Dracarys

Team Referrence Library

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Contents

多边形与圆面积交

```
double areaCT(Point pa, Point pb, double r) {
  if (pa.len() < pb.len()) swap(pa, pb);
  if (sign(pb.len()) == 0) return 0;
  double a = pb.len(), b = pa.len(), c = (pb - pa).len();
  double sinB = fabs(det(pb, pb - pa) / a / c),
       cosB = dot(pb, pb - pa) / a / c,
       sinC = fabs(det(pa, pb) / a/ b),
       cosC = dot(pa, pb) / a / b;
  double B = atan2(sinB, cosB), C = atan2(sinC, cosC);
  if (a > r) {
    S = C / 2 * r * r;
    h = a * b * sinC / c;
    if (h < r && B < PI / 2) {
      S -= (acos(h / r) * r * r - h * sqrt(r * r - h * h));
    }
  } else if (b > r) {
    double theta = PI - B - asin(sinB / r * a);
    S = a * r * sin(theta) / 2 + (C - theta) / 2 * r * r;
  } else {
    S = sinC * a * b / 2;
  }
  return S;
}
```

二维几何

```
#include <iostream>
#include <cmath>
#include <vector>

using namespace std;

const double PI = acos(-1.0);
const double EPS = 1e-8;

int sign(double x)
{
  return x < -EPS ? -1 : x > EPS;
}

double newSqrt(double x)
{
  return x < 0 ? 0 : sqrt(x);
}

struct Point {
  double x, y;
  Point(double x = 0, double y = 0) : x(x), y(y) {}
  Point operator + (const Point &that) const {
    return Point(x + that.x, y + that.y);
  }
  Point operator - (const Point &that) const {
    return Point(x - that.x, y - that.y);
  }
  Point operator * (const double &that) const {
    return Point(x * that, y * that);
  }
  Point operator / (const double &that) const {
    return Point(x / that, y / that);
  }
  Point rotate(const double ang) { // 逆时针旋转 ang 弧度
    return Point(cos(ang) * x - sin(ang) * y, cos(ang) * y + sin(ang) * x);
  }
  Point turn90() { // 逆时针旋转 90 度
    return Point(-y, x);
  }
  double len2() const {
    return x * x + y * y;
  }
  double len() const {
    return sqrt(x * x + y * y);
  }
  Point unit() const {
    return *this / len();
  }
  int operator < (const Point &that) const {
    int d = sign(x - that.x); if (d) return d < 0;
    return sign(y - that.y) < 0;
  }
};
double det(Point a, Point b)
{
  return a.x * b.y - b.x * a.y;
}
double dot(Point a, Point b)
{
  return a.x * b.x + a.y * b.y;
}
double det(Point s, Point a, Point b)
{
```

```
  return (a.x - s.x) * (b.y - s.y) - (b.x - s.x) * (a.y - s.y);
}

struct Line {
  Point a, b;
  Line(Point a, Point b) : a(a), b(b) {}
};

Point isLL(const Line &l1, const Line &l2) {
  double s1 = det(l2.b - l2.a, l1.a - l2.a),
       s2 = -det(l2.b - l2.a, l1.b - l2.a);
  return (l1.a * s2 + l1.b * s1) / (s1 + s2);
}
bool onSeg(const Line &l, const Point &p) { // 点在线段上
  return sign(det(p - l.a, l.b - l.a)) == 0 && sign(dot(p - l.a, p - l.b)) <= 0;
}
Point projection(const Line &l, const Point &p) { // 点到直线投影
  return l.a + (l.b - l.a) * (dot(p - l.a, l.b - l.a) / (l.b - l.a).len2());
}
double disToLine(const Line &l, const Point &p) {
  return abs(det(p - l.a, l.b - l.a) / (l.b - l.a).len());
}
double disToSeg(const Line &l, const Point &p) { // 点到线段距离
  return sign(dot(p - l.a, l.b - l.a)) * sign(dot(p - l.b, l.a - l.b)) != 1 ?
