Dracarys

Team Referrence Library

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上海交通大学 Shanghai Jiao Tong University			Page 1
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多边形与圆面积交

```
1 point ORI;
 2 double r;
 3 \mid int n;
 4 | point info[maxn];
   // 用有向面积,划分成一个三角形和圆的面积的交
 6 double area2(point pa, point pb) {
     if (pa.len() < pb.len()) swap(pa, pb);</pre>
     if (pb.len() < eps) return 0;</pre>
 9
     double a, b, c, B, C, sinB, cosB, sinC, cosC, S, h, theta;
     a = pb.len();
10
     b = pa.len();
11
     c = (pb - pa).len();
12
     cosB = dot(pb, pb - pa) / a / c;
13
14
     B = acos(cosB);
     cosC = dot(pa, pb) / a / b;
15
16
     C = acos(cosC);
17
     if (a > r) {
18
       S = (C/2)*r*r;
19
       h = a*b*sin(C)/c;
20
       if (h < r \&\& B < PI/2) S -= (acos(h/r)*r*r - h*sqrt(r*r-h*h));
     } else if (b > r) {
21
       theta = PI - B - asin(sin(B)/r*a);
22
       S = .5*a*r*sin(theta) + (C-theta)/2*r*r;
23
     } else {
24
25
       S = .5*sin(C)*a*b;
26
     //printf("res = %.4f\n", S);
27
28
     return S;
29
30 double area() {
     double S = 0;
31
     for (int i = 0; i < n; ++i) {
32
       S += area2(info[i], info[i + 1]) * Sign(cross(info[i], info[i + 1]));
33
34
     return fabs(S);
35
36 }
```

二维几何

```
#include <iostream>
#include <cmath>
#include <vector>

using namespace std;
```

```
7 const double PI = acos(-1.0);
   const double EPS = 1e-8:
10 int sign(double x)
11
     return x \leftarrow -EPS ? -1 : x > EPS;
12
13
14
15
   double newSqrt(double x)
16
17
     return x < 0 ? 0 : sqrt(x);
18
19
20
   struct Point {
     double x, y;
21
     Point(double x = 0, double y = 0) : x(x), y(y) {}
22
     Point operator + (const Point &that) const {
23
       return Point(x + that.x, y + that.y);
24
25
     Point operator - (const Point &that) const {
26
       return Point(x - that.x, y - that.y);
27
28
     Point operator * (const double &that) const {
29
       return Point(x * that, y * that);
30
31
     Point operator / (const double &that) const {
32
       return Point(x / that, y / that);
33
34
     Point rotate(const double ang) { // 逆时针旋转 ang 弧度
35
       return Point(cos(ang) * x - sin(ang) * y, cos(ang) * y + sin(ang) * x);
36
37
38
     Point turn90() { // 逆时针旋转 90 度
       return Point(-y, x);
39
40
41
     double len2() const {
42
       return x * x + y * y;
43
     double len() const {
44
       return sqrt(x * x + y * y);
45
46
47
     Point unit() const {
48
       return *this / len();
49
50
51 double det(Point a, Point b)
```

```
52 | {
     return a.x * b.y - b.x * a.y;
53
54 | }
55
   double dot(Point a, Point b)
56 | {
     return a.x * b.x + a.y * b.y;
57
58 }
59
60 struct Line {
61
     Point a, b;
62
     Line(Point a, Point b) : a(a), b(b) {}
63 | };
64
65 Point isLL(const Line &10, const Line &11) {
66
     double s0 = det(l1.b - l1.a, l0.a - l1.a),
67
          s1 = -det(11.b - 11.a, 10.b - 11.a);
68
     return (10.a * s1 + 10.b * s0) / (s0 + s1);
69 | }
   bool onSeg(const Line &1, const Point &p) { // 点在线段上
70
     return sign(det(p - 1.a, 1.b - 1.a)) == 0 && sign(dot(p - 1.a, p - 1.b)) <= 0;
71
72
   Point projection(const Line &l, const Point &p) { // 点到直线投影
73
     return l.a + (l.b - l.a) * (dot(p - l.a, l.b - l.a) / (l.b - l.a).len2());
74
75
   double disToLine(const Line &1, const Point &p) {
76
     return abs(det(p - 1.a, 1.b - 1.a) / (1.b - 1.a).len());
77
78 }
   ˈdouble disToSeg(const Line &l, const Point &p) { // 点到线段距离
79
80
     return sign(dot(p - 1.a, 1.b - 1.a)) * sign(dot(p - 1.b, 1.a - 1.b)) != 1 ?
81
       disToLine(1, p) : min((p - 1.a).len(), (p - 1.b).len());
82 }
83 | Point symmetryPoint(const Point a, const Point b) { // 点 b 关于点 a 的中心对称点
84
     return a + a - b;
85 }
86 | Point reflection(const Line &1, const Point &p) { // 点关于直线的对称点
     return symmetryPoint(projection(1, p), p);
87
88 }
8g struct Circle {
     Point o;
90
     double r:
91
92
     Circle (Point o = Point(0, 0), double r = 0) : o(o), r(r) {}
93 | };
   // 求圆与直线的交点
   | bool isCL(Circle a, Line 1, Point &p1, Point &p2) {
95
     if (sign(det(l.a - a.o, l.b - a.o) / (l.a - l.b).len()) > 0) return false;
```

```
Point o = isLL(Line(a.o., a.o + (1.b - 1.a).turn90()), 1);
 97
 98
      Point delta = (1.b - 1.a).unit() * newSqrt(a.r * a.r - (o - a.o).len2()):
      p1 = o + delta:
 99
100
      p2 = o - delta;
      return true;
101
102
103
    // 求圆与圆的交面积
104
    double areaCC(const Circle &c1, const Circle &c2) {
106
      double d = (c1.o - c2.o).len();
      if (sign(d - (c1.r + c2.r)) > 0) {
107
        return 0;
108
109
110
      if (sign(d - abs(c1.r - c2.r)) < 0) {
111
        double r = min(c1.r, c2.r);
        return r * r * PI;
112
113
      double x = (d * d + c1.r * c1.r - c2.r * c2.r) / (2 * d),
114
           t1 = acos(x / c1.r), t2 = acos((d - x) / c2.r);
115
      return c1.r * c1.r * t1 + c2.r * c2.r * t2 - d * c1.r * sin(t1);
116
117 }
118
    // 求圆与圆的交点,注意调用前要先判定重圆
119
    bool isCC(Circle a, Circle b, Point &p1, Point &p2) {
120
121
      double s1 = (a.o - b.o).len();
      if (sign(s1 - a.r - b.r)) > 0 \mid | sign(s1 - abs(a.r - b.r)) < 0) return false;
122
      double s2 = (a.r * a.r - b.r * b.r) / s1;
123
124
      double aa = (s1 + s2) * 0.5, bb = (s1 - s2) * 0.5;
      Point o = (b.o - a.o) * (aa + bb)) + a.o;
125
126
      Point delta = (b.o - a.o).unit().turn90() * newSqrt(a.r * a.r - aa * aa);
      p1 = o + delta, p2 = o - delta;
127
128
      return true;
120
130
    // 求点到圆的切点,按关于点的左手方向返回两个点
132
    bool tanCP(const Circle &c, const Point &p0, Point &p1, Point &p2)
133
      double x = (p0 - c.o).len2(), d = x - c.r * c.r;
134
      if (d < EPS) return false;</pre>
135
      Point p = (p0 - c.o) * (c.r * c.r / x);
136
137
      Point delta = ((p0 - c.o) * (-c.r * sqrt(d) / x)).turn90();
138
      p1 = c.o + p + delta;
      p2 = c.o + p - delta;
139
140
      return true;
141 }
```

```
142
    // 求圆到圆的外共切线, 按关于 c1.o 的左手方向返回两条线
143
    vector<Line> extanCC(const Circle &c1, const Circle &c2)
145
146
      vector<Line> ret;
      if (sign(c1.r - c2.r) == 0) {
147
148
        Point dir = c2.o - c1.o;
        dir = (dir * (c1.r / dir.len())).turn90();
149
150
        ret.push_back(Line(c1.o + dir, c2.o + dir));
        ret.push_back(Line(c1.o - dir, c2.o - dir));
151
      } else {
152
        Point p = (c1.0 * -c2.r + c2.o * c1.r) / (c1.r - c2.r);
153
        Point p1, p2, q1, q2;
154
        if (tanCP(c1, p, p1, p2) && tanCP(c2, p, q1, q2)) {
155
156
          if (c1.r < c2.r) swap(p1, p2), swap(q1, q2);
          ret.push_back(Line(p1, q1));
157
158
          ret.push_back(Line(p2, q2));
        }
159
160
     }
161
      return ret;
162 }
163
    // 求圆到圆的内共切线, 按关于 c1.o 的左手方向返回两条线
164
    vector<Line> intanCC(const Circle &c1, const Circle &c2)
166 | {
167
      vector<Line> ret;
168
      Point p = (c1.0 * c2.r + c2.0 * c1.r) / (c1.r + c2.r);
169
      Point p1, p2, q1, q2;
      if (tanCP(c1, p, p1, p2) && tanCP(c2, p, q1, q2)) {
170
171
        ret.push_back(Line(p1, q1));
        ret.push_back(Line(p2, q2));
172
     }
173
174
      return ret;
175 | }
176
177
178 | int main()
179 | {
180
      return 0;
181
```

$n \log n$ 半平面交

```
#define cross(p1,p2,p3)((p2.x-p1.x)*(p3.y-p1.y)-(p3.x-p1.x)*(p2.y-p1.y))
#define crossOp(p1,p2,p3) sign(cross(p1,p2,p3))
Point isSS(Point p1,Point p2,Point q1,Point q2){
```

```
double a1=cross(q1,q2,p1),a2=-cross(q1,q2,p2);
5
     return(p1*a2+p2*a1)/(a1+a2);
6 }
7 | struct Border{
     void setAlpha(){ alpha=atan2(p2.y-p1.y,p2.x-p1.x);}
   }border[MAX N BORDER];
10
   int n:
   bool operator<(const Border&a,const Border&b){</pre>
11
12
     int c=sign(a.alpha-b.alpha);
13
     if(c!=0) return c==1;
     return crossOp(b.p1,b.p2,a.p1)>=0;
14
15
   bool operator==(const Border&a,const Border&b){ return sign(a.alpha-b.alpha)==0;}
16
   void add(double x,double y,double nx,double ny){
17
     border[n].p1=Point(x,y);border[n].p2=Point(nx,ny);
18
     border[n].setAlpha();n++;
19
20
   Point isBorder(const Border&a,const Border&b) { return isSS(a.p1,a.p2,b.p1,b.p2);}
21
   Border que[MAX N BORDER]; int qh,qt;
23
   bool check(const Border&a,const Border&b,const Border&me){
     Point is=isBorder(a,b); return crossOp(me.p1,me.p2,is)>0;
24
25
26
   void convexIntersection(){
     qh=qt=0; sort(border,border+n); n=unique(border,border+n)-border;
27
28
     for(int i=0;i<n;++i){</pre>
       Border cur=border[i];
29
       while(qh+1<qt&&!check(que[qt-2],que[qt-1],cur)) --qt;</pre>
30
31
       while(qh+1<qt&&!check(que[qh],que[qh+1],cur)) ++qh;</pre>
       que[qt++]=cur;
32
33
     while(qh+1<qt&&!check(que[qt-2],que[qt-1],que[qh])) --qt;</pre>
34
     while(qh+1<qt&&!check(que[qh],que[qh+1],que[qt-1])) ++qh;</pre>
35
36
37
   void calcArea(){
     static Point ps[MAX_N_BORDER]; int cnt=0;
38
39
     if(qt-qh<=2){ puts("0.0"); return; }</pre>
     for(int i=qh;i<qt;++i){</pre>
       int next=i+1==qt?qh:i+1; ps[cnt++]=isBorder(que[i],que[next]);
41
42
     double area=0:
43
44
     for(int i=0;i<cnt;++i) area += ps[i].det(ps[(i+1) % cnt]);</pre>
     area/=2; area=fabsl(area);
45
46
     cout.setf(ios::fixed); cout.precision(1); cout<<area<<endl;</pre>
47 }
48 void halfPlaneIntersection(){
```

```
cin>>n; for(int i=0;i<n;++i) border[i].read();
add(0,0,LARGE,0); add(LARGE,LARGE);
add(LARGE,LARGE); add(0,LARGE,0,0);
convexIntersection(); calcArea();
}</pre>
```

