# Notes for ACMICPC World Finals 2013

# ACMICPC World Finals 2013 参考资料

Chinese Edition 中文版

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### 计算几何

```
line point make line(point a, point b){ //====两点求线
    line h; h.a=b.y-a.y; h.b=-(b.x-a.x); h.c=-a.x*b.y + a.y*b.x;
    return h;
//=======线段平移 D 的长度
line move d(line a,const double d){
 return (line){a.a,a.b,a.c+d*sqrt(a.a*a.a+a.b*a.b)};
int PointInPolygon(point cp, point a[], int n){
     int i , k , d1 , d2 ,wn=0; a[n]=a[0];
     rep(i,n){
        if ( PointOnSegment ( cp,a[i],a[i+1] ) ) return 2;
        k=cmp(area(a[i],a[i+1],cp));
        d1=cmp(a[i+0].y-cp.y); d2=cmp(a[i+1].y-cp.y);
        if (k>0 && d1<=0 && d2>0) wn++;
        if (k<0 && d2<=0 && d1>0) wn--:
} return wn!=0:}
void CircleCenter(point p0 , point p1 , point p2 , point &cp ){
    double a1=p1.x-p0.x , b1=p1.y-p0.y , c1=(sqr(a1)+sqr(b1)) / 2 ;
    double a2=p2.x-p0.x , b2=p2.y-p0.y , c2=(sqr(a2)+sqr(b2)) / 2 ;
    double d = a1*b2 - a2*b1;
    cp.x = p0.x + (c1*b2 - c2*b1) / d;
    cp.y = p0.y + (a1*c2 - a2*c1) / d;
}// 三角形内心
double Incenter(point A, point B, point C, point &cp ){
    double s, p, r, a, b, c;
   a = dis(B, C), b = dis(C, A), c = dis(A, B); p = (a + b + c) / 2;
   s = sqrt(p*(p-a)*(p-b)*(p-c)); r = s/p;
   cp.x = (a*A.x + b*B. x + c*C.x) / (a + b + c);
    cp.y = (a*A.y + b*B. y + c*C.y) / (a + b + c);
    return r ;
```

```
}// 三角形 垂心
void Orthocenter(point A, point B, point C, point &cp ){
    CircleCenter(A, B, C, cp );
    cp.x = A.x + B.x + C.x - 2 * cp.x ; cp.y = A.y + B.y + C.y - 2 * cp.y ;}
// 园外一点p0,半径为r, 直线ax+by+c=0 的交点
int CircleLine(point p0 , double r , double a , double b , double c , point
&cp1 , point &cp2 ) {
    double aa = a*a, bb = b*b, s = aa + bb;
    double d = r*r*s - sqr (a*p0.x+b*p0.y+c);
    if (d+eps<0) return 0; if (d<eps) d=0; else d=sqrt(d);</pre>
    double ab = a*b, bd = b*d, ad = a*d;
    double xx = bb*p0.x - ab*p0.v - a*c:
    double yy = aa*p0.y - ab*p0.x - b*c;
    cp2.x = (xx + bd) / s; cp2.y = (yy - ad) / s;
    cp1.x = (xx - bd) / s ; cp1.y = (yy + ad) / s ;
    if( d>eps ) return 2 ; else return 1 ;
}// 两园交线|P - P1| = r1 and |P - P2| = r2 of the ax + by + c = 0 form
void CommonAxis (point p1 , double r1 , point p2 , double r2 , double &a , double
&b , double &c ){
    double sx = p2.x + p1.x, mx = p2.x - p1.x;
    double sy = p2.y + p1.y, my = p2.y - p1.y;
    a = 2*mx; b = 2*my; c = -sx*mx - sy*my - (r1+r2)*(r1-r2);
}// 两园交点 两个圆不能共圆心,请特判
int CircleCrossCircle( point p1 , double r1 , point p2 , double r2 , point &cp1 ,
point &cp2 ){
    double mx = p2.x - p1.x, sx = p2.x+p1.x, mx2 = mx*mx;
    double my = p2.y - p1.y, sy = p2.y+p1.y, my2 = my*my;
    double sq = mx2 + my2, d = -(sq - sqr(r1-r2))*(sq - sqr(r1+r2));
    if (d+eps < 0) return 0; if (d<eps) d=0; else d = sqrt(d);
    double x = mx^* ( (r1+r2)^* (r1-r2) + mx^*sx ) + sx^*my2 ;
    double y = my^* ( (r1+r2)^* (r1-r2) + my^*sy ) + sy^*mx2 ;
    double dx = mx*d, dy = my*d; sq *= 2;
```

```
cp1.x = (x - dy) / sq ; cp1.y = (y + dx) / sq ;
                                                                               S += area2(ob, oc) * sign(det(ob, oc));
   cp2.x = (x + dy) / sq; cp2.y = (y - dx) / sq;
                                                                               S += area2(oc, oa) * sign(det(oc, oa)); return abs(S);
   if ( d>eps ) return 2 ; else return 1 ;
                                                                           }//=====半平面交
void rebuild(point a, point b){//逆时针,ab左侧
                                                                               int i,t;double k1,k2;sol[m]=sol[0]; t=0;
double twoCircleAreaUnion(point a, point b , double r1, double r2){
   if (r1+r2<=(a-b).dist()) return 0;</pre>
                                                                               foru(i,1,m){ k1=area(a,b,sol[i]); k2=area(a,b,sol[i-1]);
   if (r1+(a-b).dist()<=r2) return pi*r1*r1;
                                                                                if (cmp(k1)*cmp(k2)<0){
   if (r2+(a-b).dist()<=r1) return pi*r2*r2;
                                                                                     tmp[t].x=(sol[i].x*k2-sol[i-1].x*k1) / (k2-k1);
   double c1,c2 , ans=0;
                                                                                     tmp[t].y=(sol[i].y*k2-sol[i-1].y*k1) / (k2-k1); t++;
                                                                                 } if (cmp(area(a,b,sol[i])) >=0){ tmp[t]=sol[i]; t++;}}
   c1=(r1*r1-r2*r2+(a-b).dis())/(a-b).dist()/r1/2.0;
   c2=(r2*r2-r1*r1+(a-b).dis())/(a-b).dist()/r2/2.0;
                                                                               m=t; rep(i,m) sol[i]=tmp[i];
   double s1,s2; s1=acos(c1); s2=acos(c2);
                                                                           }//====nlogn半平面交
   ans+=s1*r1*r1-r1*r1*sin(s1)*cos(s1);
                                                                           bool check(const Plane &u, const Plane &v, const Plane &w) {
   ans+=s2*r2*r2-r2*r2*sin(s2)*cos(s2);
                                                                               return intersect(u, v).in(w);
   return ans;
                                                                           }
}//====多边形和圆相交的面积用有向面积,划分成一个三角形和圆的面积的交
                                                                           void build(vector <Plane> planes) {
double area2(point pa, point pb) {
                                                                               int head = 0, tail = 0;
   if (pa.len() < pb.len()) swap(pa, pb); if (pb.len() < eps) return 0;</pre>
                                                                               for (int i = 0; i < (int)planes.size(); ++ i) {</pre>
                                                                                  while (tail - head > 1 && !check(queue[tail - 2], queue[tail - 1],
   double a, b, c, B, C, sinB, cosB, sinC, cosC, S, h, theta;
                                                                           planes[i])) {
   a = pb.len(); b = pa.len(); c = (pb-pa).len();
   cosB=dot(pb,pb-pa)/a/c; sinB=fabs(det(pb,pb-pa)/a/c);
                                                                                      tail --;
   cosC=dot(pa, pb) / a / b; sinC=fabs(det(pa,pb)/a/b);
   B=atan2(sinB , cosB); C=atan2(sinC, cosC);
                                                                                  while (tail - head > 1 && !check(queue[head + 1], queue[head], planes[i]))
   if (a > r) { S = C/2*r*r; h = a*b*sinC/c;
                                                                           {
        if (h < r \& B < PI/2) S -= (acos(h/r)*r*r - h*sqrt(r*r-h*h));
                                                                                      head ++;
   else if (b > r) { theta = PI - B - asin(sinB/r*a);
                                                                                  queue[tail ++] = planes[i];
        S = .5*a*r*sin(theta) + (C-theta)/2*r*r;
   else S = .5*sinC*a*b; return S; }// a, b, c, r fixed
                                                                               while (tail - head > 2 && !check(queue[tail - 2], queue[tail - 1],
double area(const point &o) {
                                                                           queue[head])) {
   double S = 0; point oa = a-o, ob = b-o, oc = c-o;
                                                                                  tail --:
   S += area2(oa, ob) * sign(det(oa, ob));
                                                                               }
```

```
while (tail - head > 2 && !check(queue[head + 1], queue[head], queue[tail
                                                                              }
                                                                               //check一个点是否在三角形里(exclusive)
- 1])) {
       head ++;
                                                                               int dot inplane ex(point3 p,plane3 s)
   }
                                                                               int dot inplane ex(point3 p,point3 s1,point3 s2,point3 s3){
                                                                                   return dot_inplane_in(p,s1,s2,s3)&&vlen(det(p-s1,p-s2))>eps&&
三维几何
                                                                                       vlen(det(p-s2,p-s3))>eps&&vlen(det(p-s3,p-s1))>eps;
//vlen(point3 P):length of vector; zero(double x):if fabs(x)<eps) return true;</pre>
double vlen(point3 p);
                                                                               //check if two point and a segment in one plane have the same side
//平面法向量
                                                                               int same side(point3 p1,point3 p2,point3 l1,point3 l2)
point3 pvec(point3 s1,point3 s2,point3 s3){return det((s1-s2),(s2-s3));}
                                                                               int same side(point3 p1,point3 p2,line3 l){
//check共线
                                                                                   return dot(det(1.a-1.b,p1-1.b),det(1.a-1.b,p2-1.b))>eps;
int dots inline(point3 p1,point3 p2,point3 p3){
                                                                               }
    return vlen(det(p1-p2,p2-p3))<eps;}</pre>
                                                                               //check if two point and a segment in one plane have the opposite side
//check共平面
                                                                               int opposite side(point3 p1,point3 p2,point3 l1,point3 l2)
int dots onplane(point3 a,point3 b,point3 c,point3 d){
                                                                               int opposite side(point3 p1,point3 p2,line3 l){
    return zero(dot(pvec(a,b,c),d-a));}
                                                                                   return dot(det(1.a-1.b,p1-1.b), det(1.a-1.b,p2-1.b))<-eps;
//check在线段上(end point inclusive)
int dot online in(point3 p,line3 1)
                                                                               //check if two point is on the same side of a plane
    int dot online in(point3 p,point3 l1,point3 l2){return
                                                                               int same side(point3 p1,point3 p2,point3 s1,point3 s2,point3 s3)
    zero(vlen(det(p-11,p-12)))&(11.x-p.x)*(12.x-p.x)<eps&(11.y-p.y)*(12.x-p.x)
                                                                               int same side(point3 p1,point3 p2,plane3 s){
    y-p.y)<eps&&(11.z-p.z)*(12.z-p.z)<eps;}
                                                                                   return dot(pvec(s),p1-s.a)*dot(pvec(s),p2-s.a)>eps;
//check在线段上(end point exclusive)
                                                                              }
                                                                               //check if two point is on the opposite side of a plane
int dot_online_ex(point3 p,line3 1)
int dot online ex(point3 p,point3 l1,point3 l2){ return
                                                                               int opposite side(point3 p1,point3 p2,point3 s1,point3 s2,point3 s3)
    dot online in(p,11,12)\&\&(!zero(p.x-11.x)||!zero(p.y-11.y)||!zero(p.z-
                                                                               int opposite side(point3 p1,point3 p2,plane3 s){
    11.z) &&(!zero(p.x-12.x)||!zero(p.y-12.y)||!zero(p.z-12.z));
                                                                                   return dot(pvec(s),p1-s.a)*dot(pvec(s),p2-s.a)<-eps;</pre>
                                                                              }
//check一个点是否在三角形里(inclusive)
                                                                               //check if two straight line is parallel
int dot inplane in(point3 p,plane3 s)
                                                                               int parallel(point3 u1,point3 u2,point3 v1,point3 v2)
int dot_inplane_in(point3 p,point3 s1,point3 s2,point3 s3){
                                                                               int parallel(line3 u,line3 v){     return vlen(det(u.a-u.b,v.a-v.b))<eps; }</pre>
    return zero(vlen(det(s1-s2,s1-s3))-vlen(det(p-s1,p-s2))-
                                                                              //check if two plane is parallel
        vlen(det(p-s2,p-s3))-vlen(det(p-s3,p-s1)));
                                                                               int parallel(point3 u1,point3 u2,point3 u3,point3 v1,point3 v2,point3 v3)
```

```
int parallel(plane3 u,plane3 v){return vlen(det(pvec(u),pvec(v)))<eps;}</pre>
                                                                                  return !same side(1.a,1.b,s)&&!same side(s.a,s.b,1.a,1.b,s.c)&&
//check if a plane and a line is parallel
                                                                                       !same side(s.b,s.c,l.a,l.b,s.a)&&!same side(s.c,s.a,l.a,l.b,s.b);
int parallel(point3 11,point3 12,point3 s1,point3 s2,point3 s3)
int parallel(line3 1,plane3 s){ return zero(dot(1.a-1.b,pvec(s))); }
                                                                              //check线段和三角形是否有交点(end point and border exclusive)
//check if two line is perpendicular
                                                                              int intersect_ex(point3 11,point3 12,point3 s1,point3 s2,point3 s3)
int perpendicular(point3 u1,point3 u2,point3 v1,point3 v2)
                                                                              int intersect ex(line3 l,plane3 s){
int perpendicular(line3 u,line3 v){return zero(dot(u.a-u.b,v.a-v.b)); }
                                                                                  return opposite side(l.a,l.b,s)&&opposite side(s.a,s.b,l.a,l.b,s.c)&&
//check if two plane is perpendicular
                                                                                  opposite side(s.b,s.c,l.a,l.b,s.a)&&opposite side(s.c,s.a,l.a,l.b,s.b)
int perpendicular(point3 u1, point3 u2, point3 u3, point3 v1, point3 v2, point3 v3)
                                                                              ;}
                                                                              //calculate the intersection of two line
int perpendicular(plane3 u,plane3 v){ return zero(dot(pvec(u),pvec(v))); }
                                                                              //Must you should ensure they are co-plane and not parallel
//check if plane and line is perpendicular
                                                                              point3 intersection(point3 u1,point3 u2,point3 v1,point3 v2)
int perpendicular(point3 l1,point3 l2,point3 s1,point3 s2,point3 s3)
                                                                              point3 intersection(line3 u,line3 v){