    disToLine(l, p) : min((p - l.a).len(), (p - l.b).len());
}
Point symmetryPoint(const Point a, const Point b) { // 点 b 关于点 a 的中心对称点
  return a + a - b;
}
Point reflection(const Line &l, const Point &p) { // 点关于直线的对称点
  return symmetryPoint(projection(l, p), p);
}
struct Circle {
  Point o;
  double r;
  Circle (Point o = Point(0, 0), double r = 0) : o(o), r(r) {}
};

// 求圆与直线的交点
bool isCL(Circle a, Line l, Point &p1, Point &p2) {
  if (sign(det(l.a - a.o, l.b - a.o) / (l.a - l.b).len()) > 0) return false;
  Point o = isLL(Line(a.o, a.o + (l.b - l.a).turn90()), l);
  Point delta = (l.b - l.a).unit() * newSqrt(a.r * a.r - (o - a.o).len2());
  p1 = o + delta;
  p2 = o - delta;
  return true;
}

// 求圆与圆的交面积
double areaCC(const Circle &c1, const Circle &c2) {
  double d = (c1.o - c2.o).len();
  if (sign(d - (c1.r + c2.r)) >= 0) {
    return 0;
  }
  if (sign(d - abs(c1.r - c2.r)) <= 0) {
    double r = min(c1.r, c2.r);
    return r * r * PI;
  }
  double x = (d * d + c1.r * c1.r - c2.r * c2.r) / (2 * d),
       t1 = acos(x / c1.r), t2 = acos((d - x) / c2.r);
  return c1.r * c1.r * t1 + c2.r * c2.r * t2 - d * c1.r * sin(t1);
}

// 求圆与圆的交点，注意调用前要先判定重圆
bool isCC(Circle a, Circle b, Point &p1, Point &p2) {
  double s1 = (a.o - b.o).len();
  if (sign(s1 - a.r - b.r) > 0 || sign(s1 - abs(a.r - b.r)) < 0) return false;
  double s2 = (a.r * a.r - b.r * b.r) / s1;
  double aa = (s1 + s2) * 0.5, bb = (s1 - s2) * 0.5;
  Point o = (b.o - a.o) * (aa / (aa + bb)) + a.o;
  Point delta = (b.o - a.o).unit().turn90() * newSqrt(a.r * a.r - aa * aa);
  p1 = o + delta, p2 = o - delta;
  return true;
}

// 求点到圆的切点，按关于点的左手方向返回两个点
bool tanCP(const Circle &c, const Point &p0, Point &p1, Point &p2)
{
  double x = (p0 - c.o).len2(), d = x - c.r * c.r;
  if (d < EPS) return false;
  Point p = (p0 - c.o) * (c.r * c.r / x);
  Point delta = ((p0 - c.o) * (-c.r * sqrt(d) / x)).turn90();
  p1 = c.o + p + delta;
  p2 = c.o + p - delta;
  return true;
}

// 求圆到圆的外共切线，按关于 c1.o 的左手方向返回两条线
vector<Line> extanCC(const Circle &c1, const Circle &c2)
{
```

```
  vector<Line> ret;
  if (sign(c1.r - c2.r) == 0) {
    Point dir = c2.o - c1.o;
    dir = (dir * (c1.r / dir.len())).turn90();
    ret.push_back(Line(c1.o + dir, c2.o + dir));
    ret.push_back(Line(c1.o - dir, c2.o - dir));
  } else {
    Point p = (c1.o * -c2.r + c2.o * c1.r) / (c1.r - c2.r);
    Point p1, p2, q1, q2;
    if (tanCP(c1, p, p1, p2) && tanCP(c2, p, q1, q2)) {
      if (c1.r < c2.r) swap(p1, p2), swap(q1, q2);
      ret.push_back(Line(p1, q1));
      ret.push_back(Line(p2, q2));
    }
  }
  return ret;
}

// 求圆到圆的内共切线，按关于 c1.o 的左手方向返回两条线
vector<Line> intanCC(const Circle &c1, const Circle &c2)
{
  vector<Line> ret;
  Point p = (c1.o * c2.r + c2.o * c1.r) / (c1.r + c2.r);
  Point p1, p2, q1, q2;
  if (tanCP(c1, p, p1, p2) && tanCP(c2, p, q1, q2)) {
    ret.push_back(Line(p1, q1));
    ret.push_back(Line(p2, q2));
  }
  return ret;
}

bool contain(vector<Point> polygon, Point p) { // 判断点 p
  ↪ 是否被多边形包含，包括落在边界上
  int ret = 0, n = polygon.size();
  for(int i = 0; i < n; ++ i) {
    Point u = polygon[i], v = polygon[(i + 1) % n];
    if (onSeg(Line(u, v), p)) return true;
    if (sign(u.y - v.y) <= 0) swap(u, v);
    if (sign(p.y - u.y) > 0 || sign(p.y - v.y) <= 0) continue;
    ret += sign(det(p, v, u)) > 0;
  }
  return ret & 1;
}

vector<Point> convexCut(const vector<Point>&ps, Line l) { // 用半平面 (q1,q2)
  ↪ 的逆时针方向去切凸多边形
  vector<Point> qs;
  int n = ps.size();