Delaunay 三角剖分

```
1 /*
2 Delaunay Triangulation 随机增量算法:
3 节点数至少为点数的 6 倍,空间消耗较大注意计算内存使用
   建图的过程在 build 中,注意初始化内存池和初始三角形的坐标范围 (Triangulation::LOTS)
   Triangulation::find 返回包含某点的三角形
6 | Triangulation::add_point 将某点加入三角剖分
   某个 Triangle 在三角剖分中当且仅当它的 has children 为 0
8 \mid 如果要找到三角形 u 的邻域,则枚举它的所有 u.edge[i].tri, 该条边的两个点为 u.p[(i+1)%3],
     \hookrightarrow u.p[(i+2)\%3]
9 | */
10 \mid const int N = 100000 + 5;
11 const int MAX TRIS = N * 6;
12 const double EPSILON = 1e-6;
13 const double PI = acos(-1.0);
   using namespace std;
14
15
16 | struct Point {
17
     double x,y;
18
     Point(): x(0), y(0) {}
     Point(double x, double y) : x(x), y(y) {}
19
     inline bool operator == (Point const& that) const {
20
21
       return x == that.x && y == that.y;
22
23 | };
24
   inline double sqr(double x) { return x*x; }
25
   double dist sqr(Point const& a, Point const& b) {
26
     return sqr(a.x-b.x) + sqr(a.y-b.y);
27
28
29 bool in circumcircle(Point const& p1, Point const& p2, Point const& p3, Point const&
     → p4) {
     double u11 = p1.x - p4.x;
30
     double u21 = p2.x - p4.x;
31
32
     double u31 = p3.x - p4.x;
     double u12 = p1.y - p4.y;
33
     double u22 = p2.y - p4.y;
34
     double u32 = p3.y - p4.y;
35
36
     double u13 = sqr(p1.x) - sqr(p4.x) + sqr(p1.y) - sqr(p4.y);
```

```
double u23 = sqr(p2.x) - sqr(p4.x) + sqr(p2.y) - sqr(p4.y);
37
38
     double u33 = sqr(p3.x) - sqr(p4.x) + sqr(p3.y) - sqr(p4.y);
     double det = -u13*u22*u31 + u12*u23*u31 + u13*u21*u32 - u11*u23*u32 - u12*u21*u33

→ + u11*u22*u33:

     return det > EPSILON;
40
41
42
   double side(Point const& a, Point const& b, Point const& p) {
     return (b.x-a.x)*(p.y-a.y) - (b.y-a.y)*(p.x-a.x);
43
44
45
   typedef int SideRef;
   struct Triangle;
   typedef Triangle* TriangleRef;
   struct Edge {
     TriangleRef tri;
     SideRef
                 side;
     Edge() : tri(0), side(0) {}
     Edge(TriangleRef tri, SideRef side) : tri(tri), side(side) {}
53
54
55
   struct Triangle {
     Point p[3];
     Edge edge[3];
57
     TriangleRef children[3];
     Triangle() {}
59
60
     Triangle(Point const& p0, Point const& p1, Point const& p2) {
61
       p[0] = p0; p[1] = p1; p[2] = p2;
62
       children[0] = children[1] = children[2] = 0;
63
64
     bool has_children() const {
65
       return children[0] != 0;
66
67
     int num_children() const {
68
       return children[0] == 0 ? 0
69
         : children[1] == 0 ? 1
         : children[2] == 0 ? 2 : 3;
70
71
     bool contains(Point const& q) const {
72
       double a = side(p[0],p[1],q);
73
       double b = side(p[1],p[2],q);
74
       double c = side(p[2], p[0], q);
75
       return a >= -EPSILON && b >= -EPSILON && c >= -EPSILON;
76
77
   } triange pool[MAX TRIS], *tot triangles;
   void set edge(Edge a, Edge b) {
79
    if (a.tri) a.tri->edge[a.side] = b;
```

```
81
      if (b.tri) b.tri->edge[b.side] = a;
                                                                                                         set edge(Edge(tab,0), Edge(tbc,1));
                                                                                              125
 82
      if (a.tri && b.tri) {
                                                                                              126
                                                                                                         set_edge(Edge(tbc,0), Edge(tca,1));
 83
        assert(a.tri->p[(a.side+1)%3] == b.tri->p[(b.side+2)%3]);
                                                                                                         set_edge(Edge(tca,0), Edge(tab,1));
                                                                                              127
 84
        assert(a.tri->p[(a.side+2)%3] == b.tri->p[(b.side+1)%3]);
                                                                                              128
                                                                                                         set_edge(Edge(tab,2), root->edge[2]);
 85
                                                                                                         set_edge(Edge(tbc,2), root->edge[0]);
                                                                                              129
 86
                                                                                                         set_edge(Edge(tca,2), root->edge[1]);
                                                                                              130
 87
    class Triangulation {
                                                                                                         root->children[0] = tab;
                                                                                              131
 88
      public:
                                                                                                         root->children[1] = tbc;
                                                                                              132
 89
        Triangulation() {
                                                                                              133
                                                                                                         root->children[2] = tca;
 90
          const double LOTS = 1e6;
                                                                                                         flip(tab,2);
                                                                                              134
                                                                                                         flip(tbc,2);
          the_root = new(tot_triangles++)
 91
                                                                                              135

¬ Triangle(Point(-LOTS,-LOTS), Point(+LOTS,-LOTS), Point(0,+LOTS));
                                                                                              136
                                                                                                         flip(tca,2);
        }
 92
                                                                                              137
                                                                                                       void flip(TriangleRef tri, SideRef pi) {
 93
        ~Triangulation() {}
                                                                                              138
        TriangleRef find(Point p) const {
                                                                                                         TriangleRef trj = tri->edge[pi].tri;
 94
                                                                                              139
          return find(the_root,p);
                                                                                                         int pj = tri->edge[pi].side;
                                                                                              140
 95
 96
                                                                                                         if (!trj) return;
                                                                                              141
                                                                                                         if (!in circumcircle(tri->p[0],tri->p[1],tri->p[2],trj->p[p]])) return;
        void add point(Point const& p) {
 97
                                                                                              142
                                                                                                         assert(tri->p[(pi+2)%3] == trj->p[(pj+1)%3]);
 98
          add point(find(the root,p),p);
                                                                                              143
 99
        }
                                                                                              144
                                                                                                         assert(tri->p[(pi+1)%3] == trj->p[(pj+2)%3]);
      private:
                                                                                                         /* flip edge between tri,trj */
100
                                                                                              145
        TriangleRef the_root;
                                                                                              146
                                                                                                        TriangleRef trk = new(tot_triangles++) Triangle(tri->p[(pi+1)%3], trj->p[pj],
101
        static TriangleRef find(TriangleRef root, Point const& p) {

    tri->p[pi]);
102
          for(;;) {
                                                                                                         TriangleRef trl = new(tot triangles++) Triangle(trj->p[(pj+1)%3], tri->p[pi],
103
                                                                                              ^{147}
            assert(root->contains(p));

    trj->p[pj]);

104
            if (!root->has_children()) {
                                                                                                         set edge(Edge(trk,0), Edge(trl,0));
105
                                                                                              148
106
              return root;
                                                                                                         set_edge(Edge(trk,1), tri->edge[(pi+2)%3]);
                                                                                              149
                                                                                                         set_edge(Edge(trk,2), trj->edge[(pj+1)%3]);
            } else {
107
                                                                                              150
              int flag = true;
                                                                                                         set_edge(Edge(trl,1), trj->edge[(pj+2)%3]);
108
                                                                                              151
              for (int i = 0; i < 3 && root->children[i]; ++i) {
                                                                                                         set_edge(Edge(trl,2), tri->edge[(pi+1)%3]);
109
                                                                                              152
                if (root->children[i]->contains(p)) {
                                                                                                         tri->children[0] = trk; tri->children[1] = trl; tri->children[2] = 0;
110
                                                                                              153
                   root = root->children[i];
                                                                                                         trj->children[0] = trk; trj->children[1] = trl; trj->children[2] = 0;
111
                                                                                              154
                                                                                                         flip(trk,1);
                  break:
112
                                                                                              155
                }
                                                                                              156
                                                                                                         flip(trk,2);
113
                                                                                                         flip(trl,1);
114
                                                                                              157
115
              assert(flag&&"point not found");
                                                                                              158
                                                                                                         flip(trl,2);
116
            }
                                                                                              159
          }
                                                                                              160 };
117
118
                                                                                              161
        void add_point(TriangleRef root, Point const& p) {
                                                                                              162 int n;
119
          TriangleRef tab,tbc,tca;
                                                                                              163 Point ps[N];
120
121
          /* split it into three triangles */
                                                                                              164
          tab = new(tot triangles++) Triangle(root->p[0], root->p[1], p);
122
                                                                                              165
                                                                                                  void build()
          tbc = new(tot_triangles++) Triangle(root->p[1], root->p[2], p);
                                                                                              166 {
123
                                                                                              167
          tca = new(tot_triangles++) Triangle(root->p[2], root->p[0], p);
124
                                                                                                   tot_triangles = triange_pool;
```

```
168
      cin >> n:
169
      for(int i = 0; i < n; ++ i) {
170
        int x, y;
171
        scanf("%d%d", &x, &y);
        ps[i].x = x; ps[i].y = y;
172
173
      random_shuffle(ps, ps + n);
174
      Triangulation tri;
175
176
      for(int i = 0; i < n; ++ i) {
177
        tri.add_point(ps[i]);
178
179 | }
180
181 | int main()
182 {
183
      build();
184
      return 0;
185 }
```

三维几何操作合并

```
1 | const double pi = acos(-1.0); double a[4][4];
2 int dcmp(const double &a,const double &b = 0,const double & zero = 1e-6){
     if(a-b<-zero) return -1; return a-b>zero;}
   void multi(const double a[4][4], const double b[4][4], double c[4][4]){
     for(int i=0;i<4;i++) for(int j=0;j<4;j++){
6
       c[i][j]=a[i][0]*b[0][j]; for(int k=1;k<4;k++) c[i][j]+=a[i][k]*b[k][j];
    }}
   void multi(double a[4][4],const double b[4][4]){
9
     static double c[4][4]; multi(a,b,c); memcpy(a,c,sizeof(a[0][0])*16);
10
   void Macro(){
11
     double b[4][4]={1,0,0,0,0,1,0,0,0,1,0,0,0,0,1};
12
     memcpy(a,b,sizeof(a[0][0])*16);
13
14
   void Translation(const Point 3 &s){
15
16
     double p[4][4]=\{1,0,0,0,0,1,0,0,0,0,1,0,s.x,s.y,s.z,1\};
     multi(a,p);
17
18 }
   void Scaling(const Point 3 &s){
19
     double p[4][4]=\{s.x,0,0,0,0,s.y,0,0,0,s.z,0,0,0,0,1\};
20
21
     multi(a,p);
22
   void Rotate(const Point_3 &s,double r) {
23
     double l=s.Length(),x=s.x/l,y=s.y/l,z=s.z/l,SinA=sin(r),CosA=cos(r);
24
     double p[4][4]=\{\cos A + (1-\cos A)*x*x, (1-\cos A)*x*y-\sin A*z, (1-\cos A)*x*z+\sin A*y, 0, 0\}
```

```
26
       (1-CosA)*y*x+SinA*z,CosA +(1-CosA)*y*y,(1-CosA)*y*z-SinA*x,∅,
27
       (1-\cos A)*z*x-\sin A*y, (1-\cos A)*z*y+\sin A*x, \cos A + (1-\cos A)*z*z, 0, 0, 0, 0, 1;
28
     multi(a,p);
29
   Point 3 opt(const Point 3&s){
     return Point_3( s.x*a[0][0]+s.y*a[1][0]+s.z*a[2][0]+a[3][0],
31
     s.x*a[0][1]+s.y*a[1][1]+s.z*a[2][1]+a[3][1],
32
     s.x*a[0][2]+s.y*a[1][2]+s.z*a[2][2]+a[3][2]);
33
34
   int main(){
35
36
     Macro();
     int n; for(scanf("%d",&n);n;n--) {
37
38
       char c; Point_3 p;
39
       scanf("\n%c%lf%lf%lf",&c,&p.x,&p.y,&p.z);
       if(c == 'T') Translation(p); if(c == 'S') Scaling(p);
40
       if(c == 'R'){ double r;scanf("%lf\n",&r);
41
         42
       }}
43
     for(scanf("%d",&n);n;n--) {
44
45
       Point_3 p,p2; scanf("%lf%lf",&p.x,&p.y,&p.z);
46
       p2 = opt(p); printf("%f %f %f\n",p2.x,p2.y,p2.z);
    }}
47
```

三维旋转操作

三维凸包

```
#define SIZE(X) (int(X.size()))
#define PI 3.14159265358979323846264338327950288

struct Point {
    Point cross(const Point &p) const
    { return Point(y * p.z - z * p.y, z * p.x - x * p.z, x * p.y - y * p.x); }
} info[1005];
int mark[1005][1005],n, cnt;;

double mix(const Point &a, const Point &b, const Point &c)
```

```
9 | { return a.dot(b.cross(c)); }
10 double area(int a, int b, int c)
11 | { return ((info[b] - info[a]).cross(info[c] - info[a])).length(); }
12 double volume(int a, int b, int c, int d)
13 | { return mix(info[b] - info[a], info[c] - info[a], info[d] - info[a]); }
14 | struct Face {
     int a, b, c; Face() {}
15
16
     Face(int a, int b, int c): a(a), b(b), c(c) {}
17
     int &operator [](int k)
18
     { if (k == 0) return a; if (k == 1) return b; return c; }
19|};
20 vector <Face> face;
   inline void insert(int a, int b, int c) { face.push_back(Face(a, b, c)); }
22
   void add(int v) {
     vector <Face> tmp; int a, b, c; cnt++;
23
     for (int i = 0; i < SIZE(face); i++) {</pre>
24
       a = face[i][0]; b = face[i][1]; c = face[i][2];
25
26
       if (Sign(volume(v, a, b, c)) < 0)</pre>
       mark[a][b] = mark[b][a] = mark[b][c] = mark[c][b] = mark[c][a] = mark[a][c] =
27

    cnt;

28
       else tmp.push back(face[i]);
     } face = tmp;
29
     for (int i = 0; i < SIZE(tmp); i++) {</pre>
30
       a = face[i][0]; b = face[i][1]; c = face[i][2];
31
32
       if (mark[a][b] == cnt) insert(b, a, v);
       if (mark[b][c] == cnt) insert(c, b, v);
33
       if (mark[c][a] == cnt) insert(a, c, v);
34
35 | }}
36 \mid int Find()  {
37
     for (int i = 2; i < n; i++) {
38
       Point ndir = (info[0] - info[i]).cross(info[1] - info[i]);
       if (ndir == Point()) continue; swap(info[i], info[2]);
39
       for (int j = i + 1; j < n; j++) if (Sign(volume(0, 1, 2, j)) != 0) {
40
         swap(info[j], info[3]); insert(0, 1, 2); insert(0, 2, 1); return 1;
41
42|} return 0; }
   int main() {
43
      for (; scanf("%d", &n) == 1; ) {
44
        for (int i = 0; i < n; i++) info[i].Input();</pre>
45
        sort(info, info + n); n = unique(info, info + n) - info;
46
       face.clear(); random shuffle(info, info + n);
47
48
        if (Find()) { memset(mark, 0, sizeof(mark)); cnt = 0;
         for (int i = 3; i < n; i++) add(i); vector<Point> Ndir;
49
         for (int i = 0; i < SIZE(face); ++i) {</pre>
50
           Point p = (info[face[i][0]] - info[face[i][1]]).cross(
51
                info[face[i][2]] - info[face[i][1]]);
52
```

```
53
           p = p / p.length(); Ndir.push back(p);
         } sort(Ndir.begin(), Ndir.end());
54
         int ans = unique(Ndir.begin(), Ndir.end()) - Ndir.begin();
55
56
         printf("%d\n", ans);
       } else printf("1\n");
57
  } }
58
59 // 求重心
   double calcDist(const Point &p, int a, int b, int c)
   { return fabs(mix(info[a] - p, info[b] - p, info[c] - p) / area(a, b, c)); }
   //compute the minimal distance of center of any faces
   double findDist() { //compute center of mass
64
     double totalWeight = 0; Point center(.0, .0, .0);
     Point first = info[face[0][0]];
65
66
     for (int i = 0; i < SIZE(face); ++i) {</pre>
67
       Point p = (info[face[i][0]]+info[face[i][1]]+info[face[i][2]]+first)*.25;
68
       double weight = mix(info[face[i][0]] - first, info[face[i][1]]
           - first, info[face[i][2]] - first);
69
       totalWeight += weight; center = center + p * weight;
70
     } center = center / totalWeight;
71
72
     double res = 1e100; //compute distance
     for (int i = 0; i < SIZE(face); ++i)</pre>
73
       res = min(res, calcDist(center, face[i][0], face[i][1], face[i][2]));
74
75
       return res; }
```