int perpendicular(line3 1,plane3 s){return vlen(det(1.a-1.b,pvec(s)))<eps;}</pre>
                                                                                  point3 ret=u.a;
//check 两条线段是否有交点(end point inclusive)
                                                                                  double t=((u.a.x-v.a.x)*(v.a.y-v.b.y)-(u.a.y-v.a.y)*(v.a.x-v.b.x))
                                                                                           /((u.a.x-u.b.x)*(v.a.y-v.b.y)-(u.a.y-u.b.y)*(v.a.x-v.b.x));
int intersect in(point3 u1,point3 u2,point3 v1,point3 v2)
int intersect in(line3 u,line3 v){
                                                                                  ret+=(u.b-u.a)*t:
                                                                                                       return ret:
    if (!dots onplane(u.a,u.b,v.a,v.b)) return 0;
    if (!dots inline(u.a,u.b,v.a)||!dots inline(u.a,u.b,v.b))
                                                                              //calculate the intersection of plane and line
        return !same side(u.a,u.b,v)&&!same side(v.a,v.b,u);
                                                                              point3 intersection(point3 l1,point3 l2,point3 s1,point3 s2,point3 s3)
    return dot online in(u.a,v)||dot online in(u.b,v)||
                                                                              point3 intersection(line3 1,plane3 s){
            dot online in(v.a,u)||dot online in(v.b,u);
                                                                                  point3 ret=pvec(s);
                                                                              double t=(ret.x*(s.a.x-l.a.x)+ret.y*(s.a.y-l.a.y)+ret.z*(s.a.z-l.a.z))/
//check 两条线段是否有交点(end point exclusive)
                                                                                       (ret.x*(1.b.x-1.a.x)+ret.y*(1.b.y-1.a.y)+ret.z*(1.b.z-1.a.z));
                                                                                  ret=l.a + (l.b-l.a)*t; return ret;
int intersect ex(point3 u1,point3 u2,point3 v1,point3 v2)
int intersect ex(line3 u,line3 v){
    return dots onplane(u.a,u.b,v.a,v.b)&&opposite side(u.a,u.b,v)&&
                                                                              //calculate the intersection of two plane
            opposite side(v.a,v.b,u);
                                                                              bool intersection(plane3 pl1 , plane3 pl2 , line3 &li) {
                                                                                  if (parallel(pl1,pl2)) return false;
//check线段和三角形是否有交点(end point and border inclusive)
                                                                                  li.a=parallel(pl2.a,pl2.b, pl1) ? intersection(pl2.b,pl2.c,
int intersect in(point3 11,point3 12,point3 s1,point3 s2,point3 s3)
                                                                              pl1.a,pl1.b,pl1.c) : intersection(pl2.a,pl2.b, pl1.a,pl1.b,pl1.c);
int intersect in(line3 l,plane3 s){
                                                                                  point3 fa; fa=det(pvec(pl1),pvec(pl2)); li.b=li.a+fa; return true;
```

```
for(int i=0; i<4; i++)for(int j=0; j<4; j++){
//distance from point to line
                                                                                   c[i][j]=a[i][0]*b[0][j]; for(int k=1;k<4;k++) c[i][j]+=a[i][k]*b[k][j];
double ptoline(point3 p,point3 l1,point3 l2)
                                                                              }}
double ptoline(point3 p,line3 1){
                                                                               void multi(double a[4][4],const double b[4][4]){
    return vlen(det(p-1.a,1.b-1.a))/distance(1.a,1.b);}
                                                                                   static double c[4][4]; multi(a,b,c);memcpy(a,c,sizeof(a[0][0])*16);
//distance from point to plane
                                                                              }
double ptoplane(point3 p,plane3 s){
                                                                               void Macro(){
    return fabs(dot(pvec(s),p-s.a))/vlen(pvec(s));}
                                                                                   double b[4][4]={1, 0, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 0, 0, 1};
double ptoplane(point3 p,point3 s1,point3 s2,point3 s3)
                                                                                   memcpy(a,b,sizeof(a[0][0])*16);
//distance between two line
                                 当u,v平行时有问题
                                                                              }
double linetoline(line3 u,line3 v){
                                                                               void Translation(const Point 3 &s){
    point3 n=det(u.a-u.b,v.a-v.b); return fabs(dot(u.a-v.a,n))/vlen(n);
                                                                                   double p[4][4]={1, 0, 0, 0, 0, 1, 0, 0, 0, 1, 0, s.x, s.y, s.z, 1};
                                                                                   multi(a,p);
double linetoline(point3 u1,point3 u2,point3 v1,point3 v2)
                                                                               }
//cosine value of the angle formed by two lines
                                                                               void Scaling(const Point 3 &s){
double angle cos(line3 u,line3 v){
                                                                                   double p[4][4]={s.x, 0, 0, 0, 0, s.y, 0, 0, 0, s.z, 0, 0, 0, 0, 1};
    return dot(u.a-u.b, v.a-v.b)/vlen(u.a-u.b)/vlen(v.a-v.b);
                                                                                   multi(a,p);
double angle cos(point3 u1,point3 u2,point3 v1,point3 v2)
                                                                               void Rotate(const Point 3 &s, double r) {
//cosine value of the angle formed by two planes
                                                                                   double l=s.Length(); double x=s.x/l,y=s.y/l,z=s.z/l;
double angle cos(plane3 u,plane3 v){
                                                                                   double SinA=sin(r),CosA=cos(r);
    return dot(pvec(u),pvec(v))/vlen(pvec(u))/vlen(pvec(v));}
                                                                                   double p[4][4]=\{CosA + (1 - CosA) * x * x, (1 - CosA) * x * y - SinA * z,
                                                                               (1 - CosA) * x * z + SinA * y, 0, (1 - CosA) * y * x + SinA * z,
double angle cos(point3 u1, point3 u2, point3 u3, point3 v1, point3 v2, point3 v3)
//cosine value of the angle formed by plane and line
                                                                               CosA + (1 - CosA) * y * y, (1 - CosA) * y * z - SinA * x, 0,
                                                                               (1 - CosA) * z * x - SinA * y, (1 - CosA) * z * y + SinA * x, CosA + (1 - CosA)
double angle sin(line3 l,plane3 s){
    return dot(1.a-1.b,pvec(s))/vlen(1.a-1.b)/vlen(pvec(s));}
                                                                               * z * z, 0, 0, 0, 0, 1};
double angle sin(point3 11,point3 12,point3 s1,point3 s2,point3 s3)
                                                                                   multi(a,p);
三维几何操作合并
const double pi = acos(-1.0); double a[4][4];
                                                                               Point 3 opt(const Point 3&s){
int dcmp(const double &a, const double &b = 0, const double & zero = 1e-6){
                                                                                   double x,y,z;
   if (a - b < -zero) return -1; return a - b > zero;}
                                                                                   return Point 3( s.x * a[0][0] + s.y * a[1][0] + s.z * a[2][0] + a[3][0],
void multi(const double a[4][4],const double b[4][4],double c[4][4]){
                                                                                            s.x * a[0][1] + s.y * a[1][1] + s.z * a[2][1] + a[3][1],
```

```
s.x * a[0][2] + s.y * a[1][2] + s.z * a[2][2] + a[3][2]);
                                                                                 double dot(const Point &p) const { return x * p.x + y * p.y + z * p.z; }
                                                                                 double norm() {return dot(*this);} double length() {return Sqrt(norm());}
int main(){
                                                                             };
   Macro();
   int n; for (scanf("%d", &n); n; n--) {
                                                                             int mark[1005][1005];Point info[1005];int n, cnt;
        char c; Point 3 p;
                                                                             double mix(const Point &a, const Point &b, const Point &c) {
                                                                                 return a.dot(b.cross(c));}
        scanf("\n%c%lf%lf%lf", &c, &p.x, &p.y, &p.z);
        if (c == 'T') Translation(p); if (c == 'S') Scaling(p);
                                                                             double area(int a, int b, int c) {
        if (c == 'R') \{ double r; scanf("%lf\n", &r); \}
                                                                                 return ((info[b] - info[a]).cross(info[c] - info[a])).length();}
            Rotate(p, r); //=======绕OP逆时针旋转r角度
                                                                             double volume(int a, int b, int c, int d) {
   }}
                                                                                 return mix(info[b] - info[a], info[c] - info[a], info[d] - info[a]);}
   for (scanf("%d", &n); n; n--) {
                                                                             struct Face { int a, b, c; Face() {}
        Point 3 p, p2; scanf("%lf%lf%lf", &p.x, &p.y, &p.z);
                                                                                 Face(int a, int b, int c): a(a), b(b), c(c) {}
                        printf("%f %f %f\n",p2.x,p2.y,p2.z);
        p2 = opt(p);
                                                                             int &operator [](int k) {if (k == 0) return a; if (k == 1) return b; return
}}
                                                                             c; }};
三维旋转操作
                                                                             vector <Face> face;
//a点绕Ob向量,逆时针旋转弧度angle, sin(angle), cos(angle)先求出来,减少精度问题。
                                                                             inline void insert(int a, int b, int c) { face.push back(Face(a, b, c)); }
point e1,e2,e3; point Rotate( point a, point b, double angle ){
                                                                             void add(int v) {
    b.std();//单位化,注意b不能为(0,0,0)
                                                                                 vector <Face> tmp; int a, b, c; cnt ++;
                                                                                 for (int i = 0; i < SIZE(face); i ++) {</pre>
    e3=b; double lens=a*e3;//dot(a,e3)
   e1=a - e3*lens; if (e1.len()>(1e-8)) e1.std(); else return a;
                                                                                     a = face[i][0]; b = face[i][1]; c = face[i][2];
   e2=e1/e3; //det(e1,e3)
                                                                                     if (Sign(volume(v, a, b, c)) < 0)</pre>
    double x1,y1,x,y; y1=a*e1; x1=a*e2;
                                                                             mark[a][b]=mark[b][a]=mark[b][c] = mark[c][b] = mark[c][a] = mark[a][c] = cnt;
   x=x1*cos(angle) - y1*sin(angle); y=x1*sin(angle) + y1*cos(angle);
                                                                                     else tmp.push back(face[i]); }
    return e3*lens + e1*y + e2*x; }
                                                                                 face = tmp;
三维凸包随机增量
                                                                                 for (int i = 0; i < SIZE(tmp); i ++) {</pre>
struct Point { double x, y, z; Point() \{x = y = z = 0;\}
                                                                                     a = face[i][0]; b = face[i][1]; c = face[i][2];
   Point(double x, double y, double z): x(x), y(y), z(z) {}
                                                                                     if (mark[a][b] == cnt) insert(b, a, v);
                                                                                     if (mark[b][c] == cnt) insert(c, b, v);
   bool operator <(const Point &p) const {x,y,z}
   bool operator ==(const Point &p) const {}
                                                                                     if (mark[c][a] == cnt) insert(a, c, v);
   Point cross(const Point &p) const {
                                                                             }}
       return Point(y * p.z - z * p.y, z * p.x - x * p.z, x * p.y - y * p.x);}
                                                                             int Find() {
```

```
for (int i = 2; i < n; i ++) {
                                                                                    int i; rep(i,n) a[i+n]=a[i]; a[2*n]=a[0];
       Point ndir = (info[0] - info[i]).cross(info[1] - info[i]);
                                                                                    rep(i,n) { w[i]=calc(a[i],a[i+1]);w[i+n]=w[i];}
       if (ndir == Point()) continue;
                                                                               }
       swap(info[i], info[2]);
                                                                               int find(double k,int n , double w[]){
       for (int j = i + 1; j < n; j ++)
                                                                                    if (k<=w[0] | | k>w[n-1]) return 0; int l,r,mid; l=0; r=n-1;
           if (Sign(volume(0, 1, 2, j)) != 0) {
                                                                                    while (1 \leftarrow r) { mid=(1+r)/2; if (w[mid] >= k) r=mid-1; else 1=mid+1;
              swap(info[j], info[3]); insert(0, 1, 2); insert(0, 2, 1);
                                                                                    }return r+1;
              return 1;
                                                                               }
} }
      return 0;}
                                                                               int dic(const point &a, const point &b , int l ,int r , point c[]) {
int main() {
                                                                                    int s; if (area(a,b,c[1])<0) s=-1; else s=1; int mid;</pre>
   double ans, ret; int Case;