  for (int i = 0; i < n; ++i) {
    Point p1 = ps[i], p2 = ps[(i + 1) % n];
    int d1 = sign(det(l.a, l.b, p1)), d2 = sign(det(l.a, l.b, p2));
    if (d1 >= 0) qs.push_back(p1);
    if (d1 * d2 < 0) qs.push_back(isLL(Line(p1, p2), l));
  }
  return qs;
}
vector<Point> convexHull(vector<Point> ps) { // 求点集 ps 组成的凸包
  int n = ps.size(); if (n <= 1) return ps;
  sort(ps.begin(), ps.end());
  vector<Point> qs;
  for (int i = 0; i < n; qs.push_back(ps[i++]))
    while (qs.size() > 1 && sign(det(qs[qs.size()-2],qs.back(),ps[i])) <= 0)
    ↪ qs.pop_back();
  for (int i = n - 2, t = qs.size(); i >= 0; qs.push_back(ps[i--]))
    while ((int)qs.size() > t && sign(det(qs[(int)qs.size()-2],qs.back(),ps[i])) <=
    ↪ 0) qs.pop_back();
  qs.pop_back(); return qs;
}

int main()
{
  Circle c1, c2;
  c1.o = Point(0, 0); c1.r = 10;
  c2.o = Point(10, 10); c1.r = 10;
  Point p1, p2;
  return 0;
}
```

$n \log n$ 半平面交

```
struct Point {
  int quad() const { return sign(y) == 1 || (sign(y) == 0 && sign(x) >= 0);}
};
struct Line {
  bool include(const Point &p) const { return sign(det(b - a, p - a)) > 0; }
  Line push() const{ // 将半平面向外推 eps
    const double eps = 1e-6;
    Point delta = (b - a).turn90().norm() * eps;
    return Line(a - delta, b - delta);
  }
};
```

```
bool sameDir(const Line &l0, const Line &l1) { return parallel(l0, l1) &&
  ↪ sign(dot(l0.b - l0.a, l1.b - l1.a)) == 1; }
bool operator < (const Point &a, const Point &b) {
  if (a.quad() != b.quad()) {
    return a.quad() < b.quad();
  } else {
    return sign(det(a, b)) > 0;
  }
}
bool operator < (const Line &l0, const Line &l1) {
  if (sameDir(l0, l1)) {
    return l1.include(l0.a);
  } else {
    return (l0.b - l0.a) < (l1.b - l1.a);
  }
}
bool check(const Line &u, const Line &v, const Line &w) { return
  ↪ w.include(intersect(u, v)); }
vector<Point> intersection(vector<Line> &l) {
  sort(l.begin(), l.end());
  deque<Line> q;
  for (int i = 0; i < (int)l.size(); ++i) {
    if (i && sameDir(l[i], l[i - 1])) {
      continue;
    }
    while (q.size() > 1 && !check(q[q.size() - 2], q[q.size() - 1], l[i]))
  ↪ q.pop_back();
    while (q.size() > 1 && !check(q[1], q[0], l[i])) q.pop_front();
    q.push_back(l[i]);
  }
  while (q.size() > 2 && !check(q[q.size() - 2], q[q.size() - 1], q[0]))
  ↪ q.pop_back();
  while (q.size() > 2 && !check(q[1], q[0], q[q.size() - 1])) q.pop_front();
  vector<Point> ret;
  for (int i = 0; i < (int)q.size(); ++i) ret.push_back(intersect(q[i], q[(i + 1) %
  ↪ q.size()]));
  return ret;
}
```

Delaunay 三角剖分

```
/*
Delaunay Triangulation 随机增量算法 :
节点数至少为点数的 6 倍，空间消耗较大注意计算内存使用
建图的过程在 build 中，注意初始化内存池和初始三角形的坐标范围 (Triangulation::LOTS)
Triangulation::find 返回包含某点的三角形
Triangulation::add_point 将某点加入三角剖分
某个 Triangle 在三角剖分中当且仅当它的 has_children 为 0
如果要找到三角形 u 的邻域，则枚举它的所有 u.edge[i].tri，该条边的两个点为 u.p[(i+1)%3],
  ↪ u.p[(i+2)%3]
*/
const int N = 100000 + 5, MAX_TRIS = N * 6;
const double EPSILON = 1e-6, PI = acos(-1.0);
struct Point {
  double x,y; Point():x(0),y(0){} Point(double x, double y):x(x),y(y){}
  bool operator ==(Point const& that)const {return x==that.x&&y==that.y;}
};
inline double sqr(double x) { return x*x; }
double dist_sqr(Point const& a, Point const& b){return sqr(a.x-b.x)+sqr(a.y-b.y);}
bool in_circumcircle(Point const& p1, Point const& p2, Point const& p3, Point const&
  ↪ p4) {
  double u11 = p1.x - p4.x, u21 = p2.x - p4.x, u31 = p3.x - p4.x;
  double u12 = p1.y - p4.y, u22 = p2.y - p4.y, u32 = p3.y - p4.y;
