6    if(b>=m) return (n-1)*n/2*(b/m)+solve(n,a,b%m,m);
7    return solve((a+b*n)/m,(a+b*n)%m,m,b);
8 }
```

费用流

```
1  // Q is a priority_queue<PII, vector<PII>, greater<PII>>
2  // for an edge(s, t): u is the capacity, v is the cost, nxt is the next edge,
3  // op is the opposite edge
4  // this code can not deal with negative cycles
5  typedef pair<int,int> PII;
6  struct edge{ int t,u,v; edge *nxt,*op; }E[MAXE],*V[MAXV];
7  int D[MAXN], dist[MAXN], maxflow, mincost; bool in[MAXN];
8  bool modlabel(){
```

```
while(!Q.empty()) Q.pop();
10
     for(int i=S;i<=T;++i){</pre>
       if(in[i]) D[i]=0,Q.push(PII(0,i));
11
12
       else D[i]=inf;
13
     while(!Q.empty()){
14
       int x=Q.top().first,y=Q.top().second;
15
16
       Q.pop();
       if(y==T) break;
17
18
       if(D[y]<x) continue;</pre>
        for(edge *ii=V[y];ii;ii=ii->nxt) if(ii->u){
19
         if(x+(ii->v+dist[ii->t]-dist[y])<D[ii->t]){
20
           D[ii->t]=x+(ii->v+dist[ii->t]-dist[y]);
21
           Q.push(PII(D[ii->t],ii->t));
22
         }
23
       }
24
25
26
     if(D[T]==inf) return false;
     for(int i=S;i<=T;++i) if(D[i]>D[T]) dist[i]+=D[T]-D[i];
27
     return true;
28
29
   int aug(int p,int limit){
30
     if(p==T) return maxflow+=limit,mincost+=limit*dist[S],limit;
     in[p]=1; int kk,ll=limit;
32
     for(edge *ii=V[p];ii;ii=ii->nxt) if(ii->u){
33
       if(!in[ii->t]&&dist[ii->t]+ii->v==dist[p]){
34
         kk=aug(ii->t,min(ii->u,ll));
35
         11-=kk,ii->u-=kk,ii->op->u+=kk;
36
         if(!ll) return in[p]=0,limit;
37
38
       }
39
     return limit-ll;
40
41
42 | PII mincostFlow(){
     for(int i=S;i<=T;++i) dist[i]=i==T?inf:0;</pre>
43
     while(!Q.empty()) Q.pop();
44
     Q.push(PII(0,T));
45
46
     while(!Q.empty()){
       int x=Q.top().first,y=Q.top().second;
47
48
       Q.pop();
       if(dist[y]<x) continue;</pre>
49
50
       for(edge *ii=V[y];ii;ii=ii->nxt) if(ii->op->u&ii->v+x<dist[ii->t]{
```

```
dist[ii->t]=ii->v+x;
51
         Q.push(PII(dist[ii->t],ii->t));
52
53
54
     }
     maxflow=mincost=0;
55
     do{
56
       do{
57
         memset(in,0,sizeof(in));
58
       }while(aug(S,maxflow));
59
60
     }while(modlabel());
61
     return PII(maxflow,mincost);
62 }
```

综合

定理 1: 最小覆盖数 = 最大匹配数 定理 2: 最大独立集 S 与 最小覆盖集 T 互补 复法:

- 1. 做最大匹配 . 没有匹配的空闲点 $\in S$
- 2. 如果 $u \in S$ 那么 u 的临点必然属于 T
- 3. 如果一对匹配的点中有一个属于 T 那么另外一个属于 S
- 4. 还不能确定的 . 把左子图的放入 S. 右子图放入 T

算法结束

上下界无源汇可行流 : 不用添 T->S, 判断是否流量平衡

上下界有源汇可行流 : 添 $T \to S$ (下界 0, 上界 ∞), 判断是否流量平衡

上下界最小流 : 不添 $T \to S$ 先流一遍 , 再添 $T \to S$ (下界 0 , 上界 ∞) 在残图上流一遍 , 答案为 $S \to T$ 的流量值

上下界最大流: 添 $T\to S$ (下界 0,上界 ∞)流一遍,再在残图上流一遍S到T的最大流,答案为前者的 $S\to T$ 的值 + 残图中 $S\to T$ 的最大流

