

Dracarys

Team Reference Library

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多边形与圆面积交

```

1 double areaCT(Point pa, Point pb, double r) {
2     if (pa.len() < pb.len()) swap(pa, pb);
3     if (sign(pb.len()) == 0) return 0;
4     double a = pb.len(), b = pa.len(), c = (pb - pa).len();
5     double sinB = fabs(det(pb, pb - pa) / a / c),
6         cosB = dot(pb, pb - pa) / a / c,
7         sinC = fabs(det(pa, pb) / a / b),
8         cosC = dot(pa, pb) / a / b;
9     double B = atan2(sinB, cosB), C = atan2(sinC, cosC);
10    if (a > r) {
11        S = C / 2 * r * r;
12        h = a * b * sinC / c;
13        if (h < r && B < PI / 2) {
14            S -= (acos(h / r) * r * r - h * sqrt(r * r - h * h));
15        }
16    } else if (b > r) {
17        double theta = PI - B - asin(sinB / r * a);
18        S = a * r * sin(theta) / 2 + (C - theta) / 2 * r * r;
19    } else {
20        S = sinC * a * b / 2;
21    }
22    return S;
23 }

```

二维几何

```

1 #include <iostream>
2 #include <cmath>
3 #include <vector>
4
5 using namespace std;
6
7 const double PI = acos(-1.0);
8 const double EPS = 1e-8;
9
10 int sign(double x)
11 {
12     return x < -EPS ? -1 : x > EPS;
13 }
14
15 double newSqrt(double x)
16 {
17     return x < 0 ? 0 : sqrt(x);
18 }
19

```

```

20 struct Point {
21     double x, y;
22     Point(double x = 0, double y = 0) : x(x), y(y) {}
23     Point operator + (const Point &that) const {
24         return Point(x + that.x, y + that.y);
25     }
26     Point operator - (const Point &that) const {
27         return Point(x - that.x, y - that.y);
28     }
29     Point operator * (const double &that) const {
30         return Point(x * that, y * that);
31     }
32     Point operator / (const double &that) const {
33         return Point(x / that, y / that);
34     }
35     Point rotate(const double ang) { // 逆时针旋转 ang 弧度
36         return Point(cos(ang) * x - sin(ang) * y, cos(ang) * y + sin(ang) * x);
37     }
38     Point turn90() { // 逆时针旋转 90 度
39         return Point(-y, x);
40     }
41     double len2() const {
42         return x * x + y * y;
43     }
44     double len() const {
45         return sqrt(x * x + y * y);
46     }
47     Point unit() const {
48         return *this / len();
49     }
50     int operator < (const Point &that) const {
51         int d = sign(x - that.x); if (d) return d < 0;
52         return sign(y - that.y) < 0;
53     }
54 };
55 double det(Point a, Point b)
56 {
57     return a.x * b.y - b.x * a.y;
58 }
59 double dot(Point a, Point b)
60 {
61     return a.x * b.x + a.y * b.y;
62 }
63 double det(Point s, Point a, Point b)
64 {

```

```

65     return (a.x - s.x) * (b.y - s.y) - (b.x - s.x) * (a.y - s.y);
66 }
67
68 struct Line {
69     Point a, b;
70     Line(Point a, Point b) : a(a), b(b) {}
71 };
72
73 Point isLL(const Line &l1, const Line &l2) {
74     double s1 = det(l2.b - l2.a, l1.a - l2.a),
75            s2 = -det(l2.b - l2.a, l1.b - l2.a);
76     return (l1.a * s2 + l1.b * s1) / (s1 + s2);
77 }
78 bool onSeg(const Line &l, const Point &p) { // 点在线段上
79     return sign(det(p - l.a, l.b - l.a)) == 0 && sign(dot(p - l.a, p - l.b)) <= 0;
80 }
81 Point projection(const Line &l, const Point &p) { // 点到直线投影
82     return l.a + (l.b - l.a) * (dot(p - l.a, l.b - l.a) / (l.b - l.a).len2());
83 }
84 double disToLine(const Line &l, const Point &p) {
85     return abs(det(p - l.a, l.b - l.a) / (l.b - l.a).len());
86 }
87 double disToSeg(const Line &l, const Point &p) { // 点到线段距离
88     return sign(dot(p - l.a, l.b - l.a)) * sign(dot(p - l.b, l.a - l.b)) != 1 ?
89         disToLine(l, p) : min((p - l.a).len(), (p - l.b).len());
90 }
91 Point symmetryPoint(const Point a, const Point b) { // 点 b 关于点 a 的中心对称点
92     return a + a - b;
93 }
94 Point reflection(const Line &l, const Point &p) { // 点关于直线的对称点
95     return symmetryPoint(projection(l, p), p);
96 }
97 struct Circle {
98     Point o;
99     double r;
100     Circle (Point o = Point(0, 0), double r = 0) : o(o), r(r) {}
101 };
102
103 // 求圆与直线的交点
104 bool isCL(Circle a, Line l, Point &p1, Point &p2) {
105     if (sign(det(l.a - a.o, l.b - a.o) / (l.a - l.b).len()) > 0) return false;
106     Point o = isLL(Line(a.o, a.o + (l.b - l.a).turn90()), l);
107     Point delta = (l.b - l.a).unit() * newSqrt(a.r * a.r - (o - a.o).len2());
108     p1 = o + delta;
109     p2 = o - delta;

```

```

110     return true;
111 }
112
113 // 求圆与圆的交面积
114 double areaCC(const Circle &c1, const Circle &c2) {
115     double d = (c1.o - c2.o).len();
116     if (sign(d - (c1.r + c2.r)) >= 0) {
117         return 0;
118     }
119     if (sign(d - abs(c1.r - c2.r)) <= 0) {
120         double r = min(c1.r, c2.r);
121         return r * r * PI;
122     }
123     double x = (d * d + c1.r * c1.r - c2.r * c2.r) / (2 * d),
124            t1 = acos(x / c1.r), t2 = acos((d - x) / c2.r);
125     return c1.r * c1.r * t1 + c2.r * c2.r * t2 - d * c1.r * sin(t1);
126 }
127
128 // 求圆与圆的交点, 注意调用前要先判定重圆
129 bool isCC(Circle a, Circle b, Point &p1, Point &p2) {
130     double s1 = (a.o - b.o).len();
131     if (sign(s1 - a.r - b.r) > 0 || sign(s1 - abs(a.r - b.r)) < 0) return false;
132     double s2 = (a.r * a.r - b.r * b.r) / s1;
133     double aa = (s1 + s2) * 0.5, bb = (s1 - s2) * 0.5;
134     Point o = (b.o - a.o) * (aa / (aa + bb)) + a.o;
135     Point delta = (b.o - a.o).unit().turn90() * newSqrt(a.r * a.r - aa * aa);
136     p1 = o + delta, p2 = o - delta;
137     return true;
138 }
139
140 // 求点到圆的切点, 按关于点的左手方向返回两个点
141 bool tanCP(const Circle &c, const Point &p0, Point &p1, Point &p2)
142 {
143     double x = (p0 - c.o).len2(), d = x - c.r * c.r;
144     if (d < EPS) return false;
145     Point p = (p0 - c.o) * (c.r * c.r / x);
146     Point delta = ((p0 - c.o) * (-c.r * sqrt(d) / x)).turn90();
147     p1 = c.o + p + delta;
148     p2 = c.o + p - delta;
149     return true;
150 }
151
152 // 求圆到圆的外公切线, 按关于 c1.o 的左手方向返回两条线
153 vector<Line> extanCC(const Circle &c1, const Circle &c2)
154 {

```

```

155 vector<Line> ret;
156 if (sign(c1.r - c2.r) == 0) {
157     Point dir = c2.o - c1.o;
158     dir = (dir * (c1.r / dir.len())).turn90();
159     ret.push_back(Line(c1.o + dir, c2.o + dir));
160     ret.push_back(Line(c1.o - dir, c2.o - dir));
161 } else {
162     Point p = (c1.o * -c2.r + c2.o * c1.r) / (c1.r - c2.r);
163     Point p1, p2, q1, q2;
164     if (tanCP(c1, p, p1, p2) && tanCP(c2, p, q1, q2)) {
165         if (c1.r < c2.r) swap(p1, p2), swap(q1, q2);
166         ret.push_back(Line(p1, q1));
167         ret.push_back(Line(p2, q2));
168     }
169 }
170 return ret;
171 }
172
173 // 求圆到圆的内共切线, 按关于 c1.o 的左手方向返回两条线
174 vector<Line> intanCC(const Circle &c1, const Circle &c2)
175 {
176     vector<Line> ret;
177     Point p = (c1.o * c2.r + c2.o * c1.r) / (c1.r + c2.r);
178     Point p1, p2, q1, q2;
179     if (tanCP(c1, p, p1, p2) && tanCP(c2, p, q1, q2)) {
180         ret.push_back(Line(p1, q1));
181         ret.push_back(Line(p2, q2));
182     }
183     return ret;
184 }
185
186 bool contain(vector<Point> polygon, Point p) { // 判断点 p
187     ↪ 是否被多边形包含, 包括落在边界上
188     int ret = 0, n = polygon.size();
189     for(int i = 0; i < n; ++i) {
190         Point u = polygon[i], v = polygon[(i + 1) % n];
191         if (onSeg(Line(u, v), p)) return true;
192         if (sign(u.y - v.y) <= 0) swap(u, v);
193         if (sign(p.y - u.y) > 0 || sign(p.y - v.y) <= 0) continue;
194         ret += sign(det(p, v, u)) > 0;
195     }
196     return ret & 1;
197 }
198 vector<Point> convexCut(const vector<Point>&ps, Line l) { // 用半平面 (q1,q2)
199     ↪ 的逆时针方向去切凸多边形

```

```

199 vector<Point> qs;
200 int n = ps.size();
201 for (int i = 0; i < n; ++i) {
202     Point p1 = ps[i], p2 = ps[(i + 1) % n];
203     int d1 = sign(det(l.a, l.b, p1)), d2 = sign(det(l.a, l.b, p2));
204     if (d1 >= 0) qs.push_back(p1);
205     if (d1 * d2 < 0) qs.push_back(isLL(Line(p1, p2), l));
206 }
207 return qs;
208 }
209 vector<Point> convexHull(vector<Point> ps) { // 求点集 ps 组成的凸包
210     int n = ps.size(); if (n <= 1) return ps;
211     sort(ps.begin(), ps.end());
212     vector<Point> qs;
213     for (int i = 0; i < n; qs.push_back(ps[i++]))
214         while (qs.size() > 1 && sign(det(qs[qs.size()-2], qs.back(), ps[i])) <= 0)
215             ↪ qs.pop_back();
216     for (int i = n - 2, t = qs.size(); i >= 0; qs.push_back(ps[i--]))
217         while ((int)qs.size() > t && sign(det(qs[(int)qs.size()-2], qs.back(), ps[i])) <=
218             ↪ 0) qs.pop_back();
219     qs.pop_back(); return qs;
220 }
221
222 int main()
223 {
224     Circle c1, c2;
225     c1.o = Point(0, 0); c1.r = 10;
226     c2.o = Point(10, 10); c1.r = 10;
227     Point p1, p2;
228     return 0;
229 }

```

$n \log n$ 半平面交

```

1 struct Point {
2     int quad() const { return sign(y) == 1 || (sign(y) == 0 && sign(x) >= 0); }
3 };
4 struct Line {
5     bool include(const Point &p) const { return sign(det(b - a, p - a)) > 0; }
6     Line push() const { // 将半平面向外推 eps
7         const double eps = 1e-6;
8         Point delta = (b - a).turn90().norm() * eps;
9         return Line(a - delta, b - delta);
10    }
11 };

```

```

12 bool sameDir(const Line &l0, const Line &l1) { return parallel(l0, l1) &&
    ↪ sign(dot(l0.b - l0.a, l1.b - l1.a)) == 1; }
13 bool operator < (const Point &a, const Point &b) {
14     if (a.quad() != b.quad()) {
15         return a.quad() < b.quad();
16     } else {
17         return sign(det(a, b)) > 0;
18     }
19 }
20 bool operator < (const Line &l0, const Line &l1) {
21     if (sameDir(l0, l1)) {
22         return l1.include(l0.a);
23     } else {
24         return (l0.b - l0.a) < (l1.b - l1.a);
25     }
26 }
27 bool check(const Line &u, const Line &v, const Line &w) { return
    ↪ w.include(intersect(u, v)); }
28 vector<Point> intersection(vector<Line> &l) {
29     sort(l.begin(), l.end());
30     deque<Line> q;
31     for (int i = 0; i < (int)l.size(); ++i) {
32         if (i && sameDir(l[i], l[i - 1])) {
33             continue;
34         }
35         while (q.size() > 1 && !check(q[q.size() - 2], q[q.size() - 1], l[i]))
36             ↪ q.pop_back();
37         while (q.size() > 1 && !check(q[1], q[0], l[i])) q.pop_front();
38         q.push_back(l[i]);
39     }
40     while (q.size() > 2 && !check(q[q.size() - 2], q[q.size() - 1], q[0]))
41         ↪ q.pop_back();
42     while (q.size() > 2 && !check(q[1], q[0], q[q.size() - 1])) q.pop_front();
43     vector<Point> ret;
44     for (int i = 0; i < (int)q.size(); ++i) ret.push_back(intersect(q[i], q[(i + 1) %
    ↪ q.size()]));
45     return ret;
46 }