凸包上快速询问

```
1 /*
     给定凸包, \log n 内完成各种询问, 具体操作有:
    1. 判定一个点是否在凸包内
     2. 询问凸包外的点到凸包的两个切点
     3. 询问一个向量关于凸包的切点
     4. 询问一条直线和凸包的交点
     INF 为坐标范围,需要定义点类大于号
     改成实数只需修改 sign 函数,以及把 long long 改为 double 即可
     构造函数时传入凸包要求无重点,面积非空,以及 pair(x,y) 的最小点放在第一个
9
10
11
  #include <vector>
  #include <functional>
12
  using namespace std;
14
15
  const int INF = 1000000000;
16
  struct Convex
17
18
    int n;
    vector<Point> a;
```

```
vector<Point> upper, lower:
                                                                                           66
                                                                                                  return 1 % n:
     Convex(vector<Point> a) : a( a) {
                                                                                           67
22
                                                                                           68
                                                                                                // 判定点是否在凸包内, 在边界返回 true
       n = a.size();
23
24
       int ptr = 0;
                                                                                           69
                                                                                                bool contain(Point p) {
       for(int i = 1; i < n; ++ i) if (a[ptr] < a[i]) ptr = i;
                                                                                                  if (p.x < lower[0].x || p.x > lower.back().x) return false;
25
                                                                                           70
26
       for(int i = 0; i <= ptr; ++ i) lower.push_back(a[i]);</pre>
                                                                                                  int id = lower bound(lower.begin(), lower.end(), Point(p.x, -INF)) -
                                                                                           71
                                                                                                → lower.begin():
27
       for(int i = ptr; i < n; ++ i) upper.push back(a[i]);</pre>
       upper.push back(a[0]);
                                                                                                  if (lower[id].x == p.x) {
28
                                                                                           72
                                                                                                   if (lower[id].y > p.y) return false;
29
                                                                                           73
30
     int sign(long long x) {
                                                                                           74
                                                                                                  } else if ((lower[id - 1] - p).det(lower[id] - p) < 0) return false;</pre>
       return x < 0 ? -1 : x > 0;
                                                                                                  id = lower_bound(upper.begin(), upper.end(), Point(p.x, INF), greater<Point>())
                                                                                           75
31
                                                                                                → - upper.begin();
32
     pair<long long, int> get_tangent(vector<Point> &convex, Point vec) {
                                                                                           76
                                                                                                  if (upper[id].x == p.x) {
33
       int l = 0, r = (int)convex.size() - 2;
                                                                                                   if (upper[id].y < p.y) return false;</pre>
34
                                                                                           77
       for(; l + 1 < r; ) {
35
                                                                                           78
                                                                                                 } else if ((upper[id - 1] - p).det(upper[id] - p) < 0) return false;</pre>
36
        int mid = (1 + r) / 2;
                                                                                           79
                                                                                                  return true;
        if (sign((convex[mid + 1] - convex[mid]).det(vec)) > 0) r = mid;
                                                                                           80
37
                                                                                                // 求点 p 关于凸包的两个切点,如果在凸包外则有序返回编号,多解返回任意一个图否则返回
38
         else 1 = mid:
                                                                                           81
39
       return max(make pair(vec.det(convex[r]), r), make pair(vec.det(convex[0]), 0));
                                                                                                bool get tangent(Point p, int &i0, int &i1) {
40
                                                                                           82
                                                                                           83
                                                                                                  if (contain(p)) return false;
41
                                                                                           84
42
     void update tangent(const Point &p, int id, int &i0, int &i1) {
                                                                                                  i0 = i1 = 0:
                                                                                           85
       if ((a[i0] - p).det(a[id] - p) > 0) i0 = id;
                                                                                                  int id = lower bound(lower.begin(), lower.end(), p) - lower.begin();
43
       if ((a[i1] - p).det(a[id] - p) < 0) i1 = id;</pre>
                                                                                           86
                                                                                                  binary search(0, id, p, i0, i1);
44
                                                                                           87
                                                                                                  binary search(id, (int)lower.size(), p, i0, i1);
45
46
     void binary search(int 1, int r, Point p, int &i0, int &i1) {
                                                                                           88
                                                                                                  id = lower bound(upper.begin(), upper.end(), p, greater<Point>()) -
       if (1 == r) return;
                                                                                                → upper.begin();
47
48
       update_tangent(p, 1 % n, i0, i1);
                                                                                           89
                                                                                                  binary_search((int)lower.size() - 1, (int)lower.size() - 1 + id, p, i0, i1);
       int sl = sign((a[1 \% n] - p).det(a[(1 + 1) \% n] - p));
                                                                                                  binary_search((int)lower.size() - 1 + id, (int)lower.size() - 1 +
49
       for(; l + 1 < r; ) {
                                                                                                50
        int mid = (1 + r) / 2;
                                                                                           91
                                                                                                  return true;
51
         int smid = sign((a[mid % n] - p).det(a[(mid + 1) % n] - p));
                                                                                                }
52
                                                                                           92
                                                                                                // 求凸包上和向量 vec 叉积最大的点,返回编号,有多个返回任意一个
         if (smid == sl) l = mid;
                                                                                           93
53
         else r = mid;
                                                                                                int get_tangent(Point vec) {
                                                                                           94
54
                                                                                                  pair<long long, int> ret = get_tangent(upper, vec);
55
                                                                                           95
                                                                                                  ret.second = (ret.second + (int)lower.size() - 1) % n;
56
       update tangent(p, r % n, i0, i1);
                                                                                           96
                                                                                                  ret = max(ret, get tangent(lower, vec));
                                                                                           97
57
58
     int binary search(Point u, Point v, int l, int r) {
                                                                                           98
                                                                                                  return ret.second;
       int sl = sign((v - u).det(a[1 % n] - u));
59
                                                                                           99
                                                                                                // 求凸包和直线 u,v 的交点, 如果无严格相交返回 false 。如果有则是和(i,next(i))
60
       for(; l + 1 < r; ) {
                                                                                         100
                                                                                                → 的交点, 两个点无序, 交在点上不确定返回两条线段之一。
61
         int mid = (1 + r) / 2;
62
         int smid = sign((v - u).det(a[mid % n] - u));
                                                                                         101
                                                                                                bool get intersection(Point u, Point v, int &i0, int &i1) {
63
         if (smid == sl) l = mid;
                                                                                                  int p0 = get tangent(u - v), p1 = get tangent(v - u);
                                                                                         102
         else r = mid;
                                                                                                  if (sign((v - u).det(a[p0] - u)) * sign((v - u).det(a[p1] - u)) < 0) {
64
                                                                                         103
65
                                                                                                    if (p0 > p1) swap(p0, p1);
                                                                                         104
```

圆的面积模板 $(n^2 \log n)$

```
1 // Area[i] 表示覆盖次数大于等于 i 的面积
 2 struct Tevent {
     Point p; double ang; int add;
 3
     Tevent() {}
     Tevent(const Point & p, double ang, int add): p( p), ang( ang), add( add) {}
     bool operator <(const Tevent &a) const {
       return ang < a.ang;</pre>
 8
 9| eve[N * 2];
10 int E, cnt, C;
11 Circle c[N];
12 bool g[N][N], overlap[N][N];
13 double Area[N];
14 int cX[N], cY[N], cR[N];
15 | bool contain(int i, int j) {
16
     return (sign(c[i].r - c[j].r) > 0|| sign(c[i].r - c[j].r) == 0 && i < j) &&
      \hookrightarrow c[i].contain(c[j], -1);
17 | }
18 | int main() {
19
     scanf("%d", &C);
     for (int i = 0; i < C; ++i) {
20
       scanf("%d%d%d", cX+i, cY+i, cR+i);
^{21}
       c[i].o = Point(cX[i], cY[i]);
22
       c[i].r = cR[i];
23
24
25
     for (int i = 0; i <= C; ++i) Area[i] = 0;
26
     for (int i = 0; i < C; ++i) for (int j = 0; j < C; ++j)
         overlap[i][j] = contain(i, j);
27
28
     for (int i = 0; i < C; ++i) for (int j = 0; j < C; ++j)
       g[i][j] = !(overlap[i][j] || overlap[j][i] || c[i].disjuct(c[j], -1));
29
30
      for (int i = 0; i < C; ++i) {
       E = 0; cnt = 1;
31
        for (int j = 0; j < C; ++j) if (j != i \&\& overlap[j][i]) cnt++;
32
        for (int j = 0; j < C; ++j) {
33
         if (i != j && g[i][j]) {
34
```

```
35
           Point aa, bb;
36
           isCC(c[i], c[j], aa, bb);
           double A = atan2(aa.y - c[i].o.y, aa.x - c[i].o.x);
37
38
           double B = atan2(bb.y - c[i].o.y, bb.x - c[i].o.x);
           eve[E++] = Tevent(bb, B, 1);
39
           eve[E++] = Tevent(aa, A, -1);
40
           if (B > A) cnt++;
41
42
         }
43
       if (E == 0) { //cnt 表示覆盖次数超过 cnt
44
         Area[cnt] += PI * c[i].r * c[i].r;
45
46
       } else {
         sort(eve, eve + E);
47
48
         eve[E] = eve[0];
         for (int j = 0; j < E; ++j) {
49
50
           cnt += eve[j].add;
           Area[cnt] += eve[j].p.det(eve[j + 1].p) * .5;
51
           double theta = eve[j + 1].ang - eve[j].ang;
52
           if (theta < 0) theta += PI * 2.;</pre>
53
           Area[cnt] += theta * c[i].r * c[i].r * .5 - sin(theta) * c[i].r * c[i].r *
54
      55
56
       }
57
58
     for(int i = 1; i <= C; ++ i) printf("[%d] = %.3f\n", i, Area[i] - Area[i + 1]);
59 }
```

三角形的心

```
1 | Point inCenter(const Point &A, const Point &B, const Point &C) { // 内心
     double a = (B - C).len(), b = (C - A).len(), c = (A - B).len(),
       p = (a + b + c) / 2
       s = sqrt(p * (p - a) * (p - b) * (p - c)),
       r = s / p;
     return (A * a + B * b + C * c) / (a + b + c);
   Point circumCenter(const Point &a, const Point &b, const Point &c) { // 外心
     Point bb = b - a, cc = c - a;
10
     double db = bb.len2(), dc = cc.len2(), d = 2 * det(bb, cc);
11
     return a + Point(bb.y * dc - cc.y * db, cc.x * db - bb.x * dc) / d;
12
13 }
14
   Point othroCenter(const Point &a, const Point &b, const Point &c) { // 垂心
15
16
     Point ba = b - a, ca = c - a, bc = b - c;
     double Y = ba.y * ca.y * bc.y,
```

最小覆盖球

```
int npoint, nouter; Tpoint pt[200000], outer[4],res; double radius,tmp;
   void ball() {
     Tpoint q[3]; double m[3][3], sol[3], L[3], det;
 3
     int i,j; res.x = res.y = res.z = radius = 0;
     switch ( nouter ) {
 5
     case 1: res=outer[0]; break;
      case 2: res=(outer[0]+outer[1])/2; radius=dist2(res, outer[0]); break;
 8
     case 3:
       for (i=0; i<2; ++i) q[i]=outer[i+1]-outer[0];</pre>
 9
10
       for (i=0; i<2; ++i) for(j=0; j<2; ++j) m[i][j]=dot(q[i], q[j])*2;
       for (i=0; i<2; ++i) sol[i]=dot(q[i], q[i]);</pre>
11
       if (fabs(det=m[0][0]*m[1][1]-m[0][1]*m[1][0])<eps) return;
12
13
       L[0]=(sol[0]*m[1][1]-sol[1]*m[0][1])/det;
       L[1]=(sol[1]*m[0][0]-sol[0]*m[1][0])/det;
14
       res=outer[0]+q[0]*L[0]+q[1]*L[1];
15
16
       radius=dist2(res, outer[0]);
17
       break:
18
19
       for (i=0; i<3; ++i) q[i]=outer[i+1]-outer[0], sol[i]=dot(q[i], q[i]);</pre>
       for (i=0;i<3;++i) for(j=0;j<3;++j) m[i][j]=dot(q[i],q[j])*2;
20
       det= m[0][0]*m[1][1]*m[2][2]
21
22
       + m[0][1]*m[1][2]*m[2][0]
23
       + m[0][2]*m[2][1]*m[1][0]
       - m[0][2]*m[1][1]*m[2][0]
24
       - m[0][1]*m[1][0]*m[2][2]
25
26
       - m[0][0]*m[1][2]*m[2][1];
       if ( fabs(det)<eps ) return;</pre>
27
28
       for (j=0; j<3; ++j) {
29
         for (i=0; i<3; ++i) m[i][j]=sol[i];
30
         L[j]=(m[0][0]*m[1][1]*m[2][2]
         + m[0][1]*m[1][2]*m[2][0]
31
         + m[0][2]*m[2][1]*m[1][0]
32
         - m[0][2]*m[1][1]*m[2][0]
33
34
         - m[0][1]*m[1][0]*m[2][2]
         - m[0][0]*m[1][2]*m[2][1]
35
36
         ) / det;
         for (i=0; i<3; ++i) m[i][j]=dot(q[i], q[j])*2;
37
38
       } res=outer[0];
```

```
for (i=0; i<3; ++i) res = res + q[i] * L[i];
39
40
       radius=dist2(res, outer[0]);
41 | }}
42
   void minball(int n) { ball();
     if ( nouter<4 ) for (int i=0; i<n; ++i)</pre>
43
     if (dist2(res, pt[i])-radius>eps) {
44
       outer[nouter++]=pt[i]; minball(i); --nouter;
45
46
       if (i>0) { Tpoint Tt = pt[i];
47
         memmove(&pt[1], &pt[0], sizeof(Tpoint)*i); pt[0]=Tt;
48 }}}
   int main0(){
49
     scanf("%d", &npoint);
50
     for (int i=0;i<npoint;i++) scanf("%1f%1f%1f",&pt[i].x,&pt[i].y,&pt[i].z);</pre>
51
52
     random_shuffle(pt,pt+npoint); radius=-1;
     for (int i=0;i<npoint;i++) if (dist2(res,pt[i])-radius>eps)
       nouter=1, outer[0]=pt[i], minball(i);
54
     printf("%.5f\n",sqrt(radius));
55
56 }
```

经纬度求球面最短距离

```
1 //lati 为纬度 longi 为经度 R 为半径
2 double Dist(double lati1,double longi1,double lati2,double longi2,double R) {
3 double pi=acos(-1.0); lati1*=pi/180,longi1*=pi/180,lati2*=pi/180,longi2*=pi/180;
4 double x1=cos(lati1)*sin(longi1),y1=cos(lati1)*cos(longi1),z1=sin(lati1);
5 double x2=cos(lati2)*sin(longi2),y2=cos(lati2)*cos(longi2),z2=sin(lati2);
6 double theta=acos(x1*x2+y1*y2+z1*z2); return(R*theta);
7 }
```

长方体表面两点最短距离

```
1 int r;
   void turn(int i, int j, int x, int y, int z,int x0, int y0, int L, int W, int H) {
    if (z==0) { int R = x*x+y*y; if (R< r) r=R;
     } else {
       if(i)=0 \& i < 2) turn(i+1, j, x0+L+z, y, x0+L-x, x0+L, y0, H, W, L);
       if(j)=0 \& j < 2 turn(i, j+1, x, y0+W+z, y0+W-y, x0, y0+W, L, H, W);
       if(i<=0 && i>-2) turn(i-1, j, x0-z, y, x-x0, x0-H, y0, H, W, L);
       if(j \le 0 \& j \ge 2) turn(i, j-1, x, y0-z, y-y0, x0, y0-H, L, H, W);
9 }}
10 int main(){
11
    int L, H, W, x1, y1, z1, x2, y2, z2;
12
     cin >> L >> W >> H >> x1 >> y1 >> z1 >> x2 >> y2 >> z2;
13
     if (z1!=0 && z1!=H) if (y1==0 || y1==W)
          swap(y1,z1), std::swap(y2,z2), std::swap(W,H);
14
     else swap(x1,z1), std::swap(x2,z2), std::swap(L,H);
```

```
16     if (z1==H) z1=0, z2=H-z2;
17     r=0x3fffffff; turn(0,0,x2-x1,y2-y1,z2,-x1,-y1,L,W,H);
18     cout<<r<<endl; return 0;
19 }</pre>
```

最大团

```
1 // Super Fast Maximum Clique
 2 // To Build Graph: Maxclique(Edges, Number of Nodes)
 3 // To Get Answer: mcqdyn(AnswerNodes Index Array, AnswserLength)
   typedef bool BB[N];
   struct Maxclique {
     const BB* e; int pk, level; const float Tlimit;
     struct Vertex{ int i, d; Vertex(int i):i(i),d(0){} };
     typedef vector<Vertex> Vertices; typedef vector<int> ColorClass;
 8
 9
     Vertices V; vector<ColorClass> C; ColorClass QMAX, Q;
10
     static bool desc_degree(const Vertex &vi, const Vertex &vj){
       return vi.d > vj.d;
11
12
     void init_colors(Vertices &v){
13
       const int max degree = v[0].d;
14
       for(int i = 0; i < (int)v.size(); i++) v[i].d = min(i, max degree) + 1;
15
16
17
     void set_degrees(Vertices &v){
18
       for(int i = 0, j; i < (int)v.size(); i++)
19
         for(v[i].d = j = 0; j < int(v.size()); j++)
           v[i].d += e[v[i].i][v[j].i];
20
^{21}
     struct StepCount{ int i1, i2; StepCount():i1(0),i2(0){} };
22
     vector<StepCount> S;
23
     bool cut1(const int pi, const ColorClass &A){
24
       for(int i = 0; i < (int)A.size(); i++) if (e[pi][A[i]]) return true;</pre>
25
26
       return false;
27
28
     void cut2(const Vertices &A, Vertices &B){
       for(int i = 0; i < (int)A.size() - 1; i++)
29
30
         if(e[A.back().i][A[i].i])
           B.push_back(A[i].i);
31
32
     void color sort(Vertices &R){
33
       int j = 0, maxno = 1, min k = max((int)QMAX.size() - (int)Q.size() + 1, 1);
34
35
       C[1].clear(), C[2].clear();
36
       for(int i = 0; i < (int)R.size(); i++) {</pre>
37
         int pi = R[i].i, k = 1;
38
         while(cut1(pi, C[k])) k++;
         if(k > maxno) maxno = k, C[maxno + 1].clear();
39
```

```
40
         C[k].push_back(pi);
         if(k < min_k) R[j++].i = pi;</pre>
41
42
43
       if(j > 0) R[j - 1].d = 0;
       for(int k = min_k; k <= maxno; k++)</pre>
44
         for(int i = 0; i < (int)C[k].size(); i++)</pre>
45
46
            R[j].i = C[k][i], R[j++].d = k;
47
48
     void expand_dyn(Vertices &R){// diff -> diff with no dyn
       S[level].i1 = S[level].i1 + S[level - 1].i1 - S[level].i2;//diff
49
       S[level].i2 = S[level - 1].i1;//diff
50
       while((int)R.size()) {
51
         if((int)Q.size() + R.back().d > (int)QMAX.size()){
52
            Q.push_back(R.back().i); Vertices Rp; cut2(R, Rp);
53
            if((int)Rp.size()){
54
              if((float)S[level].i1 / ++pk < Tlimit) degree_sort(Rp);//diff</pre>
55
56
              color_sort(Rp);
              S[level].i1++, level++;//diff
57
58
              expand_dyn(Rp);
              level--;//diff
59
60
61
            else if((int)Q.size() > (int)QMAX.size()) QMAX = Q;
62
            Q.pop back();
         }
63
64
          else return;
65
          R.pop_back();
66
67
68
      void mcqdyn(int* maxclique, int &sz){
69
        set_degrees(V); sort(V.begin(),V.end(), desc_degree); init_colors(V);
       for(int i = 0; i < (int)V.size() + 1; i++)S[i].i1 = S[i].i2 = 0;
70
71
        expand_dyn(V); sz = (int)QMAX.size();
       for(int i = 0; i < (int)QMAX.size(); i++) maxclique[i] = QMAX[i];</pre>
72
73
74
     void degree_sort(Vertices &R){
        set_degrees(R); sort(R.begin(), R.end(), desc_degree);
75
76
     Maxclique(const BB* conn, const int sz, const float tt = 0.025) \
77
78
      : pk(0), level(1), Tlimit(tt){
       for(int i = 0; i < sz; i++) V.push_back(Vertex(i));</pre>
79
       e = conn, C.resize(sz + 1), S.resize(sz + 1);
80
81
82 | };
```