                                                                                    while (l<=r) {
   for (scanf("%d", &Case); Case; Case --) {
                                                                                        mid=(1+r)/2; if (area(a,b,c[mid])*s <= 0) r=mid-1; else l=mid+1;
       scanf("%d", &n); for (int i = 0; i < n; i ++) info[i].read();</pre>
                                                                                    }return r+1;
       sort(info, info + n); n = unique(info, info + n) - info;
                                                                               }
       face.clear(); random shuffle(info, info + n);
                                                                               point get(const point &a, const point &b, point s1, point s2) {
       ans = ret = 0; if (Find()) {
                                                                                    double k1,k2; point tmp; k1=area(a,b,s1); k2=area(a,b,s2);
           memset(mark, 0, sizeof(mark)); cnt = 0;
                                                                                    if (cmp(k1)==0) return s1; if (cmp(k2)==0) return s2;
           for (int i = 3; i < n; i ++) add(i);</pre>
                                                                                    tmp=(s1*k2 "C s2*k1) / (k2-k1); return tmp;
           int first = face[0][0];
           for (int i = 0; i < SIZE(face); i ++) {</pre>
                                                                               bool line cross convex(point a, point b ,point c[] , int n, point &cp1, point
             ret += area(face[i][0], face[i][1], face[i][2]);
                                                                               &cp2 , double w[]) {
             ans += fabs(volume(first, face[i][0], face[i][1], face[i][2]));
                                                                                   int i,j;
                                                                                   i=find(calc(a,b),n,w);
           } ans /= 6; ret /= 2; }
                                                                                    j=find(calc(b,a),n,w);
       printf("%.3f %.3f\n", ret, ans);
                                                                                    double k1,k2;
   } return 0; }
                                                                                    k1=area(a,b,c[i]); k2=area(a,b,c[j]);
直线和凸包交点(返回最近和最远点)
                                                                                    if (cmp(k1)*cmp(k2)>0) return false; //no cross
double calc(point a, point b){
                                                                                    if (cmp(k1)==0 \mid cmp(k2)==0) { //cross a point or a line in the convex
    double k=atan2(b.y-a.y , b.x-a.x);
                                                                                        if (cmp(k1)==0) {
                                        if (k<0) k+=2*pi;return k;
}//= the convex must compare y, then xf-a[0] is the lower-right point
                                                                                            if (cmp(area(a,b,c[i+1]))==0) {cp1=c[i]; cp2=c[i+1];}
//===== three is no 3 points in line. a[] is convex 0~n-1
                                                                                            else cp1=cp2=c[i]; return true;
void prepare(point a[] ,double w[],int &n) {
                                                                                        }
```

```
if (px[j]!=-1) x[j]-=m;
        if (cmp(k2)==0) {
            if (cmp(area(a,b,c[j+1]))==0) {cp1=c[j];cp2=c[j+1];}
                                                                                             if (py[j]!=-1) y[j]+=m;
            else cp1=cp2=c[i];
                                                                                             else slack[j]-=m;}
        }return true;
                                                                                         for (j=0;j<n;j++){
   }
                                                                                             if (py[j]==-1&&!slack[j]){
   if (i>j) swap(i,j); int x,y; x=dic(a,b,i,j,c); y=dic(a,b,j,i+n,c);
                                                                                                 py[j]=par[j];
   cp1=get(a,b,c[x-1],c[x]); cp2=get(a,b,c[y-1],c[y]);
                                                                                                 if (sy[j]==-1){ adjust(j); flag=true; break;}
    return true;}
                                                                                                 px[sy[j]]=j; if (find(sy[j])){flag=true;break;}
                                                                                         }}}}
KM
const int maxn=200;const int oo=0x7ffffffff;
                                                                                 int ans=0; for (i=0;i<n;i++) ans+=w[sv[i]][i];return ans;}</pre>
int w[maxn][maxn],x[maxn],y[maxn],px[maxn],py[maxn],sy[maxn],slack[maxn];
                                                                            费用流
int par[maxn]; int n; int pa[200][2], pb[200][2], n0, m0, na, nb; char s[200][200];
                                                                            const int inf = 10000000000;
void adjust(int v){ sy[v]=py[v]; if (px[sy[v]]!=-2) adjust(px[sy[v]]);}
                                                                            int s, t, node, totalCost;
bool find(int v){for (int i=0;i<n;i++)</pre>
                                                                            vector<int> head, dist, vtx, next, c, cost;
        if (py[i]==-1){
                                                                            vector<bool> vis;
                                                                            void resize(vector<T> &a, int size, T init) //设大小、初始值
            if (slack[i]>x[v]+y[i]-w[v][i]){
                                                                            void init(int source, int target, int nodeCount) //初始化,记得清空
                slack[i]=x[v]+y[i]-w[v][i]; par[i]=v;}
            if (x[v]+y[i]==w[v][i]){
                                                                            void add(int a,int b,int cc,int cst) //双向加边
                py[i]=v; if (sy[i]==-1){adjust(i);
                                                     return 1;}
                                                                            void spfa() {
                                                                                 resize(vis, node, false); resize(dist, node, -inf);
                if (px[sy[i]]!=-1) continue; px[sy[i]]=i;
                if (find(sy[i])) return 1;
                                                                                 queue<int> q; q.push(t); vis[t]=true; dist[t]=0;
    }}return 0;}
                                                                                 while (q.size()) {
                                                                                     int u = q.front();
int km(){int i,j,m;
                                                                                                              q.pop();
    for (i=0;i<n;i++) sy[i]=-1,y[i]=0;
                                                                                     vis[u] = false;
    for (i=0;i<n;i++) {x[i]=0; for (j=0;j<n;j++) x[i]=max(x[i],w[i][j]);}</pre>
                                                                                     for (int p = head[u]; p != -1; p = next[p]) {
                                                                                         if (c[p ^ 1] && dist[u] + cost[p ^ 1] > dist[vtx[p]]) {
    bool flag;
   for (i=0;i<n;i++){</pre>
                                                                                             dist[vtx[p]] = dist[u] + cost[p ^ 1];
                                                                                             if (!vis[vtx[p]]) {
        for (j=0;j<n;j++) px[j]=py[j]=-1,slack[j]=oo;</pre>
        px[i]=-2; if (find(i)) continue; flag=false;
                                                                                                 vis[vtx[p]] = true; q.push(vtx[p]);
        for (;!flag;){
                                                                                                 if (dist[q.back()] < dist[q.front()]) {</pre>
                                                                                                      swap(q.front(), q.back());
            m=oo; for (j=0;j<n;j++) if (py[j]==-1) m=min(m,slack[j]);
            for (j=0;j<n;j++){
```

```
}}}}} //补齐上一页的括号
                                                                                 }
                                                                              }
int dfs(int u, int limit) {
                                                                              if (maxi == -inf) {
   if (u == t) {
        totalCost += limit * dist[s];
                                                                                  return false;
                                                                              }
        return limit;
                                                                              for (int i = 0; i < node; ++ i) {</pre>
   int current = 0;
                                                                                  if (vis[i]) {
   vis[u] = true;
                                                                                      dist[i] += maxi;
   for (int p = head[u]; p != -1; p = next[p]) {
                                                                                 }
                                                                              }
        if (c[p] && !vis[vtx[p]] && dist[vtx[p]] + cost[p] == dist[u])
{
                                                                              return true;
           int delta = dfs(vtx[p], min(limit - current, c[p]));
                                                                         }
           c[p] -= delta; c[p ^ 1] += delta;
                                                                          int maxCostFlow() {
           current += delta;
                                                                              spfa();
           if (current == limit) {
                                                                              totalCost = 0;
                break;
                                                                              do{
           }
                                                                                  do{
                                                                                      resize(vis, node, false);
                                                                                  }while (dfs(s, inf));
                                                                              }while (adjust());
    return current;
                                                                              return totalCost;
inline bool adjust() {
                                                                          }
   int maxi = -inf;
                                                                          无向图最小割
    for (int i = 0; i < node; ++ i) {</pre>
                                                                          #define typec int // type of res (or long long)
        if (vis[i]) {
                                                                          const typec inf = 0x3f3f3f3f; // max of res
           for (int p = head[i]; p != -1; p = next[p]) {
                                                                          const typec maxw = 1000; // maximum edge weight, g[i][j]=g[j][i]
                if (c[p] && !vis[vtx[p]]) {
                                                                          typec g[V][V], w[V]; int a[V], v[V], na[V];
                    assert(dist[vtx[p]] + cost[p] != dist[i]);
                                                                          typec mincut(int n){
                   maxi = max(maxi, dist[vtx[p]] + cost[p] - dist[i]);
                                                                              int i, j, pv, zj; typec best = maxw * n * n;
                }
                                                                              for (i = 0; i < n; i++) v[i] = i; // vertex: 0 ~ n-1
           }
                                                                              while (n > 1) {
                                                                                  for (a[v[0]] = 1, i = 1; i < n; i++) {
```

```
a[v[i]] = 0; na[i - 1] = i; w[i] = g[v[0]][v[i]];
                                                                                       v = match[u]; InBlossom[base[u]] = InBlossom[base[v]] = true;
                                                                                       u = pred[v]; if(base[u] != newbase) pred[u] = v;}}
        for (pv = v[0], i = 1; i < n; i++) {
            for (zj = -1, j = 1; j < n; j++)
                                                                               void BlossomContract(int u, int v) {
                if (|a[v[j]] && (zj < 0 | | w[j] > w[zj])) zj = j;
                                                                                   newbase = FindCommonAncestor(u, v);
            a[v[zj]] = 1;
                                                                                   for (int i = 0; i < n; i++) InBlossom[i] = 0;
            if (i == n - 1) {
                                                                                   ResetTrace(u); ResetTrace(v);
                if (best > w[zj]) best = w[zj];
                                                                                   if(base[u] != newbase) pred[u]=v;if(base[v] != newbase) pred[v]=u;
                for (i = 0; i < n; i++)
                                                                                   for(int i = 0; i < n; ++i)
                                                                                   if(InBlossom[base[i]]) {base[i]=newbase; if(!InQueue[i]) push(i);}}
                     g[v[i]][pv] = g[pv][v[i]] += g[v[zj]][v[i]];
                v[zi] = v[--n]; break;
                                                                               bool FindAugmentingPath(int u) {
            pv = v[zi];
                                                                                   bool found = false:
            for (j = 1; j < n; j++) if (!a[v[j]]) w[j] += g[v[zj]][v[j]];
                                                                                   for(int i = 0; i < n; ++i) pred[i] = -1, base[i] = i;
   }} return best;}
                                                                                   for (int i = 0; i < n; i++) InQueue[i] = 0;</pre>
一般图最大匹配 片段
                                                                                   start = u; finish = -1; head = tail = 0; push(start);