```

Delaunay 三角剖分

```

1  /*
2  Delaunay Triangulation 随机增量算法 :
3  节点数至少为点数的 6 倍, 空间消耗较大注意计算内存使用
4  建图的过程在 build 中, 注意初始化内存池和初始三角形的坐标范围 (Triangulation::LOTS)
5  Triangulation::find 返回包含某点的三角形

```

```

6  Triangulation::add_point 将某点加入三角剖分
7  某个 Triangle 在三角剖分中当且仅当它的 has_children 为 0
8  如果要找到三角形 u 的邻域, 则枚举它的所有 u.edge[i].tri, 该条边的两个点为 u.p[(i+1)%3],
    ↪ u.p[(i+2)%3]
9  */
10 const int N = 100000 + 5, MAX_TRIS = N * 6;
11 const double EPSILON = 1e-6, PI = acos(-1.0);
12 struct Point {
13     double x, y; Point():x(0),y(0){} Point(double x, double y):x(x),y(y){}
14     bool operator ==(const Point &that) const { return x==that.x && y==that.y; }
15 };
16 inline double sqr(double x) { return x*x; }
17 double dist_sqr(Point const& a, Point const& b) { return sqr(a.x-b.x)+sqr(a.y-b.y); }
18 bool in_circumcircle(Point const& p1, Point const& p2, Point const& p3, Point const&
    ↪ p4) {
19     double u11 = p1.x - p4.x, u21 = p2.x - p4.x, u31 = p3.x - p4.x;
20     double u12 = p1.y - p4.y, u22 = p2.y - p4.y, u32 = p3.y - p4.y;
21     double u13 = sqr(p1.x) - sqr(p4.x) + sqr(p1.y) - sqr(p4.y);
22     double u23 = sqr(p2.x) - sqr(p4.x) + sqr(p2.y) - sqr(p4.y);
23     double u33 = sqr(p3.x) - sqr(p4.x) + sqr(p3.y) - sqr(p4.y);
24     double det = -u13*u22*u31 + u12*u23*u31 + u13*u21*u32 - u11*u23*u32 - u12*u21*u33
    ↪ + u11*u22*u33;
25     return det > EPSILON;
26 }
27 double side(Point const& a, Point const& b, Point const& p) { return
    ↪ (b.x-a.x)*(p.y-a.y) - (b.y-a.y)*(p.x-a.x); }
28 typedef int SideRef; struct Triangle; typedef Triangle* TriangleRef;
29 struct Edge {
30     TriangleRef tri; SideRef side; Edge() : tri(0), side(0) {}
31     Edge(TriangleRef tri, SideRef side) : tri(tri), side(side) {}
32 };
33 struct Triangle {
34     Point p[3]; Edge edge[3]; TriangleRef children[3]; Triangle() {}
35     Triangle(Point const& p0, Point const& p1, Point const& p2) {
36         p[0]=p0;p[1]=p1;p[2]=p2;children[0]=children[1]=children[2]=0;
37     }
38     bool has_children() const { return children[0] != 0; }
39     int num_children() const {
40         return children[0] == 0 ? 0
41             : children[1] == 0 ? 1
42             : children[2] == 0 ? 2 : 3;
43     }
44     bool contains(Point const& q) const {
45         double a=side(p[0],p[1],q), b=side(p[1],p[2],q), c=side(p[2],p[0],q);
46         return a >= -EPSILON && b >= -EPSILON && c >= -EPSILON;

```

```

47 }
48 } triangle_pool[MAX_TRIS], *tot_triangles;
49 void set_edge(Edge a, Edge b) {
50     if (a.tri) a.tri->edge[a.side] = b;
51     if (b.tri) b.tri->edge[b.side] = a;
52 }
53 class Triangulation {
54 public:
55     Triangulation() {
56         const double LOTS = 1e6;
57         the_root = new(tot_triangles++)
    ↪ Triangle(Point(-LOTS, -LOTS), Point(+LOTS, -LOTS), Point(0, +LOTS));
58     }
59     TriangleRef find(Point p) const { return find(the_root, p); }
60     void add_point(Point const& p) { add_point(find(the_root, p), p); }
61 private:
62     TriangleRef the_root;
63     static TriangleRef find(TriangleRef root, Point const& p) {
64         for( ; ; ) {
65             if (!root->has_children()) return root;
66             else for (int i = 0; i < 3 && root->children[i] ; ++i)
67                 if (root->children[i]->contains(p))
68                     {root = root->children[i]; break;}
69         }
70     }
71     void add_point(TriangleRef root, Point const& p) {
72         TriangleRef tab, tbc, tca;
73         tab = new(tot_triangles++) Triangle(root->p[0], root->p[1], p);
74         tbc = new(tot_triangles++) Triangle(root->p[1], root->p[2], p);
75         tca = new(tot_triangles++) Triangle(root->p[2], root->p[0], p);
76         set_edge(Edge(tab, 0), Edge(tbc, 1)); set_edge(Edge(tbc, 0), Edge(tca, 1));
77         set_edge(Edge(tca, 0), Edge(tab, 1)); set_edge(Edge(tab, 2), root->edge[2]);
78         set_edge(Edge(tbc, 2), root->edge[0]); set_edge(Edge(tca, 2), root->edge[1]);
79         root->children[0] = tab; root->children[1] = tbc; root->children[2] = tca;
80         flip(tab, 2); flip(tbc, 2); flip(tca, 2);
81     }
82     void flip(TriangleRef tri, SideRef pi) {
83         TriangleRef trj = tri->edge[pi].tri; int pj = tri->edge[pi].side;
84         if (!trj || !in_circumcircle(tri->p[0], tri->p[1], tri->p[2], trj->p[pj])) return;
85         TriangleRef trk = new(tot_triangles++) Triangle(tri->p[(pi+1)%3], trj->p[pj],
    ↪ tri->p[pi]);
86         TriangleRef trl = new(tot_triangles++) Triangle(trj->p[(pj+1)%3], tri->p[pi],
    ↪ trj->p[pj]);
87         set_edge(Edge(trk, 0), Edge(trl, 0));
88         set_edge(Edge(trk, 1), tri->edge[(pi+2)%3]); set_edge(Edge(trk, 2),
    ↪ trj->edge[(pj+1)%3]);

```

```

89         set_edge(Edge(trl, 1), trj->edge[(pj+2)%3]); set_edge(Edge(trl, 2),
    ↪ tri->edge[(pi+1)%3]);
90         tri->children[0] = trk; tri->children[1] = trl; tri->children[2] = 0;
91         trj->children[0] = trk; trj->children[1] = trl; trj->children[2] = 0;
92         flip(trk, 1); flip(trk, 2); flip(trl, 1); flip(trl, 2);
93     }
94 };
95 int n; Point ps[N];
96 void build(){
97     tot_triangles = triangle_pool; cin >> n;
98     for(int i = 0; i < n; ++i) scanf("%lf%lf", &ps[i].x, &ps[i].y);
99     random_shuffle(ps, ps + n); Triangulation tri;
100     for(int i = 0; i < n; ++i) tri.add_point(ps[i]);
101 }

```

三维几何操作合并

```

1 struct Point3D {
2     double x, y, z;
3 };
4 Point3D det(const Point3D &a, const Point3D &b) {
5     return Point3D(a.y * b.z - a.z * b.y, a.z * b.x - a.x * b.z, a.x * b.y - a.y *
    ↪ b.x);
6 }
7 // 平面法向量 : 平面上两个向量叉积
8 // 点共平面 : 平面上一点与之的向量点积法向量为 0
9 // 点在线段 ( 直线 ) 上 : 共线且两边点积非正
10 // 点在三角形内 ( 不包含边界, 需再判断是与某条边共线 )
11 bool pointInTri(const Point3D &a, const Point3D &b, const Point3D &c, const Point3D
    ↪ &p) {
12     return sign(det(a - b, a - c).len() - det(p - a, p - b).len() - det(p - b, p -
    ↪ c).len() - det(p - c, p - a).len()) == 0;
13 }
14 // 共平面的两点是否在这平面上一条直线的同侧
15 bool sameSide(const Point3D &a, const Point3D &b, const Point3D &p0, const Point3D
    ↪ &p1) {
16     return sign(dot(det(a - b, p0 - b), det(a - b, p1 - b))) > 0;
17 }
18 // 两点在平面同侧 : 点积法向量符号相同
19 // 两直线平行 / 垂直 : 同二维
20 // 平面平行 / 垂直 : 判断法向量
21 // 线面垂直 : 法向量和直线平行
22 // 判断空间线段是否相交 : 四点共面两线段不平行相互在异侧
23 // 线段和三角形是否相交 : 线段在三角形平面不同侧
    ↪ 三角形任意两点在线段和第三点组成的平面的不同侧

```

```

24 // 求空间直线交点
25 Point3D intersection(const Point3D &a0, const Point3D &b0, const Point3D &a1, const
    ↪ Point3D &b1) {
26     double t = ((a0.x - a1.x) * (a1.y - b1.y) - (a0.y - a1.y) * (a1.x - b1.x)) /
    ↪ ((a0.x - b0.x) * (a1.y - b1.y) - (a0.y - b0.y) * (a1.x - b1.x));
27     return a0 + (b0 - a0) * t;
28 }
29 // 求平面和直线的交点
30 Point3D intersection(const Point3D &a, const Point3D &b, const Point3D &c, const
    ↪ Point3D &l0, const Point3D &l1) {
31     Point3D p = pVec(a, b, c); // 平面法向量
32     double t = (p.x * (a.x - l0.x) + p.y * (a.y - l0.y) + p.z * (a.z - l0.z)) / (p.x *
    ↪ (l1.x - l0.x) + p.y * (l1.y - l0.y) + p.z * (l1.z - l0.z));
33     return l0 + (l1 - l0) * t;
34 }
35 // 求平面交线：取不平行的一条直线的一个交点，以及法向量叉积得到直线方向
36 // 点到直线距离：叉积得到三角形的面积除以底边
37 // 点到平面距离：点积法向量
38 // 直线间距离：平行时随便取一点求距离，否则叉积方向向量得到方向点积计算长度
39 // 直线夹角：点积 平面夹角：法向量点积
40 // 三维向量旋转操作(绕向量 s 旋转 ang 角度)，对于右手系 s 指向观察者时逆时针
41 // 矩阵版
42 void rotate(const Point3D &s, double ang) {
43     double l = s.len(), x = s.x / l, y = s.y / l, z = s.z / l, sinA = sin(ang), cosA =
    ↪ cos(ang);
44     double p[4][4] = {cosA + (1 - cosA) * x * x, (1 - cosA) * x * y - sinA * z, (1 -
    ↪ cosA) * x * z + sinA * y, 0,
45         (1 - cosA) * y * x + sinA * z, cosA + (1 - cosA) * y * y, (1 - cosA) * y * z -
    ↪ sinA * x, 0,
46         (1 - cosA) * z * x - sinA * y, (1 - cosA) * z * y + sinA * x, cosA + (1 - cosA)
    ↪ * z * z, 0,
47         0, 0, 0, 1 };
48 }
49 // 计算版：把需要旋转的向量按照 s 分解，做二维旋转，再回到三维

```

三维凸包

```

1 #define SIZE(X) (int(X.size()))
2 #define PI 3.14159265358979323846264338327950288
3 struct Point {
4     Point cross(const Point &p) const
5     { return Point(y * p.z - z * p.y, z * p.x - x * p.z, x * p.y - y * p.x); }
6 } info[1005];
7 int mark[1005][1005], n, cnt;
8 double mix(const Point &a, const Point &b, const Point &c)
9 { return a.dot(b.cross(c)); }