极大团计数

```
1 //Bool g[][] 为图的邻接矩阵, 图点的标号由 1 至 n
   void dfs(int size){
     int i, j, k, t, cnt, best = 0;
 3
     if (ne[size]==ce[size]){ if (ce[size]==0) ++ans; return; }
      for (t=0, i=1; i<=ne[size]; ++i) {
 5
       for (cnt=0, j=ne[size]+1; j<=ce[size]; ++j)</pre>
       if (!g[list[size][i]][list[size][j]]) ++cnt;
       if (t==0 || cnt<best) t=i, best=cnt;</pre>
 9
     } if (t && best<=0) return;</pre>
      for (k=ne[size]+1; k<=ce[size]; ++k) {</pre>
10
11
       if (t>0){ for (i=k; i<=ce[size]; ++i)
12
           if (!g[list[size][t]][list[size][i]]) break;
          swap(list[size][k], list[size][i]);
13
       } i=list[size][k]; ne[size+1]=ce[size+1]=0;
14
15
        for (j=1; j<k; ++j)if (g[i][list[size][j]])</pre>
16
           list[size+1][++ne[size+1]]=list[size][j];
17
        for (ce[size+1]=ne[size+1], j=k+1; j<=ce[size]; ++j)</pre>
18
       if (g[i][list[size][j]]) list[size+1][++ce[size+1]]=list[size][j];
19
       dfs(size+1); ++ne[size]; --best;
20
        for (j=k+1, cnt=0; j<=ce[size]; ++j) if (!g[i][list[size][j]]) ++cnt;</pre>
        if (t==0 || cnt<best) t=k, best=cnt;</pre>
21
        if (t && best<=0) break;
22
23 | }}
24 | void work(){
25
     ne[0]=0; ce[0]=0;
26
     for (int i=1; i<=n; ++i) list[0][++ce[0]]=i;</pre>
27
     ans=0; dfs(0);
28 }
```

KM

```
1 //Bool g[][] 为图的邻接矩阵,图点的标号由 1 至 n
 2 void dfs(int size){
     int i, j, k, t, cnt, best = 0;
     if (ne[size]==ce[size]){ if (ce[size]==0) ++ans; return; }
     for (t=0, i=1; i<=ne[size]; ++i) {
 6
       for (cnt=0, j=ne[size]+1; j<=ce[size]; ++j)</pre>
       if (!g[list[size][i]][list[size][j]]) ++cnt;
       if (t==0 || cnt<best) t=i, best=cnt;</pre>
     } if (t && best<=0) return;</pre>
10
     for (k=ne[size]+1; k<=ce[size]; ++k) {</pre>
11
       if (t>0){ for (i=k; i<=ce[size]; ++i)
12
           if (!g[list[size][t]][list[size][i]]) break;
         swap(list[size][k], list[size][i]);
13
       } i=list[size][k]; ne[size+1]=ce[size+1]=0;
14
```

```
for (j=1; j<k; ++j)if (g[i][list[size][j]])</pre>
15
16
            list[size+1][++ne[size+1]]=list[size][j];
       for (ce[size+1]=ne[size+1], j=k+1; j<=ce[size]; ++j)</pre>
17
18
        if (g[i][list[size][j]]) list[size+1][++ce[size+1]]=list[size][j];
       dfs(size+1); ++ne[size]; --best;
19
        for (j=k+1, cnt=0; j<=ce[size]; ++j) if (!g[i][list[size][j]]) ++cnt;</pre>
20
21
       if (t==0 || cnt<best) t=k, best=cnt;</pre>
        if (t && best<=0) break;</pre>
22
23 | }}
   void work(){
24
     ne[0]=0; ce[0]=0;
25
26
     for (int i=1; i<=n; ++i) list[0][++ce[0]]=i;
27
     ans=0; dfs(0);
28 }
```

最小树形图

```
//Bool g[][] 为图的邻接矩阵,图点的标号由 1 至 n
   void dfs(int size){
     int i, j, k, t, cnt, best = 0;
     if (ne[size]==ce[size]){ if (ce[size]==0) ++ans; return; }
     for (t=0, i=1; i<=ne[size]; ++i) {
       for (cnt=0, j=ne[size]+1; j<=ce[size]; ++j)</pre>
       if (!g[list[size][i]][list[size][j]]) ++cnt;
       if (t==0 || cnt<best) t=i, best=cnt;</pre>
     } if (t && best<=0) return;</pre>
10
     for (k=ne[size]+1; k<=ce[size]; ++k) {</pre>
11
       if (t>0){ for (i=k; i<=ce[size]; ++i)
           if (!g[list[size][t]][list[size][i]]) break;
12
         swap(list[size][k], list[size][i]);
13
       } i=list[size][k]; ne[size+1]=ce[size+1]=0;
14
       for (j=1; j<k; ++j)if (g[i][list[size][j]])</pre>
15
16
           list[size+1][++ne[size+1]]=list[size][j];
       for (ce[size+1]=ne[size+1], j=k+1; j<=ce[size]; ++j)</pre>
17
18
       if (g[i][list[size][j]]) list[size+1][++ce[size+1]]=list[size][j];
       dfs(size+1); ++ne[size]; --best;
19
       for (j=k+1, cnt=0; j<=ce[size]; ++j) if (!g[i][list[size][j]]) ++cnt;</pre>
20
       if (t==0 | cnt<best) t=k, best=cnt;
21
       if (t && best<=0) break;
22
23 }}
   void work(){
24
     ne[0]=0; ce[0]=0;
25
26
     for (int i=1; i<=n; ++i) list[0][++ce[0]]=i;</pre>
     ans=0; dfs(0);
27
28
```

无向图最小割

```
int cost[maxn][maxn],seq[maxn],len[maxn],n,m,pop,ans;
2 | bool used[maxn];
   void Init(){
3
     int i,j,a,b,c;
     for(i=0;i<n;i++) for(j=0;j<n;j++) cost[i][j]=0;</pre>
5
     for(i=0;i<m;i++){</pre>
       scanf("%d %d %d",&a,&b,&c); cost[a][b]+=c; cost[b][a]+=c;
7
8
9
     pop=n; for(i=0;i<n;i++) seq[i]=i;
10
   void Work(){
11
     ans=inf; int i,j,k,l,mm,sum,pk;
12
      while(pop > 1){
13
        for(i=1;i<pop;i++) used[seq[i]]=0; used[seq[0]]=1;</pre>
14
        for(i=1;i<pop;i++) len[seq[i]]=cost[seq[0]][seq[i]];</pre>
15
16
       pk=0; mm=-inf; k=-1;
17
        for(i=1;i<pop;i++) if(len[seq[i]] > mm){ mm=len[seq[i]]; k=i; }
18
        for(i=1;i<pop;i++){</pre>
19
         used[seq[l=k]]=1;
20
          if(i==pop-2) pk=k;
          if(i==pop-1) break;
21
          mm=-inf;
22
         for(j=1;j<pop;j++) if(!used[seq[j]])</pre>
23
           if((len[seq[j]]+=cost[seq[1]][seq[j]]) > mm)
24
              mm=len[seq[j]], k=j;
25
26
       sum=0;
27
28
        for(i=0;i<pop;i++) if(i != k) sum+=cost[seq[k]][seq[i]];</pre>
       ans=min(ans,sum);
29
30
        for(i=0;i<pop;i++)</pre>
         cost[seq[k]][seq[i]]=cost[seq[i]][seq[k]]+=cost[seq[pk]][seq[i]];
31
32
       seq[pk]=seq[--pop];
33
     printf("%d\n",ans);
34
35 | }
```

带花树

```
vector<int> link[maxn];
int n,match[maxn],Queue[maxn],head,tail;
int pred[maxn],base[maxn],start,finish,newbase;
bool InQueue[maxn],InBlossom[maxn];
void push(int u){ Queue[tail++]=u;InQueue[u]=true; }
int pop(){ return Queue[head++]; }
int FindCommonAncestor(int u,int v){
```

```
bool InPath[maxn];
     for(int i=0;i<n;i++) InPath[i]=0;</pre>
     while(true){ u=base[u];InPath[u]=true;if(u=start) break;u=pred[match[u]]; }
10
11
     while(true){ v=base[v];if(InPath[v]) break;v=pred[match[v]]; }
12
     return v;
13
    void ResetTrace(int u){
14
15
16
      while(base[u]!=newbase){
       v=match[u];
17
18
       InBlossom[base[u]]=InBlossom[base[v]]=true;
       u=pred[v];
19
20
       if(base[u]!=newbase) pred[u]=v;
21
22
   void BlossomContract(int u,int v){
23
      newbase=FindCommonAncestor(u,v);
24
     for (int i=0;i<n;i++)</pre>
25
26
     InBlossom[i]=0;
27
     ResetTrace(u);ResetTrace(v);
28
     if(base[u]!=newbase) pred[u]=v;
     if(base[v]!=newbase) pred[v]=u;
29
      for(int i=0;i<n;++i)</pre>
     if(InBlossom[base[i]]){
31
32
       base[i]=newbase;
       if(!InQueue[i]) push(i);
33
34
35
   bool FindAugmentingPath(int u){
37
     bool found=false;
38
     for(int i=0;i<n;++i) pred[i]=-1,base[i]=i;</pre>
      for (int i=0;i<n;i++) InQueue[i]=0;</pre>
39
      start=u;finish=-1; head=tail=0; push(start);
      while(head<tail){</pre>
41
42
       int u=pop();
       for(int i=link[u].size()-1;i>=0;i--){
43
          int v=link[u][i];
44
         if(base[u]!=base[v]&&match[u]!=v)
45
46
           if(v==start||(match[v]>=0&&pred[match[v]]>=0))
              BlossomContract(u,v);
47
48
            else if(pred[v]==-1){
              pred[v]=u;
49
              if(match[v]>=0) push(match[v]);
50
              else{ finish=v; return true; }
51
52
```

```
}
53
54
      return found;
55
56
   void AugmentPath(){
57
58
     int u=finish,v,w;
      while(u>=0){ v=pred[u];w=match[v];match[v]=u;match[u]=v;u=w; }
59
6o | }
61
   void FindMaxMatching(){
62
      for(int i=0;i<n;++i) match[i]=-1;</pre>
63
      for(int i=0;i<n;++i) if(match[i]==-1) if(FindAugmentingPath(i)) AugmentPath();</pre>
64 | }
```

动态最小生成树

```
/* 动态最小生成树 Q(logQ)^2
     (qx[i],qy[i]) 表示将编号为 qx[i] 的边的权值改为 qy[i]
     删除一条边相当于将其权值改为 ∞
 3
     加入一条边相当于将其权值从 ∞ 变成某个值 */
   const int qsize=maxm+3*maxq;
 6 | int x[qsize],y[qsize],z[qsize], qx[maxq],qy[maxq],n,m,Q;
 7 | void init(){
     scanf("%d%d",&n,&m);
     for(int i=0;i<m;i++) scanf("%d%d%d",x+i,y+i,z+i);</pre>
     scanf("%d",&Q);
10
11
     for(int i=0;i<Q;i++){ scanf("%d%d",qx+i,qy+i); qx[i]--; }</pre>
12 }
13 | int a[maxn],*tz;
   int find(int x){
     int root=x; while(a[root]) root=a[root];
15
16
     int next; while(next=a[x]){ a[x]=root; x=next; }
     return root;
17
18 }
   inline bool cmp(const int &a,const int &b){ return tz[a]<tz[b]; }
   int kx[maxn],ky[maxn],kt, vd[maxn],id[maxm], app[maxm];
^{21}
   bool extra[maxm];
   void solve(int *qx,int *qy,int Q,int n,int *x,int *y,int *z,int m,long long ans){
     if(Q==1){
23
       for(int i=1;i<=n;i++) a[i]=0;</pre>
24
       z[qx[0]]=qy[0];
25
26
       for(int i=0;i<m;i++) id[i]=i;tz=z;</pre>
27
       sort(id,id+m,cmp); int ri,rj;
28
       for(int i=0;i<m;i++){</pre>
         ri=find(x[id[i]]); rj=find(y[id[i]]);
29
         if(ri!=rj){ ans+=z[id[i]]; a[ri]=rj; }
30
31
```

```
printf("%I64d\n",ans);
32
33
        return;
34
35
     int ri,rj;
36
     //contract
37
     kt=0;
38
     for(int i=1;i<=n;i++) a[i]=0;</pre>
     for(int i=0;i<Q;i++){</pre>
39
40
        ri=find(x[qx[i]]); rj=find(y[qx[i]]); if(ri!=rj) a[ri]=rj;
41
     int tm=0;
42
      for(int i=0;i<m;i++) extra[i]=true;</pre>
43
     for(int i=0;i<Q;i++) extra[ qx[i] ]=false;</pre>
44
45
      for(int i=0;i<m;i++) if(extra[i]) id[tm++]=i;</pre>
     tz=z; sort(id,id+tm,cmp);
      for(int i=0;i<tm;i++){</pre>
47
        ri=find(x[id[i]]); rj=find(y[id[i]]);
48
        if(ri!=rj){
49
          a[ri]=rj; ans += z[id[i]];
50
51
          kx[kt]=x[id[i]]; ky[kt]=y[id[i]]; kt++;
       }
52
53
     for(int i=1;i<=n;i++) a[i]=0;
54
     for(int i=0;i<kt;i++) a[ find(kx[i]) ]=find(ky[i]);</pre>
55
56
     int n2=0;
     for(int i=1;i<=n;i++) if(a[i]==0)
57
     vd[i]=++n2;
      for(int i=1;i<=n;i++) if(a[i])</pre>
59
     vd[i]=vd[find(i)];
60
61
     int m2=0, *Nx=x+m, *Ny=y+m, *Nz=z+m;
      for(int i=0;i<m;i++) app[i]=-1;</pre>
63
      for(int i=0;i<Q;i++) if(app[qx[i]]==-1){</pre>
64
       Nx[m2]=vd[x[qx[i]]; Ny[m2]=vd[y[qx[i]]; Nz[m2]=z[qx[i]];
65
        app[qx[i]]=m2; m2++;
66
67
      for(int i=0;i<Q;i++){ z[ qx[i] ]=qy[i]; qx[i]=app[qx[i]]; }</pre>
      for(int i=1;i<=n2;i++) a[i]=0;</pre>
69
      for(int i=0;i<tm;i++){</pre>
        ri=find(vd[ x[id[i]] ]); rj=find(vd[ y[id[i]] ]);
70
        if(ri!=rj){
71
72
          a[ri]=rj; Nx[m2]=vd[ x[id[i]] ];
          Ny[m2]=vd[ y[id[i]] ]; Nz[m2]=z[id[i]]; m2++;
73
74
75
76
     int mid=Q/2;
```

```
solve(qx,qy,mid,n2,Nx,Ny,Nz,m2,ans);
solve(qx+mid,qy+mid,Q-mid,n2,Nx,Ny,Nz,m2,ans);

your work(){ if(Q) solve(qx,qy,Q,n,x,y,z,m,0); }
int main(){init(); work(); return 0; }
```

```
Hopcroft
int from[1010], wh[1010], g[1010];
2 int num[100010],nxt[100010],tot;
3 int n,m,ans,h,t,q[1010],dx[1010],dy[1010];
   bool bfs(){
     bool ret=false;
     h=0;t=0;
     for(int i=0;i<n;i++) if(wh[i]==-1) t++, q[t]=i;
     memset(dx,0,sizeof(dx)), memset(dy,0,sizeof(dy));
9
     while(h++<t){</pre>
       for(int i=g[q[h]];i!=0;i=nxt[i])
10
         if(dy[num[i]]==0){
11
           dy[num[i]]=dx[q[h]]+1;
12
13
           if(from[num[i]]==-1) ret=true;
           else{
14
              dx[from[num[i]]]=dx[q[h]]+2;
15
16
              q[++t]=from[num[i]];
17
18
         }
19
20
     return ret;
^{21}
   bool dfs(int x){
^{22}
     for(int i=g[x];i!=0;i=nxt[i]){
23
       if(dy[num[i]]==dx[x]+1){
24
         dy[num[i]]=0;
25
26
         if(from[num[i]]==-1||dfs(from[num[i]])){
            wh[x]=num[i];from[num[i]]=x;return true;
27
28
         }
29
30
     return false;
31
32
   void hopcroft(){
33
     memset(from,-1,sizeof(from)), memset(wh,-1,sizeof(wh));
34
     while(bfs())
35
36
       for(int i=0;i<n;i++)</pre>
37
         if(wh[i]==-1&&dfs(i)) ans++;
38 }
```

```
39 | void insert(int x,int y){ tot++;num[tot]=y;nxt[tot]=g[x];g[x]=tot; }
   int main(){
40
     while(scanf("%d %d",&n,&m)==2){
41
42
       tot=0; memset(g,0,sizeof(g));
       for(int i=0;i<n;i++){</pre>
43
         int x; scanf("%d",&x);
44
         for(int j=0;j<x;j++){</pre>
45
46
           int y; scanf("%d",&y);
47
            y--; insert(i,y);
48
         }
       }
49
50
       ans=0; hopcroft(); printf("%d\n",ans);
51
52
```