```
Stirling 公式 n! = \sqrt{2\pi n} (\frac{n}{e})^n
```

Stirling 数

第一类:n 个元素的项目分作 k 个环排列的方法数目 $s(n,k)=(-1)^{n+k}|s(n,k)|$ |s(n,0)|=0,|s(1,1)|=1, |s(n,k)|=|s(n-1,k-1)|+(n-1)*|s(n-1,k)| 第二类:n 个元素的集定义 k 个等价类的方法数 S(n,1)=S(n,n)=1,S(n,k)=S(n-1,k-1)+k*S(n-1,k)

积分表

```
\int \frac{1}{1+x^2} dx = \tan^{-1} x \qquad \int \frac{1}{a^2+x^2} dx = \frac{1}{a} \tan^{-1} \frac{x}{a} \qquad \int \frac{x}{a^2+x^2} dx = \frac{1}{2} \ln|a^2+x^2| \qquad \int \frac{x^2}{a^2+x^2} dx = x - a \tan^{-1} \frac{x}{a} \qquad \int \frac{x^3}{a^2+x^2} dx = \frac{1}{2} x^2 - \frac{1}{2} a^2 \ln|a^2+x^2|
 Integrals of Rational Functions
Integrals with Roots  \int \frac{x}{\sqrt{x\pm a}} dx = \frac{2}{3} (x\mp 2a) \sqrt{x\pm a} \qquad \int \sqrt{\frac{x}{a-x}} dx = -\sqrt{x(a-x)} - a \tan^{-1} \frac{\sqrt{x(a-x)}}{x-a} \qquad \int \sqrt{\frac{x}{a+x}} dx = \sqrt{x(a+x)} - a \ln\left[\sqrt{x} + \sqrt{x+a}\right] \qquad \int x \sqrt{x^2 \pm a^2} dx = \frac{1}{3} \left(x^2 \pm a^2\right)^{3/2} 
\int x\sqrt{ax+b}dx = \frac{2}{15a^2}(-2b^2 + abx + 3a^2x^2)\sqrt{ax+b} \qquad \int \sqrt{x(ax+b)}dx = \frac{1}{4a^{3/2}}\left[(2ax+b)\sqrt{ax(ax+b)} - b^2\ln\left|a\sqrt{x} + \sqrt{a(ax+b)}\right|\right] \qquad \int \sqrt{x^2 \pm a^2}dx = \frac{1}{2}x\sqrt{x^2 \pm a^2} \pm \frac{1}{2}a^2\ln\left|x + \sqrt{x^2 \pm a^2}\right| + \frac{1}{2}a^2\ln\left|x + \sqrt{x^2
\int \sqrt{x^3(ax+b)}dx = \left[\frac{b}{12a} - \frac{b^2}{8a^2x} + \frac{x}{3}\right] \sqrt{x^3(ax+b)} + \frac{b^3}{8a^{5/2}} \ln\left|a\sqrt{x} + \sqrt{a(ax+b)}\right| \qquad \int \sqrt{a^2 - x^2}dx = \frac{1}{2}x\sqrt{a^2 - x^2} + \frac{1}{2}a^2 \tan^{-1}\frac{x}{\sqrt{a^2 - x^2}} \qquad \int \frac{x^2}{\sqrt{x^2 + a^2}}dx = \frac{1}{2}x\sqrt{x^2 \pm a^2} \mp \frac{1}{2}a^2 \ln\left|x + \sqrt{x^2 \pm a^2}\right| + \frac{1}{2}a^2 \ln
\int \frac{1}{\sqrt{x^2 + a^2}} dx = \ln \left| x + \sqrt{x^2 \pm a^2} \right| \int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1} \frac{x}{a} \int \frac{x}{\sqrt{x^2 \pm a^2}} dx = \sqrt{x^2 \pm a^2} \int \frac{x}{\sqrt{a^2 - x^2}} dx = -\sqrt{a^2 - x^2} \int \sqrt{ax^2 + bx + c} dx = \frac{b + 2ax}{4a} \sqrt{ax^2 + bx + c} + \frac{4ac - b^2}{8a^{3/2}} \ln \left| 2ax + b + 2\sqrt{a(ax^2 + bx + c)} \right| = -\sqrt{a^2 - x^2}
 \int x \sqrt{ax^2 + bx + c} = \frac{1}{48a^{5/2}} \left( 2\sqrt{a}\sqrt{ax^2 + bx + c} \right) \times \left( -3b^2 + 2abx + 8a(c + ax^2) \right) + 3(b^3 - 4abc) \ln \left| b + 2ax + 2\sqrt{a}\sqrt{ax^2 + bx + c} \right| 
\int \frac{1}{\sqrt{ax^2 + bx + c}} dx = \frac{1}{\sqrt{a}} \ln \left| 2ax + b + 2\sqrt{a(ax^2 + bx + c)} \right| 
\int \frac{x}{\sqrt{ax^2 + bx + c}} dx = \frac{1}{a} \sqrt{ax^2 + bx + c} - \frac{b}{2a^{3/2}} \ln \left| 2ax + b + 2\sqrt{a(ax^2 + bx + c)} \right| \qquad \int \frac{dx}{(a^2 + x^2)^{3/2}} = \frac{x}{a^2 \sqrt{a^2 + bx}} \qquad \text{Integrals with Logarithms} \qquad \int \ln(ax + b) dx = \left(x + \frac{b}{a}\right) \ln(ax + b) - x, a \neq 0
\int \frac{\ln ax}{x} dx = \frac{1}{2} (\ln ax)^2 \qquad \int \ln(x^2 + a^2) dx = x \ln(x^2 + a^2) + 2a \tan^{-1} \frac{x}{a} - 2x \qquad \int \ln(x^2 - a^2) dx = x \ln(x^2 - a^2) + a \ln \frac{x+a}{x-a} - 2x \qquad \int x \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{bx}{2a} + \frac{bx}{2a