const int maxn=310;
                                                                                   while(head < tail) {</pre>
                                                                                       int u = pop();
vector<int> link[maxn];
int n; int match[maxn]; int Queue[maxn], head, tail; int pred[maxn],
                                                                                       for(int i = link[u].size() - 1; i >= 0; i--) {
base[maxn]:
                                                                                            int v = link[u][i];
bool InQueue[maxn], InBlossom[maxn]; bool use[maxn]; //===这个点是否有用
                                                                                            if(use[u] && use[v] && base[u] != base[v] && match[u] != v)
                                                                                            if(v == start || (match[v] >= 0 && pred[match[v]] >= 0))
int start, finish; int newbase;
void push(int u) {    Queue[tail++] = u; InQueue[u] = true; }
                                                                                                BlossomContract(u, v);
int pop() { return Queue[head++];}
                                                                                            else if(pred[v] == -1) {pred[v] = u;
int FindCommonAncestor(int u, int v) {
                                                                                                if(match[v] >= 0) push(match[v]);
    bool InPath[maxn]; for (int i = 0; i < n; i++) InPath[i] = 0;</pre>
                                                                                                else {finish = v; return true;}
    while(true) {
                                                                                   }}} return found;}
        u = base[u]; InPath[u] = true;
                                                                               void AugmentPath() {
        if(u == start) break; u = pred[match[u]];}
                                                                                   int u, v, w; u = finish;
    while(true) {v = base[v]; if(InPath[v]) break; v = pred[match[v]]; }
                                                                               while(u >= 0) { v = pred[u]; w = match[v]; match[v] = u; match[u] = v; u = w;}}
    return v;}
                                                                               void FindMaxMatching() {
void ResetTrace(int u) {
                                                                                   for(int i = 0; i < n; ++i) match[i] = -1;</pre>
   int v;
                                                                                   for(int i = 0; i < n; ++i)
    while(base[u] != newbase) {
                                                                                     if(match[i] == -1 && use[i])if(FindAugmentingPath(i)) AugmentPath();}
```

```
int main() {
                                                                                         for ( j=1 , k=0 ; j <= n ; j ++) if ( !used[j] && i!=j )</pre>
    foru(i,0,n) link[i].clear(); memset(use,1,sizeof(use));
                                                                                              if ( k==0 || g[j][i] < g[k][i] ) k=j;
//======编号从0~n-1 , link[i] push back所有i号点连向的点。 双向边
                                                                                         eg[i] = k;
    FindMaxMatching(); k=0;rep(i,n) if (match[i]>=0) k++;
                                                                                     } memset(pass,0,sizeof(pass));
    printf("%d\n",k/2); return 0;
                                                                                     for ( i=1;i<=n;i++) if (!used[i] && !pass[i] && i!=</pre>
                                                                                 root )combine(i,sum);
有向图最小生成树
const int maxn=1100; int n,m , g[maxn][maxn] , used[maxn] , pass[maxn] ;
                                                                                 for ( i =1; i<=n ; i ++) if ( !used[i] && i!= root ) sum+=g[eg[i]][i];
int eg[maxn] , more , queue[maxn];
                                                                                 return sum ; }
void combine (int id , int &sum ) {
                                                                             int main(){
    int tot = 0 , from , i , j , k ;
                                                                                int i,j,k,test,cases; cases=0; scanf("%d%d",&n,&m);
    for ( ; id!=0 && !pass[ id ] ; id=eg[id] ) {
                                                                                foru(i,1,n) foru(j,1,n) g[i][j]=1000001;
        queue[tot++]=id ; pass[id]=1; }
                                                                                foru(i,1,m) {scanf("%d%d",&j,&k);j++;k++;scanf("%d",&g[j][k]);}
    for ( from=0; from<tot && queue[from]!=id ; from++);</pre>
                                                                                k=mdst(1); if (k>1000000) printf("Possums!\n"); //===no
    if ( from==tot ) return ;
                                                                                else printf("%d\n",k); return 0;}
                                                                             Hopcroft
    more = 1;
    for ( i=from ; i<tot ; i++) {
                                                                             #define maxn 50005 #define maxm 150005
        sum+=g[eg[queue[i]]][queue[i]];
                                                                             inline int Maxmatch(){
        if ( i!=from ) {
                                                                                 memset(mk,-1,sizeof(mk)); memset(cx,-1,sizeof(cx));
                                                                                 memset(cy,-1,sizeof(cy));
            used[queue[i]]=1;
            for ( j = 1 ; j <= n ; j++) if ( !used[j] )
                                                                                 for (int p=1,fl=1,h,tail;fl;++p){
                                                                                     fl=0; h=tail=0;
                if ( g[queue[i]][j]<g[id][j] ) g[id][j]=g[queue[i]][j] ;}}</pre>
                                                                                     for (int i=0; i< n; ++i) if (cx[i]==-1)
    for ( i=1; i<=n ; i++) if ( !used[i] && i!=id ) {</pre>
        for ( j=from ; j<tot ; j++){ k=queue[j];</pre>
                                                                                          q[++tail]=i,pre[i]=-1,src[i]=i;
            if ( g[i][id]>g[i][k]-g[eg[k]][k] )
                                                                                     for (h=1;h<=tail;++h){</pre>
                                                                                          int u=q[h]; if (cx[src[u]]!=-1) continue;
g[i][id]=g[i][k]-g[eg[k]][k]; }}
int mdst( int root ) { // return the total length of MDST
                                                                                         for (int pp=head[u],v=vtx[pp];pp=next[pp],v=vtx[pp])
                                                                                          if (mk[v]!=p) { mk[v]=p; q[++tail]=cy[v];
    int i , j , k , sum = 0 ;
    memset ( used , 0 , sizeof ( used ) );
                                                                                              if (cy[v] > = 0) {
    for ( more =1; more ; ) {
                                                                                                  pre[cy[v]]=u; src[cy[v]]=src[u];continue;
                                                                                              } int d,e,t;
        more = 0; memset (eg,0,sizeof(eg));
        for ( i=1 ; i <= n ; i ++) if ( !used[i] && i!=root ) {</pre>
```

```
for
                                                                                 }return 0;}
(--tail,fl=1,d=u,e=v;d!=-1;t=cx[d],cx[d]=e,cy[e]=d,e=t,d=pre[d]);
                                                                            Manacher
                                                                            void manacher(char text[], int n, int palindrome[]) {
                break:
                            } } }
int res=0; for (int i=0;i<n;++i) res+=(cx[i]!=-1);return res;}</pre>
                                                                                palindrome[0] = 1;
割点缩块 /*考虑割点的无向图缩块*/
                                                                                for (int i = 1, j = 0, i < (n << 1) - 1; ++ i) {
const int maxn = 100000+5; const int maxm = 200000+5;
                                                                                    int p = i >> 1;
int e[maxm],prev[maxm],info[maxn],dfn[maxn],low[maxn],stack[maxn];
                                                                                    int q = i - p;
                                                                                    int r = (j + 1 \Rightarrow 1) + palindrome[j] - 1;
vector<int> Block[maxn]; int cntB,cnt,top,tote;
void insertE( int x,int y ){
                                                                                    palindrome[i] = r < q? 0: min(r - q + 1, palindrome[(j << 1))
    ++tote; e[tote]=v; prev[tote]=info[x]; info[x]=tote;}
                                                                             - i]);
                                                                                    while (0 <= p - palindrome[i] && q + palindrome[i] < n
void Min( int &x,int y ){if(y < x) x = y;}
void Dfs( int x,int father ){
                                                                                            && text[p - palindrome[i]] == text[q + palindrome[i]])
    dfn[x] = low[x] = ++cnt; stack[++top] = x;
                                                                            {
   for(int t=info[x];t;t=prev[t])
                                                                                        palindrome[i] ++;
        if(dfn[e[t]] == 0) {
                                                                                    if (q + palindrome[i] - 1 > r) {
            int tmp = top; Dfs(e[t],x); Min(low[x],low[e[t]]);
            if(low[e[t]] >= dfn[x]){
                                                                                        j = i;
                Block[++cntB].clear();
                for(int k=tmp+1;k<=top;++k)</pre>
                                                                                }
Block[cntB].push back(stack[k]);
                Block[cntB].push back(x); top=tmp; }
                                                                            回文串//=o(n) 统计出, r(i) 表示 (i-r[i]+1 , i)==(i+r[i] , i+1)
        }else if(e[t]!=father) Min(low[x],dfn[e[t]]);}
                                                                            void calc_radius(char s[]){
int main(){
                                                                                 for (int i=0,j=0,k=0;i<len;){
    int n,m; scanf("%d%d",&n,&m); memset(info,0,sizeof(info)); tote=0;
                                                                                     while (i - j >= 0 \&\& i+j+1 < len \&\& s[i-j] == s[i+j+1]) j++;
    for(int i=0;i<m;++i){</pre>
                                                                                     radius[i] = j; k = 1;
        int x,y; scanf("%d%d",&x,&y); insertE(x,y); insertE(y,x);}
                                                                                     while (k <= radius[i] && radius[i-k] < radius[i] - k) {</pre>
    memset(dfn,0,sizeof(dfn)); cnt=top=cntB=0;
                                                                                         radius[i+k] = min(radius[i-k],radius[i] - k); k++;
   for(int i=1;i<=n;++i) if(dfn[i] == 0) Dfs(i,-1);</pre>
                                                                                    j = max(j - k, 0); i += k;
    printf("%d\n",cntB);
                                                                            }}
    for(int i=1;i<=cntB;++i){</pre>
                                                                            dc3
     for(int j=0;j<Block[i].size();++j) printf("%d</pre>
                                                                            //DC3 待排序的字符串放在r 数组中,从r[0]到r[n-1],长度为n,且最大值小于m。
",Block[i][j]);puts("");
```

```
//约定除r[n-1]外所有的r[i]都大于0, r[n-1]=0。
//函数结束后,结果放在sa 数组中,从sa[0]到sa[n-1]。
#define maxn 10000
#define F(x) ((x)/3+((x)%3==1?0:tb))
#define G(x) ((x)<tb?(x)*3+1:((x)-tb)*3+2)
int wa[maxn],wb[maxn],wv[maxn],wss[maxn]; //必须这么大
int s[maxn*3],sa[maxn*3];
int c0(int *r,int a,int b){return
    r[a]==r[b]&&r[a+1]==r[b+1]&&r[a+2]==r[b+2];
int c12(int k,int *r,int a,int b){
    if(k==2) return r[a]< r[b] | | | r[a] == r[b] & & c12(1,r,a+1,b+1);
    else return r[a]<r[b]||r[a]==r[b]&&wv[a+1]<wv[b+1];</pre>
void sort(int *r,int *a,int *b,int n,int m){
    int i; for(i=0;i<n;i++) wv[i]=r[a[i]];</pre>
    for(i=0;i<m;i++) wss[i]=0; for(i=0;i<n;i++) wss[wv[i]]++;
    for(i=1;i<m;i++) wss[i]+=wss[i-1];</pre>
    for(i=n-1;i>=0;i--) b[--wss[wv[i]]]=a[i];
void dc3(int *r,int *sa,int n,int m){
    int i,j,*rn=r+n,*san=sa+n,ta=0,tb=(n+1)/3,tbc=0,p;
    r[n]=r[n+1]=0;
    for(i=0;i<n;i++) if(i%3!=0) wa[tbc++]=i;</pre>
    sort(r+2,wa,wb,tbc,m); sort(r+1,wb,wa,tbc,m);
    sort(r,wa,wb,tbc,m);
    for(p=1,rn[F(wb[0])]=0,i=1;i<tbc;i++)
        rn[F(wb[i])]=c0(r,wb[i-1],wb[i])?p-1:p++;
    if (p<tbc) dc3(rn,san,tbc,p);</pre>
    else for (i=0;i<tbc;i++) san[rn[i]]=i;</pre>
    for (i=0;i<tbc;i++) if(san[i]<tb) wb[ta++]=san[i]*3;</pre>
    if(n%3==1) wb[ta++]=n-1;
    sort(r,wb,wa,ta,m);
```

```
for(i=0;i<tbc;i++) wv[wb[i]=G(san[i])]=i;</pre>
    for(i=0,j=0,p=0;i<ta && j<tbc;p++)</pre>
         sa[p]=c12(wb[j]%3,r,wa[i],wb[j])?wa[i++]:wb[j++];
    for(;i<ta;p++) sa[p]=wa[i++]; for(;j<tbc;p++) sa[p]=wb[j++];}</pre>
int main(){
    int n, m=0; scanf("%d",&n);
    for (int i=0;i<n;i++) scanf("%d",&s[i]),s[i]++,m=max(s[i]+1,m);</pre>
    printf("%d\n",m); s[n++]=0; dc3(s,sa,n,m);
    for (int i=0;i<n;i++) printf("%d ",sa[i]);printf("\n");</pre>
}
最大团搜索算法
Int g[][]为图的邻接矩阵。 MC(V)表示点集V的最大团
令Si={vi, vi+1, ..., vn}, mc[i]表示MC(Si). 倒着算mc[i], 那么显然MC(V)=mc[1]
此外有mc[i]=mc[i+1] or mc[i]=mc[i+1]+1
void init(){
    int i, j;for (i=1; i<=n; ++i) for (j=1; j<=n; ++j) scanf("%d", &g[i][j]);</pre>
}
void dfs(int size){
    int i, j, k;
    if (len[size]==0) {    if (size>ans) {        ans=size; found=true;} return;}
    for (k=0; k<len[size] && !found; ++k) {</pre>
        if (size+len[size]-k<=ans) break;</pre>
        i=list[size][k]; if (size+mc[i]<=ans) break;</pre>
        for (j=k+1, len[size+1]=0; j<len[size]; ++j)</pre>
        if (g[i][list[size][j]])
list[size+1][len[size+1]++]=list[size][j];
        dfs(size+1);}}
void work(){
    int i, j;
                 mc[n]=ans=1;
    for (i=n-1; i; --i) {found=false; len[1]=0;
        for (j=i+1; j<=n; ++j) if (g[i][j]) list[1][len[1]++]=j;</pre>
        dfs(1); mc[i]=ans;}}
```