```

```

10 double area(int a, int b, int c)
11 { return ((info[b] - info[a]).cross(info[c] - info[a])).length(); }
12 double volume(int a, int b, int c, int d)
13 { return mix(info[b] - info[a], info[c] - info[a], info[d] - info[a]); }
14 struct Face {
15     int a, b, c; Face() {}
16     Face(int a, int b, int c): a(a), b(b), c(c) {}
17     int &operator [](int k)
18     { if (k == 0) return a; if (k == 1) return b; return c; }
19 };
20 vector<Face> face;
21 inline void insert(int a, int b, int c) { face.push_back(Face(a, b, c)); }
22 void add(int v) {
23     vector<Face> tmp; int a, b, c; cnt++;
24     for (int i = 0; i < SIZE(face); i++) {
25         a = face[i][0]; b = face[i][1]; c = face[i][2];
26         if (Sign(volume(v, a, b, c)) < 0)
27             mark[a][b] = mark[b][a] = mark[b][c] = mark[c][b] = mark[c][a] = mark[a][c] =
    ↪ cnt;
28         else tmp.push_back(face[i]);
29     } face = tmp;
30     for (int i = 0; i < SIZE(tmp); i++) {
31         a = face[i][0]; b = face[i][1]; c = face[i][2];
32         if (mark[a][b] == cnt) insert(b, a, v);
33         if (mark[b][c] == cnt) insert(c, b, v);
34         if (mark[c][a] == cnt) insert(a, c, v);
35     }
36 int Find() {
37     for (int i = 2; i < n; i++) {
38         Point ndir = (info[0] - info[i]).cross(info[1] - info[i]);
39         if (ndir == Point()) continue; swap(info[i], info[2]);
40         for (int j = i + 1; j < n; j++) if (Sign(volume(0, 1, 2, j)) != 0) {
41             swap(info[j], info[3]); insert(0, 1, 2); insert(0, 2, 1); return 1;
42         } return 0; }
43 int main() {
44     for (; scanf("%d", &n) == 1; ) {
45         for (int i = 0; i < n; i++) info[i].Input();
46         sort(info, info + n); n = unique(info, info + n) - info;
47         face.clear(); random_shuffle(info, info + n);
48         if (Find()) { memset(mark, 0, sizeof(mark)); cnt = 0;
49             for (int i = 3; i < n; i++) add(i); vector<Point> Ndir;
50             for (int i = 0; i < SIZE(face); ++i) {
51                 Point p = (info[face[i][0]] - info[face[i][1]]).cross(
52                     info[face[i][2]] - info[face[i][1]]);
53                 p = p / p.length(); Ndir.push_back(p);

```



```

54     } sort(Ndir.begin(), Ndir.end());
55     int ans = unique(Ndir.begin(), Ndir.end()) - Ndir.begin();
56     printf("%d\n", ans);
57     } else printf("1\n");
58 } }
59 // 求重心
60 double calcDist(const Point &p, int a, int b, int c)
61 { return fabs(mix(info[a] - p, info[b] - p, info[c] - p) / area(a, b, c)); }
62 //compute the minimal distance of center of any faces
63 double findDist() { //compute center of mass
64     double totalWeight = 0; Point center(.0, .0, .0);
65     Point first = info[face[0][0]];
66     for (int i = 0; i < SIZE(face); ++i) {
67         Point p = (info[face[i][0]]+info[face[i][1]]+info[face[i][2]]+first)*.25;
68         double weight = mix(info[face[i][0]] - first, info[face[i][1]]
69             - first, info[face[i][2]] - first);
70         totalWeight += weight; center = center + p * weight;
71     } center = center / totalWeight;
72     double res = 1e100; //compute distance
73     for (int i = 0; i < SIZE(face); ++i)
74         res = min(res, calcDist(center, face[i][0], face[i][1], face[i][2]));
75     return res; }

```

凸包上快速询问

```

1  /*
2   给定凸包, log n 内完成各种询问, 具体操作有 :
3   1. 判定一个点是否在凸包内
4   2. 询问凸包外的点到凸包的两个切点
5   3. 询问一个向量关于凸包的切点
6   4. 询问一条直线和凸包的交点
7   INF 为坐标范围, 需要定义点类大于号
8   改成实数只需修改 sign 函数, 以及把 long long 改为 double 即可
9   构造函数时传入凸包要求无重点, 面积非空, 以及 pair(x,y) 的最小点放在第一个
10 */
11 const int INF = 1000000000;
12 struct Convex
13 {
14     int n;
15     vector<Point> a, upper, lower;
16     Convex(vector<Point> _a) : a(_a) {
17         n = a.size();
18         int ptr = 0;
19         for(int i = 1; i < n; ++ i) if (a[ptr] < a[i]) ptr = i;
20         for(int i = 0; i <= ptr; ++ i) lower.push_back(a[i]);
21         for(int i = ptr; i < n; ++ i) upper.push_back(a[i]);

```

```

22     upper.push_back(a[0]);
23 }
24 int sign(long long x) { return x < 0 ? -1 : x > 0; }
25 pair<long long, int> get_tangent(vector<Point> &convex, Point vec) {
26     int l = 0, r = (int)convex.size() - 2;
27     for( ; l + 1 < r; ) {
28         int mid = (l + r) / 2;
29         if (sign((convex[mid + 1] - convex[mid]).det(vec)) > 0) r = mid;
30         else l = mid;
31     }
32     return max(make_pair(vec.det(convex[r]), r), make_pair(vec.det(convex[0]), 0));
33 }
34 void update_tangent(const Point &p, int id, int &i0, int &i1) {
35     if ((a[i0] - p).det(a[id] - p) > 0) i0 = id;
36     if ((a[i1] - p).det(a[id] - p) < 0) i1 = id;
37 }
38 void binary_search(int l, int r, Point p, int &i0, int &i1) {
39     if (l == r) return;
40     update_tangent(p, l % n, i0, i1);
41     int s1 = sign((a[l % n] - p).det(a[(l + 1) % n] - p));
42     for( ; l + 1 < r; ) {
43         int mid = (l + r) / 2;
44         int smid = sign((a[mid % n] - p).det(a[(mid + 1) % n] - p));
45         if (smid == s1) l = mid;
46         else r = mid;
47     }
48     update_tangent(p, r % n, i0, i1);
49 }
50 int binary_search(Point u, Point v, int l, int r) {
51     int s1 = sign((v - u).det(a[l % n] - u));
52     for( ; l + 1 < r; ) {
53         int mid = (l + r) / 2;
54         int smid = sign((v - u).det(a[mid % n] - u));
55         if (smid == s1) l = mid;
56         else r = mid;
57     }
58     return l % n;
59 }
60 // 判定点是否在凸包内, 在边界返回 true
61 bool contain(Point p) {
62     if (p.x < lower[0].x || p.x > lower.back().x) return false;
63     int id = lower_bound(lower.begin(), lower.end(), Point(p.x, -INF)) -
        lower.begin();
64     if (lower[id].x == p.x) {
65         if (lower[id].y > p.y) return false;

```



```

40     for (int j = 0; j < C; ++j) {
41         if (j != i && !overlap(c[j], c[i]) && !overlap(c[i], c[j]) && intersect(c[i],
42             ↪ c[j])) {
43             addEvent(c[i], c[j], evt, cnt);
44         }
45     }
46     if (evt.size() == 0) {
47         area[cnt] += PI * c[i].r * c[i].r;
48     } else {
49         sort(evt.begin(), evt.end());
50         evt.push_back(evt.front());
51         for (int j = 0; j + 1 < (int)evt.size(); ++j) {
52             cnt += evt[j].delta;
53             area[cnt] += det(evt[j].p, evt[j + 1].p) / 2;
54             double ang = evt[j + 1].ang - evt[j].ang;
55             if (ang < 0) {
56                 ang += PI * 2;
57             }
58             area[cnt] += ang * c[i].r * c[i].r / 2 - sin(ang) * c[i].r * c[i].r / 2;
59         }
60     }
61 }

```

三角形的心

```

1 Point inCenter(const Point &A, const Point &B, const Point &C) { // 内心
2     double a = (B - C).len(), b = (C - A).len(), c = (A - B).len(),
3         s = fabs(det(B - A, C - A)),
4         r = s / p;
5     return (A * a + B * b + C * c) / (a + b + c);
6 }
7 Point circumCenter(const Point &a, const Point &b, const Point &c) { // 外心
8     Point bb = b - a, cc = c - a;
9     double db = bb.len2(), dc = cc.len2(), d = 2 * det(bb, cc);
10    return a - Point(bb.y * dc - cc.y * db, cc.x * db - bb.x * dc) / d;
11 }
12 Point orthoCenter(const Point &a, const Point &b, const Point &c) { // 垂心
13     Point ba = b - a, ca = c - a, bc = b - c;
14     double Y = ba.y * ca.y * bc.y,
15         A = ca.x * ba.y - ba.x * ca.y,
16         x0 = (Y + ca.x * ba.y * b.x - ba.x * ca.y * c.x) / A,
17         y0 = -ba.x * (x0 - c.x) / ba.y + ca.y;
18     return Point(x0, y0);
19 }

```

最小覆盖球

```

1 int nouter; Tpoint outer[4], res; double radius;
2 void ball() {

```

```

3 Tpoint q[3]; double m[3][3], sol[3], L[3], det;
4 int i, j; res.x = res.y = res.z = radius = 0;
5 for (i=0; i<3; ++i) q[i]=outer[i+1]-outer[0], sol[i]=dot(q[i], q[i]);
6 for (i=0; i<3; ++i) for (j=0; j<3; ++j) m[i][j]=dot(q[i], q[j])*2;
7 det= m[0][0]*m[1][1]*m[2][2]
8 + m[0][1]*m[1][2]*m[2][0]
9 + m[0][2]*m[2][1]*m[1][0]
10 - m[0][2]*m[1][1]*m[2][0]
11 - m[0][1]*m[1][0]*m[2][2]
12 - m[0][0]*m[1][2]*m[2][1];
13 if ( fabs(det)<eps ) return;
14 for (j=0; j<3; ++j) {
15     for (i=0; i<3; ++i) m[i][j]=sol[i];
16     L[j]=( m[0][0]*m[1][1]*m[2][2]
17 + m[0][1]*m[1][2]*m[2][0]
18 + m[0][2]*m[2][1]*m[1][0]
19 - m[0][2]*m[1][1]*m[2][0]
20 - m[0][1]*m[1][0]*m[2][2]
21 - m[0][0]*m[1][2]*m[2][1]
22 ) / det;
23     for (i=0; i<3; ++i) m[i][j]=dot(q[i], q[j])*2;
24 } res=outer[0];
25 for (i=0; i<3; ++i ) res = res + q[i] * L[i];
26 radius=dist2(res, outer[0]);
27 }

```

经纬度求球面最短距离

```

1 double sphereDis(double lon1, double lat1, double lon2, double lat2, double R) {
2     return R * acos(cos(lat1) * cos(lat2) * cos(lon1 - lon2) + sin(lat1) * sin(lat2));
3 }

```

长方体表面两点最短距离

```

1 int r;
2 void turn(int i, int j, int x, int y, int z, int x0, int y0, int L, int W, int H) {
3     if (z==0) { int R = x*x+y*y; if (R<r) r=R;
4     } else {
5         if(i>=0 && i< 2) turn(i+1, j, x0+L+z, y, x0+L-x, x0+L, y0, H, W, L);
6         if(j>=0 && j< 2) turn(i, j+1, x, y0+W+z, y0+W-y, x0, y0+W, L, H, W);
7         if(i<=0 && i>-2) turn(i-1, j, x0-z, y, x-x0, x0-H, y0, H, W, L);
8         if(j<=0 && j>-2) turn(i, j-1, x, y0-z, y-y0, x0, y0-H, L, H, W);
9     }
10 int main(){
11     int L, H, W, x1, y1, z1, x2, y2, z2;
12     cin >> L >> W >> H >> x1 >> y1 >> z1 >> x2 >> y2 >> z2;

```

```

13  if (z1!=0 && z1!=H) if (y1==0 || y1==W)
14      swap(y1,z1), std::swap(y2,z2), std::swap(W,H);
15  else swap(x1,z1), std::swap(x2,z2), std::swap(L,H);
16  if (z1==H) z1=0, z2=H-z2;
17  r=0x3fffffff; turn(0,0,x2-x1,y2-y1,z2,-x1,-y1,L,W,H);
18  cout<<r<<endl; return 0;
19  }

```

最大团

```

1  // Super Fast Maximum Clique
2  // To Build Graph: Maxclique(Edges, Number of Nodes)
3  // To Get Answer: mcqdyn(AnswerNodes Index Array, AnswerLength)
4  typedef bool BB[N];
5  struct Maxclique {
6      const BB* e; int pk, level; const float Tlimit;
7      struct Vertex{ int i, d; Vertex(int i):i(i),d(0){} };
8      typedef vector<Vertex> Vertices; typedef vector<int> ColorClass;
9      Vertices V; vector<ColorClass> C; ColorClass QMAX, Q;
10     static bool desc_degree(const Vertex &vi, const Vertex &vj){
11         return vi.d > vj.d;
12     }
13     void init_colors(Vertices &v){
14         const int max_degree = v[0].d;
15         for(int i = 0; i < (int)v.size(); i++) v[i].d = min(i, max_degree) + 1;
16     }
17     void set_degrees(Vertices &v){
18         for(int i = 0, j; i < (int)v.size(); i++)
19             for(v[i].d = j = 0; j < (int)(v.size()); j++)
20                 v[i].d += e[v[i].i][v[j].i];
21     }
22     struct StepCount{ int i1, i2; StepCount():i1(0),i2(0){} };
23     vector<StepCount> S;
24     bool cut1(const int pi, const ColorClass &A){
25         for(int i = 0; i < (int)A.size(); i++) if (e[pi][A[i]]) return true;
26         return false;
27     }
28     void cut2(const Vertices &A, Vertices &B){
29         for(int i = 0; i < (int)A.size() - 1; i++)
30             if(e[A.back().i][A[i].i])
31                 B.push_back(A[i].i);
32     }
33     void color_sort(Vertices &R){
34         int j = 0, maxno = 1, min_k = max((int)QMAX.size() - (int)Q.size() + 1, 1);
35         C[1].clear(), C[2].clear();
36         for(int i = 0; i < (int)R.size(); i++) {