素数判定

```
int strong_pseudo_primetest(long long n,int base) {
       long long n2=n-1,res;
       int s=0;
3
       while(n2\%2==0) n2>>=1,s++;
5
       res=powmod(base,n2,n);
       if((res==1)||(res==n-1)) return 1;
7
       s--;
8
       while(s>=0) {
           res=mulmod(res,res,n);
9
           if(res==n-1) return 1;
10
11
           s--;
12
       return 0; // n is not a strong pseudo prime
13
14
   int isprime(long long n) {
15
16
     static LL testNum[]={2,3,5,7,11,13,17,19,23,29,31,37};
17
     static LL lim[]={4,0,1373653LL,25326001LL,25000000000LL,2152302898747LL, \
18
     3474749660383LL,341550071728321LL,0,0,0,0);
     if(n<2||n==3215031751LL) return 0;
19
     for(int i=0;i<12;++i){
20
       if(n<lim[i]) return 1;</pre>
21
22
       if(strong_pseudo_primetest(n,testNum[i])==0) return 0;
23
24
     return 1;
25
```

启发式分解

```
int ansn; LL ans[1000];
LL func(LL x,LL n){ return(mod_mul(x,x,n)+1)%n; }
```

```
3 | LL Pollard(LL n){
     LL i,x,y,p;
     if(Rabin_Miller(n)) return n;
     if(!(n&1)) return 2;
     for(i=1;i<20;i++){
       x=i; y=func(x,n); p=gcd(y-x,n);
 9
       while(p==1) {x=func(x,n); y=func(func(y,n),n); p=gcd((y-x+n)%n,n)%n;}
       if(p==0||p==n) continue;
10
11
       return p;
12
13 | }
  void factor(LL n){
14
     LL x;
15
16
     x=Pollard(n);
     if(x==n){ ans[ansn++]=x; return; }
17
18
     factor(x), factor(n/x);
19 }
```

二次剩余

```
void calcH(int &t, int &h, const int p) {
     int tmp = p - 1; for (t = 0; (tmp & 1) == 0; tmp /= 2) t++; h = tmp;
 3 | }
   // solve equation x^2 \mod p = a
   bool solve(int a, int p, int &x, int &y) {
     srand(19920225);
     if (p == 2) { x = y = 1; return true; }
     int p2 = p / 2, tmp = power(a, p2, p);
     if (tmp == p - 1) return false;
     if ((p + 1) \% 4 == 0) {
10
       x = power(a, (p + 1) / 4, p); y = p - x; return true;
11
     } else {
12
13
       int t, h, b, pb; calcH(t, h, p);
14
       if (t >= 2) {
         do \{b = rand() \% (p - 2) + 2;
15
16
         } while (power(b, p / 2, p) != p - 1);
         pb = power(b, h, p);
17
18
       } int s = power(a, h / 2, p);
19
       for (int step = 2; step <= t; step++) {</pre>
20
         int ss = (((long long)(s * s) % p) * a) % p;
         for (int i = 0; i < t - step; i++) ss = ((long long)ss * ss) % p;
21
         if (ss + 1 == p) s = (s * pb) % p; pb = ((long long)pb * pb) % p;
22
       x = ((long long)s * a) % p; y = p - x;
23
     } return true;
24
25 | }
```

Pell 方程

```
1 ULL A,B,p[maxn],q[maxn],a[maxn],g[maxn],h[maxn];
   int main() {
3
     for (int test=1, n;scanf("%d",&n) && n;++test) {
       printf("Case %d: ",test);
       if (fabs(sqrt(n)-floor(sqrt(n)+1e-7))<=1e-7) {</pre>
         int a=(int)(floor(sqrt(n)+1e-7)); printf("%d %d\n",a,1);
         // 求 x^2 - ny^2 = 1 的最小正整数根, n 不是完全平方数
9
         p[1]=q[0]=h[1]=1;p[0]=q[1]=g[1]=0;
10
         a[2]=(int)(floor(sqrt(n)+1e-7));
         for (int i=2;i;++i) {
11
           g[i]=-g[i-1]+a[i]*h[i-1]; h[i]=(n-sqr(g[i]))/h[i-1];
12
           a[i+1]=(g[i]+a[2])/h[i]; p[i]=a[i]*p[i-1]+p[i-2];
13
14
           q[i]=a[i]*q[i-1]+q[i-2];
           if (sqr((ULL)(p[i]))-n*sqr((ULL)(q[i]))==1){
15
16
             A=p[i];B=q[i];break; }
17
         } cout << A << ' ' << B <<endl;</pre>
18
       }}}
```

蔡勒公式

```
int zeller(int y,int m,int d) {
   if (m<=2) y--,m+=12; int c=y/100; y%=100;
   int w=((c>>2)-(c<<1)+y+(y>>2)+(13*(m+1)/5)+d-1)%7;
   if (w<0) w+=7; return(w);
}</pre>
```

Schreier-Sims

```
namespace Schreier_Sims_Algorithm{
     struct Permutation{
       vector<int> P;
       Permutation(){}
       Permutation(int n){
         P.resize(n);
8
       Permutation inv()const{
         Permutation ret(P.size());
         for(int i = 0; i < int(P.size()); ++i) ret.P[P[i]] = i;</pre>
10
         return ret;
11
12
13
       int &operator [](const int &dn){
         return P[dn];
14
15
16
       void resize(const size_t &sz){
```

```
P.resize(sz);
                                                                                                62
                                                                                                       for(int i = 0; i < n; ++i){
17
                                                                                               63
18
                                                                                                         ret *= buckets[i].size();
                                                                                                64
19
       size_t size()const{
20
         return P.size();
                                                                                                65
                                                                                                       return ret;
                                                                                                66
21
       const int &operator [](const int &dn)const{
                                                                                                67
22
         return P[dn];
                                                                                                68
                                                                                                     bool inGroup(const Permutation &g){
23
                                                                                                69
                                                                                                       return fastFilter(g, false) == -1;
       }
24
25
                                                                                                70
                                                                                                     }
26
     Permutation operator *(const Permutation &a, const Permutation &b){
                                                                                                71
       Permutation ret(a.size());
                                                                                                     void solve(const Bucket &gen,int _n){// m perm[0..n - 1]s
                                                                                                72
27
28
       for(int i = 0; i < (int)a.size(); ++i){</pre>
                                                                                                       n = _n, m = gen.size();
                                                                                                73
                                                                                                       {//clear all
29
         ret[i] = b[a[i]];
                                                                                                74
                                                                                                         vector<Bucket> _buckets(n);
30
       }
                                                                                                75
       return ret;
                                                                                                76
                                                                                                         swap(buckets, _buckets);
31
                                                                                                77
                                                                                                         vector<Bucket> _bucketsInv(n);
32
                                                                                                78
                                                                                                         swap(bucketsInv, _bucketsInv);
33
     typedef vector<Permutation> Bucket;
                                                                                                         vector<Table> lookupTable(n);
                                                                                                79
34
     typedef vector<int> Table;
                                                                                                80
                                                                                                         swap(lookupTable, lookupTable);
35
     typedef pair<int,int> pii;
                                                                                                81
                                                                                                       }
36
     int n, m;
                                                                                                82
                                                                                                       for(int i = 0; i < n; ++i){
37
     vector<Bucket> buckets, bucketsInv;
                                                                                                83
                                                                                                         lookupTable[i].resize(n);
38
      vector<Table> lookupTable;
                                                                                                         fill(lookupTable[i].begin(), lookupTable[i].end(), -1);
                                                                                                84
39
                                                                                                85
40
      int fastFilter(const Permutation &g, bool addToGroup = true){
                                                                                                86
                                                                                                       Permutation id(n);
41
       int n = buckets.size();
                                                                                                87
                                                                                                       for(int i = 0; i < n; ++i){
42
       Permutation p;
                                                                                                88
                                                                                                         id[i] = i;
43
       for(int i = 0; i < n; ++i){
                                                                                                89
                                                                                                       }
44
         int res = lookupTable[i][p[i]];
                                                                                                       for(int i = 0; i < n; ++i){
                                                                                                90
45
46
         if(res == -1){
                                                                                                         buckets[i].push_back(id);
                                                                                                91
           if(addToGroup){
                                                                                                         bucketsInv[i].push_back(id);
47
                                                                                                92
48
              buckets[i].push_back(p);
                                                                                                         lookupTable[i][i] = 0;
                                                                                                93
              bucketsInv[i].push_back(p.inv());
49
                                                                                                       }
                                                                                                94
              lookupTable[i][p[i]] = (int)buckets[i].size() - 1;
                                                                                                       for(int i = 0; i < m; ++i){
50
                                                                                                95
                                                                                                96
                                                                                                         fastFilter(gen[i]);
51
           }
52
           return i;
                                                                                                97
                                                                                                98
                                                                                                       queue<pair<point,point> > toUpdate;
53
         p = p * bucketsInv[i][res];
                                                                                                       for(int i = 0; i < n; ++i){
54
                                                                                                99
                                                                                                         for(int j = i; j < n; ++j){}
          swap(i1,i2);
55
                                                                                              100
56
       }
                                                                                                           for(int k = 0; k < (int)buckets[i].size(); ++k){</pre>
                                                                                              101
                                                                                                             for(int 1 = 0; 1 < (int)buckets[j].size(); ++1){</pre>
57
       return -1;
                                                                                              102
58
                                                                                              103
                                                                                                                toUpdate.push(make_pair(pii(i,k), pii(j,l)));
                                                                                              104
59
     long long calcTotalSize(){
                                                                                                           }
60
                                                                                              105
       long long ret = 1;
61
                                                                                              106
                                                                                                         }
```

```
107
108
        while(!toUpdate.empty()){
          pii a = toUpdate.front().first;
109
110
          pii b = toUpdate.front().second;
111
          toUpdate.pop();
          int res = fastFilter(buckets[a.first][a.second] * buckets[b.first][b.second]);
112
          if(res==-1) continue;
113
          pii newPair(res, (int)buckets[res].size() - 1);
114
115
          for(int i = 0; i < n; ++i){
116
            for(int j = 0; j < (int)buckets[i].size(); ++j){</pre>
              if(i <= res){
117
118
                 toUpdate.push(make_pair(pii(i , j), newPair));
119
120
              if(res<=i){</pre>
121
                 toUpdate.push(make_pair(newPair, pii(i, j)));
              }
122
123
124
125
126
127
```

Romberg

```
1 template<class T>
   double romberg(const T&f, double a, double b, double eps=1e-8){
     std::vector<double>t; double h=b-a,last,curr; int k=1,i=1;
     t.push back(h*(f(a)+f(b))/2); // 梯形
     do{ last=t.back(); curr=0; double x=a+h/2;
5
6
       for(int j=0;j<k;++j) curr+=f(x),x+=h;</pre>
       curr=(t[0]+h*curr)/2; double k1=4.0/3.0, k2=1.0/3.0;
8
       for(int j=0;j<i;j++){ double temp=k1*curr-k2*t[j];</pre>
         t[j]=curr; curr=temp; k2/=4*k1-k2; k1=k2+1; // 防止溢出
10
       } t.push back(curr); k*=2; h/=2; i++;
     } while(std::fabs(last-curr)>eps);
11
12
     return t.back();
13 | }
```

线性规划

```
8
       for (int j = 0; j < m - 1; ++ j) D[i][j] = -A[i][j];
9
       D[i][m - 1] = 1; D[i][m] = b[i];
       if (D[r][m] > D[i][m]) r = i;
10
11
     for (int j = 0; j < m - 1; ++ j) D[n][j] = c[j];
12
13
     D[n + 1][m - 1] = -1;
     for (double d; ; ) {
14
15
       if (r < n) {
16
         int t = ix[s]; ix[s] = ix[r + m]; ix[r + m] = t;
17
         D[r][s] = 1.0 / D[r][s]; vector<int> speedUp;
18
         for (int j = 0; j <= m; ++ j) if (j != s) {
           D[r][j] *= -D[r][s];
19
20
           if(D[r][j]) speedUp.push_back(j);
21
         }
         for (int i = 0; i <= n + 1; ++ i) if (i != r) {
22
           for(int j = 0; j < speedUp.size(); ++ j)</pre>
23
           D[i][speedUp[j]] += D[r][speedUp[j]] * D[i][s];
24
           D[i][s] *= D[r][s];
25
26
       } r = -1; s = -1;
27
       for (int j = 0; j < m; ++ j) if (s < 0 || ix[s] > ix[j])
28
         if (D[n + 1][i] > EPS || (D[n + 1][i] > -EPS && D[n][i] > EPS)) s = i;
       if (s < 0) break;
29
       for (int i = 0; i < n; ++ i) if (D[i][s] < -EPS)</pre>
30
         if (r < 0 \mid | (d = D[r][m] / D[r][s] - D[i][m] / D[i][s]) < -EPS
31
32
             || (d < EPS \&\& ix[r + m] > ix[i + m])) r = i;
       if (r < 0) return VD(); // 无边界
33
34
     if (D[n + 1][m] < -EPS) return VD(); // 无解
35
36
     VD \times (m - 1);
     for (int i = m; i < n + m; ++ i) if (ix[i] < m - 1) x[ix[i]] = D[i - m][m];
37
38
     return x; // 最优值在 D[n][m]
39 }
```