void FFT(Complex P[], int n, int oper)

```
极大团的计数
                                                                                  {
Bool g[][] 为图的邻接矩阵,图点的标号由1至n。
                                                                                       for (int i = 1, j = 0; i < n - 1; i++) {
void dfs(int size){
                                                                                          for (int s = n; j = s >>= 1, ~j & s;);
                                                                                          if (i < j) {</pre>
    int i, j, k, t, cnt, best = 0;
                                        bool bb;
    if (ne[size]==ce[size]){if (ce[size]==0) ++ans;return;}
                                                                                              swap(P[i], P[j]);
    for (t=0, i=1; i<=ne[size]; ++i) {</pre>
                                                                                          }
        for (cnt=0, j=ne[size]+1; j<=ce[size]; ++j)</pre>
                                                                                       }
        if (!g[list[size][i]][list[size][j]]) ++cnt;
                                                                                       Complex unit p0;
        if (t==0 || cnt<best) t=i, best=cnt;</pre>
                                                                                       for (int d = 0; (1 << d) < n; d++) {
                                                                                          int m = 1 << d, m2 = m * 2;
    if (t && best<=0) return;</pre>
                                                                                          double p0 = pi / m * oper;
    for (k=ne[size]+1; k<=ce[size]; ++k) {</pre>
                                                                                          sincos(p0, &unit p0.y, &unit p0.x);
        if (t>0){
                                                                                          for (int i = 0; i < n; i += m2) {
             for (i=k; i<=ce[size]; ++i)</pre>
                                                                                              Complex unit = 1;
                                                                                              for (int j = 0; j < m; j++) {
                 if (!g[list[size][t]][list[size][i]]) break;
             swap(list[size][k], list[size][i]);
                                                                                                  Complex &P1 = P[i + j + m], &P2 = P[i + j];
                                                                                                  Complex t = unit * P1:
         i=list[size][k]; ne[size+1]=ce[size+1]=0;
                                                                                                  P1 = P2 - t;
        for (j=1; j<k; ++j)if (g[i][list[size][j]])</pre>
                                                                                                  P2 = P2 + t;
             list[size+1][++ne[size+1]]=list[size][j];
                                                                                                  unit = unit * unit p0;
        for (ce[size+1]=ne[size+1], j=k+1; j<=ce[size]; ++j)</pre>
        if (g[i][list[size][j]]) list[size+1][++ce[size+1]]=list[size][j];
                                                                                          }
        dfs(size+1); ++ne[size]; --best;
                                                                                       }
        for (j=k+1, cnt=0; j<=ce[size]; ++j) if (!g[i][list[size][j]]) ++cnt;</pre>
                                                                                  }
        if (t==0 | cnt<best) t=k, best=cnt;</pre>
                                                                                   Simpson
        if (t && best<=0) break;</pre>
                                                                                   double simpson(const T&f, double a, double b, int n){
}}
                                                                                       const double h=(b-a)/n; double ans=f(a)+f(b);
void work(){
                                                                                       for(int i=1;i<n;i+=2)ans+=4*f(a+i*h);</pre>
    int i; ne[0]=0; ce[0]=0; for (i=1; i<=n; ++i) list[0][++ce[0]]=i;</pre>
                                                                                       for(int i=2;i<n;i+=2)ans+=2*f(a+i*h);</pre>
    ans=0; dfs(0);}
                                                                                       return ans*h/3;
                                                                                   }printf("%lf\n", simpson(test, 0, 1, (int) 1e6)
FFT
```

```
长方体表面两点最短距离
                                                                                   tmp=(long long)tmp*tmp%P;
int r;
                                                                                   if (Time&1) tmp=(long long)tmp*x%P;
                                                                                                                          return tmp;
void turn(int i, int j, int x, int y, int z,int x0, int y0, int L, int W, int
                                                                               }
H) {
                                                                               inline int rev(int x){ if (!x) return 0; return calc(x,P-2);}
    if (z==0) { int R = x*x+y*y; if (R<r) r=R;}
                                                                               inline void Compute(){
    else{
                                                                                   while (1) { b=rand()%(P-2)+2; if (calc(b,pDiv2)+1==P) return; }
        if(i)=0 \& i < 2)turn(i+1, j, x0+L+z, y, x0+L-x, x0+L, y0, H, W, L);
                                                                               }
        if(j)=0 \& j < 2)turn(i, j+1, x, y0+W+z, y0+W-y, x0, y0+W, L, H, W);
                                                                               int main(){
        if(i <= 0 \&\& i >- 2)turn(i-1, j, x0-z, y, x-x0, x0-H, y0, H, W, L);
                                                                                   srand(time(\theta)^312314); int T;
        if(j<=0 && j>-2)turn(i, j-1, x, y0-z, y-y0, x0, y0-H, L, H, W);
                                                                                   for (scanf("%d",&T);T;--T) {
                                                                                       scanf("%d%d%d%d",&a,&b,&c,&P);
}}
int main(){
                                                                                       if (P==2) {
    int L, H, W, x1, y1, z1, x2, y2, z2;
                                                                                           int cnt=0; for (int i=0;i<2;++i) if ((a*i*i+b*i+c)%P==0) ++cnt;</pre>
    cin >> L >> W >> H >> x1 >> y1 >> z1 >> x2 >> y2 >> z2;
                                                                                          printf("%d",cnt);
    if (z1!=0 \&\& z1!=H) if (y1==0 || y1==W)
                                                                                          for (int i=0;i<2;++i) if ((a*i*i+b*i+c)%P==0) printf(" %d",i);</pre>
         swap(y1,z1), std::swap(y2,z2), std::swap(W,H);
                                                                                          puts("");
    else swap(x1,z1), std::swap(x2,z2), std::swap(L,H);
                                                                                       }else {
    if (z1==H) z1=0, z2=H-z2;
                                                                                           int delta=(long long)b*rev(a)*rev(2)%P;
    r=0x3fffffff; turn(0,0,x2-x1,y2-y1,z2,-x1,-y1,L,W,H);
                                                                                           a=(long long)c*rev(a)%P-sqr( (long long)delta )%P;
    cout<<r<<endl; return 0;</pre>
                                                                                           a\%=P; a+=P; a\%=P; a=P-a; a\%=P; pDiv2=P/2;
                                                                                          if (calc(a,pDiv2)+1==P) puts("θ");
字符串的最小表示
                                                                                           else {
A[1..n]; A[n+1..n+n]=A[1..n]; i:=1; j:=2; k:=0; t:=0;
                                                                                              int t=0,h=pDiv2; while (!(h\%2)) ++t,h/=2;
while (j<=n) {
                  k=0; while (a[i+k]=a[j+k]) k++;
                                                                                              int root=calc(a,h/2);
    if (a[i+k]>a[j+k]) i=i+k+1; else j=j+k+1;
                                                                                              if (t>0) { Compute(); Pb=calc(b,h); }
    if (i==j) j++; if (i>j) swap(i,j);
                                                                                              for (int i=1;i<=t;++i) {</pre>
} printf("%d\n",i);
                                                                                                  d=(long long)root*root*a%P;
二次剩余
                                                                                                  for (int j=1;j<=t-i;++j) d=(long long)d*d%P;</pre>
/*a*x^2+b*x+c==0 (mod P) 求 0..P-1 的根 */
                                                                                                  if (d+1==P) root=(long long)root*Pb%P;
int pDiv2,P,a,b,c,Pb,d;
                                                                                                  Pb=(long long)Pb*Pb%P;
inline int calc(int x,int Time){
   if (!Time) return 1; int tmp=calc(x,Time/2);
                                                                                              root=(long long)a*root%P;
```

```
while((i=d[i])!=x){
             int root1=P-root; root-=delta;
             root%=P; if (root<0) root+=P;
                                                                                    j=i;
                                                                                    while((j=l[j])!=i){
             root1-=delta; root1%=P; if (root1<0) root1+=P;
             if (root>root1) { t=root;root=root1;root1=t; }
                                                                                        u[d[j]]=u[j]; d[u[j]]=d[j]; R[C[j]]--;
             if (root==root1) printf("1 %d\n", root);
                                                                                    }
             else printf("2 %d %d\n", root, root1);
                                                                                }
                                                                            }
   }}}return 0; }
                                                                            void uncover(int x){
Pell 方程求解
//求x^2-ny^2=1的最小正整数根,n不是完全平方数
                                                                                int i=x,j;
p[1]=1;p[0]=0; q[1]=0;q[0]=1; a[2]=(int)(floor(sqrt(n)+1e-7));
                                                                                while((i=u[i])!=x){
g[1]=0;h[1]=1;
                                                                                    j=i;
for (int i=2;i;++i) {
                                                                                    while((j=r[j])!=i){
                                                                                        u[d[j]]=j; d[u[j]]=j; R[C[j]]++;
   g[i]=-g[i-1]+a[i]*h[i-1];
                               h[i]=(n-sqr(g[i]))/h[i-1];
                               p[i]=a[i]*p[i-1]+p[i-2];
                                                                                    }
   a[i+1]=(g[i]+a[2])/h[i];
                               检查p[i],q[i]是否为解,如果是,则退出
   q[i]=a[i]*q[i-1]+q[i-2];
                                                                                }
                                                                                r[1[x]]=x; 1[r[x]]=x;
莫比乌斯函数以及 gcd=1 的对数
                                                                            }
inline void prepare()//计算莫比乌斯函数,及其前缀和sum,复杂度O(nlogn)
                                                                        public:
inline void calc(int a,int b) {
                                                                            vector<int> ans;
   for (int i=1,j,p,q;i<=a;i=j+1) {</pre>
                                                                            void resize(int n){
       p=a/i;q=b/i; j=b/q; if (a<p*j) j=a/p;
                                                                                u.resize(1,0); d.resize(1,0); l.resize(1,0); r.resize(1,0);
       ans+=(long long)(sum[j]-sum[i-1])*p*q;
                                                                                C.resize(1,-1); R.resize(1,-1);
   } }//求1..a和1..b中有多少对的gcd=1,复杂度0(sqrt(a+b))
                                                                                head.resize(n,-1); tail.resize(n,-1);
Exact Cover
                                                                                ans.resize(n,0); head0=tail0=0;
class ExactCover{
                                                                            }
                                                                            void add(vector<int> a,bool must=true){
private:
                                                                                u.push back(u.size()+a.size());
   vector<int> u,d,l,r,C,R,head,tail;
   int head0,tail0,seed;
                                                                                if(must){
   void cover(int x){
                                                                                    1.push_back(tail0); r.push_back(head0);
                                                                                    tail0=l[r[d.size()]]=r[l[d.size()]]=d.size();
       int i=x,j;
       r[1[x]]=r[x]; 1[r[x]]=1[x];
                                                                                }else{
```

```
1.push back(1.size()); r.push back(r.size());
                                                                                    min=R[x=i];
                                                                            cover(i=x);
   C.push back(C.size()); R.push back(a.size());
                                                                            while((i=d[i])!=x){
   int n=u.size(),m=a.size(),i,j;
                                                                                j=i;
    for(i=0;i<m;i++){</pre>
                                                                                while((j=r[j])!=i) cover(C[j]);
       j=a[i];
                                                                                ans[R[i]]=1;
       if(head[j]==-1){
                                                                                if(search()) return true;
           1.push back(n+i); r.push back(n+i);
                                                                                ans[R[i]]=0;
           head[j]=n+i; tail[j]=n+i;
                                                                                while((j=l[j])!=i) uncover(C[j]);
       }else{
                                                                            }
                                                                            uncover(x);
           1.push back(tail[j]); r.push back(head[j]);
           tail[j]=r[l[n+i]]=l[r[n+i]]=n+i;
                                                                            return false;
       }
                                                                        }
       u.push back(n+i-1);
                               d.push back(n+i);
                                                                    };
       C.push_back(C.back()); R.push_back(j);
                                                                    Link-Cut-Tree
    d.push back(n-1);
                                                                    void rotate(int x) {
                                                                        int t = type[x];
void select(int a){
                                                                        int y = parent[x];
   ans[a]=1; a=head[a];
                                                                        int z = children[x][1 ^ t];
   if(a==-1) return;
                                                                        type[x] = type[y];
    int x=a;
                                                                        parent[x] = parent[y];
                                                                        if (type[x] != 2) {
   while((x=r[x])!=a) cover(C[x]);
    cover(C[a]);
                                                                            children[parent[x]][type[x]] = x;
bool search(){
                                                                        type[y] = 1 ^ t;
                                                                        parent[y] = x;
    if(r[0]==0)
                   return true;
   int x,i,j,min=0x7fffffff;
                                                                        children[x][1 ^t] = y;
   i=0;
                                                                       if (z != 0) {
                                                                           type[z] = t;
    while((i=r[i])!=0)
       if(R[i]<min||!(++seed&3)&&R[i]==min)</pre>
                                                                            parent[z] = y;
```

```
type[children[x][1]] = 2;
   children[y][t] = z;
                                                                                children[x][1] = z;
   update(y);
                                                                                type[z] = 1;
                                                                                update(x);
void splay(int x) {
                                                                                z = x;
   vector <int> stack(1, x);
                                                                                x = parent[x];
   for (int i = x; type[i] != 2; i = parent[i]) {
                                                                             }
       stack.push back(parent[i]);
                                                                         }
                                                                         后缀自动机
   }
   while (!stack.empty()) {
                                                                         struct State {
       push(stack.back());
                                                                             static vector <State*> states;
       stack.pop_back();
                                                                            int id, length;
                                                                             State *parent;
   while (type[x] != 2) {
                                                                             State* go[C];
       int y = parent[x];
                                                                            State(int length) : id((int)states.size()), length(length),
       if (type[x] == type[y]) {
                                                                         parent(NULL) {
                                                                                memset(go, NULL, sizeof(go));
           rotate(y);
       } else {
                                                                                states.push_back(this);
           rotate(x);
       }
                                                                            State* extend(State* start, int token) {
       if (type[x] == 2) {
                                                                                State *p = this;
           break;
                                                                                State *np = new State(length + 1);
                                                                                while (p && !p->go[token]) {
       }
       rotate(x);
                                                                                    p->go[token] = np;
                                                                                    p = p->parent;
   update(x);
                                                                                if (!p) {
void access(int x) {
                                                                                    np->parent = start;
   int z = 0;
                                                                                } else {
   while (x != 0) {
                                                                                    State *q = p->go[token];
                                                                                    if (p\rightarrow length + 1 == q\rightarrow length) {
       splay(x);
```

```
np->parent = q;
           } else {
              State *nq = new State(p->length + 1);
              memcpy(nq->go, q->go, sizeof(q->go));
              nq->parent = q->parent;
              np->parent = q->parent = nq;
              while (p && p->go[token] == q) {
                  p->go[token] = nq;
                  p = p->parent;
              }
           }
       }
       return np;
};
差分序列
F(n) = c0 * C(n, 0) + c1 * C(n, 1) + ... + cp * C(n, p)
S(n) = F(0) + F(1) + ... + F(n)
    = c0 * C(n + 1, 1) + c1 * (n + 1, 2) + ... + cp * C(n + 1, p + 1)
求某年某月某日是星期几
int whatday(int d, int m, int y) { //day month year
   int ans; if (m == 1 || m == 2) { m += 12; y --; }
   if ((y < 1752) \mid | (y == 1752 \&\& m < 9) \mid | (y == 1752 \&\& m == 9 \&\& d < 3))
           ans = (d + 2*m + 3*(m+1)/5 + y + y/4 +5) \% 7;
   else ans = (d + 2*m + 3*(m+1)/5 + v + v/4 - v/100 + v/400)%7;
   return ans;
弦图的完美消除序列
从n到1的顺序依次给点标号(标号为i的点出现在完美消除序列的第i个)
设lable[i]表示第i个点与多少个已标号的点相邻,每次选择label[i]最大的未标号的点进行
标号。
```