```

```

37         int pi = R[i].i, k = 1;
38         while(cut1(pi, C[k])) k++;
39         if(k > maxno) maxno = k, C[maxno + 1].clear();
40         C[k].push_back(pi);
41         if(k < min_k) R[j++].i = pi;
42     }
43     if(j > 0) R[j - 1].d = 0;
44     for(int k = min_k; k <= maxno; k++)
45         for(int i = 0; i < (int)C[k].size(); i++)
46             R[j].i = C[k][i], R[j++].d = k;
47 }
48 void expand_dyn(Vertices &R){// diff -> diff with no dyn
49     S[level].i1 = S[level].i1 + S[level - 1].i1 - S[level].i2;//diff
50     S[level].i2 = S[level - 1].i1;//diff
51     while((int)R.size()) {
52         if((int)Q.size() + R.back().d > (int)QMAX.size()){
53             Q.push_back(R.back().i); Vertices Rp; cut2(R, Rp);
54             if((int)Rp.size()){
55                 if((float)S[level].i1 / ++pk < Tlimit) degree_sort(Rp);//diff
56                 color_sort(Rp);
57                 S[level].i1++, level++;//diff
58                 expand_dyn(Rp);
59                 level--;//diff
60             }
61             else if((int)Q.size() > (int)QMAX.size()) QMAX = Q;
62             Q.pop_back();
63         }
64         else return;
65         R.pop_back();
66     }
67 }
68 void mcqdyn(int* maxclique, int &sz){
69     set_degrees(V); sort(V.begin(),V.end(), desc_degree); init_colors(V);
70     for(int i = 0; i < (int)V.size() + 1; i++) S[i].i1 = S[i].i2 = 0;
71     expand_dyn(V); sz = (int)QMAX.size();
72     for(int i = 0; i < (int)QMAX.size(); i++) maxclique[i] = QMAX[i];
73 }
74 void degree_sort(Vertices &R){
75     set_degrees(R); sort(R.begin(), R.end(), desc_degree);
76 }
77 Maxclique(const BB* conn, const int sz, const float tt = 0.025) \
78 : pk(0), level(1), Tlimit(tt){
79     for(int i = 0; i < sz; i++) V.push_back(Vertex(i));
80     e = conn, C.resize(sz + 1), S.resize(sz + 1);
81 }

```

82 };

KM

```

1 // 最小匹配, 自带初始化 n <= m 方案存在 p[] 中
2 const int N = 105;
3 const int INF = 1000000000; // 严格大于最大边权
4 int n, m, a[N][N];
5 int u[N], v[N], p[N], fa[N], minv[N];
6 bool used[N];
7 int km() {
8     memset(u, 0, sizeof(int) * n);
9     for (int i = 0; i <= m; ++i) v[i] = 0, p[i] = n;
10    for (int i = 0; i < n; ++i) {
11        p[m] = i;
12        int j0 = m;
13        for (int j = 0; j <= m; ++j) minv[j] = INF, used[j] = false;
14        do {
15            used[j0] = true;
16            int i0 = p[j0], delta = INF, j1;
17            for (int j = 0; j < m; ++j) {
18                if (!used[j]) {
19                    int cur = a[i0][j] - u[i0] - v[j];
20                    if (cur < minv[j]) minv[j] = cur, fa[j] = j0;
21                    if (minv[j] < delta) delta = minv[j], j1 = j;
22                }
23            }
24            for (int j = 0; j <= m; ++j) {
25                if (used[j]) {
26                    u[p[j]] += delta, v[j] -= delta;
27                } else {
28                    minv[j] -= delta;
29                }
30            }
31            j0 = j1;
32        } while (p[j0] != n);
33        do {
34            int j1 = fa[j0];
35            p[j0] = p[j1];
36            j0 = j1;
37        } while (j0 != m);
38    }
39    return -v[m];
40 }

```

最小树形图

```

1 namespace LIUZHU{
2     const int MAXN;
3     int from[MAXN + 10][MAXN * 2 + 10];
4     int n, m;
5     int edge[MAXN + 10][MAXN * 2 + 10];
6     int sel[MAXN * 2 + 10], fa[MAXN * 2 + 10];
7     int vis[MAXN * 2 + 10];
8     const int INF; // INF >= sum( W_ij )
9     int getfa(int x){
10         if(x == fa[x]) return x;
11         return fa[x] = getfa(fa[x]);
12     }
13 void liuzhu(){ // 1-base: root is 1, answer = (sel[i], i) for i in [2..n]
14     fa[1] = 1;
15     for(int i = 2; i <= n; ++i){
16         sel[i] = 1;
17         fa[i] = i;
18         for(int j = 1; j <= n; ++j) if(fa[j] != i){
19             from[j][i] = i;
20             if(edge[sel[i]][i] > edge[j][i]) sel[i] = j;
21         }
22     }
23     int limit = n;
24     while(1){
25         int prelimit = limit;
26         memset(vis, 0, sizeof(vis));
27         vis[1] = 1;
28         for(int i = 2; i <= prelimit; ++i) if(fa[i] == i && !vis[i]){
29             int j = i;
30             while(!vis[j]){
31                 vis[j] = i;
32                 j = getfa(sel[j]);
33             }
34             if(j == 1 || vis[j] != i) continue;
35             vector<int> C;
36             int k = j;
37             do{
38                 C.push_back(k);
39                 k = getfa(sel[k]);
40             }while(k != j);
41             ++limit;
42             for(int i = 1; i <= n; ++i){
43                 edge[i][limit] = INF;
44                 from[i][limit] = limit;

```

```

45     }
46     fa[limit] = vis[limit] = limit;
47     for(int i = 0; i < int(C.size()); ++i){
48         int x = C[i];
49         fa[x] = limit;
50         for(int j = 1; j <= n; ++j){
51             if(edge[j][x] != INF && edge[j][limit] > edge[j][x] - edge[sel[x]][x]){
52                 edge[j][limit] = edge[j][x] - edge[sel[x]][x];
53                 from[j][limit] = x;
54             }
55         }
56     }
57     for(int j = 1; j <= n; ++j) if(getfa(j) == limit){
58         edge[j][limit] = INF;
59     }
60     sel[limit] = 1;
61     for(int j = 1; j <= n; ++j){
62         if(edge[sel[limit]][limit] > edge[j][limit]){
63             sel[limit] = j;
64         }
65     }
66 }
67 if(prelimit == limit) break;
68 }
69 for(int i = limit; i > 1; --i){
70     sel[from[sel[i]][i]] = sel[i];
71 }
72 }
73 }

```

无向图最小割

```

1  int cost[maxn][maxn], seq[maxn], len[maxn], n, m, pop, ans;
2  bool used[maxn];
3  void Init(){
4      int i, j, a, b, c;
5      for(i=0; i<n; i++) for(j=0; j<n; j++) cost[i][j]=0;
6      for(i=0; i<m; i++){
7          scanf("%d %d %d", &a, &b, &c); cost[a][b]+=c; cost[b][a]+=c;
8      }
9      pop=n; for(i=0; i<n; i++) seq[i]=i;
10 }
11 void Work(){
12     ans=inf; int i, j, k, l, mm, sum, pk;
13     while(pop > 1){
14         for(i=1; i<pop; i++) used[seq[i]]=0; used[seq[0]]=1;

```

```

15         for(i=1; i<pop; i++) len[seq[i]]=cost[seq[0]][seq[i]];
16         pk=0; mm=-inf; k=-1;
17         for(i=1; i<pop; i++) if(len[seq[i]] > mm){ mm=len[seq[i]]; k=i; }
18         for(i=1; i<pop; i++){
19             used[seq[l=k]]=1;
20             if(i==pop-2) pk=k;
21             if(i==pop-1) break;
22             mm=-inf;
23             for(j=1; j<pop; j++) if(!used[seq[j]])
24                 if((len[seq[j]]+cost[seq[l]][seq[j]]) > mm)
25                     mm=len[seq[j]], k=j;
26         }
27         sum=0;
28         for(i=0; i<pop; i++) if(i != k) sum+=cost[seq[k]][seq[i]];
29         ans=min(ans, sum);
30         for(i=0; i<pop; i++)
31             cost[seq[k]][seq[i]]=cost[seq[i]][seq[k]]+cost[seq[pk]][seq[i]];
32         seq[pk]=seq[--pop];
33     }
34     printf("%d\n", ans);
35 }

```

带花树

```

1  vector<int> link[maxn];
2  int n, match[maxn], Queue[maxn], head, tail;
3  int pred[maxn], base[maxn], start, finish, newbase;
4  bool InQueue[maxn], InBlossom[maxn];
5  void push(int u){ Queue[tail++]=u; InQueue[u]=true; }
6  int pop(){ return Queue[head++]; }
7  int FindCommonAncestor(int u, int v){
8      bool InPath[maxn];
9      for(int i=0; i<n; i++) InPath[i]=0;
10     while(true){ u=base[u]; InPath[u]=true; if(u==start) break; u=pred[match[u]]; }
11     while(true){ v=base[v]; if(InPath[v]) break; v=pred[match[v]]; }
12     return v;
13 }
14 void ResetTrace(int u){
15     int v;
16     while(base[u]!=newbase){
17         v=match[u];
18         InBlossom[base[u]]=InBlossom[base[v]]=true;
19         u=pred[v];
20         if(base[u]!=newbase) pred[u]=v;
21     }
22 }

```

```

23 void BlossomContract(int u,int v){
24     newbase=FindCommonAncestor(u,v);
25     for (int i=0;i<n;i++)
26         InBlossom[i]=0;
27     ResetTrace(u);ResetTrace(v);
28     if(base[u]!=newbase) pred[u]=v;
29     if(base[v]!=newbase) pred[v]=u;
30     for(int i=0;i<n;++i)
31         if(InBlossom[base[i]]){
32             base[i]=newbase;
33             if(!InQueue[i]) push(i);
34         }
35     }
36 bool FindAugmentingPath(int u){
37     bool found=false;
38     for(int i=0;i<n;++i) pred[i]=-1,base[i]=i;
39     for (int i=0;i<n;i++) InQueue[i]=0;
40     start=u;finish=-1; head=tail=0; push(start);
41     while(head<tail){
42         int u=pop();
43         for(int i=link[u].size()-1;i>=0;i--){
44             int v=link[u][i];
45             if(base[u]!=base[v]&&match[u]!=v)
46                 if(v==start||(match[v]>=0&&pred[match[v]]>=0)){
47                     BlossomContract(u,v);
48                     else if(pred[v]==-1){
49                         pred[v]=u;
50                         if(match[v]>=0) push(match[v]);
51                         else{ finish=v; return true; }
52                     }
53                 }
54             }
55         return found;
56     }
57 void AugmentPath(){
58     int u=finish,v,w;
59     while(u>=0){ v=pred[u];w=match[v];match[v]=u;match[u]=v;u=w; }
60 }
61 void FindMaxMatching(){
62     for(int i=0;i<n;++i) match[i]=-1;
63     for(int i=0;i<n;++i) if(match[i]==-1) if(FindAugmentingPath(i)) AugmentPath();
64 }

```

Hopcroft

```

1 int from[1010],wh[1010],g[1010];
2 int num[100010],nxt[100010],tot;
3 int n,m,ans,h,t,q[1010],dx[1010],dy[1010];
4 bool bfs(){
5     bool ret=false;
6     h=0;t=0;
7     for(int i=0;i<n;i++) if(wh[i]==-1) t++, q[t]=i;
8     memset(dx,0,sizeof(dx)), memset(dy,0,sizeof(dy));
9     while(h<=t){
10         for(int i=g[q[h]];i!=0;i=nxt[i])
11             if(dy[num[i]]==0){
12                 dy[num[i]]=dx[q[h]]+1;
13                 if(from[num[i]]==-1) ret=true;
14                 else{
15                     dx[from[num[i]]]=dx[q[h]]+2;
16                     q[++t]=from[num[i]];
17                 }
18             }
19     }
20     return ret;
21 }
22 bool dfs(int x){
23     for(int i=g[x];i!=0;i=nxt[i]){
24         if(dy[num[i]]==dx[x]+1){
25             dy[num[i]]=0;
26             if(from[num[i]]==-1||dfs(from[num[i]])){
27                 wh[x]=num[i];from[num[i]]=x;return true;
28             }
29         }
30     }
31     return false;
32 }
33 void hopcroft(){
34     memset(from,-1,sizeof(from)), memset(wh,-1,sizeof(wh));
35     while(bfs())
36         for(int i=0;i<n;i++)
37             if(wh[i]==-1&&dfs(i)) ans++;
38 }
39 void insert(int x,int y){ tot++;num[tot]=y;nxt[tot]=g[x];g[x]=tot; }
40 int main(){
41     while(scanf("%d %d",&n,&m)==2){
42         tot=0; memset(g,0,sizeof(g));
43         for(int i=0;i<n;i++){
44             int x; scanf("%d",&x);

