Dracarys

Team Referrence Library

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上海交通大学 Shanghai Jiao Tong University			Page 1
Contents		FFT	21
多边形与圆面积交	2	NTT	22
二维几何	2	FWT	22
$n\log n$ 半平面交	4	Manacher/ 扩展 KMP	23
Delaunay 三角剖分	5	后缀数组 (倍增)	23
三维几何操作合并	7	后缀数组 (DC3)	24
三维凸包	8	后缀自动机	24
凸包上快速询问	9	后缀树 (With Walk)	24
圆的面积模板 $(n^2 \log n)$	10	后缀树 (With Pop Front)	27
三角形的心	11	字符串最小表示	29
最小覆盖球	12	轻重链剖分	29
经纬度求球面最短距离	12	KD Tree	30
长方体表面两点最短距离	12	Splay Tree	31
最大团	13	Link Cut Tree	31
极大团计数	13	Dominator Tree	32
KM	14	DancingLinks	33
最小树形图	15	弦图相关	34
无向图最小割	15	图同构 Hash	34
带花树	16	环状最长公共子序列	34
动态最小生成树	17	直线下有多少个格点	34
Hopcroft	17	费用流	35
素数判定	18	综合	35
启发式分解	18	积分表	36
二次剩余	19	Java	36
Pell 方程	19	Vimre	37
蔡勒公式	19		
Schreier-Sims	19		
Romberg	21		
线性规划	21		

多边形与圆面积交

```
1 double areaCT(Point pa, Point pb, double r) {
     if (pa.len() < pb.len()) {</pre>
       swap(pa, pb);
 3
 4
     if (sign(pb.len()) == 0) {
 5
 6
       return 0;
 7
 8
     double a = pb.len(), b = pa.len(), c = (pb - pa).len();
 9
     double sinB = fabs(det(pb, pb - pa) / a / c),
          cosB = dot(pb, pb - pa) / a / c,
10
11
           sinC = fabs(det(pa, pb) / a/ b),
          cosC = dot(pa, pb) / a / b;
12
     double B = atan2(sinB, cosB), C = atan2(sinC, cosC);
13
14
     if (a > r) {
       S = C / 2 * r * r;
15
       h = a * b * sinC / c;
16
17
       if (h < r && B < PI / 2) {
18
         S = (acos(h / r) * r * r - h * sqrt(r * r - h * h));
19
20
     } else if (b > r) {
       double theta = PI - B - asin(sinB / r * a);
21
       S = a * r * sin(theta) / 2 + (C - theta) / 2 * r * r;
22
23
     } else {
       S = sinC * a * b / 2;
24
25
26
     return S;
27
```

二维几何

```
1 | #include <iostream>
2 | #include <cmath>
   #include <vector>
   using namespace std;
5
6
   const double PI = acos(-1.0);
8
   const double EPS = 1e-8;
   int sign(double x)
10
11
12
     return x \leftarrow -EPS ? -1 : x > EPS;
13 | }
14
15 double newSqrt(double x)
```

```
16 {
17
     return x < 0 ? 0 : sqrt(x);
18 }
19
   struct Point {
20
     double x, y;
21
     Point(double x = 0, double y = 0) : x(x), y(y) {}
22
     Point operator + (const Point &that) const {
23
24
       return Point(x + that.x, y + that.y);
25
26
     Point operator - (const Point &that) const {
       return Point(x - that.x, y - that.y);
27
28
     Point operator * (const double &that) const {
29
       return Point(x * that, y * that);
30
     }
31
     Point operator / (const double &that) const {
32
       return Point(x / that, y / that);
33
34
     Point rotate(const double ang) { // 逆时针旋转 ang 弧度
35
36
       return Point(cos(ang) * x - sin(ang) * y, cos(ang) * y + sin(ang) * x);
37
38
     Point turn90() { // 逆时针旋转 90 度
       return Point(-y, x);
39
40
41
     double len2() const {
       return x * x + y * y;
42
43
     double len() const {
44
       return sqrt(x * x + y * y);
45
46
     Point unit() const {
47
       return *this / len();
48
49
     int operator < (const Point &that) const {</pre>
50
       int d = sign(x - that.x); if (d) return d < 0;</pre>
51
       return sign(y - that.y) < 0;</pre>
52
53
54
   double det(Point a, Point b)
55
56
     return a.x * b.y - b.x * a.y;
57
58
   double dot(Point a, Point b)
59
60 {
```

```
return a.x * b.x + a.v * b.v:
61
                                                                                            106
62 }
                                                                                            107
 63 double det(Point s, Point a, Point b)
                                                                                            108
                                                                                                  p1 = o + delta:
 64 | {
                                                                                            109
                                                                                                  p2 = o - delta;
 65
      return (a.x - s.x) * (b.y - s.y) - (b.x - s.x) * (a.y - s.y);
                                                                                                  return true;
                                                                                            110
 66 | }
                                                                                            111
 67
                                                                                            112
                                                                                            113 // 求圆与圆的交面积
 68 struct Line {
 69
      Point a, b;
 70
      Line(Point a, Point b) : a(a), b(b) {}
                                                                                            115
                                                                                            116
71 | };
                                                                                                    return 0;
 72
                                                                                            117
    Point isLL(const Line &11, const Line &12) {
                                                                                            118
      double s1 = det(12.b - 12.a, 11.a - 12.a),
                                                                                            119
 74
           s2 = -det(12.b - 12.a, 11.b - 12.a);
                                                                                            120
 75
 76
      return (l1.a * s2 + l1.b * s1) / (s1 + s2);
                                                                                                    return r * r * PI;
                                                                                            121
 77
                                                                                            122
    bool onSeg(const Line &1, const Point &p) { // 点在线段上
 78
                                                                                            123
      return sign(det(p - 1.a, 1.b - 1.a)) == 0 && sign(dot(p - 1.a, p - 1.b)) <= 0;
 79
                                                                                            124
 80
                                                                                            125
 81
    Point projection(const Line &l, const Point &p) { // 点到直线投影
                                                                                            126
 82
      return 1.a + (1.b - 1.a) * (dot(p - 1.a, 1.b - 1.a) / (1.b - 1.a).len2());
                                                                                            127
 83 | }
                                                                                            128
 84 | double disToLine(const Line &1, const Point &p) {
                                                                                            129
      return abs(det(p - 1.a, 1.b - 1.a) / (1.b - 1.a).len());
 85
                                                                                            130
 86 | }
                                                                                            131
 87
    double disToSeg(const Line &1, const Point &p) { // 点到线段距离
                                                                                            132
 88
      return sign(dot(p - 1.a, 1.b - 1.a)) * sign(dot(p - 1.b, 1.a - 1.b)) != 1 ?
                                                                                            133
 89
        disToLine(1, p) : min((p - 1.a).len(), (p - 1.b).len());
                                                                                            134
 90
                                                                                            135
    Point symmetryPoint(const Point a, const Point b) { // 点 b 关于点 a 的中心对称点
                                                                                            136
 91
      return a + a - b;
                                                                                            137
                                                                                                  return true;
 92
                                                                                            138
 93
    Point reflection(const Line &1, const Point &p) { // 点关于直线的对称点
                                                                                            139
 94
      return symmetryPoint(projection(l, p), p);
95
 96 | }
    struct Circle {
                                                                                            142 {
 97
      Point o;
 98
                                                                                            143
      double r;
                                                                                            144
 99
      Circle (Point o = Point(0, 0), double r = 0) : o(o), r(r) {}
100
                                                                                            145
101 };
                                                                                            146
102
                                                                                                  p1 = c.o + p + delta;
                                                                                            147
103 // 求圆与直线的交点
                                                                                            148
                                                                                                  p2 = c.o + p - delta;
104 bool isCL(Circle a, Line 1, Point &p1, Point &p2) {
                                                                                            149
                                                                                                  return true;
     if (sign(det(l.a - a.o, l.b - a.o) / (l.a - l.b).len()) > 0) return false;
                                                                                            150 }
```

```
Point o = isLL(Line(a.o., a.o + (1.b - 1.a).turn90()), 1);
  Point delta = (1.b - 1.a).unit() * newSqrt(a.r * a.r - (o - a.o).len2()):
double areaCC(const Circle &c1, const Circle &c2) {
  double d = (c1.o - c2.o).len();
 if (sign(d - (c1.r + c2.r)) >= 0) {
  if (sign(d - abs(c1.r - c2.r)) \leftarrow 0)
    double r = min(c1.r, c2.r);
  double x = (d * d + c1.r * c1.r - c2.r * c2.r) / (2 * d),
       t1 = acos(x / c1.r), t2 = acos((d - x) / c2.r);
  return c1.r * c1.r * t1 + c2.r * c2.r * t2 - d * c1.r * sin(t1);
// 求圆与圆的交点,注意调用前要先判定重圆
bool isCC(Circle a, Circle b, Point &p1, Point &p2) {
  double s1 = (a.o - b.o).len();
  if (sign(s1 - a.r - b.r)) > 0 \mid | sign(s1 - abs(a.r - b.r)) < 0) return false;
  double s2 = (a.r * a.r - b.r * b.r) / s1;
  double aa = (s1 + s2) * 0.5, bb = (s1 - s2) * 0.5;
  Point o = (b.o - a.o) * (aa + bb)) + a.o;
  Point delta = (b.o - a.o).unit().turn90() * newSqrt(a.r * a.r - aa * aa);
  p1 = o + delta, p2 = o - delta;
// 求点到圆的切点,按关于点的左手方向返回两个点
bool tanCP(const Circle &c, const Point &p0, Point &p1, Point &p2)
  double x = (p0 - c.o).len2(), d = x - c.r * c.r;
 if (d < EPS) return false;</pre>
  Point p = (p0 - c.o) * (c.r * c.r / x);
  Point delta = ((p0 - c.o) * (-c.r * sqrt(d) / x)).turn90();
```

```
151
    // 求圆到圆的外共切线,按关于 c1.o 的左手方向返回两条线
152
    vector<Line> extanCC(const Circle &c1, const Circle &c2)
154 | {
      vector<Line> ret;
155
156
      if (sign(c1.r - c2.r) == 0) {
        Point dir = c2.o - c1.o;
157
158
        dir = (dir * (c1.r / dir.len())).turn90();
        ret.push_back(Line(c1.o + dir, c2.o + dir));
159
160
        ret.push_back(Line(c1.o - dir, c2.o - dir));
161
      } else {
162
        Point p = (c1.0 * -c2.r + c2.o * c1.r) / (c1.r - c2.r);
163
        Point p1, p2, q1, q2;
        if (tanCP(c1, p, p1, p2) && tanCP(c2, p, q1, q2)) {
164
165
         if (c1.r < c2.r) swap(p1, p2), swap(q1, q2);
166
          ret.push_back(Line(p1, q1));
167
          ret.push_back(Line(p2, q2));
168
        }
169
170
      return ret;
171
172
    // 求圆到圆的内共切线,按关于 c1.o 的左手方向返回两条线
    vector<Line> intanCC(const Circle &c1, const Circle &c2)
175 | {
176
      vector<Line> ret;
      Point p = (c1.0 * c2.r + c2.o * c1.r) / (c1.r + c2.r);
177
178
      Point p1, p2, q1, q2;
      if (tanCP(c1, p, p1, p2) && tanCP(c2, p, q1, q2)) {
179
180
        ret.push_back(Line(p1, q1));
181
        ret.push_back(Line(p2, q2));
182
     }
183
      return ret;
184 }
185
186 | bool contain(vector<Point> polygon, Point p) { // 判断点 p
      → 是否被多边形包含,包括落在边界上
      int ret = 0, n = polygon.size();
187
188
      for(int i = 0; i < n; ++ i) {
189
        Point u = polygon[i], v = polygon[(i + 1) % n];
190
        if (onSeg(Line(u, v), p)) return true;
        if (sign(u.y - v.y) \leftarrow 0) swap(u, v);
191
        if (sign(p.y - u.y) > 0 \mid | sign(p.y - v.y) <= 0) continue;
192
        ret += sign(det(p, v, u)) > 0;
193
194
```

```
return ret & 1:
195
196 }
197
    |vector<Point> convexCut(const vector<Point>&ps, Line 1) { // 用半平面 (q1,q2)
       → 的逆时针方向去切凸多边形
      vector<Point> qs;
199
200
      int n = ps.size();
201
      for (int i = 0; i < n; ++i) {
202
        Point p1 = ps[i], p2 = ps[(i + 1) \% n];
203
        int d1 = sign(det(l.a, l.b, p1)), d2 = sign(det(l.a, l.b, p2));
        if (d1 >= 0) qs.push_back(p1);
204
        if (d1 * d2 < 0) qs.push_back(isLL(Line(p1, p2), 1));</pre>
205
206
207
      return qs;
208
     vector<Point> convexHull(vector<Point> ps) { // 求点集 ps 组成的凸包
209
      int n = ps.size(); if (n <= 1) return ps;</pre>
210
      sort(ps.begin(), ps.end());
211
      vector<Point> qs;
212
      for (int i = 0; i < n; qs.push back(ps[i++]))
213
214
        while (qs.size() > 1 \&\& sign(det(qs[qs.size()-2],qs.back(),ps[i])) <= 0)

    qs.pop_back();
      for (int i = n - 2, t = qs.size(); i \ge 0; qs.push back(ps[i--]))
215
216
        while ((int)qs.size() > t && sign(det(qs[(int)qs.size()-2],qs.back(),ps[i])) <=</pre>
           → 0) qs.pop back();
      qs.pop back(); return qs;
217
218 }
219
    int main()
220
221
      Circle c1, c2;
222
223
      c1.0 = Point(0, 0); c1.r = 10;
      c2.o = Point(10, 10); c1.r = 10;
224
225
      Point p1, p2;
226
      return 0;
227
```

$n \log n$ 半平面交

```
struct Point {
   Point norm() const {
    double 1 = len();
   return Point(x / 1, y / 1);
}

int quad() const {
```

```
return sign(y) == 1 \mid \mid (sign(y) == 0 \&\& sign(x) >= 0);
 9
     }
10 };
11
   struct Line {
12
     bool include(const Point &p) const {
13
       return sign(det(b - a, p - a)) > 0;
14
     }
15
16
      Line push() const{ // 将半平面向外推 eps
17
18
       const double eps = 1e-6;
       Point delta = (b - a).turn90().norm() * eps;
19
       return Line(a - delta, b - delta);
20
21
   };
22
23
   bool sameDir(const Line &10, const Line &11) {
24
     return parallel(10, 11) && sign(dot(10.b - 10.a, 11.b - 11.a)) == 1;
25
26
27
28
   bool operator < (const Point &a, const Point &b) {</pre>
     if (a.quad() != b.quad()) {
29
       return a.quad() < b.quad();</pre>
30
     } else {
31
       return sign(det(a, b)) > 0;
32
33
34
35
   bool operator < (const Line &10, const Line &11) {
     if (sameDir(10, 11)) {
37
38
       return l1.include(10.a);
     } else {
39
       return (10.b - 10.a) < (11.b - 11.a);
40
41
42
43
   bool check(const Line &u, const Line &v, const Line &w) {
44
     return w.include(intersect(u, v));
45
46
47
   vector<Point> intersection(vector<Line> &1) {
     sort(1.begin(), 1.end());
49
     deque<Line> q;
50
     for (int i = 0; i < (int)l.size(); ++i) {</pre>
51
52
       if (i && sameDir(l[i], l[i - 1])) {
```

```
continue;
53
       }
54
       while (q.size() > 1 && !check(q[q.size() - 2], q[q.size() - 1], l[i])) {
55
56
         q.pop back();
57
58
       while (q.size() > 1 \&\& !check(q[1], q[0], l[i])) {
         q.pop_front();
59
60
       }
61
       q.push_back(l[i]);
62
63
     while (q.size() > 2 \& !check(q[q.size() - 2], q[q.size() - 1], q[0])) {
64
       q.pop_back();
65
66
     while (q.size() > 2 \&\& !check(q[1], q[0], q[q.size() - 1])) {
67
       q.pop_front();
68
     }
69
     vector<Point> ret;
     for (int i = 0; i < (int)q.size(); ++i) {</pre>
70
       ret.push back(intersect(q[i], q[(i + 1) % q.size()]));
71
72
     }
73
     return ret;
74 }
```