任取一个已标号的与当前新标号的点相邻的点,如果与其他的已标号的且与当前点相邻的点之 间没有边,则无解。

弦图里的团数等于色数,色数(从后往前)和最大独立集(从前往后)都可以按完美消除序列

```
的顺序贪心。
双人零和矩阵游戏(公式)
N*N的方阵A, 选行的玩家的最优策略是p, 选列的是q,则
   q = A逆 * e / (e转置 * A逆 * e)
   p转置 = e转置 * A逆 / (e转置 * A逆 * e)
                                        e是全为1的列向量
当A不可逆时,每个元素加上一个值就可以了。
当矩阵是m行,n列的时候:
P[1]+P[2]+....+P[m]=1; P[i]>=0
V<=sigma(P[i]*Matrix[i][j])</pre>
最大化V
质数测试
bool primeTest(LL n, LL b) {
   LL m = n - 1;
   LL counter = 0:
   while ((m \& 1) == 0) {
      m >>= 1;
       counter ++;
   LL ret = powMod(b, m, n);
   if (ret == 1 || ret == n - 1) {
       return true;
   }
   counter --:
```

while (counter >= 0) {

**if** (ret == n - 1) {

return true;

ret = multiplyMod(ret, ret, n);

```
}
       counter --;
   return false;
const int BASIC[12] = {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37};
bool isPrime(LL n) {
   if (n < 2) return false;</pre>
   if (n < 4) return true;
   if (n == 3215031751LL) return false;
   for (int i = 0; i < 12 && BASIC[i] < n; ++ i)</pre>
       if (!primeTest(n, BASIC[i])) return false;
   return true;
Pollard-Rho
LL pollardRho(LL n, LL seed) {
   LL x, y;
   x = y = rand() % (n - 1) + 1;
   LL head = 1, tail = 2;
   while (true) {
       x = multiplyMod(x, x, n);
       x = addMod(x, seed, n);
       if (x == y) return n;
       LL d = gcd(abs(x - y), n);
       if (1 < d && d < n) return d;
       head ++;
       if (head == tail) {
          y = x;
           tail <<= 1;
       }
   }
```

```
}
vector <LL> divisors;
void factorize(LL n) {
   if (n > 1) {
        if (isPrime(n)) {
           divisors.push back(n);
       } else {
            LL d = n;
            while (d >= n) {
               d = pollardRho(n, rand() % (n - 1) + 1);
           factorize(n / d); factorize(d);
        }
    }
直线下有多少个格点
求\sum_{k=0..n-1} \left| \frac{a+bk}{m} \right|, a, b > 0
LL count(LL n, LL a, LL b, LL m) {
   if (b==0) return n * (a / m);
    if (a>=m) return n * (a / m) + count(n, a % m, b, m);
   if (b>=m) return (n - 1) * n / 2 * (b / m) + count(n, a, b % m, m);
    return count((a + b * n) / m, (a + b * n) % m, m, b);
}
综合
设正整数 n 的质因数分解为 n = \prod pi^ai, 则 x^2+y^2=n 有整数解的充要条件是 n 中不存在形如
```