```



```

45     for(int j=0;j<x;j++){
46         int y; scanf("%d",&y);
47         y--; insert(i,y);
48     }
49 }
50 ans=0; hopcroft(); printf("%d\n",ans);
51 }
52 }

```

素数判定

```

1 int strong_pseudo_primetest(long long n,int base) {
2     long long n2=n-1,res;
3     int s=0;
4     while(n2%2==0) n2>>=1,s++;
5     res=powmod(base,n2,n);
6     if((res==1)|| (res==n-1)) return 1;
7     s--;
8     while(s>=0) {
9         res=mulmod(res,res,n);
10        if(res==n-1) return 1;
11        s--;
12    }
13    return 0; // n is not a strong pseudo prime
14 }
15 int isprime(long long n) {
16     static LL testNum[]={2,3,5,7,11,13,17,19,23,29,31,37};
17     static LL lim[]={4,0,1373653LL,25326001LL,2500000000LL,2152302898747LL, \
18     3474749660383LL,341550071728321LL,0,0,0,0};
19     if(n<2||n==3215031751LL) return 0;
20     for(int i=0;i<12;++i){
21         if(n<lim[i]) return 1;
22         if(strong_pseudo_primetest(n,testNum[i])==0) return 0;
23     }
24     return 1;
25 }

```

启发式分解

```

1 int ansn; LL ans[1000];
2 LL func(LL x,LL n){ return(mod_mul(x,x,n)+1)%n; }
3 LL Pollard(LL n){
4     LL i,x,y,p;
5     if(Rabin_Miller(n)) return n;
6     if(!(n&1)) return 2;
7     for(i=1;i<20;i++){
8         x=i; y=func(x,n); p=gcd(y-x,n);

```

```

9         while(p==1) {x=func(x,n); y=func(func(y,n),n); p=gcd((y-x+n)%n,n)%n;}
10        if(p==0||p==n) continue;
11        return p;
12    }
13 }
14 void factor(LL n){
15     LL x;
16     x=Pollard(n);
17     if(x==n){ ans[ansn++]=x; return; }
18     factor(x), factor(n/x);
19 }

```

二次剩余

```

1 void calcH(int &t, int &h, const int p) {
2     int tmp = p - 1; for (t = 0; (tmp & 1) == 0; tmp /= 2) t++; h = tmp;
3 }
4 // solve equation x^2 mod p = a
5 bool solve(int a, int p, int &x, int &y) {
6     srand(19920225);
7     if (p == 2) { x = y = 1; return true; }
8     int p2 = p / 2, tmp = power(a, p2, p);
9     if (tmp == p - 1) return false;
10    if ((p + 1) % 4 == 0) {
11        x = power(a, (p + 1) / 4, p); y = p - x; return true;
12    } else {
13        int t, h, b, pb; calcH(t, h, p);
14        if (t >= 2) {
15            do {b = rand() % (p - 2) + 2;
16            } while (power(b, p / 2, p) != p - 1);
17            pb = power(b, h, p);
18        } int s = power(a, h / 2, p);
19        for (int step = 2; step <= t; step++) {
20            int ss = (((long long)(s * s) % p) * a) % p;
21            for (int i = 0; i < t - step; i++) ss = ((long long)ss * ss) % p;
22            if (ss + 1 == p) s = (s * pb) % p; pb = ((long long)pb * pb) % p;
23        } x = ((long long)s * a) % p; y = p - x;
24    } return true;
25 }

```

Pell 方程

```

1 ULL A,B,p[maxn],q[maxn],a[maxn],g[maxn],h[maxn];
2 int main() {
3     for (int test=1, n;scanf("%d",&n) && n;++test) {
4         printf("Case %d: ",test);

```



```

5   if (fabs(sqrt(n)-floor(sqrt(n)+1e-7))<=1e-7) {
6       int a=(int)(floor(sqrt(n)+1e-7)); printf("%d %d\n",a,1);
7   } else {
8       // 求  $x^2 - ny^2 = 1$  的最小正整数根, n 不是完全平方数
9       p[1]=q[0]=h[1]=1;p[0]=q[1]=g[1]=0;
10      a[2]=(int)(floor(sqrt(n)+1e-7));
11      for (int i=2;i;++i) {
12          g[i]=-g[i-1]+a[i]*h[i-1]; h[i]=(n-sqr(g[i]))/h[i-1];
13          a[i+1]=(g[i]+a[2])/h[i]; p[i]=a[i]*p[i-1]+p[i-2];
14          q[i]=a[i]*q[i-1]+q[i-2];
15          if (sqr((ULL)(p[i]))-n*sqr((ULL)(q[i]))==1){
16              A=p[i];B=q[i];break; }
17      } cout << A << ' ' << B <<endl;
18  }}}}

```

日期公式

```

1  int zeller(int y,int m,int d) {
2      if (m<=2) y--,m+=12; int c=y/100; y%=100;
3      int w=((c>>2)-(c<<1)+y+(y>>2)+(13*(m+1)/5)+d-1)%7;
4      if (w<0) w+=7; return(w);
5  }
6  int getId(int y, int m, int d) {
7      if (m < 3) {y --; m += 12};
8      return 365 * y + y / 4 - y / 100 + y / 400 + (153 * m + 2) / 5 + d;
9  }

```

Schreier-Sims

```

1  struct Permutation{
2      vector<int> P;Permutation(){} Permutation(int n){ P.resize(n); }
3      Permutation inv()const{
4          Permutation ret(P.size());
5          for(int i = 0; i < int(P.size()); ++i) ret.P[P[i]] = i;
6          return ret;
7      }
8      int &operator [](const int &dn){ return P[dn]; }
9      void resize(const size_t &sz){ P.resize(sz); }
10     size_t size()const{ return P.size(); }
11     const int &operator [](const int &dn)const{ return P[dn]; }
12 };
13 Permutation operator *(const Permutation &a, const Permutation &b){
14     Permutation ret(a.size());
15     for(int i = 0; i < (int)a.size(); ++i) ret[i] = b[a[i]];
16     return ret;
17 }
18 typedef vector<Permutation> Bucket;

```

```

19 typedef vector<int> Table; typedef pair<int,int> pii;
20 int n, m;
21 vector<Bucket> buckets, bucketsInv; vector<Table> lookupTable;
22 int fastFilter(const Permutation &g, bool addToGroup = true){
23     int n = buckets.size();
24     Permutation p;
25     for(int i = 0; i < n; ++i){
26         int res = lookupTable[i][p[i]];
27         if(res == -1){
28             if(addToGroup){
29                 buckets[i].push_back(p); bucketsInv[i].push_back(p.inv());
30                 lookupTable[i][p[i]] = (int)buckets[i].size() - 1;
31             }
32             return i;
33         }
34         p = p * bucketsInv[i][res]; swap(i1,i2);
35     }
36     return -1;
37 }
38 long long calcTotalSize(){
39     long long ret = 1;
40     for(int i = 0; i < n; ++i) ret *= buckets[i].size();
41     return ret;
42 }
43 bool inGroup(const Permutation &g){ return fastFilter(g, false) == -1; }
44 void solve(const Bucket &gen,int _n){// m perm[0..n - 1]s
45     n = _n, m = gen.size();
46     //clear all
47     vector<Bucket> _buckets(n); swap(buckets, _buckets);
48     vector<Bucket> _bucketsInv(n); swap(bucketsInv, _bucketsInv);
49     vector<Table> _lookupTable(n); swap(lookupTable, _lookupTable);
50 }
51 for(int i = 0; i < n; ++i){
52     lookupTable[i].resize(n);
53     fill(lookupTable[i].begin(), lookupTable[i].end(), -1);
54 }
55 Permutation id(n);
56 for(int i = 0; i < n; ++i) id[i] = i;
57 for(int i = 0; i < n; ++i){
58     buckets[i].push_back(id); bucketsInv[i].push_back(id);
59     lookupTable[i][i] = 0;
60 }
61 for(int i = 0; i < m; ++i) fastFilter(gen[i]);
62 queue<pair<point,point> > toUpdate;
63 for(int i = 0; i < n; ++i)

```

```

64     for(int j = i; j < n; ++j)
65         for(int k = 0; k < (int)buckets[i].size(); ++k)
66             for(int l = 0; l < (int)buckets[j].size(); ++l)
67                 toUpdate.push(make_pair(pii(i,k), pii(j,l)));
68 while(!toUpdate.empty()){
69     pii a = toUpdate.front().first, b = toUpdate.front().second;
70     toUpdate.pop();
71     int res=fastFilter(buckets[a.first][a.second]*buckets[b.first][b.second]);
72     if(res==-1) continue;
73     pii newPair(res, (int)buckets[res].size() - 1);
74     for(int i = 0; i < n; ++i)
75         for(int j = 0; j < (int)buckets[i].size(); ++j){
76             if(i <= res) toUpdate.push(make_pair(pii(i, j), newPair));
77             if(res <= i) toUpdate.push(make_pair(newPair, pii(i, j)));
78         }
79     }
80 }

```

线性规划

```

1 // 求 $\max\{cx \mid Ax \leq b, x \geq 0\}$ 的解
2 typedef vector<double> VD;
3 VD simplex(vector<VD> A, VD b, VD c) {
4     int n = A.size(), m = A[0].size() + 1, r = n, s = m - 1;
5     vector<VD> D(n + 2, VD(m + 1, 0)); vector<int> ix(n + m);
6     for (int i = 0; i < n + m; ++i) ix[i] = i;
7     for (int i = 0; i < n; ++i) {
8         for (int j = 0; j < m - 1; ++j) D[i][j] = -A[i][j];
9         D[i][m - 1] = 1; D[i][m] = b[i];
10        if (D[r][m] > D[i][m]) r = i;
11    }
12    for (int j = 0; j < m - 1; ++j) D[n][j] = c[j];
13    D[n + 1][m - 1] = -1;
14    for (double d; ; ) {
15        if (r < n) {
16            int t = ix[s]; ix[s] = ix[r + m]; ix[r + m] = t;
17            D[r][s] = 1.0 / D[r][s]; vector<int> speedUp;
18            for (int j = 0; j <= m; ++j) if (j != s) {
19                D[r][j] *= -D[r][s];
20                if(D[r][j]) speedUp.push_back(j);
21            }
22            for (int i = 0; i <= n + 1; ++i) if (i != r) {
23                for(int j = 0; j < speedUp.size(); ++j)
24                    D[i][speedUp[j]] += D[r][speedUp[j]] * D[i][s];
25                D[i][s] *= D[r][s];
26            } r = -1; s = -1;

```

```

27     for (int j = 0; j < m; ++j) if (s < 0 || ix[s] > ix[j])
28         if (D[n + 1][j] > EPS || (D[n + 1][j] > -EPS && D[n][j] > EPS)) s = j;
29     if (s < 0) break;
30     for (int i = 0; i < n; ++i) if (D[i][s] < -EPS)
31         if (r < 0 || (d = D[r][m] / D[r][s] - D[i][m] / D[i][s]) < -EPS
32             || (d < EPS && ix[r + m] > ix[i + m])) r = i;
33     if (r < 0) return VD(); // 无边界
34 }
35 if (D[n + 1][m] < -EPS) return VD(); // 无解
36 VD x(m - 1);
37 for (int i = m; i < n + m; ++i) if (ix[i] < m - 1) x[ix[i]] = D[i - m][m];
38 return x; // 最优值在 D[n][m]
39 }

```

FFT

```

1 // double 精度对 $10^9 + 7$  取模最多可以做到 $2^{20}$ 
2 const int MOD = 1000003;
3 const double PI = acos(-1);
4 typedef complex<double> Complex;
5 const int N = 65536, L = 15, MASK = (1 << L) - 1;
6 Complex w[N];
7 void FFTInit() {
8     for (int i = 0; i < N; ++i) {
9         w[i] = Complex(cos(2 * i * PI / N), sin(2 * i * PI / N));
10    }
11 }
12 void FFT(Complex p[], int n) {
13     for (int i = 1, j = 0; i < n - 1; ++i) {
14         for (int s = n; j ^= s >>= 1, ~j & s;);
15         if (i < j) {
16             swap(p[i], p[j]);
17         }
18     }
19     for (int d = 0; (1 << d) < n; ++d) {
20         int m = 1 << d, m2 = m * 2, rm = n >> (d + 1);
21         for (int i = 0; i < n; i += m2) {
22             for (int j = 0; j < m; ++j) {
23                 Complex &p1 = p[i + j + m], &p2 = p[i + j];
24                 Complex t = w[rm * j] * p1;
25                 p1 = p2 - t;
26                 p2 = p2 + t;
27             }
28         }
29     }
30     Complex A[N], B[N], C[N], D[N];
31     void mul(int a[N], int b[N]) {
32         for (int i = 0; i < N; ++i) {