Delaunay 三角剖分

```
2 Delaunay Triangulation 随机增量算法:
3 节点数至少为点数的 6 倍,空间消耗较大注意计算内存使用
  建图的过程在 build 中,注意初始化内存池和初始三角形的坐标范围 (Triangulation::LOTS)
5 Triangulation::find 返回包含某点的三角形
6 Triangulation::add_point 将某点加入三角剖分
  |某个 Triangle 在三角剖分中当且仅当它的 has_children 为 0
8 | 如果要找到三角形 u 的邻域,则枚举它的所有 u.edge[i].tri, 该条边的两个点为 u.p[(i+1)%3],
     \hookrightarrow u.p[(i+2)\%3]
9 */
  const int N = 100000 + 5;
10
  const int MAX TRIS = N * 6;
12 const double EPSILON = 1e-6;
  const double PI = acos(-1.0);
  using namespace std;
14
15
16 struct Point {
17
    double x,v;
18
    Point(): x(0), y(0) {}
    Point(double x, double y) : x(x), y(y) {}
    inline bool operator == (Point const& that) const {
```

```
return x == that.x && y == that.y;
                                                                                            64
                                                                                                  bool has children() const {
                                                                                            65
22
    }
                                                                                                    return children[0] != 0;
                                                                                             66
23 | };
24
                                                                                            67
                                                                                                  int num children() const {
   inline double sqr(double x) { return x*x; }
                                                                                            68
                                                                                                    return children[0] == 0 ? 0
25
   double dist sqr(Point const& a, Point const& b) {
                                                                                            69
                                                                                                      : children[1] == 0 ? 1
26
     return sqr(a.x-b.x) + sqr(a.y-b.y);
                                                                                             70
                                                                                                      : children[2] == 0 ? 2 : 3;
27
28
   }
                                                                                             71
                                                                                                  }
   bool in_circumcircle(Point const& p1, Point const& p2, Point const& p3, Point const&
                                                                                                  bool contains(Point const& q) const {
                                                                                             72
      → p4) {
                                                                                             73
                                                                                                    double a = side(p[0],p[1],q);
     double u11 = p1.x - p4.x;
                                                                                                    double b = side(p[1],p[2],q);
30
                                                                                             74
                                                                                                    double c = side(p[2], p[0], q);
     double u21 = p2.x - p4.x;
                                                                                             75
31
                                                                                             76
                                                                                                    return a >= -EPSILON && b >= -EPSILON && c >= -EPSILON;
     double u31 = p3.x - p4.x;
32
33
     double u12 = p1.y - p4.y;
                                                                                             77
     double u22 = p2.y - p4.y;
                                                                                             78
                                                                                                } triange_pool[MAX_TRIS], *tot_triangles;
34
     double u32 = p3.y - p4.y;
                                                                                                void set_edge(Edge a, Edge b) {
35
                                                                                             79
36
     double u13 = sqr(p1.x) - sqr(p4.x) + sqr(p1.y) - sqr(p4.y);
                                                                                            80
                                                                                                  if (a.tri) a.tri->edge[a.side] = b;
     double u23 = sqr(p2.x) - sqr(p4.x) + sqr(p2.y) - sqr(p4.y);
                                                                                            81
                                                                                                  if (b.tri) b.tri->edge[b.side] = a;
37
     double u33 = sqr(p3.x) - sqr(p4.x) + sqr(p3.y) - sqr(p4.y);
                                                                                                  if (a.tri && b.tri) {
38
                                                                                            82
     double det = -u13*u22*u31 + u12*u23*u31 + u13*u21*u32 - u11*u23*u32 - u12*u21*u33
                                                                                                    assert(a.tri->p[(a.side+1)%3] == b.tri->p[(b.side+2)%3]);
39
                                                                                            83

→ + u11*u22*u33:

                                                                                            84
                                                                                                    assert(a.tri->p[(a.side+2)%3] == b.tri->p[(b.side+1)%3]);
     return det > EPSILON;
                                                                                            85
40
                                                                                            86
41
42 | double side(Point const& a, Point const& b, Point const& p) {
                                                                                            87
                                                                                                class Triangulation {
     return (b.x-a.x)*(p.y-a.y) - (b.y-a.y)*(p.x-a.x);
                                                                                            88
                                                                                                  public:
43
                                                                                            89
                                                                                                    Triangulation() {
44
                                                                                                      const double LOTS = 1e6;
                                                                                            90
45
   typedef int SideRef;
46
                                                                                             91
                                                                                                      the_root = new(tot_triangles++)
   struct Triangle;
                                                                                                        typedef Triangle* TriangleRef;
48
                                                                                            92
   struct Edge {
                                                                                                    ~Triangulation() {}
                                                                                            93
     TriangleRef tri;
                                                                                                    TriangleRef find(Point p) const {
                                                                                            94
50
     SideRef
                 side;
                                                                                            95
                                                                                                      return find(the_root,p);
51
     Edge() : tri(0), side(0) {}
                                                                                                    }
                                                                                            96
52
     Edge(TriangleRef tri, SideRef side) : tri(tri), side(side) {}
                                                                                                    void add_point(Point const& p) {
53
                                                                                            97
54|};
                                                                                            98
                                                                                                      add point(find(the root,p),p);
   struct Triangle {
                                                                                                    }
                                                                                            99
55
56
     Point p[3];
                                                                                                  private:
                                                                                           100
     Edge edge[3];
                                                                                                    TriangleRef the root;
                                                                                           101
57
     TriangleRef children[3];
                                                                                                    static TriangleRef find(TriangleRef root, Point const& p) {
58
                                                                                           102
                                                                                                      for(;;) {
59
     Triangle() {}
                                                                                           103
60
     Triangle(Point const& p0, Point const& p1, Point const& p2) {
                                                                                           104
                                                                                                        assert(root->contains(p));
61
       p[0] = p0; p[1] = p1; p[2] = p2;
                                                                                                        if (!root->has children()) {
                                                                                           105
62
       children[0] = children[1] = children[2] = 0;
                                                                                           106
                                                                                                          return root;
63
                                                                                                        } else {
                                                                                           107
```

```
108
              int flag = true:
              for (int i = 0; i < 3 && root->children[i]; ++i) {
109
                if (root->children[i]->contains(p)) {
110
111
                  root = root->children[i];
                  break;
112
                }
113
114
115
              assert(flag&&"point not found");
116
117
          }
118
        void add_point(TriangleRef root, Point const& p) {
119
          TriangleRef tab,tbc,tca;
120
          /* split it into three triangles */
121
          tab = new(tot_triangles++) Triangle(root->p[0], root->p[1], p);
122
          tbc = new(tot_triangles++) Triangle(root->p[1], root->p[2], p);
123
          tca = new(tot_triangles++) Triangle(root->p[2], root->p[0], p);
124
          set edge(Edge(tab,0), Edge(tbc,1));
125
126
          set_edge(Edge(tbc,0), Edge(tca,1));
127
          set_edge(Edge(tca,0), Edge(tab,1));
128
          set_edge(Edge(tab,2), root->edge[2]);
129
          set_edge(Edge(tbc,2), root->edge[0]);
          set edge(Edge(tca,2), root->edge[1]);
130
          root->children[0] = tab;
131
          root->children[1] = tbc;
132
          root->children[2] = tca;
133
          flip(tab,2);
134
          flip(tbc,2);
135
136
          flip(tca,2);
137
138
        void flip(TriangleRef tri, SideRef pi) {
          TriangleRef trj = tri->edge[pi].tri;
139
140
          int pj = tri->edge[pi].side;
141
          if (!trj) return;
          if (!in_circumcircle(tri->p[0],tri->p[1],tri->p[2],trj->p[pj])) return;
142
143
          assert(tri->p[(pi+2)%3] == trj->p[(pj+1)%3]);
          assert(tri->p[(pi+1)%3] == trj->p[(pj+2)%3]);
144
          /* flip edge between tri,trj */
145
          TriangleRef trk = new(tot triangles++) Triangle(tri->p[(pi+1)%3], trj->p[pj],
146

    tri->p[pi]);
147
          TriangleRef trl = new(tot_triangles++) Triangle(trj->p[(pj+1)%3], tri->p[pi],
            set edge(Edge(trk,0), Edge(trl,0));
148
          set_edge(Edge(trk,1), tri->edge[(pi+2)%3]);
149
          set_edge(Edge(trk,2), trj->edge[(pj+1)%3]);
150
```

```
set edge(Edge(trl,1), trj->edge[(pj+2)%3]);
151
152
          set edge(Edge(trl,2), tri->edge[(pi+1)%3]);
          tri->children[0] = trk; tri->children[1] = trl; tri->children[2] = 0;
153
154
          trj->children[0] = trk; trj->children[1] = trl; trj->children[2] = 0;
          flip(trk,1);
155
          flip(trk,2);
156
          flip(trl,1);
157
158
          flip(trl,2);
159
160 };
161
162 int n;
163 Point ps[N];
164
165
    void build()
166
167
      tot_triangles = triange_pool;
168
      cin >> n;
      for(int i = 0; i < n; ++ i) {
169
170
        int x, y;
171
        scanf("%d%d", &x, &y);
172
        ps[i].x = x; ps[i].y = y;
173
      random shuffle(ps, ps + n);
174
175
      Triangulation tri;
176
      for(int i = 0; i < n; ++ i) {
        tri.add_point(ps[i]);
177
178
179 }
180
181
    int main()
182 {
183
      build();
184
      return 0;
185 }
```

三维几何操作合并

```
8 // 平面法向量 : 平面上两个向量叉积
  9 // 点共平面 : 平面上一点与之的向量点积法向量为 0
10 // 点在线段 ( 直线 ) 上 : 共线且两边点积非正
11 // 点在三角形内 ( 不包含边界, 需再判断是与某条边共线 )
12 bool pointInTri(const Point3D &a, const Point3D &b, const Point3D &c, const Point3D
           → &p) {
          return sign(det(a - b, a - c).len() - det(p - a, p - b).len() - det(p - b, p -
13
               \rightarrow c).len() - det(p - c, p - a).len()) == 0;
14 | }
15 // 共平面的两点是否在这平面上一条直线的同侧
16 bool sameSide(const Point3D &a, const Point3D &b, const Point3D &p0, const Point3D
           → &p1) {
          return sign(dot(det(a - b, p0 - b), det(a - b, p1 - b))) > 0;
17
18 }
19 // 两点在平面同侧 : 点积法向量符号相同
20 // 两直线平行 / 垂直 : 同二维
21 // 平面平行 / 垂直 : 判断法向量
22 // 线面垂直 : 法向量和直线平行
23 // 判断空间线段是否相交 : 四点共面两线段不平行相互在异侧
24 // 线段和三角形是否相交 : 线段在三角形平面不同侧
           → 三角形任意两点在线段和第三点组成的平面的不同侧
25 // 求空间直线交点
26 Point3D intersection(const Point3D &a0, const Point3D &b0, const Point3D &a1, const
           → Point3D &b1) {
          double t = ((a0.x - a1.x) * (a1.y - b1.y) - (a0.y - a1.y) * (a1.x - b1.x)) /
               \hookrightarrow ((a0.x - b0.x) * (a1.y - b1.y) - (a0.y - b0.y) * (a1.x - b1.x));
28
          return a0 + (b0 - a0) * t;
29 | }
      // 求平面和直线的交点
31 Point3D intersection(const Point3D &a, const Point3D &b, const Point3D &c, const
           → Point3D &10, const Point3D &11) {
          Point3D p = pVec(a, b, c); // 平面法向量
          double t = (p.x * (a.x - 10.x) + p.y * (a.y - 10.y) + p.z * (a.z - 10.z)) / (p.x * (a.z - 10.z)) / (p.z - 10.z)) / (p.z - 10.z) / (p.z
33
               \rightarrow (11.x - 10.x) + p.y * (11.y - 10.y) + p.z * (11.z - 10.z));
          return 10 + (11 - 10) * t;
34
35 | }
36 | // 求平面交线 : 取不平行的一条直线的一个交点,以及法向量叉积得到直线方向
      // 点到直线距离 : 叉积得到三角形的面积除以底边
38 // 点到平面距离 : 点积法向量
39 // 直线间距离 : 平行时随便取一点求距离,否则又积方向向量得到方向点积计算长度
40 // 直线夹角 : 点积 平面夹角 : 法向量点积
41 // 三维向量旋转操作(绕向量 s 旋转 ang 角度),对于右手系 s 指向观察者时逆时针
42 // 矩阵版
43 | void rotate(const Point3D &s, double ang) {
          double 1 = s.len(), x = s.x / 1, y = s.y / 1, z = s.z / 1, sinA = sin(ang), cosA =

    cos(ang);
```

三维凸包

```
#define SIZE(X) (int(X.size()))
2 #define PI 3.14159265358979323846264338327950288
3 struct Point {
    Point cross(const Point &p) const
    { return Point(y * p.z - z * p.y, z * p.x - x * p.z, x * p.y - y * p.x); }
6 | \rinfo[1005]:
7 int mark[1005][1005],n, cnt;;
8 double mix(const Point &a, const Point &b, const Point &c)
g { return a.dot(b.cross(c)); }
10 double area(int a, int b, int c)
11 | { return ((info[b] - info[a]).cross(info[c] - info[a])).length(); }
12 double volume(int a, int b, int c, int d)
13 | { return mix(info[b] - info[a], info[c] - info[a], info[d] - info[a]); }
14 | struct Face {
    int a, b, c; Face() {}
15
    Face(int a, int b, int c): a(a), b(b), c(c) {}
16
17
     int &operator [](int k)
18
     { if (k == 0) return a; if (k == 1) return b; return c; }
19
   vector <Face> face;
   inline void insert(int a, int b, int c) { face.push back(Face(a, b, c)); }
   void add(int v) {
22
     vector <Face> tmp; int a, b, c; cnt++;
23
24
     for (int i = 0; i < SIZE(face); i++) {</pre>
25
       a = face[i][0]; b = face[i][1]; c = face[i][2];
26
       if (Sign(volume(v, a, b, c)) < 0)</pre>
       mark[a][b] = mark[b][a] = mark[b][c] = mark[c][b] = mark[c][a] = mark[a][c] =
27

    cnt;

28
       else tmp.push back(face[i]);
     } face = tmp;
20
     for (int i = 0; i < SIZE(tmp); i++) {</pre>
30
       a = face[i][0]; b = face[i][1]; c = face[i][2];
31
       if (mark[a][b] == cnt) insert(b, a, v);
32
```

```
if (mark[b][c] == cnt) insert(c, b, v);
33
       if (mark[c][a] == cnt) insert(a, c, v);
34
35 | }}
36 \mid int Find() {
     for (int i = 2; i < n; i++) {
37
38
       Point ndir = (info[0] - info[i]).cross(info[1] - info[i]);
       if (ndir == Point()) continue; swap(info[i], info[2]);
39
       for (int j = i + 1; j < n; j++) if (Sign(volume(0, 1, 2, j)) != 0) {
40
41
         swap(info[j], info[3]); insert(0, 1, 2); insert(0, 2, 1); return 1;
42 | } return 0; }
43 | int main() {
     for (; scanf("%d", &n) == 1; ) {
44
       for (int i = 0; i < n; i++) info[i].Input();</pre>
45
       sort(info, info + n); n = unique(info, info + n) - info;
46
       face.clear(); random_shuffle(info, info + n);
47
48
       if (Find()) { memset(mark, 0, sizeof(mark)); cnt = 0;
         for (int i = 3; i < n; i++) add(i); vector<Point> Ndir;
49
         for (int i = 0; i < SIZE(face); ++i) {</pre>
50
           Point p = (info[face[i][0]] - info[face[i][1]]).cross(
51
52
               info[face[i][2]] - info[face[i][1]]);
           p = p / p.length(); Ndir.push back(p);
53
         } sort(Ndir.begin(), Ndir.end());
54
         int ans = unique(Ndir.begin(), Ndir.end()) - Ndir.begin();
55
56
         printf("%d\n", ans);
       } else printf("1\n");
57
58 } }
59 // 求重心
60 double calcDist(const Point &p, int a, int b, int c)
61 | { return fabs(mix(info[a] - p, info[b] - p, info[c] - p) / area(a, b, c)); }
62 //compute the minimal distance of center of any faces
63 double findDist() { //compute center of mass
     double totalWeight = 0; Point center(.0, .0, .0);
64
     Point first = info[face[0][0]];
65
66
     for (int i = 0; i < SIZE(face); ++i) {</pre>
67
       Point p = (info[face[i][0]]+info[face[i][1]]+info[face[i][2]]+first)*.25;
68
       double weight = mix(info[face[i][0]] - first, info[face[i][1]]
69
           - first, info[face[i][2]] - first);
       totalWeight += weight; center = center + p * weight;
70
     } center = center / totalWeight;
71
72
     double res = 1e100; //compute distance
73
     for (int i = 0; i < SIZE(face); ++i)</pre>
       res = min(res, calcDist(center, face[i][0], face[i][1], face[i][2]));
74
       return res; }
75
```

凸包上快速询问

```
1
      给定凸包, \log n 内完成各种询问, 具体操作有:
      1. 判定一个点是否在凸包内
3
      2. 询问凸包外的点到凸包的两个切点
      3. 询问一个向量关于凸包的切点
      4. 询问一条直线和凸包的交点
      INF 为坐标范围,需要定义点类大于号
7
      改成实数只需修改 sign 函数,以及把 long long 改为 double 即可
      构造函数时传入凸包要求无重点,面积非空,以及 pair(x,v) 的最小点放在第一个
9
10
   #include <vector>
11
   #include <functional>
   using namespace std;
13
14
   const int INF = 1000000000;
15
16
17
   struct Convex
18
19
     int n;
     vector<Point> a;
20
     vector<Point> upper, lower;
21
22
     Convex(vector<Point> _a) : a(_a) {
23
      n = a.size();
24
      int ptr = 0;
25
      for(int i = 1; i < n; ++ i) if (a[ptr] < a[i]) ptr = i;
26
       for(int i = 0; i <= ptr; ++ i) lower.push_back(a[i]);</pre>
       for(int i = ptr; i < n; ++ i) upper.push_back(a[i]);</pre>
27
28
       upper.push_back(a[0]);
29
30
     int sign(long long x) {
       return x < 0 ? -1 : x > 0;
31
32
     pair<long long, int> get tangent(vector<Point> &convex, Point vec) {
33
       int l = 0, r = (int)convex.size() - 2;
34
      for(; l + 1 < r; ) {
35
36
        int mid = (1 + r) / 2;
        if (sign((convex[mid + 1] - convex[mid]).det(vec)) > 0) r = mid;
37
38
        else 1 = mid;
39
       return max(make pair(vec.det(convex[r]), r), make pair(vec.det(convex[0]), 0));
40
41
42
     void update_tangent(const Point &p, int id, int &i0, int &i1) {
       if ((a[i0] - p).det(a[id] - p) > 0) i0 = id;
       if ((a[i1] - p).det(a[id] - p) < 0) i1 = id;</pre>
```

```
45
46
     void binary search(int 1, int r, Point p, int &i0, int &i1) {
       if (1 == r) return;
47
48
       update tangent(p, 1 % n, i0, i1);
       int sl = sign((a[1 \% n] - p).det(a[(1 + 1) \% n] - p));
49
       for(; l + 1 < r; ) {
50
         int mid = (1 + r) / 2;
51
52
         int smid = sign((a[mid % n] - p).det(a[(mid + 1) % n] - p));
53
         if (smid == sl) l = mid;
         else r = mid;
54
       }
55
56
       update tangent(p, r % n, i0, i1);
57
58
     int binary_search(Point u, Point v, int l, int r) {
       int sl = sign((v - u).det(a[1 % n] - u));
59
60
       for(; l + 1 < r; ) {
61
         int mid = (1 + r) / 2;
62
         int smid = sign((v - u).det(a[mid % n] - u));
         if (smid == sl) l = mid;
63
         else r = mid;
64
65
66
       return 1 % n;
67
68
     // 判定点是否在凸包内,在边界返回 true
     bool contain(Point p) {
69
       if (p.x < lower[0].x || p.x > lower.back().x) return false;
70
       int id = lower_bound(lower.begin(), lower.end(), Point(p.x, -INF)) -
71
          → lower.begin();
       if (lower[id].x == p.x) {
72
         if (lower[id].y > p.y) return false;
73
       } else if ((lower[id - 1] - p).det(lower[id] - p) < 0) return false;</pre>
74
       id = lower_bound(upper.begin(), upper.end(), Point(p.x, INF), greater<Point>())
75
          → - upper.begin();
       if (upper[id].x == p.x) {
76
         if (upper[id].y < p.y) return false;</pre>
77
       } else if ((upper[id - 1] - p).det(upper[id] - p) < 0) return false;</pre>
78
       return true;
79
80
81
     // 求点 p 关于凸包的两个切点,如果在凸包外则有序返回编号,多解返回任意一个図否则返回
        \hookrightarrow false
     bool get tangent(Point p, int &i0, int &i1) {
82
83
       if (contain(p)) return false;
84
85
       int id = lower_bound(lower.begin(), lower.end(), p) - lower.begin();
86
       binary search(0, id, p, i0, i1);
```

```
87
        binary search(id, (int)lower.size(), p, i0, i1);
 88
        id = lower bound(upper.begin(), upper.end(), p, greater<Point>()) -
          → upper.begin():
 89
        binary search((int)lower.size() - 1, (int)lower.size() - 1 + id, p, i0, i1);
       binary search((int)lower.size() - 1 + id, (int)lower.size() - 1 +
 90
          91
       return true:
 92
      }
      // 求凸包上和向量 vec 叉积最大的点,返回编号,有多个返回任意一个
 93
      int get_tangent(Point vec) {
 94
       pair<long long, int> ret = get_tangent(upper, vec);
 95
 96
       ret.second = (ret.second + (int)lower.size() - 1) % n;
       ret = max(ret, get_tangent(lower, vec));
 97
 98
       return ret.second;
 99
100
     // 求凸包和直线 u,v 的交点,如果无严格相交返回 false 。如果有则是和(i,next(i))
        → 的交点,两个点无序,交在点上不确定返回两条线段之一。
      bool get intersection(Point u, Point v, int &i0, int &i1) {
101
       int p0 = get tangent(u - v), p1 = get tangent(v - u);
102
       if (sign((v - u).det(a[p0] - u)) * sign((v - u).det(a[p1] - u)) < 0) {
103
104
         if (p0 > p1) swap(p0, p1);
105
         i0 = binary search(u, v, p0, p1);
106
         i1 = binary search(u, v, p1, p0 + n);
         return true;
107
108
       } else {
109
         return false:
       }
110
     }
111
112 };
```