设正整数 n 的质因数分解为 n =  $\Pi$ pi^ai,则 x^2+y^2=n 有整数解的充要条件是 n 中不存在形如pi=3(mod 4) &(and) 指数 ai 为奇数的质因数 pi

Pick 定理: 简单多边形,不自交。(严格在多边形内部的整点数\*2+在边上的整点数-2)/2=面积

定理 1: 最小覆盖数 = 最大匹配数 定理 2: 最大独立集 S 与 最小覆盖集 T 互补。 算法:

- 1. 做最大匹配,没有匹配的空闲点∈S 2. 如果 u∈S 那么 u 的临点必然属于 T
- 3. 如果一对匹配的点中有一个属于 T 那么另外一个属于 S
- 4. 还不能确定的,把左子图的放入 S,右子图放入 T 算法结束

有上下界网络流,可行流增广的流量不是实际流量。若要求实际流量应该强算一遍源点出去的 流量。

求最小下届网络流: 方法一: 加 t-s 的无穷大流, 求可行流, 然后把边反向后(减去下届网络流), 在残留网络中从汇到源做最大流。

方法二: 在求可行流的时候,不加从汇到源的无穷大边,得到最大流 X, 加上从汇到源 无穷大边后,再求最大流得到 Y。那么 Y 即是答案最小下届网络流。

gcd(2^(a)-1,2^(b)-1)=(2^gcd(a,b))-1. Fibonacci 数 gcd(Fn,Fm)=Fgcd(n,m)

Fibonacci 质数 (和前面所有的 Fibonacci 数互质) (大多已经是质数了,可能有 BUG 吧,不确定) 定理: 如果 a 是 b 的倍数,那么 Fa 是 Fb 的倍数。

二次剩余: p 为奇素数,若(a,p)=1,a 为 p 的二次剩余必要充分条件为  $a^{((p-1)/2)}$  mod p=1. (否则为 p-1)

p 为奇素数, $x^b = a \pmod{p}, x$  为 p 的 b 次剩余的必要充分条件为 若  $x^c \pmod{p-1}$  和 b 的最大公约数)) mod p=1.

最小二乘法。对于方程组 AX=b,构造方程组 $A' \times A \times x = A' \times b$ ,则 x 一定有解。混合图欧拉路算法。S 向出度过多的点连边,权值为过多的出度的一半。入度过多的点向 T 连边,权值为过多的入度的一半。若双向边(a,b)的初始方向是  $a \leftarrow b$ ,则 a 到 b 连边权值为 1.找到一条路就把路上所有边反向。

### java scl

```
public class main{
   public static StringTokenizer st; public static DataInputStream in;
   public static PrintStream out;

   public static BigInteger getsqrt(BigInteger n){
      if (n.compareTo(BigInteger.ZERO)<=0) return n;
      BigInteger x,xx,txx; xx=x=BigInteger.ZERO;</pre>
```

```
for (int t=n.bitLength()/2;t>=0;t--){
        txx=xx.add(x.shiftLeft(t+1)).add(BigInteger.ONE.shiftLeft(t+t));
        if (txx.compareTo(n)<=0){</pre>
                 x=x.add(BigInteger.ONE.shiftLeft(t)); xx=txx;
            }}return x;
    public static void main(String args[]) throws Exception{
        in=new DataInputStream(System.in);
        out=new PrintStream(new BufferedOutputStream(System.out));
        st=new StringTokenizer(in.readLine()); out.close();
    }
}//BigInteger
a.modPow(b,c);//a^b mod c; a.isProbablePrime(int certainty);
a.nextProbablePrime();
                              a.shiftLeft(int);
bitCount()
                 bitLength()
                                  clearBit(int i)
setBit(int i)
                 flipBit(int i) testBit(int i)
//BigDecimal
static int ROUND CEILING, ROUND DOWN, ROUND FLOOR,
ROUND HALF DOWN, ROUND_HALF_EVEN, ROUND_HALF_UP, ROUND_UP;
a.stripTrailingZeros();
//Vector
a.add((index),elem); a.remove(index); a.set(index,elem);
//Oueue
a.add(elem);
                 a.peek();//front
                                       a.poll();//pop
cout.setf(ios::fixed,ios::floatfield);
cout.precision(3); cout<<double(u)<<endl;</pre>
基本形 公式
```

### 椭圆:

椭圆 
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$
,其中离心率 $e = \frac{c}{a}$ , $c = \sqrt{a^2 - b^2}$ ;焦点参数 $p = \frac{b^2}{a}$ 

椭圆上(x,y)点处的曲率半径为  $R=a^2b^2\left(\frac{x^2}{a^4}+\frac{y^2}{b^4}\right)^{\frac{3}{2}}=\frac{(r_1r_2)^{\frac{3}{2}}}{ab}$ ,其中 $r_1$ 和 $r_2$ 分别为(x,y)与两焦点 $F_1$ 和 $F_2$ 的距离。设点 A 和点 M 的坐标分别为(a,0)和(x,y),则 AM 的弧长为

$$L_{AM} = a \int_0^{\arccos \frac{x}{a}} \sqrt{1 - e^2 \cos^2 t} \, dt = a \int_{\arccos \frac{x}{a}}^{\frac{\pi}{2}} \sqrt{1 - e^2 \sin^2 t} \, dt$$

椭圆的周长为 L =  $4a\int_0^{\frac{\pi}{2}}\sqrt{1-\mathrm{e}^2\sin^2t}\,\mathrm{d}t = 4a\mathrm{E}(\mathrm{e},\frac{\pi}{2})$  ,其中

$$E\left(e, \frac{\pi}{2}\right) = \frac{\pi}{2} \left[1 - \left(\frac{1}{2}\right)^2 e^2 - \left(\frac{1*3}{2*4}\right)^2 \frac{e^4}{3} - \left(\frac{1*3*5}{2*4*6}\right)^2 \frac{e^6}{5} - \cdots\right]$$

设椭圆上点 M(x, y), N(x, -y), x, y>0, A(a, 0), 原点 O(0, 0)。

扇形 OAM 的面积  $S_{OAM} = \frac{1}{2}ab \arccos \frac{x}{a}$  弓形 MAN 的面积  $S_{MAN} = ab \arccos \frac{x}{a} - xy$  方程,5 个点确定一个圆锥曲线。

 $\theta$  为(x, v)点关于椭圆中心的极角, r 为(x, v)到椭圆中心的距离, 椭圆极坐标方程:

$$x = r \cos \theta$$
,  $y = r \sin \theta$ ,  $\sharp + r^2 = \frac{b^2 a^2}{b^2 \cos^2 \theta + a^2 \sin^2 \theta}$ 

### 抛物线

标准方程  $y^2=2px$  曲率半径  $R=((p+2x)^{\wedge}(3/2))/sqrt(p)$  弧长: 设 M(x,y) 是抛物线上一点,则  $L_{OM}=\frac{p}{2}[\sqrt{\frac{2x}{p}\left(1+\frac{2x}{p}\right)}+ln(\sqrt{\frac{2x}{p}}+\sqrt{1+\frac{2x}{p}})]$  弓形面积: 设M,D是抛物线上两点,且分居一、四象限。作一条平行于MD且与抛物线相切的直线L。若M到L的距离为h。则有  $S_{MOD}=\frac{2}{3}MD\cdot h$ 

### 重心

半径为 r、圆心角为 $\theta$ 的扇形的重心与圆心的距离为( $4rsin(\theta/2)$ )/3 $\theta$ 半径为 r、圆心角为 $\theta$ 的圆弧的重心与圆心的距离为( $4rsin^3(\theta/2)$ )/( $3(\theta-sin\theta)$ ) 椭圆上半部分的重心与圆心的距离为 ( $4/3\pi$ ) b 抛物线中弓形 MOD 的重心满足 CQ=(2/5) PQ,P 是直线 L 与抛物线的切点,Q 在 MD 上且 PQ 平行 x 轴。C 是重心。

内心 r = 三角形面积/(p = 1/2(a+b+c)) I = (aA+bB+cC)/(a+b+c) 三重积公式  $a \times (b \times c) = b(a \cdot c) - c(a \cdot b)$ 

# 额外的公式

四边形: D1, D2 为对角线, M 对角线中点连线, A 为对角线夹角

- 1. a<sup>2</sup>+b<sup>2</sup>+c<sup>2</sup>+d<sup>2</sup>=D1<sup>2</sup>+D2<sup>2</sup>+4M<sup>2</sup> 2. S=D1D2sin(A)/2 (以下对圆的内接四边形)
- 3. ac+bd=D1D2 4. S=sqrt((P-a)(P-b)(P-c)(P-d)), P 为半周长 *En 边形:*R 为外接圆半径, r 为内切圆半径
  - 1. 中心角 A=2PI/n
- 2. 内角 C=(n-2)PI/n
- 3. 边长 a=2sqrt(R^2-r^2)=2Rsin(A/2)=2rtan(A/2)
- 4. 面积 S=nar/2=nr^2tan(A/2)=nR^2sin(A)/2=na^2/(4tan(A/2))
- **圆:** 1. 弧长 1=rA 2. 弦长 a=2sqrt (2hr-h^2)=2rsin(A/2)
  - 3. 弓形高 h=r-sqrt (r^2-a^2/4)=r(1-cos(A/2))=atan(A/4)/2
  - 4. 扇形面积 S1=r1/2=r^2A/2
  - 5. 弓形面积 S2=(r1-a(r-h))/2=r^2(A-sin(A))/2

**棱柱:** 1. 体积 V=Ah, A 为底面积, h 为高

- 2. 侧面积 S=1p, 1 为棱长, p 为直截面周长
- 3. 全面积 T=S+2A

- **棱锥:** 1. 体积 V=Ah/3, A 为底面积, h 为高
  - ; (以下对正棱锥)
  - 2. 侧面积 S=1p/2, 1 为斜高, p 为底面周长
- 3. 全面积 T=S+A
- **棱台:**1. 体积 V=(A1+A2+sqrt(A1A2))h/3, A1. A2 为上下底面积, h 为高(以下为正棱台)
  - 2. 侧面积 S=(p1+p2)1/2, p1. p2 为上下底面周长, 1 为斜高
  - 3. 全面积 T=S+A1+A2

# 算法

# 树的计数

## 有根树的计数

$$\Leftrightarrow$$
  $S_{n,j} = \sum_{1 \le i \le n/j} a_{n+1-ij} = S_{n-j,j} + a_{n+1-j}$ 

于是,n+1 个结点的有根树的总数为  $a_{n+1} = \frac{\sum_{1 \leq j \leq n} j a_j S_{n,j}}{n}$ 

附:  $a_1=1, a_2=1, a_3=2, a_4=4, a_5=9$  ,  $a_6=20, a_9=286$  ,  $a_{11}=1842$  无根树的计数

当 n 是奇数时,则有  $a_n - \sum_{1 \leq i \leq n/2} a_i a_{n-i}$  种不同的无根树。

当 n 是偶数时,则有这么多种不同的无根树。

$$a_n - \sum_{1 \le i \le \frac{n}{2}} a_i a_{n-i} + \frac{1}{2} a_{n/2} (a_{n/2} + 1)$$

### 代数

Burnside引理 ans = (∑每种置换下的不变的元素个数) 置换群中置换的个数

三次方程求根公式 
$$x^3 + px + q = 0$$

$$x_{j} = \omega^{j} \sqrt[3]{-\frac{q}{2} + \sqrt{\left(\frac{q}{2}\right)^{2} + \left(\frac{p}{3}\right)^{3}} + \omega^{2j} \sqrt[3]{-\frac{q}{2} - \sqrt{\left(\frac{q}{2}\right)^{2} + \left(\frac{p}{3}\right)^{3}}}$$