\int \ln\left(ax^2 + bx + c\right) dx = \frac{1}{a}\sqrt{4ac - b^2} \tan^{-1} \frac{2ax + b}{\sqrt{4ac - b^2}} - 2x + \left(\frac{b}{2a} + x\right) \ln\left(ax^2 + bx + c\right)  \int x \ln\left(a^2 - b^2x^2\right) dx = -\frac{1}{2}x^2 + \frac{1}{2}\left(x^2 - \frac{a^2}{b^2}\right) \ln\left(a^2 - b^2x^2\right)
\int x^n e^{ax} \, \mathrm{d}x = \frac{x^n e^{ax}}{a} - \frac{n}{a} \int x^{n-1} e^{ax} \, \mathrm{d}x
\int x e^{-ax^2} \, \mathrm{d}x = -\frac{1}{2a} e^{-ax^2}
\int \cos^3 ax \, dx = \frac{3\sin ax}{4a} + \frac{\sin 3ax}{12a}
\int \cos ax \sin bx \, dx = \frac{\cos((a-b)x)}{2(a-b)} - \frac{\cos((a+b)x)}{2(a+b)}, a \neq b
\int \sin^2 ax \cos bx \, dx = -\frac{\sin((2a-b)x)}{4(2a-b)} + \frac{\sin bx}{2b} - \frac{\sin((2a+b)x)}{4(2a+b)}
\int \sin^2 x \cos x \, dx = \frac{1}{3} \sin^3 x
 \int \cos^2 ax \sin bx dx = \frac{\cos[(2a-b)x]}{4(2a-b)} - \frac{\cos bx}{2b} - \frac{\cos[(2a+b)x]}{4(2a+b)} \qquad \int \cos^2 ax \sin ax dx = -\frac{1}{3a} \cos^3 ax \qquad \int \sin^2 ax \cos^2 bx dx = \frac{x}{4} - \frac{\sin 2ax}{8a} - \frac{\sin[2(a-b)x]}{16(a-b)} + \frac{\sin 2bx}{8b} - \frac{\sin[2(a+b)x]}{16(a+b)} \qquad \int \sin^2 ax \cos^2 ax dx = \frac{x}{8} - \frac{\sin 4ax}{32a} + \frac{\sin 2bx}{32a} - \frac{\sin 2ax}{16(a+b)} + \frac{\sin 2bx}{32a} - \frac{\sin 2ax}{32a} - \frac{\sin 2ax}{32a} + \frac{\sin 2ax}{32a} - \frac{\sin 2ax}{32a} + \frac{\sin 2
 \int \tan ax dx = -\frac{1}{a} \ln \cos ax \qquad \int \tan^2 ax dx = -x + \frac{1}{a} \tan ax \qquad \int \tan^3 ax dx = \frac{1}{a} \ln \cos ax + \frac{1}{2a} \sec^2 ax \qquad \int \sec x dx = \ln |\sec x + \tan x| = 2 \tanh^{-1} \left(\tan \frac{x}{2}\right) \qquad \int \sec^2 ax dx = \frac{1}{a} \tan ax
\int \sec^3 x \, dx = \frac{1}{2} \sec x \tan x + \frac{1}{2} \ln|\sec x + \tan x|
\int \sec x \tan x dx = \sec x
\int \sec^2 x \tan x dx = \frac{1}{2} \sec^2 x
\int \sec^n x \tan x dx = \frac{1}{2} \sec^n x, n \neq 0
\int \csc x dx = \ln|\tan \frac{x}{2}| = \ln|\csc x - \cot x| + C
\int \csc^2 ax dx = -\frac{1}{a} \cot ax \int \csc^3 x dx = -\frac{1}{2} \cot x \csc x + \frac{1}{2} \ln|\csc x - \cot x| \int \csc^n x \cot x dx = -\frac{1}{n} \csc^n x, n \neq 0 \int \sec x \csc x dx = \ln|\tan x|  Products of Trigonometric Functions and Monomials
 \int x \cos x dx = \cos x + x \sin x \qquad \qquad \int x \cos ax dx = \frac{1}{a^2} \cos ax + \frac{x}{a} \sin ax \qquad \qquad \int x^2 \cos x dx = 2x \cos x + \left(x^2 - 2\right) \sin x \qquad \qquad \int x^2 \cos ax dx = \frac{2x \cos ax}{a^2} + \frac{a^2 x^2 - 2}{a^3} \sin ax \qquad \qquad \int x \sin x dx = -x \cos x + \sin x
 \int x \sin ax dx = -\frac{x \cos ax}{a} + \frac{\sin ax}{a^2} \qquad \int x^2 \sin x dx = \left(2 - x^2\right) \cos x + 2x \sin x \qquad \int x^2 \sin ax dx = \frac{2 - a^2 x^2}{a^3} \cos ax + \frac{2x \sin ax}{a^3}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Products of Trigonometric Functions and Exponentials
\int e^x \sin x dx = \frac{1}{2} e^x (\sin x - \cos x) \qquad \qquad \int e^{bx} \sin ax dx = \frac{1}{a^2 + b^2} e^{bx} (b \sin ax - a \cos ax) \qquad \qquad \int e^{bx} \cos ax dx = \frac{1}{a^2 + b^2} e^{bx} (a \sin ax + b \cos ax) \qquad \qquad \int x e^x \sin x dx = \frac{1}{2} e^x (\cos x - x \cos x + x \sin x)
   \int xe^x \cos x dx = \frac{1}{2}e^x (x \cos x - \sin x + x \sin x) \quad \int e^x \cos x dx = \frac{1}{2}e^x (\sin x + \cos x)
```