圆的面积模板 $(n^2 \log n)$

```
dRatio = ((a.r - b.r) * (a.r + b.r) / d2 + 1) / 2
14
15
           pRatio = sqr(-(d2 - sqr(a.r - b.r)) * (d2 - sqr(a.r + b.r)) / (d2 * d2 *
             \hookrightarrow 4));
16
     Point d = b.o - a.o, p = d.rotate(PI / 2),
         q0 = a.o + d * dRatio + p * pRatio,
17
18
         q1 = a.o + d * dRatio - p * pRatio;
     double ang0 = (q0 - a.o).ang(),
19
20
          ang1 = (q1 - a.o).ang();
21
     evt.push_back(Event(q1, ang1, 1));
     evt.push_back(Event(q0, ang0, -1));
22
     cnt += ang1 > ang0;
23
24
25
   bool issame(const Circle &a, const Circle &b) {
26
     return sign((a.o - b.o).len()) == 0 && sign(a.r - b.r) == 0;
27
28
29
   bool overlap(const Circle &a, const Circle &b) {
30
     return sign(a.r - b.r - (a.o - b.o).len()) >= 0;
31
32
33
   bool intersect(const Circle &a, const Circle &b) {
34
     return sign((a.o - b.o).len() - a.r - b.r) < 0;
35
36
   }
37
38 int C;
39 | Circle c[N];
   double area[N];
41
42
   void solve() {
     memset(area, 0, sizeof(double) * (C + 1));
43
     for (int i = 0; i < C; ++i) {
44
       int cnt = 1;
45
46
       vector<Event> evt;
       for (int j = 0; j < i; ++j) {
47
48
         if (issame(c[i], c[j])) {
           ++cnt;
49
         }
50
51
52
       for (int j = 0; j < C; ++j) {
         if (j != i && !issame(c[i], c[j]) && overlap(c[j], c[i])) {
53
           ++cnt;
54
55
56
       for (int j = 0; j < C; ++j) {
57
```

```
58 :
          if (j != i && !overlap(c[j], c[i]) && !overlap(c[i], c[j]) && intersect(c[i],
             \hookrightarrow c[j])) {
            addEvent(c[i], c[j], evt, cnt);
59
60
          }
61
        }
62
        if (evt.size() == 0) {
          area[cnt] += PI * c[i].r * c[i].r;
63
64
        } else {
65
          sort(evt.begin(), evt.end());
66
          evt.push_back(evt.front());
67
          for (int j = 0; j + 1 < (int)evt.size(); ++j) {</pre>
68
            cnt += evt[j].delta;
69
            area[cnt] += det(evt[j].p, evt[j + 1].p) / 2;
70
            double ang = evt[j + 1].ang - evt[j].ang;
71
            if (ang < 0) {
              ang += PI * 2;
72
73
            area[cnt] += ang * c[i].r * c[i].r / 2 - sin(ang) * c[i].r * c[i].r / 2;
74
75
76
        }
77
78
```

三角形的心

```
1 | Point inCenter(const Point &A, const Point &B, const Point &C) { // 内心
     double a = (B - C).len(), b = (C - A).len(), c = (A - B).len(),
       s = fabs(det(B - A, C - A)),
 3
       r = s / p;
     return (A * a + B * b + C * c) / (a + b + c);
 6
   |Point circumCenter(const Point &a, const Point &b, const Point &c) { // 外心
     Point bb = b - a, cc = c - a;
     double db = bb.len2(), dc = cc.len2(), d = 2 * det(bb, cc);
11
     return a - Point(bb.y * dc - cc.y * db, cc.x * db - bb.x * dc) / d;
12
13
   Point othroCenter(const Point &a, const Point &b, const Point &c) { // 垂心
     Point ba = b - a, ca = c - a, bc = b - c;
15
16
     double Y = ba.y * ca.y * bc.y,
          A = ca.x * ba.y - ba.x * ca.y,
17
18
          x0 = (Y + ca.x * ba.y * b.x - ba.x * ca.y * c.x) / A,
          y0 = -ba.x * (x0 - c.x) / ba.y + ca.y;
19
     return Point(x0, y0);
20
21
```

最小覆盖球

```
int npoint, nouter; Tpoint pt[200000], outer[4],res; double radius,tmp;
2 void ball() {
     Tpoint q[3]; double m[3][3], sol[3], L[3], det;
     int i,j; res.x = res.y = res.z = radius = 0;
     switch ( nouter ) {
5
     case 1: res=outer[0]; break;
     case 2: res=(outer[0]+outer[1])/2; radius=dist2(res, outer[0]); break;
7
     case 3:
9
       for (i=0; i<2; ++i) q[i]=outer[i+1]-outer[0];</pre>
10
       for (i=0; i<2; ++i) for(j=0; j<2; ++j) m[i][j]=dot(q[i], q[j])*2;
       for (i=0; i<2; ++i) sol[i]=dot(q[i], q[i]);</pre>
11
       if (fabs(det=m[0][0]*m[1][1]-m[0][1]*m[1][0])<eps) return;</pre>
12
       L[0]=(sol[0]*m[1][1]-sol[1]*m[0][1])/det;
13
14
       L[1]=(sol[1]*m[0][0]-sol[0]*m[1][0])/det;
       res=outer[0]+q[0]*L[0]+q[1]*L[1];
15
16
       radius=dist2(res, outer[0]);
17
       break:
18
     case 4:
19
       for (i=0; i<3; ++i) q[i]=outer[i+1]-outer[0], sol[i]=dot(q[i], q[i]);</pre>
       for (i=0;i<3;++i) for(j=0;j<3;++j) m[i][j]=dot(q[i],q[j])*2;
20
       det= m[0][0]*m[1][1]*m[2][2]
21
22
       + m[0][1]*m[1][2]*m[2][0]
       + m[0][2]*m[2][1]*m[1][0]
23
24
       - m[0][2]*m[1][1]*m[2][0]
       - m[0][1]*m[1][0]*m[2][2]
25
26
       - m[0][0]*m[1][2]*m[2][1];
27
       if ( fabs(det)<eps ) return;</pre>
28
       for (j=0; j<3; ++j) {
29
         for (i=0; i<3; ++i) m[i][j]=sol[i];
30
         L[j]=(m[0][0]*m[1][1]*m[2][2]
         + m[0][1]*m[1][2]*m[2][0]
31
32
         + m[0][2]*m[2][1]*m[1][0]
         - m[0][2]*m[1][1]*m[2][0]
33
         - m[0][1]*m[1][0]*m[2][2]
34
35
         - m[0][0]*m[1][2]*m[2][1]
36
         ) / det:
         for (i=0; i<3; ++i) m[i][j]=dot(q[i], q[j])*2;
37
38
       } res=outer[0];
       for (i=0; i<3; ++i ) res = res + q[i] * L[i];</pre>
39
       radius=dist2(res, outer[0]);
40
41 | }}
42 | void minball(int n) { ball();
     if ( nouter<4 ) for (int i=0; i<n; ++i)</pre>
     if (dist2(res, pt[i])-radius>eps) {
```

```
outer[nouter++]=pt[i]; minball(i); --nouter;
45
46
       if (i>0) { Tpoint Tt = pt[i];
47
         memmove(&pt[1], &pt[0], sizeof(Tpoint)*i); pt[0]=Tt;
48 }}}
   int main0(){
49
     scanf("%d", &npoint);
50
     for (int i=0;i<npoint;i++) scanf("%1f%1f%1f",&pt[i].x,&pt[i].y,&pt[i].z);</pre>
51
52
     random_shuffle(pt,pt+npoint); radius=-1;
53
     for (int i=0;i<npoint;i++) if (dist2(res,pt[i])-radius>eps)
       nouter=1, outer[0]=pt[i], minball(i);
54
     printf("%.5f\n",sqrt(radius));
55
56
```

经纬度求球面最短距离

```
1 //lati 为纬度 longi 为经度 R 为半径
2 double Dist(double lati1,double longi1,double lati2,double longi2,double R) {
3 double pi=acos(-1.0); lati1*=pi/180,longi1*=pi/180,lati2*=pi/180,longi2*=pi/180;
4 double x1=cos(lati1)*sin(longi1),y1=cos(lati1)*cos(longi1),z1=sin(lati1);
5 double x2=cos(lati2)*sin(longi2),y2=cos(lati2)*cos(longi2),z2=sin(lati2);
6 double theta=acos(x1*x2+y1*y2+z1*z2); return(R*theta);
7 }
```

长方体表面两点最短距离

```
1 int r;
 2 | void turn(int i, int j, int x, int y, int z, int x0, int y0, int L, int W, int H) {
    if (z==0) { int R = x*x+y*y; if (R< r) r=R;
     } else {
 4
       if(i)=0 \& i < 2) turn(i+1, j, x0+L+z, y, x0+L-x, x0+L, y0, H, W, L);
       if(j \ge 0 \&\& j < 2) turn(i, j+1, x, y0+W+z, y0+W-y, x0, y0+W, L, H, W);
       if(i <= 0 \&\& i >- 2) turn(i-1, j, x0-z, y, x-x0, x0-H, y0, H, W, L);
       if(j<=0 && j>-2) turn(i, j-1, x, y0-z, y-y0, x0, y0-H, L, H, W);
9 | }}
10 int main(){
     int L, H, W, x1, y1, z1, x2, y2, z2;
     cin >> L >> W >> H >> x1 >> y1 >> z1 >> x2 >> y2 >> z2;
     if (z1!=0 \&\& z1!=H) if (y1==0 || y1==W)
13
14
           swap(y1,z1), std::swap(y2,z2), std::swap(W,H);
15
     else swap(x1,z1), std::swap(x2,z2), std::swap(L,H);
16
     if (z1==H) z1=0, z2=H-z2;
     r=0x3fffffff; turn(0,0,x2-x1,y2-y1,z2,-x1,-y1,L,W,H);
17
18
     cout<<r<<endl; return 0;</pre>
19 }
```

最大团

```
1 // Super Fast Maximum Clique
 2 // To Build Graph: Maxclique(Edges, Number of Nodes)
 3 // To Get Answer: mcqdyn(AnswerNodes Index Array, AnswserLength)
   typedef bool BB[N];
   struct Maxclique {
     const BB* e; int pk, level; const float Tlimit;
     struct Vertex{ int i, d; Vertex(int i):i(i),d(0){} };
 8
     typedef vector<Vertex> Vertices; typedef vector<int> ColorClass;
     Vertices V; vector<ColorClass> C; ColorClass QMAX, Q;
 9
     static bool desc_degree(const Vertex &vi, const Vertex &vj){
10
       return vi.d > vj.d;
11
12
13
     void init colors(Vertices &v){
       const int max degree = v[0].d;
14
       for(int i = 0; i < (int)v.size(); i++) v[i].d = min(i, max degree) + 1;
15
16
     void set_degrees(Vertices &v){
17
18
       for(int i = 0, j; i < (int)v.size(); i++)</pre>
19
         for(v[i].d = j = 0; j < int(v.size()); j++)
           v[i].d += e[v[i].i][v[j].i];
20
21
22
     struct StepCount{ int i1, i2; StepCount():i1(0),i2(0){} };
      vector<StepCount> S;
23
24
      bool cut1(const int pi, const ColorClass &A){
       for(int i = 0; i < (int)A.size(); i++) if (e[pi][A[i]]) return true;
25
26
       return false;
27
28
     void cut2(const Vertices &A, Vertices &B){
29
       for(int i = 0; i < (int)A.size() - 1; i++)
         if(e[A.back().i][A[i].i])
30
           B.push_back(A[i].i);
31
32
     void color sort(Vertices &R){
33
       int j = 0, maxno = 1, min_k = max((int)QMAX.size() - (int)Q.size() + 1, 1);
34
       C[1].clear(), C[2].clear();
35
36
       for(int i = 0; i < (int)R.size(); i++) {</pre>
         int pi = R[i].i, k = 1;
37
38
         while(cut1(pi, C[k])) k++;
         if(k > maxno) maxno = k, C[maxno + 1].clear();
39
40
         C[k].push back(pi);
         if(k < min_k) R[j++].i = pi;</pre>
41
42
       if(j > 0) R[j - 1].d = 0;
43
       for(int k = min_k; k <= maxno; k++)</pre>
44
```

```
for(int i = 0; i < (int)C[k].size(); i++)</pre>
45
46
           R[j].i = C[k][i], R[j++].d = k;
47
48
     void expand dyn(Vertices &R){// diff -> diff with no dyn
       S[level].i1 = S[level].i1 + S[level - 1].i1 - S[level].i2;//diff
49
       S[level].i2 = S[level - 1].i1;//diff
50
       while((int)R.size()) {
51
         if((int)Q.size() + R.back().d > (int)QMAX.size()){
52
           Q.push_back(R.back().i); Vertices Rp; cut2(R, Rp);
53
           if((int)Rp.size()){
54
             if((float)S[level].i1 / ++pk < Tlimit) degree_sort(Rp);//diff</pre>
55
56
              color_sort(Rp);
             S[level].i1++, level++;//diff
57
58
             expand_dyn(Rp);
             level--;//diff
59
60
           }
61
           else if((int)Q.size() > (int)QMAX.size()) QMAX = Q;
62
           Q.pop back();
63
         }
64
         else return;
65
         R.pop_back();
66
       }
67
68
     void mcqdyn(int* maxclique, int &sz){
69
        set degrees(V); sort(V.begin(), V.end(), desc degree); init colors(V);
       for(int i = 0; i < (int)V.size() + 1; i++)S[i].i1 = S[i].i2 = 0;
70
71
       expand_dyn(V); sz = (int)QMAX.size();
72
       for(int i = 0; i < (int)QMAX.size(); i++) maxclique[i] = QMAX[i];</pre>
73
     void degree_sort(Vertices &R){
74
       set_degrees(R); sort(R.begin(), R.end(), desc_degree);
75
76
     Maxclique(const BB* conn, const int sz, const float tt = 0.025) \
77
78
      : pk(0), level(1), Tlimit(tt){
       for(int i = 0; i < sz; i++) V.push_back(Vertex(i));</pre>
79
80
       e = conn, C.resize(sz + 1), S.resize(sz + 1);
81
82 };
```

极大团计数

```
1 //Bool g[][] 为图的邻接矩阵,图点的标号由 1 至 n
2 void dfs(int size){
3    int i, j, k, t, cnt, best = 0;
4    if (ne[size]==ce[size]){    if (ce[size]==0) ++ans; return; }
5    for (t=0, i=1; i<=ne[size]; ++i) {
```

```
for (cnt=0, j=ne[size]+1; j<=ce[size]; ++j)</pre>
        if (!g[list[size][i]][list[size][j]]) ++cnt;
 8
        if (t==0 || cnt<best) t=i, best=cnt;</pre>
 9
      } if (t && best<=0) return;</pre>
      for (k=ne[size]+1; k<=ce[size]; ++k) {</pre>
10
        if (t>0){ for (i=k; i<=ce[size]; ++i)
11
12
            if (!g[list[size][t]][list[size][i]]) break;
          swap(list[size][k], list[size][i]);
13
        } i=list[size][k]; ne[size+1]=ce[size+1]=0;
14
        for (j=1; j<k; ++j)if (g[i][list[size][j]])</pre>
15
16
            list[size+1][++ne[size+1]]=list[size][j];
        for (ce[size+1]=ne[size+1], j=k+1; j<=ce[size]; ++j)</pre>
17
18
        if (g[i][list[size][j]]) list[size+1][++ce[size+1]]=list[size][j];
19
        dfs(size+1); ++ne[size]; --best;
        for (j=k+1, cnt=0; j<=ce[size]; ++j) if (!g[i][list[size][j]]) ++cnt;</pre>
20
        if (t==0 || cnt<best) t=k, best=cnt;</pre>
^{21}
        if (t && best<=0) break;
22
23 | }}
   void work(){
24
25
      ne[0]=0; ce[0]=0;
26
     for (int i=1; i<=n; ++i) list[0][++ce[0]]=i;
27
      ans=0; dfs(0);
28 }
```