```

```

31  A[i] = Complex(a[i] >> L, a[i] & MASK);
32  B[i] = Complex(b[i] >> L, b[i] & MASK);
33  }
34  FFT(A, N), FFT(B, N);
35  for (int i = 0; i < N; ++i) {
36      int j = (N - i) % N;
37      Complex da = (A[i] - conj(A[j])) * Complex(0, -0.5),
38      db = (A[i] + conj(A[j])) * Complex(0.5, 0),
39      dc = (B[i] - conj(B[j])) * Complex(0, -0.5),
40      dd = (B[i] + conj(B[j])) * Complex(0.5, 0);
41      C[j] = da * dd + da * dc * Complex(0, 1);
42      D[j] = db * dd + db * dc * Complex(0, 1);
43  }
44  FFT(C, N), FFT(D, N);
45  for (int i = 0; i < N; ++i) {
46      long long da = (long long)(C[i].imag() / N + 0.5) % MOD,
47      db = (long long)(C[i].real() / N + 0.5) % MOD,
48      dc = (long long)(D[i].imag() / N + 0.5) % MOD,
49      dd = (long long)(D[i].real() / N + 0.5) % MOD;
50      a[i] = ((dd << (L * 2)) + ((db + dc) << L) + da) % MOD;
51  }
52  }

```

```

20  for (i = 2; i < M; i++) {
21      int Len = k + Next[k], L = Next[i - k];
22      if (L < Len - i) {
23          Next[i] = L;
24      } else {
25          for (j = max(0, Len - i); i + j < M && a[j] == a[i + j]; j++);
26          Next[i] = j;
27          k = i;
28      }
29  }
30  for (j = 0; j < N && j < M && a[j] == b[j]; j++);
31  ret[0] = j;
32  k = 0;
33  for (i = 1; i < N; i++) {
34      int Len = k + ret[k], L = Next[i - k];
35      if (L < Len - i) {
36          ret[i] = L;
37      } else {
38          for (j = max(0, Len - i); j < M && i + j < N && a[j] == b[i + j]; j++);
39          ret[i] = j;
40          k = i;
41      }
42  }
43  }

```

Manacher/ 扩展 KMP

```

1  void Manacher(char text[], int n, int palindrome[]) {
2      palindrome[0] = 1;
3      for (int i = 1, j = 0, i < (n << 1) - 1; ++ i) {
4          int p = i >> 1;
5          int q = i - p;
6          int r = (j + 1 >> 1) + palindrome[j] - 1;
7          palindrome[i] = r < q ? 0 : min(r - q + 1, palindrome[(j << 1) - i]);
8          while (0 <= p - palindrome[i] && q + palindrome[i] < n && text[p -
↪ palindrome[i]] == text[q + palindrome[i]]) {
9              palindrome[i] ++;
10         }
11         if (q + palindrome[i] - 1 > r) {
12             j = i;
13         }
14     }
15 }
16 void ExtendedKMP(char *a, char *b, int M, int N, int *Next, int *ret) { // a ->
↪ 模式串 b -> 匹配串
17     int i, j, k;
18     for (j = 0; 1 + j < M && a[j] == a[1 + j]; j++); Next[1] = j;
19     k = 1;

```

后缀数组 (倍增)

```

1  int rank[MAX_N], height[MAX_N];
2  int cmp(int *x, int a, int b, int d) {
3      return x[a] == x[b] && x[a + d] == x[b + d];
4  }
5  void doubling(int *a, int N, int M) {
6      static int sRank[MAX_N], tmpA[MAX_N], tmpB[MAX_N];
7      int *x = tmpA, *y = tmpB;
8      for (int i = 0; i < M; ++i) sRank[i] = 0;
9      for (int i = 0; i < N; ++i) ++sRank[x[i] = a[i]];
10     for (int i = 1; i < M; ++i) sRank[i] += sRank[i - 1];
11     for (int i = N - 1; i >= 0; --i) sa[--sRank[x[i]]] = i;
12     for (int d = 1, p = 0; p < N; M = p, d <= 1) {
13         p = 0; for (int i = N - d; i < N; ++i) y[p++] = i;
14         for (int i = 0; i < N; ++i) if (sa[i] >= d) y[p++] = sa[i] - d;
15         for (int i = 0; i < M; ++i) sRank[i] = 0;
16         for (int i = 0; i < N; ++i) ++sRank[x[i]];
17         for (int i = 1; i < M; ++i) sRank[i] += sRank[i - 1];
18         for (int i = N - 1; i >= 0; --i) sa[--sRank[x[y[i]]]] = y[i];
19         swap(x, y); x[sa[0]] = 0; p = 1;

```

```

20     for(int i=1;i<N;++i) x[sa[i]]=cmp(y,sa[i],sa[i-1],d)?p-1:p++;
21 }
22 }
23 void calcHeight(){
24     for(int i=0;i<N;++i) rank[sa[i]]=i;
25     int cur=0; for(int i=0;i<N;++i)
26         if(rank[i]){
27             if(cur) cur--;
28             for(;a[i+cur]==a[sa[rank[i]-1]+cur];++cur);
29             height[rank[i]]=cur;
30         }
31 }

```

后缀自动机

```

1 struct State {
2     int length;
3     State *parent,*go[C];
4     State(int length = 0):length(length),parent(NULL){
5         memset(go,0,sizeof(go));
6     }
7     State* extend(State*, int token);
8 } node_pool[V], *tot_node;
9 State* State::extend(State *start,int token){
10     State *p=this;
11     State *np=new(tot_node++) State(this->length+1);
12     while(p!=NULL&&p->go[token]==NULL)
13         p->go[token]=np, p=p->parent;
14     if(p==NULL) np->parent=start;
15     else{
16         State *q=p->go[token];
17         if(p->length+1==q->length) np->parent=q;
18         else{
19             State *nq=new(tot_node++) State(p->length+1);
20             memcpy(nq->go,q->go,sizeof(q->go));
21             nq->parent=q->parent;
22             np->parent=q->parent=nq;
23             while(p!=NULL&&p->go[token]==q)
24                 p->go[token]=nq, p=p->parent;
25         }
26     }
27     return np;
28 }

```

后缀树 (With Pop Front)

```

1 int pos, text[N];
2 struct Node {
3     int l, r;
4     Node *suf, *ch[C];
5     int dgr;
6     Node *fa;
7     Node(int l = -1, int r = INF) : l(l), r(r) {
8         suf = fa = NULL;
9         memset(ch, 0, sizeof(ch));
10        dgr = 0;
11    }
12    Node* addEdge(Node *t) {
13        int c = text[t->l];
14        dgr += !ch[c];
15        ch[c] = t;
16        t->fa = this;
17        return t;
18    }
19    int len() {
20        return min(r, pos + 1) - l;
21    }
22 };
23
24 int top;
25 Node pool[N << 1], *root, *nxtSuf, *cur;
26 int remCnt, curP, curLen;
27 long long size;
28 queue<Node*> leaves;
29 void init() {
30     top = 0, pos = -1;
31     remCnt = 0, curP = 0, curLen = 0;
32     nxtSuf = NULL;
33     root = cur = new(pool + (top++)) Node(-1, -1);
34     size = 0;
35     while (leaves.size()) leaves.pop();
36 }
37 void link(Node *u) {
38     if (nxtSuf) nxtSuf->suf = u;
39     nxtSuf = u;
40 }
41 bool walk(Node *u) {
42     int len = u->len();
43     if (curLen >= len) {
44         curP += len, curLen -= len, cur = u;

```

```

45     return true;
46 }
47 return false;
48 }
49 void extend(int c) {
50     text[++pos] = c;
51     nxtSuf = NULL;
52     ++remCnt;
53     while (remCnt) {
54         curP = curLen ? curP : pos;
55         int curE = text[curP];
56         if (!cur->ch[curE]) {
57             leaves.push(cur->addEdge(new(pool + (top++)) Node(pos)));
58             link(cur);
59         } else {
60             Node *nxt = cur->ch[curE];
61             if (walk(nxt)) continue;
62             if (text[nxt->l + curLen] == c) {
63                 ++curLen;
64                 link(cur);
65                 break;
66             }
67             Node *split = new(pool + (top++)) Node(nxt->l, nxt->l + curLen);
68             cur->addEdge(split);
69             leaves.push(split->addEdge(new(pool + (top++)) Node(pos)));
70             nxt->l += curLen;
71             split->addEdge(nxt);
72             link(split);
73         }
74         --remCnt;
75         if (cur == root && curLen > 0) {
76             curP = pos - (--curLen);
77         } else {
78             cur = cur->suf ? cur->suf : root;
79         }
80     }
81     size += leaves.size();
82 }
83 void finish() {
84     nxtSuf = NULL;
85     for (int i = 0; i < top; ++i) if (pool[i].r == INF) link(pool + i);
86     while (remCnt > 0) {
87         if (curLen) {
88             int curE = text[curP];
89             Node *nxt = cur->ch[curE];

```

```

90         if (walk(nxt)) continue;
91         Node *split = new(pool + (top++)) Node(nxt->l, nxt->l + curLen);
92         leaves.push(cur->addEdge(split));
93         nxt->l += curLen;
94         split->addEdge(nxt);
95         link(split);
96     } else {
97         leaves.push(cur);
98         link(cur);
99     }
100     --remCnt;
101     if (cur == root && curLen > 0) {
102         --curLen;
103         curP = pos - remCnt + 1;
104     } else {
105         cur = cur->suf ? cur->suf : root;
106     }
107 }
108 if (nxtSuf != root) link(root);
109 }
110 void eraseUp(Node *u) {
111     size -= u->len();
112     int ch = text[u->l];
113     u = u->fa;
114     u->ch[ch] = NULL;
115     --(u->dgr);
116 }
117 void erase() {
118     Node *u = leaves.front();
119     leaves.pop();
120     while (u->dgr == 0 && u != cur) eraseUp(u);
121     if (u == cur) {
122         if (cur->dgr == 0 && curLen == 0) {
123             int len = u->len();
124             curLen = len;
125             curP = pos - len + 1;
126             cur = cur->fa;
127             eraseUp(u);
128         }
129         if (curLen) {
130             int curE = text[curP];
131             if (!cur->ch[curE]) {
132                 Node *leaf = new(pool + (top++)) Node(pos - curLen + 1);
133                 leaves.push(cur->addEdge(leaf));
134                 size += leaf->len();

```

```

135     --remCnt;
136     if (cur == root && curLen > 0) {
137         curP = pos - (--curLen) + 1;
138     } else {
139         cur = cur->suf ? cur->suf : root;
140     }
141     while (curLen && walk(cur->ch[text[curP]])) continue;
142 }}}}
143 int n;
144 char s[N], buf[N];
145 int ord[N], stop, sord[N << 1];
146 void dfs(Node *u) {
147     sord[u - pool] = stop++;
148     for (int i = 0; i < C; ++i) {
149         if (u->ch[i]) {
150             dfs(u->ch[i]);
151         }
152     }
153 }
154 void getOrd() {
155     init();
156     for (int i = 0; i < n; ++i) extend(s[i] - 'a');
157     finish();
158     stop = 0;
159     dfs(root);
160     int i = 0;
161     while (leaves.size()) {
162         ord[i++] = sord[leaves.front() - pool];
163         leaves.pop();
164     }
165 }

```

字符串最小表示

```

1 std::string find(std::string s) {
2     int i,j,k,l,N=s.length(); s+=s;
3     for(i=0,j=1;j<N;){
4         for(k=0;k<N&&s[i+k]==s[j+k];k++);
5         if(k>=N) break;
6         if(s[i+k]<s[j+k]) j+=k+1;
7         else l=i+k,i=j,j=max(l,j)+1;
8     }
9     return s.substr(i,N);
10 }

```

轻重链剖分

```

1 struct Tree(){}*root[N];
2 int father[N],size[N],depth[N];
3 int bfsOrd[N],pathId[N],ordInPath[N],sqn[N];
4 void doBfs(int s){
5     int qh=0,qt=0,*que=bfsOrd; father[s]=-1; depth[s]=0;
6     for(que[qt++]=s;qh<qt;){
7         int u=que[qh++];
8         foreach(iter,adj[u]){
9             int v=*iter; if(v==father[u]) continue;
10            father[v]=u; depth[v]=depth[u]+1; que[qt++]=v;
11        }
12    }
13 }
14 void doSplit(){
15     for(int i=N-1;i>=0;--i){
16         int u=bfsOrd[i]; size[u]=1;
17         foreach(iter,adj[u]){
18             int v=*iter; if(v==father[u]) continue; size[u]+=size[v];
19         }
20     }
21     memset(pathId,-1,sizeof pathId);
22     for(int i=0;i<N;++i){
23         int top=bfsOrd[i],cnt=0;
24         if(pathId[top]!=-1) continue;
25         for(int next,u=top;u!=-1;u=next){
26             sqn[cnt]=val[u]; ordInPath[u]=cnt; pathId[u]=top; ++cnt;
27             next=-1;
28             foreach(iter,adj[u]){
29                 int v=*iter; if(v==father[u]) continue;
30                 if(next<0||size[next]<size[v]) next=v;
31             }
32         }
33         root[top]=new Tree(0,cnt,sqn);
34     }
35 }
36 void prepare(){ doBfs(0); doSplit(); }