FFT

```
/*
doublePDD10^9+7PDDDDD2^20
3 */
4
5 const int MOD = 1000003;
6
7 const double PI = acos(-1);
8
9 typedef complex<double> Complex;
10
```

```
11 const int N = 65536, L = 15, MASK = (1 << L) - 1;
12
13 | Complex w[N];
14
   void FFTInit() {
15
16
     for (int i = 0; i < N; ++i) {
       w[i] = Complex(cos(2 * i * PI / N), sin(2 * i * PI / N));
17
18
19
20
   void FFT(Complex p[], int n) {
^{21}
     for (int i = 1, j = 0; i < n - 1; ++i) {
22
       for (int s = n; j = s >= 1, \sim j \& s;);
23
24
       if (i < j) {
         swap(p[i], p[j]);
25
26
       }
27
28
     for (int d = 0; (1 << d) < n; ++d) {
       int m = 1 << d, m2 = m * 2, rm = n >> (d + 1);
29
30
       for (int i = 0; i < n; i += m2) {
         for (int j = 0; j < m; ++j) {
31
32
           Complex &p1 = p[i + j + m], &p2 = p[i + j];
           Complex t = w[rm * j] * p1;
33
34
           p1 = p2 - t;
35
           p2 = p2 + t;
36
         }
37
38
39
40
   Complex A[N], B[N], C[N], D[N];
41
42
   void mul(int a[N], int b[N]) {
43
     for (int i = 0; i < N; ++i) {
44
45
       A[i] = Complex(a[i] >> L, a[i] & MASK);
46
       B[i] = Complex(b[i] >> L, b[i] & MASK);
47
48
     FFT(A, N);
49
     FFT(B, N);
     for (int i = 0; i < N; ++i) {
50
       int j = (N - i) \% N;
51
       Complex da = (A[i] - conj(A[j])) * Complex(0, -0.5),
52
           db = (A[i] + conj(A[j])) * Complex(0.5, 0),
53
           dc = (B[i] - conj(B[j])) * Complex(0, -0.5),
54
           dd = (B[i] + conj(B[j])) * Complex(0.5, 0);
```

```
56
       C[j] = da * dd + da * dc * Complex(0, 1);
       D[j] = db * dd + db * dc * Complex(0, 1);
57
58
59
     FFT(C, N);
     FFT(D, N);
60
61
     for (int i = 0; i < N; ++i) {
62
       long long da = (long long)(C[i].imag() / N + 0.5) % MOD,
63
             db = (long long)(C[i].real() / N + 0.5) % MOD,
64
             dc = (long long)(D[i].imag() / N + 0.5) % MOD,
65
             dd = (long long)(D[i].real() / N + 0.5) % MOD;
66
       a[i] = ((dd << (L * 2)) + ((db + dc) << L) + da) % MOD;
67
68 }
```

NTT

```
1 //R 是 2^n*q+1 形质数 p 的原根
   void NFT(int P[], int n, int oper) {
     for (int i = 1, j = 0; i < n - 1; ++i) {
       for (int s = n; j ^= s >>= 1, ~j & s;);
       if (i < j) {
         swap(P[i], P[j]);
     for (int d = 0; (1 << d) < n; ++d) {
       int m = 1 << d, m2 = m * 2;
10
11
       int unit_p0 = powmod(R, (MOD - 1) / m2);
       if (oper < 0) {
12
         unit_p0 = inverse(unit_p0);
13
14
15
       for (int i = 0; i < n; i += m2) {
16
         int unit = 1;
17
         for (int j = 0; j < m; ++j) {
18
           int &P1 = P[i + j + m],
             P2 = P[i + j];
19
           int t = (long long)unit * P1 % MOD;
20
           P1 = (P2 - t + MOD) \% MOD;
21
22
           P2 = (P2 + t) \% MOD;
           unit = (long long)unit * unit_p0 % MOD;
23
24
25
26
27
```

FWT

```
void FWT(int a[N], int N) {
     for (int d = 1; d < N; d <<= 1) {
 3
       int d2 = d \ll 1;
       for (int i = 0; i < N; i += d2) {
 4
         int *x = a + i, *y = a + i + d;
 5
         for (int j = 0; j < d; ++j, ++x, ++y) {
           if ((*x += *y) >= MOD) {
              *x -= MOD:
 9
10
           if ((*y = *x - (*y << 1)) < 0) {
              if ((*y += MOD) < 0) {
11
                *y += MOD;
12
13
             }
14
           }
15
16
       }
17
18
19
   void xorPow(int a[N], int n, int b[N]) {
20
     memset(b, 0, sizeof(int) * N);
21
     b[0] = 1;
22
     FWT(a, N);
23
     FWT(b, N);
24
     while(n) {
25
26
       if (n & 1) {
         dot(b, a, N);
27
28
29
       dot(a, a, N);
       n >>= 1;
30
31
32
     FWT(b, N);
     norm(b, N);
33
34 | }
```

回文串 manacher

```
for(int i=1,j=0;i!=(n<<1)-1;++i){
  int p=i>>1,q=i-p,r=((j+1)>>1)+l[j]-1;
  l[i]=r<q?0:min(r-q+1,l[(j<<1)-i]);
  while(p-l[i]!=-1&&q+l[i]!=n&&s[p-l[i]]==s[q+l[i]]) l[i]++;
  if(q+l[i]-1>r) j=i;
  a+=l[i];
}
```

后缀数组(倍增)

```
int rank[MAX N],height[MAX N];
   int cmp(int *x,int a,int b,int d){
     return x[a]==x[b]&&x[a+d]==x[b+d];
4
   void doubling(int *a,int N,int M){
     static int sRank[MAX_N],tmpA[MAX_N],tmpB[MAX_N];
     int *x=tmpA,*y=tmpB;
     for(int i=0;i<M;++i) sRank[i]=0;</pre>
     for(int i=0;i<N;++i) ++sRank[x[i]=a[i]];</pre>
     for(int i=1;i<M;++i) sRank[i]+=sRank[i-1];</pre>
10
     for(int i=N-1;i>=0;--i) sa[--sRank[x[i]]]=i;
12
      for(int d=1,p=0;p<N;M=p,d<<=1){</pre>
        p=0; for(int i=N-d;i<N;++i) y[p++]=i;</pre>
13
        for(int i=0;i<N;++i) if(sa[i]>=d) y[p++]=sa[i]-d;
14
        for(int i=0;i<M;++i) sRank[i]=0;</pre>
15
16
        for(int i=0;i<N;++i) ++sRank[x[i]];</pre>
17
        for(int i=1;i<M;++i) sRank[i]+=sRank[i-1];</pre>
18
        for(int i=N-1;i>=0;--i) sa[--sRank[x[y[i]]]]=y[i];
        swap(x,y); x[sa[0]]=0; p=1;
19
        for(int i=1;i<N;++i) x[sa[i]]=cmp(y,sa[i],sa[i-1],d)?p-1:p++;</pre>
20
21
22
   void calcHeight(){
24
     for(int i=0;i<N;++i) rank[sa[i]]=i;</pre>
     int cur=0; for(int i=0;i<N;++i)</pre>
25
26
     if(rank[i]){
       if(cur) cur--;
27
28
       for(;a[i+cur]==a[sa[rank[i]-1]+cur];++cur);
       height[rank[i]]=cur;
29
30
31
```

后缀数组 (DC3)

```
1 // 待排序的字符串放在 r 数组中,从 r[0] 到 r[n-1], 长度为 n,且最大值小于 m 2 // 约定除 r[n-1] 外所有的 r[i] 都大于 0, r[n-1]=0 3 // 函数结束后,结果放在 sa 数组中,从 sa[0] 到 sa[n-1] 4 #define maxn 10000 5 #define F(x) ((x)/3+((x)%3==1?0:tb)) 6 #define G(x) ((x)<tb?(x)*3+1:((x)-tb)*3+2) 7 int wa[maxn],wb[maxn],wv[maxn],wss[maxn]; // 必须这么大 8 int s[maxn*3],sa[maxn*3]; 9 int c0(int *r,int a,int b){return r[a]==r[b]&&r[a+1]==r[b+1]&&r[a+2]==r[b+2];} 10 int c12(int k,int *r,int a,int b){
```

```
if(k==2) return r[a] < r[b] | | r[a] = = r[b] & c12(1,r,a+1,b+1);
11
12
      else return r[a] < r[b] | | r[a] == r[b] & wv[a+1] < wv[b+1];
13 | }
   void sort(int *r,int *a,int *b,int n,int m){
14
      int i; for(i=0;i<n;i++) wv[i]=r[a[i]];</pre>
15
16
      for(i=0;i<m;i++) wss[i]=0; for(i=0;i<n;i++) wss[wv[i]]++;</pre>
      for(i=1;i<m;i++) wss[i]+=wss[i-1];</pre>
17
18
      for(i=n-1;i>=0;i--) b[--wss[wv[i]]]=a[i];
19
20
   void dc3(int *r,int *sa,int n,int m){
      int i,j,*rn=r+n,*san=sa+n,ta=0,tb=(n+1)/3,tbc=0,p;
^{21}
      r[n]=r[n+1]=0;
22
      for(i=0;i<n;i++) if(i%3!=0) wa[tbc++]=i;</pre>
23
24
      sort(r+2,wa,wb,tbc,m); sort(r+1,wb,wa,tbc,m); sort(r,wa,wb,tbc,m);
      for(p=1,rn[F(wb[0])]=0,i=1;i<tbc;i++)
25
26
        rn[F(wb[i])]=c0(r,wb[i-1],wb[i])?p-1:p++;
      if(p<tbc) dc3(rn,san,tbc,p);</pre>
27
28
      else for(i=0;i<tbc;i++) san[rn[i]]=i;</pre>
      for (i=0;i<tbc;i++) if(san[i]<tb) wb[ta++]=san[i]*3;</pre>
29
30
      if(n\%3==1) wb[ta++]=n-1;
      sort(r,wb,wa,ta,m); for(i=0;i<tbc;i++) wv[wb[i]=G(san[i])]=i;</pre>
31
      for(i=0,j=0,p=0;i<ta && j<tbc;p++)</pre>
32
        sa[p]=c12(wb[j]%3,r,wa[i],wb[j])?wa[i++]:wb[j++];
33
      for(;i<ta;p++) sa[p]=wa[i++]; for(;j<tbc;p++) sa[p]=wb[j++];}</pre>
34
   int main(){
35
36
      int n, m=0; scanf("%d",&n);
      for (int i=0;i<n;i++) scanf("%d",&s[i]),s[i]++,m=max(s[i]+1,m);</pre>
37
38
      printf("%d\n",m); s[n++]=0; dc3(s,sa,n,m);
      for (int i=0;i<n;i++) printf("%d ",sa[i]);printf("\n");</pre>
39
40
```

后缀自动机

```
struct State {
     int length;
     State *parent,*go[C];
     State(int length):length(length),parent(NULL){
5
       memset(go,0,sizeof(go));
6
     State* extend(State *start,int token){
8
       State *p=this;
9
       State *np=new State(this->length+1);
10
       while(p!=NULL&&p->go[token]==NULL)
11
         p->go[token]=np, p=p->parent;
12
       if(p==NULL) np->parent=start;
13
       else{
```

```
14
         State *q=p->go[token];
15
         if(p->length+1==q->length) np->parent=q;
16
17
           State *nq=new State(p->length+1);
18
           memcpy(nq->go,q->go,sizeof(q->go));
19
           nq->parent=q->parent;
20
           np->parent=q->parent=nq;
21
           while(p!=NULL&&p->go[token]==q)
22
             p->go[token]=nq, p=p->parent;
23
         }
       }
24
25
       return np;
26
27
   };
  后缀树 (With Walk)
  struct State {
          int length;
          State *parent,*go[C];
          State(int length):length(length),parent(NULL){
                  memset(go,0,sizeof(go));
          State* extend(State *start,int token){
                  State *p=this;
                  State *np=new State(this->length+1);
                  while(p!=NULL&&p->go[token]==NULL)
                           p->go[token]=np, p=p->parent;
                  if(p==NULL) np->parent=start;
                  else{
                           State *q=p->go[token];
                           if(p->length+1==q->length) np->parent=q;
                           else{
                                   State *nq=new State(p->length+1);
                                   memcpy(nq->go,q->go,sizeof(q->go));
                                   nq->parent=q->parent;
                                   np->parent=q->parent=nq;
                                   while(p!=NULL&&p->go[token]==q)
                                           p->go[token]=nq, p=p->parent;
                  }
                  return np;
          }
  };
  后缀树 (With Pop Front)
  struct State {
          int length;
          State *parent,*go[C];
          State(int length):length(length),parent(NULL){
                  memset(go,0,sizeof(go));
          State* extend(State *start, int token){
```

```
State *p=this:
                   State *np=new State(this->length+1);
                   while(p!=NULL&&p->go[token]==NULL)
                           p->go[token]=np, p=p->parent;
                   if(p==NULL) np->parent=start;
                   else{
                           State *q=p->go[token];
                           if(p->length+1==q->length) np->parent=q;
                           else{
                                   State *nq=new State(p->length+1);
                                   memcpy(nq->go,q->go,sizeof(q->go));
                                   nq->parent=q->parent;
                                   np->parent=q->parent=nq;
                                   while(p!=NULL&&p->go[token]==q)
                                           p->go[token]=nq, p=p->parent;
                   return np;
          }
  };
  字符串最小表示
1 | std::string find(std::string s) {
     int i,j,k,l,N=s.length(); s+=s;
     for(i=0,j=1;j<N;){</pre>
3
       for(k=0;k<N&&s[i+k]==s[j+k];k++);</pre>
4
       if(k>=N) break;
5
6
       if(s[i+k]<s[j+k]) j+=k+1;
       else l=i+k,i=j,j=max(l,j)+1;
8
9
     return s.substr(i,N);
10
```

轻重链剖分

```
1 | struct Tree(){}*root[N];
2 int father[N], size[N], depth[N];
3 | int bfsOrd[N],pathId[N],ordInPath[N],sqn[N];
   void doBfs(int s){
     int qh=0,qt=0,*que=bfsOrd; father[s]=-1; depth[s]=0;
6
     for(que[qt++]=s;qh<qt;){</pre>
       int u=que[qh++];
8
       foreach(iter,adj[u]){
         int v=*iter; if(v==father[u]) continue;
9
         father[v]=u; depth[v]=depth[u]+1; que[qt++]=v;
10
       }
11
12
13
   void doSplit(){
     for(int i=N-1;i>=0;--i){
15
```

```
16
        int u=bfsOrd[i]; size[u]=1;
17
       foreach(iter,adj[u]){
18
         int v=*iter; if(v==father[u]) continue; size[u]+=size[v];
19
       }
20
     memset(pathId,-1,sizeof pathId);
21
22
     for(int i=0;i<N;++i){</pre>
23
       int top=bfsOrd[i],cnt=0;
24
       if(pathId[top]!=-1) continue;
25
       for(int next,u=top;u!=-1;u=next){
26
         sqn[cnt]=val[u]; ordInPath[u]=cnt; pathId[u]=top; ++cnt;
         next=-1;
27
28
         foreach(iter,adj[u]){
29
           int v=*iter; if(v==father[u]) continue;
30
           if(next<0||size[next]<size[v]) next=v;</pre>
         }
31
32
       root[top]=new Tree(0,cnt,sqn);
33
34
35
   void prepare(){ doBfs(0); doSplit(); }
```