KM

```
// 最小匹配, 自带初始化 n <= m 方案存在 p[] 中
2
   const int N = 105;
   const int INF = 10000000000; // 严格大于最大边权
6
   int n, m, a[N][N];
   int u[N], v[N], p[N], fa[N];
10
11
   int minv[N];
12
   bool used[N];
13
14
   int km() {
15
16
     for (int i = 0; i < n; ++i) {
       u[i] = 0;
17
18
     for (int i = 0; i <= m; ++i) {
19
       v[i] = 0;
20
```

```
p[i] = n;
21
22
     for (int i = 0; i < n; ++i) {
23
24
       p[m] = i;
       int j0 = m;
25
26
       for (int j = 0; j <= m; ++j) {
27
         minv[j] = INF;
28
         used[j] = false;
29
30
       do {
         used[j0] = true;
31
         int i0 = p[j0], delta = INF, j1;
32
         for (int j = 0; j < m; ++j) {
33
34
           if (!used[j]) {
              int cur = a[i0][j] - u[i0] - v[j];
35
36
              if (cur < minv[j]) {</pre>
                minv[j] = cur;
37
38
                fa[j] = j0;
39
40
              if (minv[j] < delta) {</pre>
                delta = minv[j];
41
                j1 = j;
42
43
           }
44
45
46
         for (int j = 0; j <= m; ++j) {
           if (used[j]) {
47
48
              u[p[j]] += delta;
              v[j] -= delta;
49
50
           } else {
              minv[j] -= delta;
51
           }
52
         }
53
         j0 = j1;
54
       } while (p[j0] != n);
55
56
       do {
         int j1 = fa[j0];
57
58
         p[j0] = p[j1];
         j0 = j1;
59
60
       } while (j0 != m);
61
62
     return -v[m];
63
```

最小树形图

```
namespace LIUZHU{
     const int MAXN;
     int from [MAXN + 10][MAXN * 2 + 10];
     int edge[MAXN + 10][MAXN * 2 + 10];
     int sel[MAXN * 2 + 10], fa[MAXN * 2 + 10];
      int vis[MAXN * 2 + 10];
     const int INF;// INF >= sum( W_ij )
     int getfa(int x){
       if(x == fa[x]) return x;
10
       return fa[x] = getfa(fa[x]);
11
12
13
     void liuzhu(){ // 1-base: root is 1, answer = (sel[i], i) for i in [2..n]
       fa[1] = 1;
14
15
       for(int i = 2; i <= n; ++i){
16
         sel[i] = 1;
         fa[i] = i;
17
18
         for(int j = 1; j <= n; ++j) if(fa[j] != i){
19
           from[j][i] = i;
           if(edge[sel[i]][i] > edge[j][i]) sel[i] = j;
20
21
22
       int limit = n;
23
24
       while(1){
         int prelimit = limit;
25
26
         memset(vis, 0, sizeof(vis));
         vis[1] = 1;
27
28
         for(int i = 2; i <= prelimit; ++i) if(fa[i] == i && !vis[i]){</pre>
29
           int j = i;
           while(!vis[j]){
30
              vis[j] = i;
31
             j = getfa(sel[j]);
32
33
           if(j == 1 || vis[j] != i) continue;
34
35
           vector<int> C;
36
           int k = j;
37
38
              C.push_back(k);
              k = getfa(sel[k]);
39
40
           }while(k != j);
           ++limit;
41
           for(int i = 1; i <= n; ++i){
42
              edge[i][limit] = INF;
43
              from[i][limit] = limit;
44
```

```
45
46
            fa[limit] = vis[limit] = limit;
            for(int i = 0; i < int(C.size()); ++i){</pre>
47
48
              int x = C[i];
              fa[x] = limit;
49
50
              for(int j = 1; j <= n; ++j){
                if(edge[j][x] != INF && edge[j][limit] > edge[j][x] - edge[sel[x]][x]){
51
                  edge[j][limit] = edge[j][x] - edge[sel[x]][x];
52
                  from[j][limit] = x;
53
                }
54
              }
55
56
            for(int j = 1; j <= n; ++j) if(getfa(j) == limit){</pre>
57
58
              edge[j][limit] = INF;
59
60
            sel[limit] = 1;
61
            for(int j = 1; j <= n; ++j){
62
              if(edge[sel[limit]][limit] > edge[j][limit]){
63
                sel[limit] = j;
64
             }
65
66
         if(prelimit == limit) break;
67
68
69
       for(int i = limit; i > 1; --i){
         sel[from[sel[i]][i]] = sel[i];
70
71
7^2
73 | }
```

无向图最小割

```
int cost[maxn][maxn],seq[maxn],len[maxn],n,m,pop,ans;
bool used[maxn];
void Init(){
   int i,j,a,b,c;
   for(i=0;i<n;i++) for(j=0;j<n;j++) cost[i][j]=0;
   for(i=0;i<m;i++){
      scanf("%d %d %d",&a,&b,&c); cost[a][b]+=c; cost[b][a]+=c;
   }
   pop=n; for(i=0;i<n;i++) seq[i]=i;
}
void Work(){
   ans=inf; int i,j,k,l,mm,sum,pk;
   while(pop > 1){
      for(i=1;i<pop;i++) used[seq[i]]=0; used[seq[0]]=1;</pre>
```

```
for(i=1;i<pop;i++) len[seq[i]]=cost[seq[0]][seq[i]];</pre>
15
16
        pk=0: mm=-inf: k=-1:
17
        for(i=1;i<pop;i++) if(len[seq[i]] > mm){ mm=len[seq[i]]; k=i; }
18
        for(i=1;i<pop;i++){</pre>
          used[seq[l=k]]=1;
19
          if(i==pop-2) pk=k;
20
          if(i==pop-1) break;
21
22
          mm=-inf:
23
          for(j=1;j<pop;j++) if(!used[seq[j]])</pre>
            if((len[seq[j]]+=cost[seq[1]][seq[j]]) > mm)
24
              mm=len[seq[j]], k=j;
25
26
       }
27
       sum=0;
28
        for(i=0;i<pop;i++) if(i != k) sum+=cost[seq[k]][seq[i]];</pre>
       ans=min(ans,sum);
29
        for(i=0;i<pop;i++)</pre>
30
          cost[seq[k]][seq[i]]=cost[seq[i]][seq[k]]+=cost[seq[pk]][seq[i]];
31
32
       seq[pk]=seq[--pop];
33
34
     printf("%d\n",ans);
35 | }
```

带花树

```
1 vector<int> link[maxn];
   int n,match[maxn],Queue[maxn],head,tail;
3 int pred[maxn],base[maxn],start,finish,newbase;
   bool InQueue[maxn],InBlossom[maxn];
   void push(int u){ Queue[tail++]=u;InQueue[u]=true; }
   int pop(){ return Queue[head++]; }
   int FindCommonAncestor(int u,int v){
8
     bool InPath[maxn];
     for(int i=0;i<n;i++) InPath[i]=0;</pre>
     while(true){ u=base[u];InPath[u]=true;if(u==start) break;u=pred[match[u]]; }
10
     while(true){ v=base[v];if(InPath[v]) break;v=pred[match[v]]; }
11
     return v;
12
13
   void ResetTrace(int u){
14
     int v:
15
16
     while(base[u]!=newbase){
       v=match[u];
17
18
       InBlossom[base[u]]=InBlossom[base[v]]=true;
19
       u=pred[v];
       if(base[u]!=newbase) pred[u]=v;
20
21
22 }
```

```
void BlossomContract(int u,int v){
      newbase=FindCommonAncestor(u,v);
24
25
     for (int i=0;i<n;i++)</pre>
26
     InBlossom[i]=0;
     ResetTrace(u);ResetTrace(v);
27
28
     if(base[u]!=newbase) pred[u]=v;
29
     if(base[v]!=newbase) pred[v]=u;
30
     for(int i=0;i<n;++i)</pre>
31
     if(InBlossom[base[i]]){
32
       base[i]=newbase;
       if(!InQueue[i]) push(i);
33
34
35
   bool FindAugmentingPath(int u){
36
     bool found=false;
37
38
     for(int i=0;i<n;++i) pred[i]=-1,base[i]=i;</pre>
     for (int i=0;i<n;i++) InQueue[i]=0;</pre>
39
     start=u;finish=-1; head=tail=0; push(start);
40
      while(head<tail){</pre>
41
42
       int u=pop();
       for(int i=link[u].size()-1;i>=0;i--){
43
         int v=link[u][i];
44
         if(base[u]!=base[v]&&match[u]!=v)
45
46
           if(v==start||(match[v]>=0&&pred[match[v]]>=0))
              BlossomContract(u,v);
47
48
            else if(pred[v]==-1){
              pred[v]=u;
49
              if(match[v]>=0) push(match[v]);
50
              else{ finish=v; return true; }
51
           }
52
       }
53
54
55
     return found;
56
    void AugmentPath(){
57
58
     int u=finish,v,w;
     while(u>=0){ v=pred[u];w=match[v];match[v]=u;match[u]=v;u=w; }
59
60
   void FindMaxMatching(){
     for(int i=0;i<n;++i) match[i]=-1;</pre>
62
     for(int i=0;i<n;++i) if(match[i]==-1) if(FindAugmentingPath(i)) AugmentPath();</pre>
64 }
```

动态最小生成树

```
/* 动态最小生成树 Q(logQ)^2
     (qx[i],qy[i]) 表示将编号为 qx[i] 的边的权值改为 qy[i]
     删除一条边相当于将其权值改为 ∞
 3
     加入一条边相当于将其权值从 ∞ 变成某个值 */
   const int qsize=maxm+3*maxq;
 5
   int x[qsize],y[qsize],z[qsize], qx[maxq],qy[maxq],n,m,Q;
   void init(){
 8
     scanf("%d%d",&n,&m);
     for(int i=0;i<m;i++) scanf("%d%d%d",x+i,y+i,z+i);</pre>
 9
     scanf("%d",&Q);
10
     for(int i=0;i<Q;i++){ scanf("%d%d",qx+i,qy+i); qx[i]--; }</pre>
11
12 }
13 | int a[maxn],*tz;
14 int find(int x){
15
     int root=x; while(a[root]) root=a[root];
16
     int next; while(next=a[x]){ a[x]=root; x=next; }
     return root;
17
18 }
   inline bool cmp(const int &a,const int &b){ return tz[a]<tz[b]; }
   int kx[maxn],ky[maxn],kt, vd[maxn],id[maxm], app[maxm];
20
   bool extra[maxm];
21
   void solve(int *qx,int *qy,int Q,int n,int *x,int *y,int *z,int m,long long ans){
22
     if(Q==1){
23
24
       for(int i=1;i<=n;i++) a[i]=0;
       z[qx[0]]=qy[0];
25
26
       for(int i=0;i<m;i++) id[i]=i;tz=z;</pre>
       sort(id,id+m,cmp); int ri,rj;
27
28
       for(int i=0;i<m;i++){</pre>
29
         ri=find(x[id[i]]); rj=find(y[id[i]]);
         if(ri!=rj){ ans+=z[id[i]]; a[ri]=rj; }
30
31
       printf("%I64d\n",ans);
32
33
       return;
34
     int ri,rj;
35
36
     //contract
     kt=0;
37
38
     for(int i=1;i<=n;i++) a[i]=0;</pre>
     for(int i=0;i<Q;i++){</pre>
39
40
       ri=find(x[qx[i]]); rj=find(y[qx[i]]); if(ri!=rj) a[ri]=rj;
41
     int tm=0;
42
     for(int i=0;i<m;i++) extra[i]=true;</pre>
43
     for(int i=0;i<Q;i++) extra[ qx[i] ]=false;</pre>
44
```

```
for(int i=0;i<m;i++) if(extra[i]) id[tm++]=i;</pre>
45
46
     tz=z; sort(id,id+tm,cmp);
     for(int i=0;i<tm;i++){</pre>
47
48
       ri=find(x[id[i]]); rj=find(y[id[i]]);
       if(ri!=rj){
49
         a[ri]=rj; ans += z[id[i]];
50
         kx[kt]=x[id[i]]; ky[kt]=y[id[i]]; kt++;
51
       }
52
53
     for(int i=1;i<=n;i++) a[i]=0;
54
     for(int i=0;i<kt;i++) a[ find(kx[i]) ]=find(ky[i]);</pre>
55
56
     int n2=0;
     for(int i=1;i<=n;i++) if(a[i]==0)
57
58
     vd[i]=++n2;
     for(int i=1;i<=n;i++) if(a[i])</pre>
59
60
     vd[i]=vd[find(i)];
61
     int m2=0, *Nx=x+m, *Ny=y+m, *Nz=z+m;
     for(int i=0;i<m;i++) app[i]=-1;</pre>
62
63
     for(int i=0;i<Q;i++) if(app[qx[i]]==-1){</pre>
64
       Nx[m2]=vd[x[qx[i]];Ny[m2]=vd[y[qx[i]];Nz[m2]=z[qx[i]];
65
       app[qx[i]]=m2; m2++;
66
67
     for(int i=0;i<0;i++){ z[qx[i]]=qy[i]; qx[i]=app[qx[i]]; }
68
     for(int i=1;i<=n2;i++) a[i]=0;</pre>
69
     for(int i=0;i<tm;i++){</pre>
       ri=find(vd[ x[id[i]] ]); rj=find(vd[ y[id[i]] ]);
70
71
       if(ri!=rj){
72
         a[ri]=rj; Nx[m2]=vd[ x[id[i]] ];
         Ny[m2]=vd[ y[id[i]] ]; Nz[m2]=z[id[i]]; m2++;
73
       }
74
75
76
     int mid=0/2;
     solve(qx,qy,mid,n2,Nx,Ny,Nz,m2,ans);
77
78
     solve(qx+mid,qy+mid,Q-mid,n2,Nx,Ny,Nz,m2,ans);
79
   void work(){ if(Q) solve(qx,qy,Q,n,x,y,z,m,0); }
81 | int main(){init(); work(); return 0; }
```

Hopcroft

```
int from[1010],wh[1010],g[1010];
int num[100010],nxt[100010],tot;
int n,m,ans,h,t,q[1010],dx[1010],dy[1010];
bool bfs(){
bool ret=false;
h=0;t=0;
```

```
for(int i=0;i<n;i++) if(wh[i]==-1) t++, q[t]=i;</pre>
8
     memset(dx,0,sizeof(dx)), memset(dy,0,sizeof(dy));
     while(h++<t){</pre>
10
        for(int i=g[q[h]];i!=0;i=nxt[i])
         if(dy[num[i]]==0){
11
            dy[num[i]]=dx[q[h]]+1;
12
           if(from[num[i]]==-1) ret=true;
13
            else{
14
15
              dx[from[num[i]]]=dx[q[h]]+2;
16
              q[++t]=from[num[i]];
17
18
         }
19
20
     return ret;
^{21}
   bool dfs(int x){
^{22}
      for(int i=g[x];i!=0;i=nxt[i]){
23
       if(dy[num[i]]==dx[x]+1){
24
         dy[num[i]]=0;
25
         if(from[num[i]]==-1||dfs(from[num[i]])){
26
            wh[x]=num[i];from[num[i]]=x;return true;
27
         }
28
29
30
31
     return false;
32
   void hopcroft(){
33
     memset(from,-1,sizeof(from)), memset(wh,-1,sizeof(wh));
34
     while(bfs())
35
36
       for(int i=0;i<n;i++)</pre>
         if(wh[i]==-1&&dfs(i)) ans++;
37
38 }
   void insert(int x,int y){ tot++;num[tot]=y;nxt[tot]=g[x];g[x]=tot; }
   int main(){
40
     while(scanf("%d %d",&n,&m)==2){
41
42
        tot=0; memset(g,0,sizeof(g));
        for(int i=0;i<n;i++){</pre>
43
         int x; scanf("%d",&x);
44
         for(int j=0;j<x;j++){</pre>
45
46
           int y; scanf("%d",&y);
           y--; insert(i,y);
47
48
         }
49
        ans=0; hopcroft(); printf("%d\n",ans);
50
51
```

```
52 }
```

素数判定

```
int strong_pseudo_primetest(long long n,int base) {
       long long n2=n-1,res;
3
       int s=0;
4
       while(n2\%2==0) n2>>=1,s++;
5
       res=powmod(base,n2,n);
6
       if((res==1)||(res==n-1)) return 1;
       s--;
8
       while(s>=0) {
9
           res=mulmod(res,res,n);
           if(res==n-1) return 1;
10
11
           s--;
12
13
       return 0; // n is not a strong pseudo prime
14 }
   int isprime(long long n) {
15
16
     static LL testNum[]={2,3,5,7,11,13,17,19,23,29,31,37};
     static LL lim[]={4,0,1373653LL,25326001LL,25000000000LL,2152302898747LL, \
17
     3474749660383LL,341550071728321LL,0,0,0,0);
18
     if(n<2||n==3215031751LL) return 0;
19
     for(int i=0;i<12;++i){
20
       if(n<lim[i]) return 1;</pre>
21
       if(strong_pseudo_primetest(n,testNum[i])==0) return 0;
22
23
24
     return 1;
25
```

启发式分解

```
1 int ansn; LL ans[1000];
   LL func(LL x,LL n){ return(mod_mul(x,x,n)+1)%n; }
3 LL Pollard(LL n){
     LL i,x,y,p;
     if(Rabin_Miller(n)) return n;
     if(!(n&1)) return 2;
     for(i=1;i<20;i++){
8
       x=i; y=func(x,n); p=gcd(y-x,n);
       while(p==1) {x=func(x,n); y=func(func(y,n),n); p=gcd((y-x+n)%n,n)%n;}
       if(p==0||p==n) continue;
10
11
       return p;
12
13
   void factor(LL n){
     LL x;
15
```

二次剩余

```
void calcH(int &t, int &h, const int p) {
     int tmp = p - 1; for (t = 0; (tmp & 1) == 0; tmp /= 2) t++; h = tmp;
 3 | }
   // solve equation x^2 \mod p = a
   bool solve(int a, int p, int &x, int &y) {
     srand(19920225);
     if (p == 2) \{ x = y = 1; return true; \}
     int p2 = p / 2, tmp = power(a, p2, p);
     if (tmp == p - 1) return false;
     if ((p + 1) \% 4 == 0) {
10
       x = power(a, (p + 1) / 4, p); y = p - x; return true;
11
     } else {
12
       int t, h, b, pb; calcH(t, h, p);
13
       if (t >= 2) {
14
         do \{b = rand() \% (p - 2) + 2;
15
16
         } while (power(b, p / 2, p) != p - 1);
         pb = power(b, h, p);
17
18
       } int s = power(a, h / 2, p);
       for (int step = 2; step <= t; step++) {</pre>
19
         int ss = (((long long)(s * s) % p) * a) % p;
20
         for (int i = 0; i < t - step; i++) ss = ((long long)ss * ss) % p;
21
22
         if (ss + 1 == p) s = (s * pb) % p; pb = ((long long)pb * pb) % p;
       x = ((long long)s * a) % p; y = p - x;
23
     } return true;
24
25 | }
```