```

Splay Tree

```

1 // 注意初始化内存池和 null 节点
2 struct Node{
3     int rev,size; Node *ch[2],*p;
4     void set(Node*,int); int dir(); void update(); void relax(); void appRev();
5 } nodePool[MAX_NODE],*curNode,*null;
6 Node *newNode(){

```

```

7   Node *t=curNode++; t->rev=0, t->size=1;
8   t->ch[0]=t->ch[1]=t->p=null; return t;
9 }
10 struct Splay{
11     Node *root;
12     Splay(){ root=newNode(); root->set(newNode(),0); root->update(); }
13     void rot(Node *t){
14         Node *p=t->p; int d=t->dir();
15         p->relax(); t->relax();
16         if(p==root) root=t;
17         p->set(t->ch[!d],d); p->p->set(t,p->dir()); t->set(p,!d);
18         p->update();
19     }
20     void splay(Node *t,Node *f=null){
21         for(t->relax();t->p!=f;){
22             if(t->p->p==f) rot(t);
23             else t->dir()==t->p->dir()? (rot(t->p),rot(t)):(rot(t),rot(t));
24             t->update();
25         }
26     };
27     void initNull(){ curNode=nodePool;null=curNode++;null->size=0; }
28     void Node::set(Node *t,int _d){ ch[_d]=t; t->p=this; }
29     int Node::dir(){ return this==p->ch[1]; }
30     void Node::update(){ size=ch[0]->size+ch[1]->size+1; }
31     void Node::relax(){ if(rev) ch[0]->appRev(), ch[1]->appRev(), rev=false; }
32     void Node::appRev(){ if(this==null) return; rev^=true; swap(ch[0],ch[1]); }

```

Link Cut Tree

```

1 // 注意初始化 null 节点, 单点的 is_root 初始为 true
2 struct Node{
3     Node *ch[2], *p;
4     int is_root, rev;
5     bool dir();
6     void set(Node*, bool);
7     void update();
8     void relax();
9     void app_rev();
10 } *null;
11 void rot(Node *t){
12     Node *p=t->p; bool d=t->dir();
13     p->relax(); t->relax(); p->set(t->ch[!d],d);
14     if(p->is_root) t->p=p->p, swap(p->is_root,t->is_root);
15     else p->p->set(t,p->dir());
16     t->set(p,!d); p->update();
17 }

```

```

18 void splay(Node *t){
19     for(t->relax();!t->is_root;){
20         if(t->p->is_root) rot(t);
21         else t->dir()==t->p->dir()? (rot(t->p),rot(t)):(rot(t),rot(t));
22         t->update();
23     }
24     void access(Node *t){
25         for(Node *s=null; t!=null; s=t,t=t->p){
26             splay(t);
27             if (t->p == null) { /*TODO*/ }
28             t->ch[1]->is_root=true; s->is_root=false;
29             t->ch[1]=s; t->update();
30         }
31     }
32     bool Node::dir(){ return this==p->ch[1]; }
33     void Node::set(Node *t,bool _d){ ch[_d]=t; t->p=this; }
34     void Node::update(){ }
35     void Node::app_rev(){ if (this == null) return; rev ^= true; swap(ch[0], ch[1]); }
36     void Node::relax() { if(this==null) return; if (rev) { ch[0]->app_rev();
37         ↪ ch[1]->app_rev(); rev = false; } }
38     void make_root(Node *u) { access(u); splay(u); u->app_rev(); }

```

Dominator Tree

```

1 vector<int> prec[N], succ[N];
2 vector<int> ord;
3 int stamp, vis[N];
4 int num[N];
5 int fa[N];
6 void dfs(int u) {
7     vis[u] = stamp;
8     num[u] = ord.size();
9     ord.push_back(u);
10    for (int i = 0; i < (int)succ[u].size(); ++i) {
11        int v = succ[u][i];
12        if (vis[v] != stamp) {
13            fa[v] = u;
14            dfs(v);
15        }
16    }
17 }
18 int fs[N], mins[N], dom[N], sem[N];
19 int find(int u) {
20     if (u != fs[u]) {
21         int v = fs[u];
22         fs[u] = find(fs[u]);

```

```

23     if (mins[v] != -1 && num[sem[mins[v]]] < num[sem[mins[u]]]) {
24         mins[u] = mins[v];
25     }
26 }
27 return fs[u];
28 }
29 void merge(int u, int v) { fs[u] = v; }
30 vector<int> buf[N];
31 int buf2[N];
32 void mark(int source) {
33     ord.clear();
34     ++stamp;
35     dfs(source);
36     for (int i = 0; i < (int)ord.size(); ++i) {
37         int u = ord[i];
38         fs[u] = u, mins[u] = -1, buf2[u] = -1;
39     }
40     for (int i = (int)ord.size() - 1; i > 0; --i) {
41         int u = ord[i], p = fa[u];
42         sem[u] = p;
43         for (int j = 0; j < (int)prec[u].size(); ++j) {
44             int v = prec[u][j];
45             if (use[v] != stamp) continue;
46             if (num[v] > num[u]) {
47                 find(v); v = sem[mins[v]];
48             }
49             if (num[v] < num[sem[u]]) {
50                 sem[u] = v;
51             }
52         }
53         buf[sem[u]].push_back(u);
54         mins[u] = u;
55         merge(u, p);
56         while (buf[p].size()) {
57             int v = buf[p].back();
58             buf[p].pop_back();
59             find(v);
60             if (sem[v] == sem[mins[v]]) {
61                 dom[v] = sem[v];
62             } else {
63                 buf2[v] = mins[v];
64             }
65         }
66     }
67     dom[ord[0]] = ord[0];

```

```

68     for (int i = 0; i < (int)ord.size(); ++i) {
69         int u = ord[i];
70         if (~buf2[u]) {
71             dom[u] = dom[buf2[u]];
72         }
73     }
74 }

```

DancingLinks

```

1 struct node{
2     node *left,*right,*up,*down,*col; int row,cnt;
3 }*head,*col[MAXC],Node[MAXNODE],*ans[MAXNODE];
4 int totNode;
5 void insert(const std::vector<int> &V,int rownum){
6     std::vector<node*> N;
7     for(int i=0;i<(int)V.size();++i){
8         node* now=Node+(totNode++); now->row=rownum;
9         now->col=now->up=col[V[i]], now->down=col[V[i]]->down;
10        now->up->down=now, now->down->up=now;
11        now->col->cnt++; N.push_back(now);
12    }
13    for(int i=0;i<(int)V.size();++i)
14        N[i]->right=N[(i+1)%V.size()], N[i]->left=N[(i-1+V.size())%V.size()];
15 }
16 void Remove(node *x){
17     x->left->right=x->right, x->right->left=x->left;
18     for(node *i=x->down;i!=x;i=i->down)
19         for(node *j=i->right;j!=i;j=j->right)
20             j->up->down=j->down, j->down->up=j->up, --(j->col->cnt);
21 }
22 void Resume(node *x){
23     for(node *i=x->up;i!=x;i=i->up)
24         for(node *j=i->left;j!=i;j=j->left)
25             j->up->down=j->down->up=j, ++(j->col->cnt);
26     x->left->right=x, x->right->left=x;
27 }
28 bool search(int tot){
29     if(head->right==head) return true;
30     node *choose=NULL;
31     for(node *i=head->right;i!=head;i=i->right){
32         if(choose==NULL||choose->cnt>i->cnt) choose=i;
33         if(choose->cnt<2) break;
34     }
35     Remove(choose);
36     for(node *i=choose->down;i!=choose;i=i->down){

```



```

37     for(node *j=i->right;j!=i;j=j->right) Remove(j->col);
38     ans[tot]=i;
39     if(search(tot+1)) return true;
40     ans[tot]=NULL;
41     for(node *j=i->left;j!=i;j=j->left) Resume(j->col);
42 }
43 Resume(choose);
44 return false;
45 }
46 void prepare(int totC){
47     head=Node+totC;
48     for(int i=0;i<totC;++i) col[i]=Node+i;
49     totNode=totC+1;
50     for(int i=0;i<totC;++i){
51         (Node+i)->right=Node+(i+1)%(totC+1);
52         (Node+i)->left=Node+(i+totC)%(totC+1);
53         (Node+i)->up=(Node+i)->down=Node+i;
54     }
55 }

```

环状最长公共子序列

```

1 int n, a[N << 1], b[N << 1];
2 bool has(int i, int j) { return a[(i - 1) % n] == b[(j - 1) % n];}
3 const int DELTA[3][2] = {{0, -1}, {-1, -1}, {-1, 0}};
4 int from[N][N];
5 int solve() {
6     memset(from, 0, sizeof(from));
7     int ret = 0;
8     for (int i = 1; i <= 2 * n; ++ i) {
9         from[i][0] = 2;
10        int left = 0, up = 0;
11        for (int j = 1; j <= n; ++ j) {
12            int upleft = up + 1 + !from[i - 1][j];
13            if (!has(i, j)) upleft = INT_MIN;
14            int max = std::max(left, std::max(upleft, up));
15            if (left == max) {
16                from[i][j] = 0;
17            } else if (upleft == max) {
18                from[i][j] = 1;
19            } else {
20                from[i][j] = 2;
21            }
22            left = max;
23        }
24        if (i >= n) {

```

```

25        int count = 0;
26        for (int x = i, y = n; y;) {
27            int t = from[x][y];
28            count += t == 1;
29            x += DELTA[t][0];
30            y += DELTA[t][1];
31        }
32        ret = std::max(ret, count);
33        int x = i - n + 1, y = 0;
34        from[x][0] = 0;
35        while (y <= n && from[x][y] == 0) y++;
36        for (; x <= i; ++ x) {
37            from[x][y] = 0;
38            if (x == i) break;
39            for (; y <= n; ++ y) {
40                if (from[x + 1][y] == 2) break;
41                if (y + 1 <= n && from[x + 1][y + 1] == 1) {
42                    y++;
43                    break;
44                }
45            }
46        }

```

直线下有多少个格点

```

1 LL solve(LL n,LL a,LL b,LL m){
2     // 计算 for (int i=0;i<n;++i) s+=floor((a+b*i)/m)
3     //n,m,a,b>0
4     if(b==0) return n*(a/m);
5     if(a>m) return n*(a/m)+solve(n,a%m,b,m);
6     if(b>m) return (n-1)*n/2*(b/m)+solve(n,a,b%m,m);
7     return solve((a+b*n)/m,(a+b*n)%m,b);
8 }

```

费用流

```

1 // Q is a priority_queue<PII, vector<PII>, greater<PII> >
2 // for an edge(s, t): u is the capacity, v is the cost, nxt is the next edge,
3 // op is the opposite edge
4 // this code can not deal with negative cycles
5 typedef pair<int,int> PII;
6 struct edge{ int t,u,v; edge *nxt,*op; }E[MAXE],*V[MAXV];
7 int D[MAXN], dist[MAXN], maxflow, mincost; bool in[MAXN];
8 bool modlabel(){
9     while(!Q.empty()) Q.pop();
10    for(int i=S;i<=T;++i) if(in[i]) D[i]=0,Q.push(PII(0,i)); else D[i]=inf;

```

```

11 while(!Q.empty()){
12     int x=Q.top().first,y=Q.top().second; Q.pop();
13     if(y==T) break; if(D[y]<x) continue;
14     for(edge *ii=V[y];ii;ii=ii->nxt) if(ii->u)
15         if(x+(ii->v+dist[ii->t]-dist[y])<D[ii->t]){
16             D[ii->t]=x+(ii->v+dist[ii->t]-dist[y]);
17             Q.push(PII(D[ii->t],ii->t));
18         }
19     }
20     if(D[T]==inf) return false;
21     for(int i=S;i<=T;++i) if(D[i]>D[T]) dist[i]+=D[T]-D[i];
22     return true;
23 }
24 int aug(int p,int limit){
25     if(p==T) return maxflow+=limit,mincost+=limit*dist[S],limit;
26     in[p]=1; int kk,ll=limit;
27     for(edge *ii=V[p];ii;ii=ii->nxt) if(ii->u){
28         if(!in[ii->t]&&dist[ii->t]+ii->v==dist[p]){
29             kk=aug(ii->t,min(ii->u,ll)); ll=kk,ii->u=kk,ii->op->u+=kk;
30             if(!ll) return in[p]=0,limit;

```

```

31     }
32     }
33     return limit-ll;
34 }
35 PII mincostFlow(){
36     for(int i=S;i<=T;++i) dist[i]=i==T?inf:0;
37     while(!Q.empty()) Q.pop(); Q.push(PII(0,T));
38     while(!Q.empty()){
39         int x=Q.top().first,y=Q.top().second; Q.pop(); if(dist[y]<x) continue;
40         for(edge *ii=V[y];ii;ii=ii->nxt) if(ii->op->u&&ii->v+x<dist[ii->t]
41             dist[ii->t]=ii->v+x,Q.push(PII(dist[ii->t],ii->t));
42     }
43     maxflow=mincost=0;
44     do{
45         do{
46             memset(in,0,sizeof(in));
47         }while(aug(S,maxflow));
48     }while(modlabel());
49     return PII(maxflow,mincost);
50 }