其中 j=0,1,2,  $\omega = (-1+i\sqrt{3})/2$ 

当求解 $ax^3 + bx^2 + cx + d = 0$  时, 令 x = y - b/3a 再求解y,即转化成  $x^3 + px + q = 0$ 的形式

## 组合公式

$$\sum_{k=1}^{n} (2k-1)^2 = \frac{n(4n^2-1)}{3} \qquad \sum_{k=1}^{n} k^3 = \left(\frac{n(n+1)}{2}\right)^2$$

$$\sum_{k=1}^{n} (2k-1)^3 = n^2(2n^2-1) \qquad \sum_{k=1}^{n} k^4 = \frac{n(n+1)(2n+1)(3n^2+3n-1)}{30}$$

$$\sum_{k=1}^{n} k^5 = \frac{n^2(n+1)^2(2n^2+2n-1)}{12} \qquad \sum_{k=1}^{n} k(k+1) = \frac{n(n+1)(n+2)}{3}$$

$$\sum_{k=1}^{n} k(k+1)(k+2) = \frac{n(n+1)(n+2)(n+3)}{4}$$

$$\sum_{k=1}^{n} k(k+1)(k+2)(k+3) = \frac{n(n+1)(n+2)(n+3)(n+4)}{5}$$

错排:  $D_n = n! \left(1 - \frac{1}{t!} + \frac{1}{2!} - \frac{1}{2!} + \dots + \frac{(-1)^n}{n!} = (n-1)(D_{n-2} - D_{n-1})\right)$ 

### 三角公式

 $\sin(\alpha \pm \beta) = \sin\alpha \cos\beta \pm \cos\alpha \sin\beta \qquad \cos(\alpha \pm \beta) = \cos\alpha \cos\beta \mp \sin\alpha \sin\beta$ 

$$\tan(\alpha \pm \beta) = \frac{\tan(\alpha) \pm \tan(\beta)}{1 \mp \tan(\alpha) \tan(\beta)} \qquad \tan(\alpha) \pm \tan(\beta) = \frac{\sin(\alpha \pm \beta)}{\cos(\alpha) \cos(\beta)}$$

$$\sin(\alpha) + \sin(\beta) = 2 \sin \frac{(\alpha + \beta)}{2} \cos \frac{(\alpha - \beta)}{2} \quad \sin(\alpha) - \sin(\beta) = 2 \cos \frac{(\alpha + \beta)}{2} \sin \frac{(\alpha - \beta)}{2}$$

$$\cos(\alpha) + \cos(\beta) = 2 \cos \frac{(\alpha + \beta)}{2} \cos \frac{(\alpha - \beta)}{2} \quad \cos(\alpha) - \cos(\beta) =$$

$$-2 \sin \frac{(\alpha + \beta)}{2} \sin \frac{(\alpha - \beta)}{2}$$

$$\sin(n\alpha) = n\cos^{n-1}\alpha \sin\alpha - \binom{n}{3} \cos^{n-3}\alpha \sin^{3}\alpha + \binom{n}{5} \cos^{n-5}\alpha \sin^{5}\alpha - \cdots$$

$$\cos(n\alpha) = \cos^{n}\alpha - \binom{n}{2} \cos^{n-2}\alpha \sin^{2}\alpha + \binom{n}{4} \cos^{n-4}\alpha \sin^{4}\alpha - \cdots$$

### 积分表

$(\arcsin x)' = \frac{1}{\sqrt{1 - x^2}}$	$(\arccos x)' = -\frac{1}{\sqrt{1-x^2}}$		$(\arctan x)' = \frac{1}{1+x^2}$
$a^x \rightarrow a^x/lna$	$sinx \rightarrow -cos$	x	$\cos x \to \sin x$
$tanx \rightarrow -lncosx$	$\sec x \to \ln \tan(x/2)$	$+ \pi/4)$	$\tan^2 x \to tanx - x$
$cscx \rightarrow lntan\frac{x}{2}$	$\sin^2 x \to \frac{x}{2} - \frac{1}{2} \sin x \cos x$		$\cos^2 x \to \frac{x}{2} + \frac{1}{2} \sin x \cos x$
$\sec^2 x \to tanx$	$\frac{1}{\sqrt{a^2 - x^2}} \to \arcsin\left(\frac{x}{a}\right)$		$csc^2x \rightarrow -cotx$
$\frac{1}{a^2 - x^2}( x  <  a ) \rightarrow$	$\frac{1}{x^2 - a^2}( x  >  a ) \to \frac{1}{2a} \ln \frac{(x - a)}{x + a}$		
$\sqrt{a^2 - x^2} \to \frac{x}{2} \sqrt{a^2 - x}$	$\frac{1}{\sqrt{x^2 + a^2}} \to \ln\left(x + \sqrt{a^2 + x^2}\right)$		
$\sqrt{a^2 + x^2} \to \frac{x}{2}\sqrt{a^2 + x^2} + \frac{a}{2}$	$\frac{1}{\sqrt{x^2 - a^2}} \to \ln\left(x + \sqrt{x^2 - a^2}\right)$		
$\sqrt{x^2 - a^2} \to \frac{x}{2}\sqrt{x^2 - a^2} - \frac{a}{2}$	$\frac{1}{x\sqrt{a^2 - x^2}} \to -\frac{1}{a} \ln \frac{a + \sqrt{a^2 - x^2}}{x}$		
$\frac{1}{x\sqrt{x^2 - a^2}} \to \frac{1}{a}$		$\frac{1}{x^2} \to -\frac{1}{a} \ln \frac{a + \sqrt{a^2 + x^2}}{x}$	

$\frac{1}{\sqrt{2ax - x^2}} \to \arccos(1 - \frac{x}{a})$	$\frac{x}{ax+b} \to \frac{x}{a} - \frac{b}{a^2} \ln(ax+b)$		
$\sqrt{2ax - x^2} \to \frac{x - a}{2} \sqrt{2ax - x^2} + \frac{a^2}{2} \arcsin(\frac{x}{a} - 1)$			
$\frac{1}{x\sqrt{ax+b}}(b<0) \to \frac{2}{\sqrt{-b}}\arctan\sqrt{\frac{ax+b}{-b}}$	$x\sqrt{ax+b} \to \frac{2(3ax-2b)}{15a^2}(ax+b)^{\frac{3}{2}}$		
$\frac{1}{x\sqrt{ax+b}}(b>0) \to \frac{1}{\sqrt{-b}} \ln \frac{\sqrt{ax+b} - \sqrt{b}}{\sqrt{ax+b} + \sqrt{b}}$	$\frac{x}{\sqrt{ax+b}} \to \frac{2(ax-2b)}{3a^2} \sqrt{ax+b}$		
$\frac{1}{x^2\sqrt{ax+b}} \to -\frac{\sqrt{ax+b}}{bx} - \frac{a}{2b} \int \frac{dx}{x\sqrt{ax+b}}$	$\frac{\sqrt{ax+b}}{x} \to 2\sqrt{ax+b} + b \int \frac{dx}{x\sqrt{ax+b}}$		
$\frac{1}{\sqrt{(ax+b)^n}}(n>2) \to \frac{-2}{a(n-2)} \cdot \frac{1}{\sqrt{(ax+b)^{n-2}}}$			
$\frac{1}{ax^2 + c}(a > 0, c > 0) \to \frac{1}{\sqrt{ac}}\arctan(x\sqrt{\frac{a}{c}})$	$\frac{x}{ax^2 + c} \to \frac{1}{2a} \ln(ax^2 + c)$		
$\frac{1}{ax^2 + c}(a+,c-) \to \frac{1}{2\sqrt{-ac}} ln \frac{x\sqrt{a} - \sqrt{-c}}{x\sqrt{a} + \sqrt{-c}}$	$\frac{1}{-ac} \ln \frac{x\sqrt{a} - \sqrt{-c}}{x\sqrt{a} + \sqrt{-c}} \qquad \frac{1}{x(ax^2 + c)} \to \frac{1}{2c} \ln \frac{x^2}{ax^2 + c}$		
$\frac{1}{ax^2 + c}(a -, c +) \rightarrow \frac{1}{2\sqrt{-ac}} ln \frac{\sqrt{c} + x\sqrt{-a}}{\sqrt{c} - x\sqrt{-a}} \qquad x\sqrt{ax^2 + c} \rightarrow \frac{1}{3a} \sqrt{(ax^2 + c)^3}$			
$\frac{1}{(ax^2+c)^n}(n>1) \to \frac{x}{2c(n-1)(ax^2+c)^{n-1}} + \frac{2n-3}{2c(n-1)} \int \frac{dx}{(ax^2+c)^{n-1}}$			
$\frac{x^{n}}{ax^{2} + c}(n \neq 1) \to \frac{x^{n-1}}{a(n-1)} - \frac{c}{a} \int \frac{x^{n-2}}{ax^{2} + c} dx \qquad \frac{1}{x^{2}(ax^{2} + c)} \to \frac{-1}{cx} - \frac{a}{c} \int \frac{dx}{ax^{2} + c}$			
$\frac{1}{x^2(ax^2+c)^n}(n \ge 2) \to \frac{1}{c} \int \frac{dx}{x^2(ax^2+c)^{n-1}} - \frac{a}{c} \int \frac{dx}{(ax^2+c)^n}$			
$\sqrt{ax^2 + c}(a > 0) \to \frac{x}{2}\sqrt{ax^2 + c} + \frac{c}{2\sqrt{a}}\ln\left(x\sqrt{a} + \sqrt{ax^2 + c}\right)$			
$\sqrt{ax^2 + c}(a < 0) \to \frac{x}{2}\sqrt{ax^2 + c} + \frac{c}{2\sqrt{-a}}\arcsin\left(x\sqrt{\frac{-a}{c}}\right) \qquad \frac{1}{\sqrt{ax^2 + c}}(a < 0)$			
$\frac{1}{\sqrt{ax^2 + c}}(a > 0) \to \frac{1}{\sqrt{a}} \ln\left(x\sqrt{a} + \sqrt{ax^2}\right)$	$rac{1}{\sqrt{-a}} \arcsin\left(x\sqrt{-\frac{a}{c}}\right)$		

$\sin^2 ax \to \frac{x}{2} - \frac{1}{4a} \sin 2ax$	$\cos^2 ax \to \frac{x}{2} + \frac{1}{4a}\sin 2ax$		$\frac{1}{\sin ax} \to \frac{1}{a} \ln \tan \frac{ax}{2}$
$\frac{1}{\cos^2 ax} \to \frac{1}{a} \tan ax$	$\frac{1}{\cos ax} \to \frac{1}{a} \ln \tan \left( \frac{\pi}{4} + \frac{ax}{2} \right)$		$\ln(ax) \to x \ln(ax) - x$
$\sin^3 ax \to \frac{-1}{a}\cos ax + \frac{1}{3a}\cos^3 ax$		$\cos^3 ax \to \frac{1}{a}\sin ax - \frac{1}{3a}\sin^3 ax$	
$\frac{1}{\sin^2 ax} \to -\frac{1}{a}\cot ax$	$xln(ax) \rightarrow \frac{x^2}{2}$	$-\ln(ax) - \frac{x^2}{4}$	$\cos ax \to \frac{1}{a}\sin ax$
$x^2 e^{ax} \to \frac{e^{ax}}{a^3} (a^2 x^2 - 2ax + 2)$		$(\ln(ax))^2 \to x(\ln(ax))^2 - 2x\ln(ax) + 2x$	
$x^2 \ln(ax) \to \frac{x^3}{3} \ln(ax) - \frac{x^3}{9}$		$x^{n} \ln(ax) \to \frac{x^{n+1}}{n+1} \ln(ax) - \frac{x^{n+1}}{(n+1)^{2}}$	
$\sin(\ln ax) \to \frac{x}{2} [\sin(\ln ax) - \cos(\ln ax)]$		$\cos(\ln ax) \to \frac{x}{2} [\sin(\ln ax) + \cos(\ln ax)]$	