Pell 方程

```
1 ULL A,B,p[maxn],q[maxn],a[maxn],g[maxn],h[maxn];
2 | int main() {
     for (int test=1, n;scanf("%d",&n) && n;++test) {
       printf("Case %d: ",test);
4
       if (fabs(sqrt(n)-floor(sqrt(n)+1e-7))<=1e-7) {</pre>
6
         int a=(int)(floor(sqrt(n)+1e-7)); printf("%d %d\n",a,1);
       } else {
         // 求 x^2 - ny^2 = 1 的最小正整数根, n 不是完全平方数
8
9
         p[1]=q[0]=h[1]=1;p[0]=q[1]=g[1]=0;
10
         a[2]=(int)(floor(sqrt(n)+1e-7));
         for (int i=2;i;++i) {
11
           g[i]=-g[i-1]+a[i]*h[i-1]; h[i]=(n-sqr(g[i]))/h[i-1];
12
```

蔡勒公式

```
int zeller(int y,int m,int d) {
   if (m<=2) y--,m+=12; int c=y/100; y%=100;
   int w=((c>>2)-(c<<1)+y+(y>>2)+(13*(m+1)/5)+d-1)%7;
   if (w<0) w+=7; return(w);
}</pre>
```

Schreier-Sims

```
namespace Schreier_Sims_Algorithm{
     struct Permutation{
       vector<int> P;
3
       Permutation(){}
       Permutation(int n){
         P.resize(n);
       Permutation inv()const{
         Permutation ret(P.size());
10
         for(int i = 0; i < int(P.size()); ++i) ret.P[P[i]] = i;</pre>
11
         return ret;
12
       int &operator [](const int &dn){
13
14
         return P[dn];
15
16
       void resize(const size_t &sz){
         P.resize(sz);
17
18
       size_t size()const{
19
20
         return P.size();
21
       const int &operator [](const int &dn)const{
22
         return P[dn];
23
24
25
26
     Permutation operator *(const Permutation &a, const Permutation &b){
27
       Permutation ret(a.size());
28
       for(int i = 0; i < (int)a.size(); ++i){
         ret[i] = b[a[i]];
29
```

```
vector<Bucket> buckets(n);
30
                                                                                               75
                                                                                               76
                                                                                                         swap(buckets, buckets);
31
       return ret;
     }
                                                                                                         vector<Bucket> _bucketsInv(n);
32
                                                                                               77
33
                                                                                               78
                                                                                                         swap(bucketsInv, bucketsInv);
     typedef vector<Permutation> Bucket;
                                                                                                         vector<Table> lookupTable(n);
                                                                                               79
34
                                                                                                         swap(lookupTable, lookupTable);
     typedef vector<int> Table;
                                                                                               80
35
                                                                                               81
36
     typedef pair<int,int> pii;
                                                                                               82
     int n, m;
                                                                                                       for(int i = 0; i < n; ++i){
37
     vector<Bucket> buckets, bucketsInv;
                                                                                               83
38
                                                                                                         lookupTable[i].resize(n);
     vector<Table> lookupTable;
                                                                                               84
                                                                                                         fill(lookupTable[i].begin(), lookupTable[i].end(), -1);
39
                                                                                               85
40
                                                                                               86
     int fastFilter(const Permutation &g, bool addToGroup = true){
                                                                                                       Permutation id(n);
41
       int n = buckets.size();
                                                                                               87
                                                                                                       for(int i = 0; i < n; ++i){
42
                                                                                               88
43
       Permutation p;
                                                                                                         id[i] = i;
       for(int i = 0; i < n; ++i){
                                                                                               89
44
         int res = lookupTable[i][p[i]];
                                                                                                       for(int i = 0; i < n; ++i){
45
                                                                                               90
46
         if(res == -1){
                                                                                                         buckets[i].push_back(id);
                                                                                               91
           if(addToGroup){
                                                                                                         bucketsInv[i].push back(id);
                                                                                               92
47
             buckets[i].push back(p);
48
                                                                                                         lookupTable[i][i] = 0;
                                                                                               93
             bucketsInv[i].push_back(p.inv());
                                                                                                       }
49
                                                                                               94
50
             lookupTable[i][p[i]] = (int)buckets[i].size() - 1;
                                                                                                       for(int i = 0; i < m; ++i){
                                                                                               95
           }
                                                                                               96
                                                                                                         fastFilter(gen[i]);
51
           return i;
52
                                                                                               97
         }
                                                                                               98
                                                                                                       queue<pair<point,point> > toUpdate;
53
         p = p * bucketsInv[i][res];
                                                                                                       for(int i = 0; i < n; ++i){
                                                                                               99
54
                                                                                                         for(int j = i; j < n; ++j){}
         swap(i1,i2);
                                                                                              100
55
56
                                                                                                           for(int k = 0; k < (int)buckets[i].size(); ++k){</pre>
       }
                                                                                              101
                                                                                                             for(int 1 = 0; 1 < (int)buckets[j].size(); ++1){</pre>
57
       return -1;
                                                                                              102
58
                                                                                                               toUpdate.push(make_pair(pii(i,k), pii(j,l)));
                                                                                              103
                                                                                                             }
59
                                                                                              104
60
     long long calcTotalSize(){
                                                                                              105
61
       long long ret = 1;
                                                                                              106
                                                                                                         }
62
       for(int i = 0; i < n; ++i){
                                                                                                       }
                                                                                              107
63
                                                                                              108
                                                                                                       while(!toUpdate.empty()){
         ret *= buckets[i].size();
64
                                                                                                         pii a = toUpdate.front().first;
                                                                                              109
65
       return ret;
                                                                                              110
                                                                                                         pii b = toUpdate.front().second;
66
                                                                                                         toUpdate.pop();
                                                                                              111
67
                                                                                                         int res = fastFilter(buckets[a.first][a.second] * buckets[b.first][b.second]);
                                                                                              112
68
     bool inGroup(const Permutation &g){
                                                                                                         if(res==-1) continue;
                                                                                              113
       return fastFilter(g, false) == -1;
                                                                                                         pii newPair(res, (int)buckets[res].size() - 1);
69
                                                                                              114
                                                                                                         for(int i = 0; i < n; ++i){
70
                                                                                              115
                                                                                              116
                                                                                                           for(int j = 0; j < (int)buckets[i].size(); ++j){</pre>
71
     void solve(const Bucket &gen,int n){// m perm[0..n - 1]s
                                                                                                             if(i <= res){</pre>
72
                                                                                              117
                                                                                              118
                                                                                                               toUpdate.push(make pair(pii(i , j), newPair));
       n = _n, m = gen.size();
73
       {//clear all
                                                                                                             }
74
                                                                                              119
```

Romberg

```
1 template<class T>
 2 double romberg(const T&f,double a,double b,double eps=1e-8){
     std::vector<double>t; double h=b-a,last,curr; int k=1,i=1;
     t.push_back(h*(f(a)+f(b))/2); // 梯形
     do{ last=t.back(); curr=0; double x=a+h/2;
 5
       for(int j=0;j<k;++j) curr+=f(x),x+=h;</pre>
 7
       curr=(t[0]+h*curr)/2; double k1=4.0/3.0, k2=1.0/3.0;
 8
       for(int j=0;j<i;j++){ double temp=k1*curr-k2*t[j];</pre>
         t[j]=curr; curr=temp; k2/=4*k1-k2; k1=k2+1; // 防止溢出
 9
       } t.push_back(curr); k*=2; h/=2; i++;
10
     } while(std::fabs(last-curr)>eps);
11
     return t.back();
12
13 | }
```

线性规划

```
1 // 求\max\{cx \mid Ax \le b, x \ge 0\}的解
2 typedef vector<double> VD;
3 | VD simplex(vector<VD> A, VD b, VD c) {
     int n = A.size(), m = A[0].size() + 1, r = n, s = m - 1;
     vector\langle VD \rangle D(n + 2, VD(m + 1, 0)); vector\langle int \rangle ix(n + m);
6
     for (int i = 0; i < n + m; ++ i) ix[i] = i;
     for (int i = 0; i < n; ++ i) {
8
       for (int j = 0; j < m - 1; ++ j) D[i][j] = -A[i][j];
       D[i][m - 1] = 1; D[i][m] = b[i];
       if (D[r][m] > D[i][m]) r = i;
10
11
      for (int j = 0; j < m - 1; ++ j) D[n][j] = c[j];
12
     D[n + 1][m - 1] = -1;
13
      for (double d; ; ) {
14
15
       if (r < n) {
16
         int t = ix[s]; ix[s] = ix[r + m]; ix[r + m] = t;
         D[r][s] = 1.0 / D[r][s]; vector<int> speedUp;
17
18
         for (int j = 0; j <= m; ++ j) if (j != s) {
           D[r][j] *= -D[r][s];
19
           if(D[r][j]) speedUp.push_back(j);
20
```

```
21
         }
22
         for (int i = 0; i <= n + 1; ++ i) if (i != r) {
23
           for(int j = 0; j < speedUp.size(); ++ j)</pre>
24
           D[i][speedUp[j]] += D[r][speedUp[j]] * D[i][s];
           D[i][s] *= D[r][s];
25
26
       } r = -1; s = -1;
       for (int j = 0; j < m; ++ j) if (s < 0 || ix[s] > ix[j])
27
28
         if (D[n + 1][j] > EPS || (D[n + 1][j] > -EPS && D[n][j] > EPS)) s = j;
29
       if (s < 0) break;
       for (int i = 0; i < n; ++ i) if (D[i][s] < -EPS)
30
         if (r < 0 \mid | (d = D[r][m] / D[r][s] - D[i][m] / D[i][s]) < -EPS
31
             || (d < EPS \&\& ix[r + m] > ix[i + m])) r = i;
32
       if (r < 0) return VD(); // 无边界
33
34
     if (D[n + 1][m] < -EPS) return VD(); // 无解
35
36
     VD \times (m - 1);
     for (int i = m; i < n + m; ++ i) if (ix[i] < m - 1) x[ix[i]] = D[i - m][m];
37
38
     return x; // 最优值在 D[n][m]
39 }
```

FFT

```
// double 精度对10^9 + 7 取模最多可以做到2^20
   const int MOD = 1000003;
   const double PI = acos(-1);
   typedef complex<double> Complex;
   const int N = 65536, L = 15, MASK = (1 << L) - 1;
10
11 | Complex w[N];
12
   void FFTInit() {
13
     for (int i = 0; i < N; ++i) {
14
       w[i] = Complex(cos(2 * i * PI / N), sin(2 * i * PI / N));
15
16
17
18
   void FFT(Complex p[], int n) {
19
     for (int i = 1, j = 0; i < n - 1; ++i) {
20
       for (int s = n; j ^= s >>= 1, ~j & s;);
21
       if (i < j) {
22
         swap(p[i], p[j]);
23
```

```
24
25
26
     for (int d = 0; (1 << d) < n; ++d) {
27
       int m = 1 << d, m2 = m * 2, rm = n >> (d + 1);
28
       for (int i = 0; i < n; i += m2) {
29
         for (int j = 0; j < m; ++j) {
30
           Complex &p1 = p[i + j + m], &p2 = p[i + j];
31
           Complex t = w[rm * j] * p1;
32
           p1 = p2 - t;
33
           p2 = p2 + t;
34
       }
35
36
37
38
   Complex A[N], B[N], C[N], D[N];
39
40
   void mul(int a[N], int b[N]) {
41
     for (int i = 0; i < N; ++i) {
42
       A[i] = Complex(a[i] >> L, a[i] & MASK);
43
       B[i] = Complex(b[i] >> L, b[i] & MASK);
44
45
46
     FFT(A, N);
     FFT(B, N);
47
48
     for (int i = 0; i < N; ++i) {
       int j = (N - i) \% N;
49
       Complex da = (A[i] - conj(A[j])) * Complex(0, -0.5),
50
           db = (A[i] + conj(A[j])) * Complex(0.5, 0),
51
           dc = (B[i] - conj(B[j])) * Complex(0, -0.5),
52
           dd = (B[i] + conj(B[j])) * Complex(0.5, 0);
53
       C[j] = da * dd + da * dc * Complex(0, 1);
54
       D[i] = db * dd + db * dc * Complex(0, 1);
55
56
     FFT(C, N);
57
58
     FFT(D, N);
59
     for (int i = 0; i < N; ++i) {
60
       long long da = (long long)(C[i].imag() / N + 0.5) % MOD,
61
             db = (long long)(C[i].real() / N + 0.5) % MOD,
62
             dc = (long long)(D[i].imag() / N + 0.5) % MOD,
63
             dd = (long long)(D[i].real() / N + 0.5) % MOD;
64
       a[i] = ((dd << (L * 2)) + ((db + dc) << L) + da) % MOD;
65
66 }
```

NTT

```
1 //R 是 2^n*a+1 形质数 p 的原根
   void NFT(int P[], int n, int oper) {
     for (int i = 1, j = 0; i < n - 1; ++i) {
 4
       for (int s = n; j ^= s >= 1, ~j \& s;);
       if (i < j) {
 5
         swap(P[i], P[j]);
 9
     for (int d = 0; (1 << d) < n; ++d) {
       int m = 1 << d, m2 = m * 2;
10
       int unit p0 = powmod(R, (MOD - 1) / m2);
11
12
       if (oper < 0) {
13
         unit_p0 = inverse(unit_p0);
14
15
       for (int i = 0; i < n; i += m2) {
16
         int unit = 1;
17
         for (int j = 0; j < m; ++j) {
18
           int &P1 = P[i + j + m],
19
             &P2 = P[i + j];
20
           int t = (long long)unit * P1 % MOD;
21
           P1 = (P2 - t + MOD) \% MOD;
22
           P2 = (P2 + t) \% MOD;
           unit = (long long)unit * unit p0 % MOD;
23
24
25
26
27
```

FWT

```
void FWT(int a[N], int N) {
     for (int d = 1; d < N; d <<= 1) {
3
       int d2 = d \ll 1;
       for (int i = 0; i < N; i += d2) {
         int *x = a + i, *y = a + i + d;
         for (int j = 0; j < d; ++j, ++x, ++y) {
          if ((*x += *y) >= MOD) {
             *x -= MOD;
10
           if ((*y = *x - (*y << 1)) < 0) {
11
             if ((*y += MOD) < 0) {
12
               *v += MOD;
             }
13
14
15
```

```
16
17
18 }
19
   void xorPow(int a[N], int n, int b[N]) {
20
     memset(b, 0, sizeof(int) * N);
21
     b[0] = 1;
22
     FWT(a, N);
23
     FWT(b, N);
24
     while(n) {
25
26
       if (n & 1) {
         dot(b, a, N);
27
28
29
       dot(a, a, N);
30
       n >>= 1;
31
     FWT(b, N);
32
33
     norm(b, N);
34 | }
```

Manacher/ 扩展 KMP

```
1 | void Manacher(char text[], int n, int palindrome[]) {
2
     palindrome[0] = 1;
     for (int i = 1, j = 0, i < (n << 1) - 1; ++ i) {
       int p = i \gg 1;
       int q = i - p;
       int r = (j + 1 \gg 1) + palindrome[j] - 1;
       palindrome[i] = r < q ? 0 : min(r - q + 1, palindrome[(j << 1) - i]);
8
       while (∅ <= p - palindrome[i] && q + palindrome[i] < n && text[p -
          → palindrome[i]] == text[q + palindrome[i]]) {
         palindrome[i] ++;
9
10
       if (q + palindrome[i] - 1 > r) {
11
         j = i;
12
       }
13
14
15
16
17 void ExtendedKMP(char *a, char *b, int M, int N, int *Next, int *ret) {// a ->
      → 模式串 b -> 匹配串
18
     int i, j, k;
     for (j = 0; 1 + j < M \&\& a[j] == a[1 + j]; j++); Next[1] = j;
19
20
     for (i = 2; i < M; i++) {
^{21}
       int Len = k + Next[k], L = Next[i - k];
^{22}
```

```
if (L < Len - i) {</pre>
23
         Next[i] = L;
24
25
       } else {
26
         for (j = max(0, Len - i); i + j < M && a[j] == a[i + j]; j++);
27
         Next[i] = j;
28
         k = i;
29
30
31
     for (j = 0; j < N && j < M && a[j] == b[j]; j++);
     ret[0] = j;
32
     k = 0;
33
     for (i = 1; i < N; i++) {
34
       int Len = k + ret[k], L = Next[i - k];
35
36
       if (L < Len - i) {
         ret[i] = L;
37
38
       } else {
         for (j = max(0, Len - i); j < M && i + j < N && a[j] == b[i + j]; j++);
39
40
         ret[i] = j;
         k = i;
41
42
43
44 | }
```

后缀数组(倍增)

```
1 int rank[MAX_N],height[MAX_N];
   int cmp(int *x,int a,int b,int d){
     return x[a]==x[b]&&x[a+d]==x[b+d];
4
   void doubling(int *a,int N,int M){
     static int sRank[MAX_N],tmpA[MAX_N],tmpB[MAX_N];
     int *x=tmpA,*y=tmpB;
     for(int i=0;i<M;++i) sRank[i]=0;</pre>
     for(int i=0;i<N;++i) ++sRank[x[i]=a[i]];</pre>
     for(int i=1;i<M;++i) sRank[i]+=sRank[i-1];</pre>
10
      for(int i=N-1;i>=0;--i) sa[--sRank[x[i]]]=i;
11
      for(int d=1,p=0;p<N;M=p,d<<=1){
12
       p=0; for(int i=N-d;i<N;++i) y[p++]=i;</pre>
13
       for(int i=0;i<N;++i) if(sa[i]>=d) y[p++]=sa[i]-d;
14
        for(int i=0;i<M;++i) sRank[i]=0;</pre>
15
        for(int i=0;i<N;++i) ++sRank[x[i]];</pre>
16
17
        for(int i=1;i<M;++i) sRank[i]+=sRank[i-1];</pre>
18
       for(int i=N-1;i>=0;--i) sa[--sRank[x[y[i]]]]=y[i];
        swap(x,y); x[sa[0]]=0; p=1;
19
        for(int i=1;i<N;++i) x[sa[i]]=cmp(y,sa[i],sa[i-1],d)?p-1:p++;</pre>
20
21
```

```
22 }
23
   void calcHeight(){
     for(int i=0;i<N;++i) rank[sa[i]]=i;</pre>
24
25
     int cur=0; for(int i=0;i<N;++i)</pre>
26
     if(rank[i]){
       if(cur) cur--;
27
28
       for(;a[i+cur]==a[sa[rank[i]-1]+cur];++cur);
29
       height[rank[i]]=cur;
30
31 }
```