```

积分表

Integrals of Rational Functions	$\int \frac{1}{1+x^2} dx = \tan^{-1} x$	$\int \frac{1}{a^2+x^2} dx = \frac{1}{a} \tan^{-1} \frac{x}{a}$	$\int \frac{x}{a^2+x^2} dx = \frac{1}{2} \ln a^2 + x^2 $	$\int \frac{x^2}{a^2+x^2} dx = x - a \tan^{-1} \frac{x}{a}$	$\int \frac{x^3}{a^2+x^2} dx = \frac{1}{2} x^2 - \frac{1}{2} a^2 \ln a^2 + x^2 $
$\int \frac{1}{ax^2+bx+c} dx = \frac{2}{\sqrt{4ac-b^2}} \tan^{-1} \frac{2ax+b}{\sqrt{4ac-b^2}}$	$\int \frac{1}{(x+a)(x+b)} dx = \frac{1}{b-a} \ln \frac{a+x}{b+x}, a \neq b$	$\int \frac{x}{(x+a)^2} dx = \frac{a}{a+x} + \ln a+x $	$\int \frac{x}{ax^2+bx+c} dx = \frac{1}{2a} \ln ax^2 + bx + c - \frac{b}{a\sqrt{4ac-b^2}} \tan^{-1} \frac{2ax+b}{\sqrt{4ac-b^2}}$		
Integrals with Roots	$\int \frac{x}{\sqrt{x \pm a}} dx = \frac{2}{3} (x \mp 2a) \sqrt{x \pm a}$	$\int \sqrt{\frac{x}{a-x}} dx = -\sqrt{x(a-x)} - a \tan^{-1} \frac{\sqrt{x(a-x)}}{x-a}$	$\int \sqrt{\frac{x}{a+x}} dx = \sqrt{x(a+x)} - a \ln [\sqrt{x} + \sqrt{x+a}]$	$\int x \sqrt{x^2 \pm a^2} dx = \frac{1}{3} (x^2 \pm a^2)^{3/2}$	
$\int x \sqrt{ax+b} dx = \frac{2}{15a^2} (-2b^2 + abx + 3a^2 x^2) \sqrt{ax+b}$	$\int \sqrt{x(ax+b)} dx = \frac{1}{4a^{3/2}} \left[(2ax+b) \sqrt{ax(ax+b)} - b^2 \ln \left a\sqrt{x} + \sqrt{a(ax+b)} \right \right]$	$\int \sqrt{x^2 \pm a^2} dx = \frac{1}{2} x \sqrt{x^2 \pm a^2} \pm \frac{1}{2} a^2 \ln \left x + \sqrt{x^2 \pm a^2} \right $			
$\int \sqrt{x^3(ax+b)} dx = \left[\frac{b}{12a} - \frac{b^2}{8a^2 x} + \frac{x}{3} \right] \sqrt{x^3(ax+b)} + \frac{b^3}{8a^{5/2}} \ln \left a\sqrt{x} + \sqrt{a(ax+b)} \right $	$\int \sqrt{a^2 - x^2} dx = \frac{1}{2} x \sqrt{a^2 - x^2} + \frac{1}{2} a^2 \tan^{-1} \frac{x}{\sqrt{a^2 - x^2}}$	$\int \frac{x^2}{\sqrt{x^2 \pm a^2}} dx = \frac{1}{2} x \sqrt{x^2 \pm a^2} \mp \frac{1}{2} a^2 \ln \left x + \sqrt{x^2 \pm a^2} \right $			
$\int \frac{1}{\sqrt{x^2 \pm a^2}} dx = \ln \left x + \sqrt{x^2 \pm a^2} \right $	$\int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1} \frac{x}{a}$	$\int \frac{x}{\sqrt{x^2 \pm a^2}} dx = \sqrt{x^2 \pm a^2}$	$\int \frac{x}{\sqrt{a^2 - x^2}} dx = -\sqrt{a^2 - x^2}$	$\int \sqrt{ax^2 + bx + c} dx = \frac{b+2ax}{4a} \sqrt{ax^2 + bx + c} + \frac{4ac-b^2}{8a^{3/2}} \ln \left 2ax + b + 2\sqrt{a(ax^2 + bx + c)} \right $	
$\int x \sqrt{ax^2 + bx + c} dx = \frac{1}{48a^{5/2}} \left(2\sqrt{a} \sqrt{ax^2 + bx + c} \times (-3b^2 + 2abx + 8a(c + ax^2)) + 3(b^3 - 4abc) \ln \left b + 2ax + 2\sqrt{a} \sqrt{ax^2 + bx + c} \right \right)$	$\int \frac{1}{\sqrt{ax^2 + bx + c}} dx = \frac{1}{\sqrt{a}} \ln \left 2ax + b + 2\sqrt{a(ax^2 + bx + c)} \right $				
$\int \frac{x}{\sqrt{ax^2 + bx + c}} dx = \frac{1}{a} \sqrt{ax^2 + bx + c} - \frac{b}{2a^{3/2}} \ln \left 2ax + b + 2\sqrt{a(ax^2 + bx + c)} \right $	$\int \frac{dx}{(a^2+x^2)^{3/2}} = \frac{x}{a^2 \sqrt{a^2+x^2}}$	Integrals with Logarithms	$\int \ln(ax+b) dx = \left(x + \frac{b}{a} \right) \ln(ax+b) - x, a \neq 0$		
$\int \frac{\ln x}{x} dx = \frac{1}{2} (\ln x)^2$	$\int \ln(x^2 + a^2) dx = x \ln(x^2 + a^2) + 2a \tan^{-1} \frac{x}{a} - 2x$	$\int \ln(x^2 - a^2) dx = x \ln(x^2 - a^2) + a \ln \frac{x+a}{x-a} - 2x$	$\int x \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4} x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2} \right) \ln(ax+b)$		
$\int \ln(ax^2 + bx + c) dx = \frac{1}{a} \sqrt{4ac - b^2} \tan^{-1} \frac{2ax+b}{\sqrt{4ac-b^2}} - 2x + \left(\frac{b}{2a} + x \right) \ln(ax^2 + bx + c)$	$\int x \ln(a^2 - b^2 x^2) dx = -\frac{1}{2} x^2 + \frac{1}{2} \left(x^2 - \frac{a^2}{b^2} \right) \ln(a^2 - b^2 x^2)$	Integrals with Exponentials			
$\int x^n e^{ax} dx = \frac{x^n e^{ax}}{a} - \frac{n}{a} \int x^{n-1} e^{ax} dx$	$\int x e^{-ax^2} dx = -\frac{1}{2a} e^{-ax^2}$	Integrals with Trigonometric Functions	$\int \sin^3 ax dx = -\frac{3 \cos ax}{4a} + \frac{\cos 3ax}{12a}$	$\int \cos^2 ax dx = \frac{x}{2} + \frac{\sin 2ax}{4a}$	
$\int \cos^3 ax dx = \frac{3 \sin ax}{4a} + \frac{\sin 3ax}{12a}$	$\int \cos ax \sin bxdx = \frac{\cos[(a-b)x]}{2(a-b)} - \frac{\cos[(a+b)x]}{2(a+b)}, a \neq b$	$\int \sin^2 ax \cos bxdx = -\frac{\sin[(2a-b)x]}{4(2a-b)} + \frac{\sin bx}{2b} - \frac{\sin[(2a+b)x]}{4(2a+b)}$	$\int \sin^2 x \cos x dx = \frac{1}{3} \sin^3 x$		
$\int \cos^2 ax \sin bxdx = \frac{\cos[(2a-b)x]}{4(2a-b)} - \frac{\cos bx}{2b} - \frac{\cos[(2a+b)x]}{4(2a+b)}$	$\int \cos^2 ax \sin ax dx = -\frac{1}{3a} \cos^3 ax$	$\int \sin^2 ax \cos^2 bxdx = \frac{x}{4} - \frac{\sin 2ax}{8a} - \frac{\sin[2(a-b)x]}{16(a-b)} + \frac{\sin 2bx}{8b} - \frac{\sin[2(a+b)x]}{16(a+b)}$	$\int \sin^2 ax \cos^2 ax dx = \frac{x}{8} - \frac{\sin 4ax}{32a}$		
$\int \tan ax dx = -\frac{1}{a} \ln \cos ax$	$\int \tan^2 ax dx = -x + \frac{1}{a} \tan ax$	$\int \tan^3 ax dx = \frac{1}{a} \ln \cos ax + \frac{1}{2a} \sec^2 ax$	$\int \sec x dx = \ln \sec x + \tan x = 2 \tanh^{-1} \left(\tan \frac{x}{2} \right)$	$\int \sec^2 ax dx = \frac{1}{a} \tan ax$	
$\int \sec^3 x dx = \frac{1}{2} \sec x \tan x + \frac{1}{2} \ln \sec x + \tan x $	$\int \sec x \tan x dx = \sec x$	$\int \sec^2 x \tan x dx = \frac{1}{2} \sec^2 x$	$\int \sec^n x \tan x dx = \frac{1}{n} \sec^n x, n \neq 0$	$\int \csc x dx = \ln \left \tan \frac{x}{2} \right = \ln \csc x - \cot x + C$	
$\int \csc^2 ax dx = -\frac{1}{a} \cot ax$	$\int \csc^3 x dx = -\frac{1}{2} \cot x \csc x + \frac{1}{2} \ln \csc x - \cot x $	$\int \csc^n x \cot x dx = -\frac{1}{n} \csc^n x, n \neq 0$	$\int \sec x \csc x dx = \ln \tan x $	Products of Trigonometric Functions and Monomials	
$\int x \cos x dx = \cos x + x \sin x$	$\int x \cos ax dx = \frac{1}{a^2} \cos ax + \frac{x}{a} \sin ax$	$\int x^2 \cos x dx = 2x \cos x + (x^2 - 2) \sin x$	$\int x^2 \cos ax dx = \frac{2x \cos ax}{a^2} + \frac{a^2 x^2 - 2}{a^3} \sin ax$	$\int x \sin x dx = -x \cos x + \sin x$	
$\int x \sin ax dx = -\frac{x \cos ax}{a} + \frac{\sin ax}{a^2}$	$\int x^2 \sin x dx = (2 - x^2) \cos x + 2x \sin x$	$\int x^2 \sin ax dx = \frac{2-a^2 x^2}{a^3} \cos ax + \frac{2x \sin ax}{a^2}$	Products of Trigonometric Functions and Exponentials		
$\int e^x \sin x dx = \frac{1}{2} e^x (\sin x - \cos x)$	$\int e^{bx} \sin ax dx = \frac{1}{a^2 + b^2} e^{bx} (b \sin ax - a \cos ax)$	$\int e^{bx} \cos ax dx = \frac{1}{a^2 + b^2} e^{bx} (a \sin ax + b \cos ax)$	$\int x e^x \sin x dx = \frac{1}{2} e^x (\cos x - x \cos x + x \sin x)$		
$\int x e^x \cos x dx = \frac{1}{2} e^x (x \cos x - \sin x + x \sin x)$	$\int e^x \cos x dx = \frac{1}{2} e^x (\sin x + \cos x)$				

Java

```

1 import java.io.*;
2 import java.util.*;
3 import java.math.*;
4
5 public class Main{
6     BufferedReader reader = new BufferedReader(new InputStreamReader(System.in));
7     PrintWriter writer = new PrintWriter(System.out);
8     StringTokenizer tokenizer = null;
9
10    void solve() throws Exception {
11    }
12    void run()throws Exception{
13        try{

```

```

14        while (true) {
15            solve();
16        }
17    }
18    catch(Exception e){
19    }
20    finally{
21        reader.close();
22        writer.close();
23    }
24    }
25    String next()throws Exception{
26        for(;tokenizer == null || !tokenizer.hasMoreTokens();){
27            tokenizer = new StringTokenizer(reader.readLine());

```

```
28     }
29     return tokenizer.nextToken();
30 }
31 int nextInt()throws Exception{
32     return Integer.parseInt(next());
33 }
34 double nextDouble()throws Exception{
35     return Double.parseDouble(next());
36 }
37 BigInteger nextBigInteger()throws Exception{
38     return new BigInteger(next());
39 }
40 public static void main(String args[])throws Exception{
41     (new Main()).run();
42 }
43 }
```

Vimrc

```
1 \begin{lstlisting}
2 set nu ai ci si mouse=a ts=4 sts=4 sw=4
3
4 nmap<C-A> ggVG
5 vmap<C-C> "+y
6
7 nmap<F3> : vs %<.in <CR>
8 nmap<F5> : !./%< <CR>
9 nmap<F8> : !./%< <%<.in <CR>
10 nmap<F9> : !g++ % -o %< -Wall <CR>
11
12 "nmap<F4> : !gedit % <CR>
13 "autocmd BufNewFile *.cpp 0r ~/temp.cpp
14 "set hlsearch incsearch
15
16 "syntax on
17 "filetype plugin indent on
18 \end{lstlisting}
```