KD Tree

```
#include <cstdio>
2 #include <vector>
  #include <iostream>
   #include <algorithm>
   using namespace std;
7 \mid // 带插入版本 ,没有写内存回收 ,空间复杂度 n \log n ,如果不需要插入可以大大简化
8 // N 为最大点数, D 为每个点的最大维度, d 为实际维度
|\mathfrak{g}|// 以查找最近点为例 ret 为当前最近点的距离的平方 ,用来剪枝 ,查询 k 近或 k 远的方法类似
10 // 使用时注意先 initNull
   const long long INF = (int)1e9 + 10;
11
   const int N = 2000000 + 10;
12
13
   const int D = 5;
   const double SCALE = 0.75;
14
   struct Point { int x[D]; } buf[N];
16 int d;
   struct Node {
18
    int depth, size;
19
    Node *ch[2], *p;
20
     Point val, maxv, minv;
     void set(Node *t, int d) { ch[d] = t; t->p = this; }
     bool dir() { return this == p->ch[1]; }
22
```

```
bool balanced() {
                                                                                                  68
23
                                                                                                  69
        return (double)max(ch[0]->size, ch[1]->size) <= (double)size * SCALE;
                                                                                                          Node *p = t->p;
24
                                                                                                          int tot = 0;
25
                                                                                                  70
26
      void update() {
                                                                                                  71
        size = ch[0]->size + ch[1]->size + 1;
27
                                                                                                  72
28
        for(int i = 0; i < d; ++ i) {
                                                                                                  73
          \max v.x[i] = \max(val.x[i], \max(ch[0]->\max v.x[i], ch[1]->\max v.x[i]));
29
                                                                                                  74
30
          minv.x[i] = min(val.x[i], min(ch[0]->minv.x[i], ch[1]->minv.x[i]));
                                                                                                  75
31
                                                                                                  76
32
                                                                                                  77
   } nodePool[N], *totNode, *null;
                                                                                                  78
33
   Node* newNode(Point p, int depth) {
                                                                                                  79
                                                                                                  80
                                                                                                          int dir = 0;
      Node *t = totNode ++;
35
                                                                                                  81
36
     t \rightarrow ch[0] = t \rightarrow ch[1] = t \rightarrow p = null;
     t->depth = depth;
                                                                                                  82
                                                                                                            last = cur;
37
38
                                                                                                  83
     t-val = t-maxv = t-minv = p;
                                                                                                  84
     t \rightarrow size = 1;
39
                                                                                                  85
     return t;
40
                                                                                                  86
41
42 long long ret;
                                                                                                  87
   int ctr;
                                                                                                  88
   int cmp(const Point &a, const Point &b) { return a.x[ctr] < b.x[ctr]; }
                                                                                                  89
                                                                                                            t->update();
   struct KDTree {
45
                                                                                                  90
                                                                                                          }
46
      Node *root;
                                                                                                  91
      KDTree() { root = null; }
                                                                                                  92
47
48
      KDTree(Point *a, int n) {
                                                                                                  93
        root = build(a, 0, n - 1, 0);
49
                                                                                                  94
50
                                                                                                  95
      Node *build(Point *a, int l, int r, int depth) {
                                                                                                  96
51
        if (1 > r) return null;
52
                                                                                                  97
        ctr = depth;
                                                                                                  98
53
        sort(a + 1, a + r + 1, cmp);
                                                                                                  99
54
        int mid = (1 + r) >> 1;
                                                                                                 100
55
56
        Node *t = newNode(a[mid], depth);
                                                                                                 101
        t->set(build(a, l, mid - 1, (depth + 1) % d), 0);
57
                                                                                                 102
58
        t->set(build(a, mid + 1, r, (depth + 1) % d), 1);
                                                                                                 103
        t->update();
59
                                                                                                 104
60
        return t;
                                                                                                 105
61
                                                                                                 106
62
      void tranverse(Node *t, Point *vec, int &tot) {
                                                                                                 107
63
        if (t == null) return;
                                                                                                 108
64
        vec[tot ++] = t->val;
                                                                                                 109
65
        tranverse(t->ch[0], vec, tot);
                                                                                                 110
66
        tranverse(t->ch[1], vec, tot);
                                                                                                          } else {
                                                                                                 111
67
                                                                                                 112
```

```
void rebuild(Node *t) {
 tranverse(t, buf, tot);
 Node *u = build(buf, 0, tot - 1, t->depth);
 p->set(u, t->dir());
 for( ; p != null; p = p->p) p->update();
 if (t == root) root = u;
void insert(Point p) {
 if (root == null) { root = newNode(p, 0); return; }
 Node *cur = root, *last = null;
 for( ; cur != null; ) {
   dir = (p.x[cur->depth] > cur->val.x[cur->depth]);
   cur = cur->ch[dir];
 Node *t = newNode(p, (last->depth + 1) % d), *bad = null;
 last->set(t, dir);
 for( ; t != null; t = t->p) {
   if (!t->balanced()) bad = t;
 if (bad != null) rebuild(bad);
long long calcEval(Point u, Node *t, int d) {
 long long l = t \rightarrow minv.x[d], r = t \rightarrow maxv.x[d], x = u.x[d];
 if (x >= 1 && x <= r) return 0LL;
 long long ret = min(abs(x - 1), abs(x - r));
  return ret * ret;
void updateAns(Point u, Point p) {
 // 在这里更新答案
void query(Node *t, Point p) {
 if (t == null) return;
  updateAns(t->val, p);
  long long evalLeft = calcEval(p, t->ch[0], t->depth);
  long long evalRight = calcEval(p, t->ch[1], t->depth);
  if (evalLeft <= evalRight) {</pre>
   query(t->ch[0], p);
   if (ret > evalRight) query(t->ch[1], p);
    query(t->ch[1], p);
```

```
if (ret > evalLeft) query(t->ch[0], p);
113
        }
114
115
116
      void query(Point p) {
117
        query(root, p);
118
119 };
120 void initNull() {
      totNode = nodePool;
121
      null = totNode ++;
122
      null->size = 0;
123
      for(int i = 0; i < d; ++ i) {
124
        null->maxv.x[i] = -INF;
125
126
        null->minv.x[i] = INF;
127
128 }
```

Splay Tree

```
// 注意初始化内存池和 null 节点
2 struct Node{
     int rev,size; Node *ch[2],*p;
     void set(Node*,int); int dir(); void update(); void relax(); void appRev();
   } nodePool[MAX_NODE],*curNode,*null;
6 | Node *newNode(){
     Node *t=curNode++; t->rev=0, t->size=1;
8
     t->ch[0]=t->ch[1]=t->p=null; return t;
9
   struct Splay{
10
     Node *root;
11
     Splay(){ root=newNode(); root->set(newNode(),0); root->update(); }
12
     void rot(Node *t){
13
       Node *p=t->p; int d=t->dir();
14
       p->relax(); t->relax();
15
16
       if(p==root) root=t;
       p->set(t->ch[!d],d); p->p->set(t,p->dir()); t->set(p,!d);
17
18
       p->update();
19
     void splay(Node *t,Node *f=null){
20
       for(t->relax();t->p!=f;)
21
         if(t->p->p==f) rot(t);
22
23
         else t->dir()==t->p->dir()?(rot(t->p),rot(t)):(rot(t),rot(t));
       t->update();
24
25
26
27 | void initNull(){ curNode=nodePool;null=curNode++;null->size=0; }
```

```
void Node::set(Node *t,int _d){ ch[_d]=t; t->p=this; }
int Node::dir(){ return this==p->ch[1]; }
void Node::update(){ size=ch[0]->size+ch[1]->size+1;}
void Node::relax(){ if(rev) ch[0]->appRev(), ch[1]->appRev(), rev=false; }
void Node::appRev(){ if(this==null) return; rev^=true; swap(ch[0],ch[1]); }
```

Link Cut Tree

```
1 // 注意初始化 null 节点, 单点的 is root 初始为 true
2 struct Node{
     Node *ch[2], *p;
     int is_root, rev;
     bool dir();
     void set(Node*, bool);
     void update();
     void relax();
     void app_rev();
    *null;
   void rot(Node *t){
11
     Node *p=t->p; bool d=t->dir();
     p->relax(); t->relax(); p->set(t->ch[!d],d);
13
     if(p->is_root) t->p=p->p,swap(p->is_root,t->is_root);
14
15
     else p->p->set(t,p->dir());
16
     t->set(p,!d); p->update();
17
18
   void splay(Node *t){
     for(t->relax();!t->is_root;)
19
20
       if(t->p->is_root) rot(t);
21
       else t->dir()==t->p->dir() ?(rot(t->p),rot(t)) :(rot(t),rot(t));
22
     t->update();
23
   void access(Node *t){
24
     for(Node *s=null; t!=null; s=t,t=t->p){
25
26
       splay(t);
       if (t->p == null) { /*TODO*/ }
27
       t->ch[1]->is_root=true; s->is_root=false;
28
       t->ch[1]=s; t->update();
29
30
31
   bool Node::dir(){ return this==p->ch[1]; }
   void Node::set(Node *t,bool _d){ ch[_d]=t; t->p=this; }
   void Node::update(){ }
   void Node::app_rev(){ if (this == null) return; rev ^= true; swap(ch[0], ch[1]); }
35
   void Node::relax() { if(this==null) return; if (rev) { ch[0]->app_rev();
```

```
37 | void make_root(Node *u) { access(u); splay(u); u->app_rev(); }
```

Dominator Tree

```
1 vector<int> prec[N], succ[N];
 2
   vector<int> ord;
 3
 4
   int stamp, vis[N];
 5
 6
   int num[N];
 8
   int fa[N];
 9
10
   void dfs(int u) {
11
12
     vis[u] = stamp;
13
     num[u] = ord.size();
     ord.push_back(u);
14
      for (int i = 0; i < (int)succ[u].size(); ++i) {</pre>
15
16
       int v = succ[u][i];
17
       if (vis[v] != stamp) {
18
         fa[v] = u;
         dfs(v);
19
20
^{21}
22
23
   int fs[N], mins[N];
24
25
26
   int dom[N], sem[N];
27
28
   int find(int u) {
     if (u != fs[u]) {
29
30
       int v = fs[u];
       fs[u] = find(fs[u]);
31
       if (mins[v] != -1 && num[sem[mins[v]]] < num[sem[mins[u]]]) {</pre>
32
33
         mins[u] = mins[v];
       }
34
35
36
     return fs[u];
37
38
39
   void merge(int u, int v) {
40
     fs[u] = v;
41
42
```

```
43 \mid \text{vector} < \text{int} > \text{buf[N]};
44
   int buf2[N];
45
46
   void mark(int source) {
47
48
     ord.clear();
      ++stamp;
49
      dfs(source);
50
      for (int i = 0; i < (int)ord.size(); ++i) {</pre>
51
       int u = ord[i];
52
       fs[u] = u;
53
        mins[u] = -1;
54
        buf2[u] = -1;
55
56
      for (int i = (int)ord.size() - 1; i > 0; --i) {
57
58
        int u = ord[i], p = fa[u];
        sem[u] = p;
59
60
        for (int j = 0; j < (int)prec[u].size(); ++j) {</pre>
61
          int v = prec[u][j];
          if (use[v] != stamp) {
62
63
            continue;
64
65
          if (num[v] > num[u]) {
66
            find(v);
67
            v = sem[mins[v]];
68
69
          if (num[v] < num[sem[u]]) {</pre>
            sem[u] = v;
70
71
72
        buf[sem[u]].push_back(u);
73
        mins[u] = u;
74
        merge(u, p);
75
76
        while (buf[p].size()) {
          int v = buf[p].back();
77
78
          buf[p].pop_back();
          find(v);
79
80
          if (sem[v] == sem[mins[v]]) {
81
            dom[v] = sem[v];
82
          } else {
83
            buf2[v] = mins[v];
84
85
86
87
      dom[ord[0]] = ord[0];
```

```
for (int i = 0; i < (int)ord.size(); ++i) {
   int u = ord[i];
   if (~buf2[u]) {
      dom[u] = dom[buf2[u]];
   }
   }
   }
}</pre>
```

DancingLinks

```
1 struct node{
     node *left,*right,*up,*down,*col; int row,cnt;
   }*head,*col[MAXC],Node[MAXNODE],*ans[MAXNODE];
   int totNode;
   void insert(const std::vector<int> &V,int rownum){
     std::vector<node*> N;
      for(int i=0;i<int(V.size());++i){</pre>
 8
       node* now=Node+(totNode++); now->row=rownum;
       now->col=now->up=col[V[i]], now->down=col[V[i]]->down;
 9
       now->up->down=now, now->down->up=now;
10
11
       now->col->cnt++; N.push back(now);
12
      for(int i=0;i<int(V.size());++i)</pre>
13
       N[i]->right=N[(i+1)%V.size()], N[i]->left=N[(i-1+V.size())%V.size()];
14
15 | }
16
   void Remove(node *x){
     x->left->right=x->right, x->right->left=x->left;
17
18
      for(node *i=x->down;i!=x;i=i->down)
        for(node *j=i->right;j!=i;j=j->right)
19
         j->up->down=j->down, j->down->up=j->up, --(j->col->cnt);
20
^{21}
   void Resume(node *x){
^{22}
     for(node *i=x->up;i!=x;i=i->up)
23
        for(node *j=i->left;j!=i;j=j->left)
24
         j->up->down=j->down->up=j, ++(j->col->cnt);
25
26
     x->left->right=x, x->right->left=x;
27
28
   bool search(int tot){
     if(head->right==head) return true;
29
     node *choose=NULL;
30
      for(node *i=head->right;i!=head;i=i->right){
31
       if(choose==NULL||choose->cnt>i->cnt) choose=i;
32
       if(choose->cnt<2) break;</pre>
33
34
     Remove(choose);
35
36
     for(node *i=choose->down;i!=choose;i=i->down){
```

```
for(node *j=i->right; j!=i; j=j->right) Remove(j->col);
37
38
        ans[tot]=i:
       if(search(tot+1)) return true;
39
40
        ans[tot]=NULL;
       for(node *j=i->left;j!=i;j=j->left) Resume(j->col);
41
42
     Resume(choose):
43
     return false:
44
45
46
    void prepare(int totC){
     head=Node+totC;
47
     for(int i=0;i<totC;++i) col[i]=Node+i;</pre>
48
     totNode=totC+1;
49
50
     for(int i=0;i<=totC;++i){</pre>
       (Node+i)->right=Node+(i+1)%(totC+1);
51
        (Node+i)->left=Node+(i+totC)%(totC+1);
52
        (Node+i)->up=(Node+i)->down=Node+i;
53
54
55
```

弦图相关

- 1. 团数 < 色数,弦图团数 = 色数
- 2. 设 next(v) 表示 N(v) 中最前的点 . 令 w* 表示所有满足 $A\in B$ 的 w 中最后的一个点,判断 $v\cup N(v)$ 是否为极大团 ,只需判断是否存在一个 w,满足 Next(w)=v 且 $|N(v)|+1\le |N(w)|$ 即可 .
- 3. 最小染色: 完美消除序列从后往前依次给每个点染色 ,给每个点染上可以染的最小的颜色
- 4. 最大独立集: 完美消除序列从前往后能选就选
- 5. 弦图最大独立集数 = 最小团覆盖数 ,最小团覆盖 : 设最大独立集为 $\{p_1,p_2,\dots,p_t\}$,则 $\{p_1\cup N(p_1),\dots,p_t\cup N(p_t)\}$ 为最小团覆盖

图同构 Hash

$$F_t(i) = (F_{t-1}(i) \times A + \sum_{i \to j} F_{t-1}(j) \times B + \sum_{j \to i} F_{t-1}(j) \times C + D \times (i = a)) \mod P$$

枚举点 a 迭代 K 次后求得的就是 a 点所对应的 hash 值 其中 K , A , B , C , D , P 为 hash 参数 ,可自选

直线下有多少个格点

```
1 LL solve(LL n, LL a, LL b, LL m) {
2    // 计算 for (int i=0;i<n;++i) s+=floor((a+b*i)/m)
3    //n,m,a,b>0
4    if(b==0) return n*(a/m);
5    if(a>=m) return n*(a/m)+solve(n,a%m,b,m);
6    if(b>=m) return (n-1)*n/2*(b/m)+solve(n,a,b%m,m);
```

```
7 return solve((a+b*n)/m,(a+b*n)%m,m,b);
8 }
```