后缀数组 (DC3)

```
1 1// 待排序的字符串放在 r 数组中, 从 r[0] 到 r[n-1], 长度为 n, 且最大值小于 m
 2 // 约定除 r[n-1] 外所有的 r[i] 都大于 0, r[n-1]=0
 3 // 函数结束后, 结果放在 sa 数组中, 从 sa[0] 到 sa[n-1]
   #define maxn 10000
   #define F(x) ((x)/3+((x)%3==1?0:tb))
 6 | #define G(x) ((x)<tb?(x)*3+1:((x)-tb)*3+2)
 7 int wa[maxn],wb[maxn],wv[maxn],wss[maxn]; // 必须这么大
 8 int s[maxn*3],sa[maxn*3];
 9 \mid \text{int c0(int *r,int a,int b)} \{ \text{return r[a]} == \text{r[b]} \& \text{r[a+1]} == \text{r[b+1]} \& \& \text{r[a+2]} == \text{r[b+2]}; \}
10 int c12(int k,int *r,int a,int b){
     if(k==2) return r[a] < r[b] | | r[a] == r[b] & c12(1, r, a+1, b+1);
11
12
      else return r[a]<r[b]||r[a]==r[b]&&wv[a+1]<wv[b+1];
13 | }
   void sort(int *r,int *a,int *b,int n,int m){
14
     int i; for(i=0;i<n;i++) wv[i]=r[a[i]];</pre>
15
16
     for(i=0;i<m;i++) wss[i]=0; for(i=0;i<n;i++) wss[wv[i]]++;</pre>
      for(i=1;i<m;i++) wss[i]+=wss[i-1];</pre>
17
18
      for(i=n-1;i>=0;i--) b[--wss[wv[i]]]=a[i];
19
   void dc3(int *r,int *sa,int n,int m){
20
     int i,j,*rn=r+n,*san=sa+n,ta=0,tb=(n+1)/3,tbc=0,p;
21
      r[n]=r[n+1]=0;
22
      for(i=0;i<n;i++) if(i%3!=0) wa[tbc++]=i;</pre>
23
24
      sort(r+2,wa,wb,tbc,m); sort(r+1,wb,wa,tbc,m); sort(r,wa,wb,tbc,m);
25
      for(p=1,rn[F(wb[0])]=0,i=1;i<tbc;i++)
26
       rn[F(wb[i])]=c0(r,wb[i-1],wb[i])?p-1:p++;
      if(p<tbc) dc3(rn,san,tbc,p);</pre>
27
      else for(i=0;i<tbc;i++) san[rn[i]]=i;</pre>
28
29
      for (i=0;i<tbc;i++) if(san[i]<tb) wb[ta++]=san[i]*3;</pre>
30
      if(n%3==1) wb[ta++]=n-1;
      sort(r,wb,wa,ta,m); for(i=0;i<tbc;i++) wv[wb[i]=G(san[i])]=i;</pre>
31
      for(i=0,j=0,p=0;i<ta && j<tbc;p++)</pre>
32
        sa[p]=c12(wb[j]%3,r,wa[i],wb[j])?wa[i++]:wb[j++];
33
```

```
34     for(;i<ta;p++) sa[p]=wa[i++]; for(;j<tbc;p++) sa[p]=wb[j++];}
35     int main(){
36         int n,m=0;         scanf("%d",&n);
37         for (int i=0;i<n;i++) scanf("%d",&s[i]),s[i]++,m=max(s[i]+1,m);
38         printf("%d\n",m); s[n++]=0; dc3(s,sa,n,m);
39         for (int i=0;i<n;i++) printf("%d ",sa[i]);printf("\n");
40    }</pre>
```

后缀自动机

```
struct State {
     int length;
     State *parent,*go[C];
     State(int length):length(length),parent(NULL){
5
       memset(go,0,sizeof(go));
6
     }
     State* extend(State *start,int token){
       State *p=this;
       State *np=new State(this->length+1);
9
       while(p!=NULL&&p->go[token]==NULL)
10
11
         p->go[token]=np, p=p->parent;
       if(p==NULL) np->parent=start;
12
13
       else{
         State *q=p->go[token];
14
         if(p->length+1==q->length) np->parent=q;
15
16
         else{
17
           State *nq=new State(p->length+1);
18
           memcpy(nq->go,q->go,sizeof(q->go));
19
           nq->parent=q->parent;
20
           np->parent=q->parent=nq;
21
           while(p!=NULL&&p->go[token]==q)
22
             p->go[token]=nq, p=p->parent;
         }
23
       }
24
25
       return np;
26
27 };
```

后缀树 (With Walk)

```
int pos;

struct Node {
  int l, r;

Node *suf, *ch[C];
```

```
8
     Node (int l = -1, int r = INF) : l(1), r(r) {
 9
10
       memset(ch, 0, sizeof(ch));
11
12
13
     int len() {
       return min(r, pos + 1) - 1;
14
15
16 | };
17
18
   int top;
19
20 | Node pool[N << 1];
^{21}
22 Node *root, *nxtSuf, *cur;
23
   int text[N];
24
25
26
   int remCnt, curP, curLen;
27
28
   void init() {
     top = 0, pos = -1, remCnt = 0, curP = 0, curLen = 0;
29
     nxtSuf = NULL;
30
     root = cur = new(pool + (top++)) Node(-1, -1);
31
32
33
   void link(Node *u) {
34
     if (nxtSuf) {
35
36
       nxtSuf->suf = u;
37
38
     nxtSuf = u;
39
40
   bool walk(Node *u) {
41
     int len = u->len();
42
     if (curLen >= len) {
43
       curP += len;
44
       curLen -= len;
45
46
       cur = u;
47
       return true;
48
     return false;
49
50
51
```

```
52 void extend(int c) {
     text[++pos] = c;
53
     nxtSuf = NULL;
54
55
     ++remCnt;
56
     while (remCnt) {
       curP = curLen ? curP : pos;
57
58
       int curE = text[curP];
       if (!cur->ch[curE]) {
59
         cur->ch[curE] = new(pool + (top++)) Node(pos);
60
61
         link(cur);
62
       } else {
63
         Node *nxt = cur->ch[curE];
64
         if (walk(nxt)) {
65
           continue;
66
         }
67
         if (text[nxt->l + curLen] == c) {
68
           ++curLen;
69
           link(cur);
           break;
70
         }
71
72
         Node *split = new(pool + (top++)) Node(nxt->1, nxt->1 + curLen);
         cur->ch[curE] = split;
73
         split->ch[c] = new(pool + (top++)) Node(pos);
74
         nxt->1 += curLen;
75
76
         split->ch[text[nxt->l]] = nxt;
77
         link(split);
78
       }
79
       --remCnt;
80
       if (cur == root && curLen > 0) {
81
         --curLen;
82
         curP = pos - remCnt + 1;
83
       } else {
84
         cur = cur->suf ? cur->suf : root;
85
86
87
88
89
   void finish() {
     nxtSuf = NULL;
     for (int i = 0; i < top; ++i) {
91
       if (pool[i].r == INF) {
92
         link(pool + i);
93
       }
94
95
     while (remCnt > 0) {
```

```
if (curLen) {
                                                                                                         if (curLen >= len) {
                                                                                              142
 97
 98
          int curE = text[curP];
                                                                                                           curP += len;
                                                                                              143
          Node *nxt = cur->ch[curE];
                                                                                                           curLen -= len;
 99
                                                                                              144
100
          if (walk(nxt)) {
                                                                                              145
                                                                                                           cur = nxt;
101
            continue;
                                                                                              146
                                                                                                        } else {
102
                                                                                              147
                                                                                                           break;
          Node *split = new(pool + (top++)) Node(nxt->1, nxt->1 + curLen);
103
                                                                                              148
          cur->ch[curE] = split;
104
                                                                                              149
                                                                                                      }
105
          nxt->1 += curLen;
                                                                                              150
                                                                                                    }
          split->ch[text[nxt->1]] = nxt;
106
                                                                                              151
          link(split);
                                                                                                     void walk(int c) {
107
                                                                                              152
108
        } else {
                                                                                                       buf[++pos] = c;
                                                                                              153
          link(cur);
                                                                                                      while (curLen) {
109
                                                                                              154
        }
                                                                                                        Node *nxt = cur->ch[buf[curP]];
110
                                                                                              155
111
        --remCnt;
                                                                                              156
                                                                                                        if (nxt->l + curlen <= ::pos && text[nxt->l + curlen] == c) {
        if (cur == root && curLen > 0) {
                                                                                                           ++totLen;
112
                                                                                              157
          --curLen;
                                                                                              158
                                                                                                           ++curLen;
113
          curP = pos - remCnt + 1;
                                                                                                          break;
                                                                                              159
114
                                                                                              160
                                                                                                        } else {
        } else {
115
          cur = cur->suf ? cur->suf : root;
                                                                                              161
                                                                                                           --totLen;
116
117
                                                                                              162
                                                                                                           if (cur == root && curLen > 0) {
                                                                                              163
118
                                                                                                             --curLen;
      if (nxtSuf != root) {
                                                                                              164
                                                                                                             curP = pos - curLen;
119
        link(root);
                                                                                              165
                                                                                                          } else {
120
                                                                                              166
                                                                                                             cur = cur->suf;
121
122 }
                                                                                              167
                                                                                                          }
                                                                                              168
                                                                                                           descend();
123
                                                                                                        }
124 int buf[N];
                                                                                              169
125
                                                                                              170
126 struct Walker {
                                                                                              171
                                                                                                       if (curLen == 0) {
      Node *cur, *root;
                                                                                              172
                                                                                                        curP = pos;
127
128
      int curP, curLen, pos, totLen;
                                                                                                        int curE = buf[curP];
                                                                                              173
                                                                                                        while (cur && !cur->ch[curE]) {
129
                                                                                              174
      Walker(Node* root) : root(root) {
130
                                                                                              175
                                                                                                           --totLen;
                                                                                                           cur = cur->suf;
        cur = root;
                                                                                              176
131
                                                                                                        }
132
        curP = -1;
                                                                                              177
        curLen = 0;
                                                                                              178
                                                                                                        if (cur) {
133
                                                                                                          ++totLen;
        totLen = 0;
134
                                                                                              179
                                                                                                           curLen = 1;
        pos = -1;
                                                                                              180
135
136
                                                                                              181
                                                                                                        } else {
137
                                                                                              182
                                                                                                           cur = root;
138
      void descend() {
                                                                                              183
                                                                                                           totLen = 0;
        while (curLen > 0) {
                                                                                              184
139
                                                                                                        }
          Node *nxt = cur->ch[buf[curP]];
                                                                                              185
                                                                                                      }
140
          int len = nxt->len();
                                                                                              186
                                                                                                      descend();
141
```

```
187 }
188 };
```

后缀树 (With Pop Front)

```
1 int pos;
 2
   int text[N];
 3
 4
 5
   struct Node {
     int 1, r;
 7
 8
     Node *suf, *ch[C];
 9
     int dgr;
10
11
     Node *fa;
12
13
     Node (int 1 = -1, int r = INF) : 1(1), r(r) {
14
       suf = fa = NULL;
15
16
       memset(ch, 0, sizeof(ch));
       dgr = 0;
17
18
19
     Node* addEdge(Node *t) {
20
       int c = text[t->1];
21
       dgr += !ch[c];
22
       ch[c] = t;
23
       t->fa = this;
24
25
       return t;
26
27
28
     int len() {
29
       return min(r, pos + 1) - 1;
30
   };
31
32
   int top;
33
34
   Node pool[N << 1];
35
36
   Node *root, *nxtSuf, *cur;
37
38
39
   int remCnt, curP, curLen;
40
41 long long size;
```

```
42
   queue<Node*> leaves;
43
44
45
   void init() {
46
     top = 0, pos = -1;
     remCnt = 0, curP = 0, curLen = 0;
47
48
     nxtSuf = NULL;
     root = cur = new(pool + (top++)) Node(-1, -1);
49
50
     size = 0;
51
     while (leaves.size()) {
       leaves.pop();
52
53
54
55
   void link(Node *u) {
     if (nxtSuf) {
57
58
       nxtSuf->suf = u;
59
60
     nxtSuf = u;
61
62
   bool walk(Node *u) {
63
     int len = u->len();
64
65
     if (curLen >= len) {
66
       curP += len;
67
       curLen -= len;
68
       cur = u;
69
       return true;
70
     return false;
7^{1}
72
73
   void extend(int c) {
     text[++pos] = c;
75
76
     nxtSuf = NULL;
77
     ++remCnt;
78
     while (remCnt) {
       curP = curLen ? curP : pos;
79
       int curE = text[curP];
80
81
       if (!cur->ch[curE]) {
         leaves.push(cur->addEdge(new(pool + (top++)) Node(pos)));
82
83
         link(cur);
84
       } else {
85
         Node *nxt = cur->ch[curE];
86
         if (walk(nxt)) {
```

```
87
             continue;
                                                                                                          link(cur);
                                                                                               132
 88
          }
                                                                                                        }
                                                                                               133
 89
          if (text[nxt->l + curLen] == c) {
                                                                                                        --remCnt;
                                                                                               134
 90
            ++curLen;
                                                                                               135
                                                                                                        if (cur == root && curLen > 0) {
            link(cur);
                                                                                               136
                                                                                                          --curLen;
 91
            break;
                                                                                                          curP = pos - remCnt + 1;
 92
                                                                                               137
          }
                                                                                               138
                                                                                                        } else {
 93
          Node *split = new(pool + (top++)) Node(nxt->1, nxt->1 + curLen);
                                                                                               139
                                                                                                          cur = cur->suf ? cur->suf : root;
 94
          cur->addEdge(split);
 95
                                                                                               140
                                                                                                        }
 96
          leaves.push(split->addEdge(new(pool + (top++)) Node(pos)));
                                                                                               141
          nxt->1 += curLen;
                                                                                                      if (nxtSuf != root) {
                                                                                               142
 97
 98
          split->addEdge(nxt);
                                                                                                        link(root);
                                                                                               143
          link(split);
 99
                                                                                               144
        }
100
                                                                                               145
101
        --remCnt;
                                                                                               146
        if (cur == root && curLen > 0) {
                                                                                                    void eraseUp(Node *&u) {
102
                                                                                               147
          curP = pos - (--curLen);
                                                                                               148
                                                                                                      size -= u->len();
103
                                                                                                      int ch = text[u->1];
        } else {
                                                                                               149
104
          cur = cur->suf ? cur->suf : root;
                                                                                                      u = u \rightarrow fa;
                                                                                               150
105
        }
                                                                                                      u \rightarrow ch[ch] = NULL;
106
                                                                                               151
107
                                                                                               152
                                                                                                      --(u->dgr);
      size += leaves.size();
108
                                                                                               153
109 }
                                                                                               154
                                                                                                    void erase() {
110
                                                                                               155
    void finish() {
                                                                                                      Node *u = leaves.front();
111
                                                                                               156
      nxtSuf = NULL;
                                                                                                      leaves.pop();
112
                                                                                               157
      for (int i = 0; i < top; ++i) {
                                                                                               158
                                                                                                      while (u->dgr == 0 \&\& u != cur) {
113
        if (pool[i].r == INF) {
                                                                                                        eraseUp(u);
114
                                                                                               159
          link(pool + i);
                                                                                               160
                                                                                                      }
115
116
        }
                                                                                               161
                                                                                                      if (u == cur) {
                                                                                               162
                                                                                                        if (cur->dgr == 0 && curLen == 0) {
117
118
      while (remCnt > 0) {
                                                                                               163
                                                                                                          int len = u->len();
        if (curLen) {
                                                                                               164
                                                                                                          curLen = len;
119
          int curE = text[curP];
                                                                                               165
                                                                                                          curP = pos - len + 1;
120
          Node *nxt = cur->ch[curE];
                                                                                               166
                                                                                                          cur = cur->fa;
121
122
          if (walk(nxt)) {
                                                                                               167
                                                                                                          eraseUp(u);
            continue;
                                                                                               168
123
                                                                                               169
                                                                                                        if (curLen) {
124
          Node *split = new(pool + (top++)) Node(nxt->1, nxt->1 + curlen);
                                                                                                          int curE = text[curP];
125
                                                                                               170
          leaves.push(cur->addEdge(split));
                                                                                                          if (!cur->ch[curE]) {
126
                                                                                               171
          nxt->1 += curLen;
                                                                                                            Node *leaf = new(pool + (top++)) Node(pos - curLen + 1);
127
                                                                                               172
128
          split->addEdge(nxt);
                                                                                               173
                                                                                                            leaves.push(cur->addEdge(leaf));
          link(split);
                                                                                                            size += leaf->len();
129
                                                                                               174
        } else {
                                                                                                            --remCnt;
130
                                                                                               175
                                                                                                            if (cur == root && curLen > 0) {
          leaves.push(cur);
                                                                                               176
131
```

```
curP = pos - (--curLen) + 1;
177
178
            } else {
               cur = cur->suf ? cur->suf : root;
179
180
181
            while (curLen && walk(cur->ch[text[curP]])) {
182
               continue;
183
184
185
186
187 }
188
189 int n;
190
    char s[N], buf[N];
191
192
    int ord[N], stop, sord[N << 1];</pre>
193
194
    void dfs(Node *u) {
195
196
      sord[u - pool] = stop++;
      for (int i = 0; i < C; ++i) {
197
198
        if (u->ch[i]) {
          dfs(u->ch[i]);
199
        }
200
201
202
203
    void getOrd() {
204
      init();
205
206
      for (int i = 0; i < n; ++i) {
        extend(s[i] - 'a');
207
208
      finish();
209
      stop = 0;
210
211
      dfs(root);
212
      int i = 0;
      while (leaves.size()) {
213
        ord[i++] = sord[leaves.front() - pool];
214
215
        leaves.pop();
216
217 }
```