```
Java
```

```
import java.io.*;
   import java.util.*;
   import java.math.*;
   public class Main{
6
     BufferedReader reader = new BufferedReader(new InputStreamReader(System.in));
     PrintWriter writer = new PrintWriter(System.out);
8
     StringTokenizer tokenizer = null;
9
10
     void solve() throws Exception {
11
     void run()throws Exception{
12
13
       try{
```

```
while (true) {
14
15
           solve();
16
17
18
       catch(Exception e){
19
20
       finally{
21
         reader.close();
         writer.close();
22
23
24
     String next()throws Exception{
25
26
       for(;tokenizer == null || !tokenizer.hasMoreTokens();){
         tokenizer = new StringTokenizer(reader.readLine());
27
```

```
28
       return tokenizer.nextToken();
29
30
     int nextInt()throws Exception{
31
32
       return Integer.parseInt(next());
33
     double nextDouble()throws Exception{
34
       return Double.parseDouble(next());
35
36
     }
     BigInteger nextBigInteger()throws Exception{
37
       return new BigInteger(next());
38
     }
39
     public static void main(String args[])throws Exception{
40
       (new Main()).run();
41
42
    }
43 }
```

Vimrc

```
1 \begin{lstlisting}
2 set nu ai ci si mouse=a ts=4 sts=4 sw=4
   nmap<C-A> ggVG
   vmap<C-C> "+y
   nmap<F3> : vs %<.in <CR>
   nmap<F5> : !./%< <CR>
   nmap<F8> : !./%< < %<.in <CR>
10 nmap<F9> : !g++ % -o %< -Wall <CR>
11
   "nmap<F4> : !gedit % <CR>
12
   "autocmd BufNewFile *.cpp Or ~/temp.cpp
13
   "set hlsearch incseach
14
15
16 "syntax on
   "filetype plugin indent on
17
18 \end{lstlisting}
```