费用流

```
1 // O is a priority queue<PII, vector<PII>, greater<PII> >
2 // for an edge(s, t): u is the capacity, v is the cost, nxt is the next edge,
3 // op is the opposite edge
4 // this code can not deal with negative cycles
5 typedef pair<int,int> PII;
6 struct edge{ int t,u,v; edge *nxt,*op; }E[MAXE],*V[MAXV];
7 int D[MAXN], dist[MAXN], maxflow, mincost; bool in[MAXN];
8 bool modlabel(){
     while(!Q.empty()) Q.pop();
     for(int i=S;i<=T;++i){</pre>
11
      if(in[i]) D[i]=0,Q.push(PII(0,i));
       else D[i]=inf;
12
     }
13
     while(!Q.empty()){
14
       int x=Q.top().first,y=Q.top().second;
15
16
       Q.pop();
       if(y==T) break;
17
18
       if(D[y]<x) continue;</pre>
       for(edge *ii=V[y];ii;ii=ii->nxt) if(ii->u){
19
         if(x+(ii->v+dist[ii->t]-dist[y])<D[ii->t]){
20
21
           D[ii->t]=x+(ii->v+dist[ii->t]-dist[y]);
22
           Q.push(PII(D[ii->t],ii->t));
         }
23
       }
24
25
     if(D[T]==inf) return false;
26
     for(int i=S;i<=T;++i) if(D[i]>D[T]) dist[i]+=D[T]-D[i];
27
28
     return true:
29
   int aug(int p,int limit){
     if(p==T) return maxflow+=limit,mincost+=limit*dist[S],limit;
31
     in[p]=1; int kk,ll=limit;
32
     for(edge *ii=V[p];ii;ii=ii->nxt) if(ii->u){
33
       if(!in[ii->t]&&dist[ii->t]+ii->v==dist[p]){
34
         kk=aug(ii->t,min(ii->u,ll));
35
36
         ll-=kk,ii->u-=kk,ii->op->u+=kk;
         if(!ll) return in[p]=0,limit;
37
38
39
     return limit-ll;
40
41 }
```

```
42 PII mincostFlow(){
     for(int i=S;i<=T;++i) dist[i]=i==T?inf:0;</pre>
43
     while(!Q.empty()) Q.pop();
44
45
     Q.push(PII(0,T));
46
     while(!Q.empty()){
       int x=Q.top().first,y=Q.top().second;
47
48
       Q.pop();
49
       if(dist[y]<x) continue;</pre>
       for(edge *ii=V[y];ii;ii=ii->nxt) if(ii->op->u&ii->v+x<dist[ii->t]{
50
51
         dist[ii->t]=ii->v+x;
         Q.push(PII(dist[ii->t],ii->t));
52
       }
53
54
     maxflow=mincost=0;
55
56
     do{
       do{
57
58
         memset(in,0,sizeof(in));
       }while(aug(S,maxflow));
59
     }while(modlabel());
60
61
     return PII(maxflow,mincost);
62 }
```

综合

定理 1: 最小覆盖数 = 最大匹配数 定理 2: 最大独立集 S 与 最小覆盖集 T 互补 算法:

- 1. 做最大匹配 . 没有匹配的空闲点 $\in S$
- 2. 如果 $u \in S$ 那么 u 的临点必然属于 T
- 3. 如果一对匹配的点中有一个属于 T 那么另外一个属于 S
- 4. 还不能确定的 , 把左子图的放入 S, 右子图放入 T

复法结束

上下界无源汇可行流 : 不用添 T->S. 判断是否流量平衡

上下界有源汇可行流 : 添 $T \to S$ (下界 0, 上界 ∞), 判断是否流量平衡

上下界最小流 : 不添 $T \to S$ 先流一遍 , 再添 $T \to S$ (下界 0 , 上界 ∞) 在残图上流一遍 , 答案为 $S \to T$ 的流量值

上下界最大流: 添 $T\to S$ (下界 0, 上界 ∞) 流一遍,再在残图上流一遍S到T的最大流,答案为前者的 $S\to T$ 的值 + 残图中 $S\to T$ 的最大流

Stirling 公式 $n! = \sqrt{2\pi n} (\frac{n}{e})^n$

Stirling 数

```
第一类:n 个元素的项目分作 k 个环排列的方法数目  |s(n,k)| = |s(n-1,k-1)| + (n-1)*|s(n-1,k)|  第二类:n 个元素的集定义 k 个等价类的方法数  |s(n,0)| = 0, |s(1,1)| = 1,   S(n,1) = S(n,n) = 1, S(n,k) = S(n-1,k-1) + k*S(n-1,k)
```

积分表

```
Integrals of Rational Functions
                                                                                                                                                                                   \int \frac{1}{1+x^2} dx = \tan^{-1} x \qquad \int \frac{1}{a^2+x^2} dx = \frac{1}{a} \tan^{-1} \frac{x}{a} \qquad \int \frac{x}{a^2+x^2} dx = \frac{1}{2} \ln|a^2+x^2| \qquad \int \frac{x^2}{a^2+x^2} dx = x - a \tan^{-1} \frac{x}{a} \qquad \int \frac{x^3}{a^2+x^2} dx = \frac{1}{2} x^2 - \frac{1}{2} a^2 \ln|a^2+x^2|
\int \frac{1}{ax^2 + bx + c} dx = \frac{2}{\sqrt{4ac - b^2}} \tan^{-1} \frac{2ax + b}{\sqrt{4ac - b^2}} \qquad \int \frac{1}{(x + a)(x + b)} dx = \frac{1}{b - a} \ln \frac{a + x}{b + x}, \ a \neq b \qquad \int \frac{x}{(x + a)^2} dx = \frac{a}{a + x} + \ln |a + x| \qquad \int \frac{x}{ax^2 + bx + c} dx = \frac{1}{2a} \ln |ax^2 + bx + c| - \frac{b}{a\sqrt{4ac - b^2}} \tan^{-1} \frac{2ax + b}{\sqrt{4ac - b^2}} \tan^{-1} \frac{2
Integrals with Roots  \int \frac{x}{\sqrt{x\pm a}} dx = \frac{2}{3} (x\mp 2a) \sqrt{x\pm a} \qquad \int \sqrt{\frac{x}{a-x}} dx = -\sqrt{x(a-x)} - a \tan^{-1} \frac{\sqrt{x(a-x)}}{x-a} \qquad \int \sqrt{\frac{x}{a+x}} dx = \sqrt{x(a+x)} - a \ln\left[\sqrt{x} + \sqrt{x+a}\right] \qquad \int x \sqrt{x^2 \pm a^2} dx = \frac{1}{3} \left(x^2 \pm a^2\right)^{3/2} 
\int x\sqrt{ax+b}dx = \frac{2}{15a^2}(-2b^2 + abx + 3a^2x^2)\sqrt{ax+b} \qquad \int \sqrt{x(ax+b)}dx = \frac{1}{4a^{3/2}}\left[(2ax+b)\sqrt{ax(ax+b)} - b^2\ln\left|a\sqrt{x} + \sqrt{a(ax+b)}\right|\right] \qquad \int \sqrt{x^2\pm a^2}dx = \frac{1}{2}x\sqrt{x^2\pm a^2}\pm \frac{1}{2}a^2\ln\left|x + \sqrt{x^2\pm a^2}\right| + \frac{1}{2}a^2\ln\left|
\int \sqrt{x^3(ax+b)}dx = \left[\frac{b}{12a} - \frac{b^2}{8a^2x} + \frac{x}{3}\right] \sqrt{x^3(ax+b)} + \frac{b^3}{8a^{5/2}} \ln\left|a\sqrt{x} + \sqrt{a(ax+b)}\right| \qquad \int \sqrt{a^2 - x^2}dx = \frac{1}{2}x\sqrt{a^2 - x^2} + \frac{1}{2}a^2 \tan^{-1}\frac{x}{\sqrt{a^2 - x^2}}dx = \frac{1}{2}x\sqrt{x^2 \pm a^2} \mp \frac{1}{2}a^2 \ln\left|x + \sqrt{x^2 \pm a^2}\right| + \frac{1}{2}a^2 \ln\left|x + \sqrt{x^2 \pm a^2}\right| + \frac{1}{2}a^2 \ln\left|x + \sqrt{a(ax+b)}\right| + \frac{1
\int x\sqrt{ax^2 + bx + c} = \frac{1}{48a^{5/2}} \left( 2\sqrt{a}\sqrt{ax^2 + bx + c} \times \left( -3b^2 + 2abx + 8a(c + ax^2) \right) \right) + 3(b^3 - 4abc) \ln \left| b + 2ax + 2\sqrt{a}\sqrt{ax^2 + bx + c} \right| 
\int \frac{x}{\sqrt{ax^2 + bx + c}} dx = \frac{1}{a} \sqrt{ax^2 + bx + c} - \frac{b}{2a^{3/2}} \ln \left| 2ax + b + 2\sqrt{a(ax^2 + bx + c)} \right| \qquad \int \frac{dx}{(a^2 + x^2)^{3/2}} = \frac{x}{a^2 \sqrt{a^2 + x^2}}  Integrals with Logarithms
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        \int \ln(ax+b)dx = \left(x+\frac{b}{a}\right)\ln(ax+b) - x, a \neq 0
\int \frac{\ln ax}{x} dx = \frac{1}{2} (\ln ax)^2 \qquad \int \ln(x^2 + a^2) dx = x \ln(x^2 + a^2) + 2a \tan^{-1} \frac{x}{a} - 2x \qquad \int \ln(x^2 - a^2) dx = x \ln(x^2 - a^2) + a \ln \frac{x+a}{x-a} - 2x \qquad \int x \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} + \frac{bx}{2a
\int \ln\left(ax^2 + bx + c\right) dx = \frac{1}{a}\sqrt{4ac - b^2} \tan^{-1} \frac{2ax + b}{\sqrt{4ac - b^2}} - 2x + \left(\frac{b}{2a} + x\right) \ln\left(ax^2 + bx + c\right) 
\int x \ln\left(a^2 - b^2x^2\right) dx = -\frac{1}{2}x^2 + \frac{1}{2}\left(x^2 - \frac{a^2}{b^2}\right) \ln\left(a^2 - b^2x^2\right)
\int x^n e^{ax} \, \mathrm{d}x = \frac{x^n e^{ax}}{a} - \frac{n}{a} \int x^{n-1} e^{ax} \, \mathrm{d}x
\int x e^{-ax^2} \, \mathrm{d}x = -\frac{1}{2a} e^{-ax^2}
\int \cos^3 ax \, dx = \frac{3\sin ax}{4a} + \frac{\sin 3ax}{12a}
\int \cos ax \sin bx \, dx = \frac{1}{2a} e^{-ax^2}
\int \cos ax \sin bx \, dx = \frac{\cos((a+b)x)}{2(a+b)} - \frac{\cos((a+b)x)}{2(a+b)}, a \neq b
\int \sin^2 ax \cos bx \, dx = -\frac{\sin((2a-b)x)}{4(2a-b)} + \frac{\sin bx}{2b} - \frac{\sin((2a+b)x)}{4(2a+b)}
\int \sin^2 x \cos x \, dx = \frac{1}{3} \sin^3 x
\int \cos^2 ax \sin bx dx = \frac{\cos[(2a-b)x]}{4(2a-b)} - \frac{\cos bx}{2b} - \frac{\cos[(2a+b)x]}{4(2a-b)} - \int \cos^2 ax \sin ax dx = -\frac{1}{3a} \cos^3 ax 
\int \sin^2 ax \cos^2 bx dx = \frac{x}{4} - \frac{\sin 2ax}{8a} - \frac{\sin[2(a-b)x]}{16(a-b)} + \frac{\sin 2bx}{8b} - \frac{\sin[2(a+b)x]}{16(a+b)} 
\int \sin^2 ax \cos^2 ax dx = \frac{x}{8} - \frac{\sin 4ax}{32a}
\int \tan ax dx = -\frac{1}{a} \ln \cos ax 
\int \tan^2 ax dx = -x + \frac{1}{a} \tan ax 
\int \tan^3 ax dx = \frac{1}{a} \ln \cos ax + \frac{1}{2a} \sec^2 ax 
\int \sec x dx = \ln |\sec x + \tan x| = 2 \tanh^{-1} (\tan \frac{x}{2}) 
\int \sec^2 ax dx = \frac{1}{a} \tan ax 
\int \sec^3 x \, dx = \frac{1}{2} \sec x \tan x + \frac{1}{2} \ln|\sec x + \tan x|
\int \sec x \tan x dx = \sec x
\int \sec^2 x \tan x dx = \frac{1}{2} \sec^2 x
\int \sec^n x \tan x dx = \frac{1}{2} \sec^n x, n \neq 0
\int \csc x dx = \ln|\tan \frac{x}{2}| = \ln|\csc x - \cot x| + C
 \int \csc^2 ax dx = -\frac{1}{a} \cot ax \int \csc^3 x dx = -\frac{1}{2} \cot x \csc x + \frac{1}{2} \ln|\csc x - \cot x| \int \csc^n x \cot x dx = -\frac{1}{n} \csc^n x, n \neq 0 \int \sec x \csc x dx = \ln|\tan x|  Products of Trigonometric Functions and Monomials
 \int x \cos x dx = \cos x + x \sin x \qquad \int x \cos ax dx = \frac{1}{a^2} \cos ax + \frac{x}{a} \sin ax \qquad \int x^2 \cos x dx = 2x \cos x + \left(x^2 - 2\right) \sin x \qquad \int x^2 \cos ax dx = \frac{2x \cos ax}{a^2} + \frac{a^2 x^2 - 2}{a^3} \sin ax \qquad \int x \sin x dx = -x \cos x + \sin x
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Products of Trigonometric Functions and Exponentials
 \int x \sin ax dx = -\frac{x \cos ax}{a} + \frac{\sin ax}{a^2} \qquad \int x^2 \sin x dx = (2 - x^2) \cos x + 2x \sin x \qquad \int x^2 \sin ax dx = \frac{2 - a^2 x^2}{3} \cos ax + \frac{2x \sin ax}{3}
 \int e^x \sin x dx = \frac{1}{2} e^x (\sin x - \cos x) \qquad \qquad \int e^{bx} \sin ax dx = \frac{1}{a^2 + b^2} e^{bx} (b \sin ax - a \cos ax) \qquad \qquad \int e^{bx} \cos ax dx = \frac{1}{a^2 + b^2} e^{bx} (a \sin ax + b \cos ax) \qquad \qquad \int x e^x \sin x dx = \frac{1}{2} e^x (\cos x - x \cos x + x \sin x)
  \int xe^x \cos x dx = \frac{1}{2}e^x (x \cos x - \sin x + x \sin x) \quad \int e^x \cos x dx = \frac{1}{2}e^x (\sin x + \cos x)
```

Java

```
import java.io.*;
import java.util.*;
import java.math.*;

public class Main{
    BufferedReader reader = new BufferedReader(new InputStreamReader(System.in));
    PrintWriter writer = new PrintWriter(System.out);
    StringTokenizer tokenizer = null;
```

```
void solve() throws Exception {
void run()throws Exception{
try{
    while (true) {
        solve();
    }
}
catch(Exception e){
}
```

```
finally{
20
         reader.close();
21
         writer.close();
22
23
       }
24
     String next()throws Exception{
25
       for(;tokenizer == null || !tokenizer.hasMoreTokens();){
26
         tokenizer = new StringTokenizer(reader.readLine());
27
28
       }
       return tokenizer.nextToken();
29
30
     int nextInt()throws Exception{
31
       return Integer.parseInt(next());
32
33
     double nextDouble()throws Exception{
34
       return Double.parseDouble(next());
35
36
     }
     BigInteger nextBigInteger()throws Exception{
37
38
       return new BigInteger(next());
     }
39
     public static void main(String args[])throws Exception{
40
       (new Main()).run();
41
42
```

```
43 | }
```

Vimrc

```
1 \begin{lstlisting}
   set nu ai ci si mouse=a ts=4 sts=4 sw=4
 3
   nmap<C-A> ggVG
   vmap<C-C> "+y
   nmap<F3> : vs %<.in <CR>
   nmap<F5> : !./%< <CR>
 g nmap<F8> : !./%< < %<.in <CR>
10 nmap<F9> : !g++ % -o %< -Wall <CR>
11
   "nmap<F4> : !gedit % <CR>
12
   "autocmd BufNewFile *.cpp 0r ~/temp.cpp
   "set hlsearch incseach
15
   "syntax on
   "filetype plugin indent on
17
18 \end{lstlisting}
```