字符串最小表示

```
std::string find(std::string s) {
int i,j,k,l,N=s.length(); s+=s;
```

```
3  for(i=0,j=1;j<N;){
4   for(k=0;k<N&&s[i+k]==s[j+k];k++);
5   if(k>=N) break;
6   if(s[i+k]<s[j+k]) j+=k+1;
7   else l=i+k,i=j,j=max(l,j)+1;
8  }
9  return s.substr(i,N);
10 }</pre>
```

轻重链剖分

```
struct Tree(){}*root[N];
   int father[N],size[N],depth[N];
   int bfsOrd[N],pathId[N],ordInPath[N],sqn[N];
   void doBfs(int s){
     int qh=0,qt=0,*que=bfsOrd; father[s]=-1; depth[s]=0;
     for(que[qt++]=s;qh<qt;){</pre>
       int u=que[qh++];
       foreach(iter,adj[u]){
9
         int v=*iter; if(v==father[u]) continue;
         father[v]=u; depth[v]=depth[u]+1; que[qt++]=v;
10
11
12
13
   void doSplit(){
14
     for(int i=N-1;i>=0;--i){
15
16
       int u=bfsOrd[i]; size[u]=1;
17
       foreach(iter,adj[u]){
18
         int v=*iter; if(v==father[u]) continue; size[u]+=size[v];
19
20
     memset(pathId,-1,sizeof pathId);
21
     for(int i=0;i<N;++i){</pre>
22
       int top=bfsOrd[i],cnt=0;
23
       if(pathId[top]!=-1) continue;
24
25
       for(int next,u=top;u!=-1;u=next){
26
         sqn[cnt]=val[u]; ordInPath[u]=cnt; pathId[u]=top; ++cnt;
         next=-1;
27
28
         foreach(iter,adj[u]){
           int v=*iter; if(v==father[u]) continue;
29
30
           if(next<0||size[next]<size[v]) next=v;</pre>
31
32
33
       root[top]=new Tree(0,cnt,sqn);
34
```

```
35 | }
36 | void prepare(){ doBfs(0); doSplit(); }
```

KD Tree

```
1 #include <cstdio>
   #include <vector>
 3 | #include <iostream>
   #include <algorithm>
 5
 6 using namespace std;
 7 \mid // 带插入版本 ,没有写内存回收 ,空间复杂度 n \log n ,如果不需要插入可以大大简化
 8 // N 为最大点数, D 为每个点的最大维度, d 为实际维度
 |\mathfrak{g}|// 以查找最近点为例 \mathsf{ret} 为当前最近点的距离的平方 ,用来剪枝 ,查询 \mathsf{k} 近或 \mathsf{k} 远的方法类似
10 // 使用时注意先 initNull
11 const long long INF = (int)1e9 + 10;
12 const int N = 2000000 + 10;
13 \mid const int D = 5;
14 const double SCALE = 0.75;
15 | struct Point { int x[D]; } buf[N];
16 | int d;
17 | struct Node {
     int depth, size;
18
     Node *ch[2], *p;
19
     Point val, maxv, minv;
20
21
     void set(Node *t, int d) { ch[d] = t; t->p = this; }
     bool dir() { return this == p->ch[1]; }
22
     bool balanced() {
23
       return (double)max(ch[0]->size, ch[1]->size) <= (double)size * SCALE;</pre>
24
25
26
     void update() {
       size = ch[0] -> size + ch[1] -> size + 1;
27
28
       for(int i = 0; i < d; ++ i) {
         \max v.x[i] = \max(val.x[i], \max(ch[0]->\max v.x[i], ch[1]->\max v.x[i]));
29
         minv.x[i] = min(val.x[i], min(ch[0]->minv.x[i], ch[1]->minv.x[i]));
30
       }
31
32
     nodePool[N], *totNode, *null;
   Node* newNode(Point p, int depth) {
     Node *t = totNode ++;
35
     t \rightarrow ch[0] = t \rightarrow ch[1] = t \rightarrow p = null;
37
     t->depth = depth;
38
     t->val = t->maxv = t->minv = p;
     t \rightarrow size = 1;
39
40
     return t;
41 | }
```

```
42 long long ret;
43
   int ctr;
   int cmp(const Point &a, const Point &b) { return a.x[ctr] < b.x[ctr]; }</pre>
44
45
   struct KDTree {
46
     Node *root;
     KDTree() { root = null; }
47
48
     KDTree(Point *a, int n) {
       root = build(a, 0, n - 1, 0);
49
50
     Node *build(Point *a, int l, int r, int depth) {
51
       if (1 > r) return null;
52
       ctr = depth;
53
       sort(a + 1, a + r + 1, cmp);
54
55
       int mid = (1 + r) >> 1;
56
       Node *t = newNode(a[mid], depth);
       t->set(build(a, l, mid - 1, (depth + 1) % d), 0);
57
58
       t->set(build(a, mid + 1, r, (depth + 1) % d), 1);
       t->update();
59
60
       return t;
61
62
     void tranverse(Node *t, Point *vec, int &tot) {
63
       if (t == null) return;
64
       vec[tot ++] = t->val;
       tranverse(t->ch[0], vec, tot);
65
       tranverse(t->ch[1], vec, tot);
66
67
68
     void rebuild(Node *t) {
69
       Node *p = t->p;
       int tot = 0;
70
71
       tranverse(t, buf, tot);
       Node *u = build(buf, 0, tot - 1, t->depth);
72
73
       p->set(u, t->dir());
       for( ; p != null; p = p->p) p->update();
74
75
       if (t == root) root = u;
76
77
     void insert(Point p) {
78
       if (root == null) { root = newNode(p, 0); return; }
       Node *cur = root, *last = null;
79
       int dir = 0;
80
81
       for( ; cur != null; ) {
82
         last = cur:
83
         dir = (p.x[cur->depth] > cur->val.x[cur->depth]);
         cur = cur->ch[dir];
84
85
86
       Node *t = newNode(p, (last->depth + 1) % d), *bad = null;
```

```
87
        last->set(t, dir);
 88
        for( ; t != null; t = t->p) {
 89
          t->update();
 90
          if (!t->balanced()) bad = t;
 91
        if (bad != null) rebuild(bad);
 92
 93
      long long calcEval(Point u, Node *t, int d) {
 94
        long long l = t \rightarrow minv.x[d], r = t \rightarrow maxv.x[d], x = u.x[d];
 95
 96
        if (x >= 1 && x <= r) return OLL;
        long long ret = min(abs(x - 1), abs(x - r));
 97
        return ret * ret;
 98
 99
      void updateAns(Point u, Point p) {
100
101
        // 在这里更新答案
      }
102
      void query(Node *t, Point p) {
103
        if (t == null) return;
104
        updateAns(t->val, p);
105
        long long evalLeft = calcEval(p, t->ch[0], t->depth);
106
107
        long long evalRight = calcEval(p, t->ch[1], t->depth);
        if (evalLeft <= evalRight) {</pre>
108
          query(t->ch[0], p);
109
          if (ret > evalRight) query(t->ch[1], p);
110
        } else {
111
          query(t->ch[1], p);
112
          if (ret > evalLeft) query(t->ch[0], p);
113
        }
114
115
116
      void query(Point p) {
        query(root, p);
117
118
      }
119 };
120
    void initNull() {
      totNode = nodePool;
121
122
      null = totNode ++;
      null->size = 0;
123
      for(int i = 0; i < d; ++ i) {
124
        null->maxv.x[i] = -INF;
125
126
        null->minv.x[i] = INF;
127
128 }
```

Splay Tree

```
1 // 注意初始化内存池和 null 节点
   struct Node{
    int rev,size; Node *ch[2],*p;
3
     void set(Node*,int); int dir(); void update(); void relax(); void appRev();
   } nodePool[MAX NODE],*curNode,*null;
   Node *newNode(){
     Node *t=curNode++; t->rev=0, t->size=1;
     t->ch[0]=t->ch[1]=t->p=null; return t;
9 }
10
   struct Splay{
     Node *root;
11
     Splay(){ root=newNode(); root->set(newNode(),0); root->update(); }
12
13
     void rot(Node *t){
       Node *p=t->p; int d=t->dir();
14
15
       p->relax(); t->relax();
16
       if(p==root) root=t;
       p->set(t->ch[!d],d); p->p->set(t,p->dir()); t->set(p,!d);
17
18
       p->update();
19
20
     void splay(Node *t,Node *f=null){
21
       for(t->relax();t->p!=f;)
22
         if(t->p->p==f) rot(t);
         else t->dir()==t->p->dir()?(rot(t->p),rot(t)):(rot(t),rot(t));
23
       t->update();
24
25
26
   void initNull(){ curNode=nodePool;null=curNode++;null->size=0; }
   void Node::set(Node *t,int d){ ch[ d]=t; t->p=this; }
29 int Node::dir(){ return this==p->ch[1]; }
   void Node::update(){ size=ch[0]->size+ch[1]->size+1;}
   void Node::relax(){ if(rev) ch[0]->appRev(), ch[1]->appRev(), rev=false; }
   void Node::appRev(){ if(this==null) return; rev^=true; swap(ch[0],ch[1]); }
```

Link Cut Tree

```
// 注意初始化 null 节点,单点的 is_root 初始为 true
struct Node{
Node *ch[2], *p;
int is_root, rev;
bool dir();
void set(Node*, bool);
void update();
void relax();
void app_rev();
} *null;
```

```
11 | void rot(Node *t){
     Node *p=t->p; bool d=t->dir();
12
     p->relax(); t->relax(); p->set(t->ch[!d],d);
13
     if(p->is_root) t->p=p->p,swap(p->is_root,t->is_root);
14
     else p->p->set(t,p->dir());
15
16
     t->set(p,!d); p->update();
17 }
18 | void splay(Node *t){
19
     for(t->relax();!t->is_root;)
20
       if(t->p->is_root) rot(t);
       else t->dir()==t->p->dir() ?(rot(t->p),rot(t)) :(rot(t),rot(t));
^{21}
     t->update();
22
23
24
   void access(Node *t){
     for(Node *s=null; t!=null; s=t,t=t->p){
25
26
       splay(t);
       if (t->p == null) { /*TODO*/ }
27
28
       t->ch[1]->is_root=true; s->is_root=false;
29
       t->ch[1]=s; t->update();
30
31
   bool Node::dir(){ return this==p->ch[1]; }
   void Node::set(Node *t,bool _d){ ch[_d]=t; t->p=this; }
34
   void Node::update(){ }
   void Node::app_rev(){ if (this == null) return; rev ^= true; swap(ch[0], ch[1]); }
   void Node::relax() { if(this==null) return; if (rev) { ch[0]->app_rev();
      37 | void make_root(Node *u) { access(u); splay(u); u->app_rev(); }
```

Dominator Tree

```
1 vector<int> prec[N], succ[N];
 2
 3 | vector<int> ord;
 5
   int stamp, vis[N];
 6
   int num[N];
 8
   int fa[N];
 9
10
11
   void dfs(int u) {
     vis[u] = stamp;
      num[u] = ord.size();
13
     ord.push_back(u);
14
      for (int i = 0; i < (int)succ[u].size(); ++i) {</pre>
15
```

```
16
        int v = succ[u][i];
       if (vis[v] != stamp) {
17
18
         fa[v] = u;
19
         dfs(v);
20
21
22
23
24
   int fs[N], mins[N];
25
26
   int dom[N], sem[N];
27
28
   int find(int u) {
29
     if (u != fs[u]) {
       int v = fs[u];
30
       fs[u] = find(fs[u]);
31
       if (mins[v] != -1 && num[sem[mins[v]]] < num[sem[mins[u]]]) {</pre>
32
         mins[u] = mins[v];
33
34
35
36
     return fs[u];
37
38
39
   void merge(int u, int v) {
40
     fs[u] = v;
41
42
   vector<int> buf[N];
43
44
45
   int buf2[N];
   void mark(int source) {
47
     ord.clear();
49
     ++stamp;
50
     dfs(source);
     for (int i = 0; i < (int)ord.size(); ++i) {</pre>
51
       int u = ord[i];
52
       fs[u] = u;
53
       mins[u] = -1;
54
       buf2[u] = -1;
55
56
     for (int i = (int)ord.size() - 1; i > 0; --i) {
57
       int u = ord[i], p = fa[u];
58
       sem[u] = p;
59
6o
       for (int j = 0; j < (int)prec[u].size(); ++j) {
```

```
61
          int v = prec[u][j];
62
          if (use[v] != stamp) {
63
            continue;
64
         }
65
          if (num[v] > num[u]) {
66
           find(v);
67
            v = sem[mins[v]];
68
69
          if (num[v] < num[sem[u]]) {</pre>
70
            sem[u] = v;
71
72
       buf[sem[u]].push_back(u);
73
74
       mins[u] = u;
75
       merge(u, p);
76
        while (buf[p].size()) {
         int v = buf[p].back();
77
78
         buf[p].pop_back();
         find(v);
79
80
         if (sem[v] == sem[mins[v]]) {
81
            dom[v] = sem[v];
82
         } else {
83
            buf2[v] = mins[v];
84
         }
85
86
87
      dom[ord[0]] = ord[0];
88
      for (int i = 0; i < (int)ord.size(); ++i) {</pre>
89
       int u = ord[i];
       if (~buf2[u]) {
90
          dom[u] = dom[buf2[u]];
91
       }
92
93
94 | }
```

DancingLinks

```
struct node{
  node *left,*right,*up,*down,*col; int row,cnt;
} *head,*col[MAXC],Node[MAXNODE],*ans[MAXNODE];
int totNode;

void insert(const std::vector<int> &V,int rownum){
  std::vector<node*> N;
  for(int i=0;i<int(V.size());++i){
    node* now=Node+(totNode++); now->row=rownum;
    now->col=now->up=col[V[i]], now->down=col[V[i]]->down;
```

```
10
       now->up->down=now, now->down->up=now;
11
       now->col->cnt++; N.push_back(now);
12
13
     for(int i=0;i<int(V.size());++i)</pre>
       N[i]->right=N[(i+1)%V.size()], N[i]->left=N[(i-1+V.size())%V.size()];
14
15
16
   void Remove(node *x){
     x->left->right=x->right, x->right->left=x->left;
17
18
     for(node *i=x->down;i!=x;i=i->down)
       for(node *j=i->right;j!=i;j=j->right)
19
         j->up->down=j->down, j->down->up=j->up, --(j->col->cnt);
20
^{21}
   void Resume(node *x){
22
     for(node *i=x->up;i!=x;i=i->up)
23
       for(node *j=i->left;j!=i;j=j->left)
24
         j->up->down=j->down->up=j, ++(j->col->cnt);
25
26
     x->left->right=x, x->right->left=x;
27
28
   bool search(int tot){
29
     if(head->right==head) return true;
     node *choose=NULL;
     for(node *i=head->right;i!=head;i=i->right){
31
       if(choose==NULL||choose->cnt>i->cnt) choose=i;
32
       if(choose->cnt<2) break;</pre>
33
34
     Remove(choose);
35
36
     for(node *i=choose->down;i!=choose;i=i->down){
       for(node *j=i->right;j!=i;j=j->right) Remove(j->col);
37
38
       ans[tot]=i;
39
       if(search(tot+1)) return true;
       ans[tot]=NULL;
40
       for(node *j=i->left;j!=i;j=j->left) Resume(j->col);
41
42
     Resume(choose);
43
     return false;
44
45
   void prepare(int totC){
     head=Node+totC;
47
     for(int i=0;i<totC;++i) col[i]=Node+i;</pre>
48
     totNode=totC+1;
49
     for(int i=0;i<=totC;++i){</pre>
50
       (Node+i)->right=Node+(i+1)%(totC+1);
51
        (Node+i)->left=Node+(i+totC)%(totC+1);
52
        (Node+i)->up=(Node+i)->down=Node+i;
53
54
```

55 | }

弦图相关

- 1. 团数 \leq 色数,弦图团数 = 色数
- 2. 设 next(v) 表示 N(v) 中最前的点 . 令 w* 表示所有满足 $A\in B$ 的 w 中最后的一个点,判断 $v\cup N(v)$ 是否为极大团 ,只需判断是否存在一个 w,满足 Next(w)=v 且 $|N(v)|+1\le |N(w)|$ 即可 .
- 3. 最小染色: 完美消除序列从后往前依次给每个点染色,给每个点染上可以染的最小的颜色
- 4. 最大独立集: 完美消除序列从前往后能选就选
- 5. 弦图最大独立集数 = 最小团覆盖数 , 最小团覆盖 : 设最大独立集为 $\{p_1,p_2,\dots,p_t\}$, 则 $\{p_1\cup N(p_1),\dots,p_t\cup N(p_t)\}$ 为最小团覆盖

图同构 Hash

$$F_t(i) = (F_{t-1}(i) \times A + \sum_{i \to j} F_{t-1}(j) \times B + \sum_{j \to i} F_{t-1}(j) \times C + D \times (i = a)) \mod P$$

枚举点 a 选代 K 次后求得的就是 a 点所对应的 hash 值 其中 K , A , B , C , D , P 为 hash 参数 , 可自选

环状最长公共子序列

```
1 int n, a[N << 1], b[N << 1];
2
3 | bool has(int i, int j) {
4
     return a[(i - 1) \% n] == b[(j - 1) \% n];
5
6
   const int DELTA[3][2] = \{\{0, -1\}, \{-1, -1\}, \{-1, 0\}\};
8
   int from[N][N];
10
   int solve() {
11
     memset(from, 0, sizeof(from));
12
     int ret = 0;
13
     for (int i = 1; i \le 2 * n; ++ i) {
14
       from[i][0] = 2;
15
16
       int left = 0, up = 0;
       for (int j = 1; j <= n; ++ j) {
17
18
         int upleft = up + 1 + !!from[i - 1][j];
         if (!has(i, j)) {
19
20
           upleft = INT MIN;
21
         int max = std::max(left, std::max(upleft, up));
22
         if (left == max) {
23
           from[i][j] = 0;
24
```

```
} else if (upleft == max) {
25
26
            from[i][j] = 1;
         } else {
27
28
            from[i][j] = 2;
         }
29
         left = max;
30
31
32
       if (i >= n) {
33
         int count = 0;
          for (int x = i, y = n; y;) {
34
           int t = from[x][y];
35
36
            count += t == 1;
           x += DELTA[t][0];
37
38
           y += DELTA[t][1];
39
          ret = std::max(ret, count);
40
          int x = i - n + 1;
          from[x][0] = 0;
42
         int y = 0;
43
         while (y \le n \&\& from[x][y] == 0) {
44
           y++;
45
46
          for (; x \le i; ++ x) \{
47
            from[x][y] = 0;
48
49
           if (x == i) {
50
              break;
51
            for (; y <= n; ++ y) {
52
              if (from[x + 1][y] == 2) {
53
54
                break;
55
56
              if (y + 1 \le n \& from[x + 1][y + 1] == 1) {
                y ++;
57
58
                break:
59
60
61
62
64
     return ret;
65
```

直线下有多少个格点

```
LL solve(LL n,LL a,LL b,LL m){
2 // 计算 for (int i=0;i<n;++i) s+=floor((a+b*i)/m)
```

```
//n.m.a.b>0
    if(b==0) return n*(a/m);
    if(a>=m) return n*(a/m)+solve(n,a%m,b,m);
    if(b>=m) return (n-1)*n/2*(b/m)+solve(n,a,b%m,m);
    return solve((a+b*n)/m,(a+b*n)%m,m,b);
8 }
```

费用流

```
1 // O is a priority queue<PII, vector<PII>, greater<PII> >
 2 \mid // for an edge(s, t): u is the capacity, v is the cost, nxt is the next edge,
 3 \mid // op is the opposite edge
 4 // this code can not deal with negative cycles
 5 typedef pair<int,int> PII;
 6 struct edge{ int t,u,v; edge *nxt,*op; }E[MAXE],*V[MAXV];
 7 int D[MAXN], dist[MAXN], maxflow, mincost; bool in[MAXN];
 8 | bool modlabel(){
     while(!Q.empty()) Q.pop();
     for(int i=S;i<=T;++i){</pre>
10
       if(in[i]) D[i]=0,Q.push(PII(0,i));
11
       else D[i]=inf;
12
     }
13
     while(!Q.empty()){
14
15
       int x=Q.top().first,y=Q.top().second;
16
       Q.pop();
17
       if(y==T) break;
18
       if(D[y]<x) continue;</pre>
       for(edge *ii=V[y];ii;ii=ii->nxt) if(ii->u){
19
         if(x+(ii->v+dist[ii->t]-dist[y])<D[ii->t]){
20
           D[ii->t]=x+(ii->v+dist[ii->t]-dist[y]);
21
           Q.push(PII(D[ii->t],ii->t));
22
         }
23
       }
24
25
26
     if(D[T]==inf) return false;
     for(int i=S;i<=T;++i) if(D[i]>D[T]) dist[i]+=D[T]-D[i];
27
     return true:
28
29
   int aug(int p,int limit){
     if(p==T) return maxflow+=limit,mincost+=limit*dist[S],limit;
31
     in[p]=1; int kk,ll=limit;
32
      for(edge *ii=V[p];ii;ii=ii->nxt) if(ii->u){
33
       if(!in[ii->t]&&dist[ii->t]+ii->v==dist[p]){
34
35
         kk=aug(ii->t,min(ii->u,ll));
36
         11-=kk,ii->u-=kk,ii->op->u+=kk;
37
         if(!ll) return in[p]=0,limit;
```

```
38
       }
39
     return limit-ll;
40
41
   PII mincostFlow(){
42
     for(int i=S;i<=T;++i) dist[i]=i==T?inf:0;</pre>
43
     while(!Q.empty()) Q.pop();
44
     Q.push(PII(0,T));
45
46
     while(!Q.empty()){
       int x=Q.top().first,y=Q.top().second;
47
48
       Q.pop();
       if(dist[y]<x) continue;</pre>
49
       for(edge *ii=V[y];ii;ii=ii->nxt) if(ii->op->u&&ii->v+x<dist[ii->t]{
50
51
         dist[ii->t]=ii->v+x;
52
         Q.push(PII(dist[ii->t],ii->t));
       }
53
54
     maxflow=mincost=0;
55
56
     do{
57
       do{
58
         memset(in,0,sizeof(in));
       }while(aug(S,maxflow));
59
60
     }while(modlabel());
61
     return PII(maxflow,mincost);
62 }
```

综合

定理 1: 最小覆盖数 = 最大匹配数 定理 2: 最大独立集 S 与 最小覆盖集 T 互补 算法:

- 1. 做最大匹配 . 没有匹配的空闲点 $\in S$
- 2. 如果 $u \in S$ 那么 u 的临点必然属于 T
- 3. 如果一对匹配的点中有一个属于 T 那么另外一个属于 S
- 4. 还不能确定的 . 把左子图的放入 S. 右子图放入 T

算法结束

上下界无源汇可行流 : 不用添 T->S, 判断是否流量平衡

上下界有源汇可行流 : 添 $T \to S$ (下界 0, 上界 ∞), 判断是否流量平衡

上下界最小流 : 不添 $T \to S$ 先流一遍 , 再添 $T \to S$ (下界 0, 上界 ∞) 在残图上流一遍 , 答案为 $S \to T$ 的流量值

上下界最大流: 添 $T \to S$ (下界 0, 上界 ∞)流一遍,再在残图上流一遍S到T的最大流,答案为前者的 $S \to T$ 的值 + 残图中 $S \to T$ 的最大流

```
Stirling 公式 n! = \sqrt{2\pi n} (\frac{n}{e})^n  |s(n,k)| = |s(n,0)| = 0, |s(1,1)| = 1, \\ |s(n,k)| = |s(n-1,k-1)| + (n-1)*|s(n-1,k)|  Stirling 数 第二类:n 个元素的项目分作 k 个环排列的方法数目  S(n,k) = |s(n-1,k-1)| + (n-1)*|s(n-1,k)|  第二类:n 个元素的项目分作 k 个环排列的方法数目
```

积分表

```
\frac{1}{1+x^2}dx = \tan^{-1}x \qquad \int \frac{1}{a^2+x^2}dx = \frac{1}{a}\tan^{-1}\frac{x}{a} \qquad \int \frac{x}{a^2+x^2}dx = \frac{1}{2}\ln|a^2+x^2| \qquad \int \frac{x^2}{a^2+x^2}dx = x - a\tan^{-1}\frac{x}{a} \qquad \int \frac{x^3}{a^2+x^2}dx = \frac{1}{2}x^2 - \frac{1}{2}a^2\ln|a^2+x^2|
Integrals with Roots \int \frac{x}{\sqrt{x\pm a}} dx = \frac{2}{3} (x\mp 2a) \sqrt{x\pm a} \qquad \int \sqrt{\frac{x}{a-x}} dx = -\sqrt{x(a-x)} - a \tan^{-1} \frac{\sqrt{x(a-x)}}{x-a} \qquad \int \sqrt{\frac{x}{a+x}} dx = \sqrt{x(a+x)} - a \ln\left[\sqrt{x} + \sqrt{x+a}\right] \qquad \int x \sqrt{x^2 \pm a^2} dx = \frac{1}{3} \left(x^2 \pm a^2\right)^{3/2} = -\sqrt{x(a-x)} - a \tan^{-1} \frac{\sqrt{x(a-x)}}{x-a} \qquad \int \sqrt{\frac{x}{a+x}} dx = \sqrt{x(a+x)} - a \ln\left[\sqrt{x} + \sqrt{x+a}\right] \qquad \int x \sqrt{x^2 \pm a^2} dx = \frac{1}{3} \left(x^2 \pm a^2\right)^{3/2} = -\sqrt{x(a-x)} - a \tan^{-1} \frac{\sqrt{x(a-x)}}{x-a} = -\sqrt{x(a-x)} - a \tan^{-1
\int x\sqrt{ax+b}dx = \frac{2}{15a^2}(-2b^2 + abx + 3a^2x^2)\sqrt{ax+b} \qquad \int \sqrt{x(ax+b)}dx = \frac{1}{4a^2}\left[(2ax+b)\sqrt{ax(ax+b)} - b^2\ln\left|a\sqrt{x} + \sqrt{a(ax+b)}\right|\right] \qquad \int \sqrt{x^2\pm a^2}dx = \frac{1}{2}x\sqrt{x^2\pm a^2}\pm \frac{1}{2}a^2\ln\left|x + \sqrt{x^2\pm a^2}\right| + \frac{1}{2}a^2\ln\left|x + \sqrt{a(ax+b)}\right|
\int \sqrt{x^3(ax+b)}dx = \left[\frac{b}{12a} - \frac{b^2}{8a^2x} + \frac{x}{3}\right] \sqrt{x^3(ax+b)} + \frac{b^3}{8a^5/2} \ln\left|a\sqrt{x} + \sqrt{a(ax+b)}\right| \qquad \int \sqrt{a^2 - x^2}dx = \frac{1}{2}x\sqrt{a^2 - x^2} + \frac{1}{2}a^2 \tan^{-1}\frac{x}{\sqrt{a^2 - x^2}}dx = \frac{1}{2}x\sqrt{x^2 \pm a^2} \mp \frac{1}{2}a^2 \ln\left|x + \sqrt{x^2 \pm a^2}\right| + \frac{1}
\int \frac{1}{\sqrt{x^2 \pm a^2}} dx = \ln \left| x + \sqrt{x^2 \pm a^2} \right| \int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1} \frac{x}{a} \int \frac{x}{\sqrt{x^2 \pm a^2}} dx = \sqrt{x^2 \pm a^2} \int \frac{x}{\sqrt{a^2 - x^2}} dx = -\sqrt{a^2 - x^2} \int \sqrt{ax^2 + bx + c} dx = \frac{b + 2ax}{4a} \sqrt{ax^2 + bx + c} + \frac{4ac - b^2}{8a^{3/2}} \ln \left| 2ax + b + 2\sqrt{a(ax^2 + bx + c)} \right| = -\sqrt{a^2 - x^2} \int \sqrt{ax^2 + bx + c} dx = \frac{b + 2ax}{4a} \sqrt{ax^2 + bx + c} + \frac{4ac - b^2}{8a^{3/2}} \ln \left| 2ax + b + 2\sqrt{a(ax^2 + bx + c)} \right| = -\sqrt{a^2 - x^2}
 \int x\sqrt{ax^2 + bx + c} = \frac{1}{48a^{5/2}} \left( 2\sqrt{a}\sqrt{ax^2 + bx + c} \times \left( -3b^2 + 2abx + 8a(c + ax^2) \right) \right) + 3(b^3 - 4abc) \ln \left| b + 2ax + 2\sqrt{a}\sqrt{ax^2 + bx + c} \right| 
\int \frac{1}{\sqrt{ax^2 + bx + c}} dx = \frac{1}{\sqrt{a}} \ln \left| 2ax + b + 2\sqrt{a(ax^2 + bx + c)} \right|
\int \frac{x}{\sqrt{ax^2 + bx + c}} dx = \frac{1}{a} \sqrt{ax^2 + bx + c} - \frac{b}{2a^{3/2}} \ln \left| 2ax + b + 2\sqrt{a(ax^2 + bx + c)} \right| \qquad \int \frac{dx}{(a^2 + x^2)^{3/2}} = \frac{x}{a^2 \sqrt{a^2 + x^2}} \qquad \text{Integrals with Logarithms} \qquad \int \ln(ax + b) dx = \left(x + \frac{b}{a}\right) \ln(ax + b) - x, a \neq 0
\int \frac{\ln ax}{x} dx = \frac{1}{2} (\ln ax)^2 \qquad \int \ln(x^2 + a^2) dx = x \ln(x^2 + a^2) + 2a \tan^{-1} \frac{x}{a} - 2x \qquad \int \ln(x^2 - a^2) dx = x \ln(x^2 - a^2) + a \ln \frac{x+a}{x-a} - 2x \qquad \int x \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b) dx = \frac{bx}{2a} - \frac{bx}{2a} + \frac{bx}{2a} - \frac{bx}{2a} + \frac{bx}{2a
\int \ln\left(ax^2 + bx + c\right) dx = \frac{1}{a}\sqrt{4ac - b^2} \tan^{-1} \frac{2ax + b}{\sqrt{4ac - b^2}} - 2x + \left(\frac{b}{2a} + x\right) \ln\left(ax^2 + bx + c\right) \qquad \int x \ln\left(a^2 - b^2x^2\right) dx = -\frac{1}{2}x^2 + \frac{1}{2}\left(x^2 - \frac{a^2}{b^2}\right) \ln\left(a^2 - b^2x^2\right) dx
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Integrals with Exponentials
\int x^n e^{ax} dx = \frac{x^n e^{ax}}{a} - \frac{n}{a} \int x^{n-1} e^{ax} dx
\int x e^{-ax^2} dx = -\frac{1}{2a} e^{-ax^2}
\int \cos^3 ax dx = \frac{3\sin ax}{4a} + \frac{\sin 3ax}{12a}
\int \cos ax \sin bx dx = \frac{\cos(a-b)x}{2(a-b)} - \frac{\cos((a+b)x)}{2(a+b)}, a \neq b
\int \sin^2 ax \cos bx dx = -\frac{\sin(2a-b)x}{4(2a-b)} + \frac{\sin bx}{2b} - \frac{\sin(2a+b)x}{4(2a+b)}
\int \sin^2 x \cos x dx = \frac{1}{3} \sin^3 x
\int \cos^2 ax \sin bx dx = \frac{\cos[(2a-b)x]}{4(2a-b)} - \frac{\cos bx}{2b} - \frac{\cos[(2a+b)x]}{4(2a+b)} \quad \int \cos^2 ax \sin ax dx = -\frac{1}{3a} \cos^3 ax \quad \int \sin^2 ax \cos^2 bx dx = \frac{x}{4} - \frac{\sin (2a-b)x}{8a} - \frac{\sin (2(a-b)x)}{16(a-b)} + \frac{\sin 2bx}{8b} - \frac{\sin (2(a+b)x)}{16(a+b)} \quad \int \sin^2 ax \cos^2 ax dx = \frac{x}{8} - \frac{\sin 4ax}{32a} + \frac{\sin 2bx}{32a} +
\int \tan ax dx = -\frac{1}{2} \ln \cos ax \qquad \int \tan^2 ax dx = -x + \frac{1}{2} \tan ax \qquad \int \tan^3 ax dx = \frac{1}{2} \ln \cos ax + \frac{1}{22} \sec^2 ax \qquad \int \sec^2 x dx = \ln |\sec x + \tan x| = 2 \tanh^{-1} \left(\tan \frac{x}{2}\right) \qquad \int \sec^2 ax dx = \frac{1}{2} \tan ax
\int \sec^3 x \, dx = \frac{1}{2} \sec x \tan x + \frac{1}{2} \ln|\sec x + \tan x|
\int \sec x \tan x \, dx = \sec x
\int \sec^2 x \tan x \, dx = \frac{1}{2} \sec^2 x
\int \sec^n x \tan x \, dx = \frac{1}{2} \sec^n x, n \neq 0
\int \csc x \, dx = \ln|\tan \frac{x}{2}| = \ln|\csc x - \cot x| + C
 \int \csc^2 ax dx = -\frac{1}{a} \cot ax \int \csc^3 x dx = -\frac{1}{2} \cot x \csc x + \frac{1}{2} \ln|\csc x - \cot x| \int \csc^n x \cot x dx = -\frac{1}{a} \csc^n x, n \neq 0 \int \sec x \csc x dx = \ln|\tan x|  Products of Trigonometric Functions and Monomials
 \int x \cos x dx = \cos x + x \sin x
\int x \cos ax dx = \frac{1}{a^2} \cos ax + \frac{x}{a} \sin ax
\int x^2 \cos x dx = 2x \cos x + (x^2 - 2) \sin x
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        \int x^2 \cos ax dx = \frac{2x \cos ax}{a^2} + \frac{a^2 x^2 - 2}{a^3} \sin ax
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                \int x \sin x dx = -x \cos x + \sin x
\int x \sin ax dx = -\frac{x \cos ax}{a} + \frac{\sin ax}{a^2} \qquad \int x^2 \sin x dx = \left(2 - x^2\right) \cos x + 2x \sin x \qquad \int x^2 \sin ax dx = \frac{2 - a^2 x^2}{a^3} \cos ax + \frac{2x \sin ax}{a^2}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           Products of Trigonometric Functions and Exponentials
 \int e^x \sin x dx = \frac{1}{2} e^x (\sin x - \cos x) \qquad \qquad \int e^{bx} \sin ax dx = \frac{1}{a^2 + b^2} e^{bx} (b \sin ax - a \cos ax) \qquad \qquad \int e^{bx} \cos ax dx = \frac{1}{a^2 + b^2} e^{bx} (a \sin ax + b \cos ax) \qquad \qquad \int x e^x \sin x dx = \frac{1}{2} e^x (\cos x - x \cos x + x \sin x)
 \int xe^x \cos x dx = \frac{1}{2}e^x (x \cos x - \sin x + x \sin x) \quad \int e^x \cos x dx = \frac{1}{2}e^x (\sin x + \cos x)
```

Java

```
import java.io.*;
import java.util.*;
import java.math.*;

public class Main{
    BufferedReader reader = new BufferedReader(new InputStreamReader(System.in));
    PrintWriter writer = new PrintWriter(System.out);
```

```
8  StringTokenizer tokenizer = null;
9
10  void solve() throws Exception {
11  }
12  void run()throws Exception{
13  try{
14  while (true) {
15  solve();
```

```
16
         }
17
       }
18
       catch(Exception e){
19
20
       finally{
         reader.close();
^{21}
         writer.close();
22
23
       }
24
     String next()throws Exception{
25
26
       for(;tokenizer == null || !tokenizer.hasMoreTokens();){
         tokenizer = new StringTokenizer(reader.readLine());
27
28
       }
       return tokenizer.nextToken();
29
30
     int nextInt()throws Exception{
31
       return Integer.parseInt(next());
32
33
     double nextDouble()throws Exception{
34
       return Double.parseDouble(next());
35
36
     BigInteger nextBigInteger()throws Exception{
37
       return new BigInteger(next());
38
     }
39
     public static void main(String args[])throws Exception{
```

```
41 (new Main()).run();
42 }
43 }
```

Vimrc

```
1 \begin{lstlisting}
2 set nu ai ci si mouse=a ts=4 sts=4 sw=4
3
   nmap<C-A> ggVG
   vmap<C-C> "+y
   nmap<F3> : vs %<.in <CR>
   nmap<F5> : !./%< <CR>
   nmap<F8> : !./%< < %<.in <CR>
10 nmap<F9> : !g++ % -o %< -Wall <CR>
11
   "nmap<F4> : !gedit % <CR>
   "autocmd BufNewFile *.cpp 0r ~/temp.cpp
13
   "set hlsearch incseach
15
16
   "syntax on
   "filetype plugin indent on
17
18 \end{lstlisting}
```