  double u13 = sqr(p1.x) - sqr(p4.x) + sqr(p1.y) - sqr(p4.y);
  double u23 = sqr(p2.x) - sqr(p4.x) + sqr(p2.y) - sqr(p4.y);
  double u33 = sqr(p3.x) - sqr(p4.x) + sqr(p3.y) - sqr(p4.y);
  double det = -u13*u22*u31 + u12*u23*u31 + u13*u21*u32 - u11*u23*u32 - u12*u21*u33
  ↪ + u11*u22*u33;
  return det > EPSILON;
}
double side(Point const& a, Point const& b, Point const& p) { return
  ↪ (b.x-a.x)*(p.y-a.y) - (b.y-a.y)*(p.x-a.x);}
typedef int SideRef; struct Triangle; typedef Triangle* TriangleRef;
struct Edge {
  TriangleRef tri; SideRef side; Edge() : tri(0), side(0) {}
  Edge(TriangleRef tri, SideRef side) : tri(tri), side(side) {}
};
struct Triangle {
  Point p[3]; Edge edge[3]; TriangleRef children[3]; Triangle() {}
  Triangle(Point const& p0, Point const& p1, Point const& p2) {
    p[0]=p0;p[1]=p1;p[2]=p2;children[0]=children[1]=children[2]=0;
  }
  bool has_children() const { return children[0] != 0; }
  int num_children() const {
    return children[0] == 0 ? 0
      : children[1] == 0 ? 1
      : children[2] == 0 ? 2 : 3;
  }
  bool contains(Point const& q) const {
    double a=side(p[0],p[1],q), b=side(p[1],p[2],q), c=side(p[2],p[0],q);
    return a >= -EPSILON && b >= -EPSILON && c >= -EPSILON;
```

```
  }
} triange_pool[MAX_TRIS], *tot_triangles;
void set_edge(Edge a, Edge b) {
  if (a.tri) a.tri->edge[a.side] = b;
  if (b.tri) b.tri->edge[b.side] = a;
}
class Triangulation {
  public:
    Triangulation() {
      const double LOTS = 1e6;
      the_root = new(tot_triangles++)
    ↪ Triangle(Point(-LOTS,-LOTS),Point(+LOTS,-LOTS),Point(0,+LOTS));
    }
    TriangleRef find(Point p) const { return find(the_root,p); }
    void add_point(Point const& p) { add_point(find(the_root,p),p); }
  private:
    TriangleRef the_root;
    static TriangleRef find(TriangleRef root, Point const& p) {
      for( ; ; ) {
        if (!root->has_children()) return root;
        else for (int i = 0; i < 3 && root->children[i] ; ++i)
            if (root->children[i]->contains(p))
              {root = root->children[i]; break;}
      }
    }
    void add_point(TriangleRef root, Point const& p) {
      TriangleRef tab,tbc,tca;
      tab = new(tot_triangles++) Triangle(root->p[0], root->p[1], p);
      tbc = new(tot_triangles++) Triangle(root->p[1], root->p[2], p);
      tca = new(tot_triangles++) Triangle(root->p[2], root->p[0], p);
      set_edge(Edge(tab,0),Edge(tbc,1));set_edge(Edge(tbc,0),Edge(tca,1));
      set_edge(Edge(tca,0),Edge(tab,1));set_edge(Edge(tab,2),root->edge[2]);
      set_edge(Edge(tbc,2),root->edge[0]);set_edge(Edge(tca,2),root->edge[1]);
      root->children[0]=tab;root->children[1]=tbc;root->children[2]=tca;
      flip(tab,2); flip(tbc,2); flip(tca,2);
    }
    void flip(TriangleRef tri, SideRef pi) {
      TriangleRef trj = tri->edge[pi].tri; int pj = tri->edge[pi].side;
      if(!trj||!in_circumcircle(tri->p[0],tri->p[1],tri->p[2],trj->p[pj])) return;
      TriangleRef trk = new(tot_triangles++) Triangle(tri->p[(pi+1)%3], trj->p[pj],
    ↪ tri->p[pi]);
      TriangleRef trl = new(tot_triangles++) Triangle(trj->p[(pj+1)%3], tri->p[pi],
    ↪ trj->p[pj]);
      set_edge(Edge(trk,0), Edge(trl,0));
      set_edge(Edge(trk,1), tri->edge[(pi+2)%3]); set_edge(Edge(trk,2),
    ↪ trj->edge[(pj+1)%3]);
      set_edge(Edge(trl,1), trj->edge[(pj+2)%3]); set_edge(Edge(trl,2),
    ↪ tri->edge[(pi+1)%3]);
      tri->children[0]=trk;tri->children[1]=trl;tri->children[2]=0;
      trj->children[0]=trk;trj->children[1]=trl;trj->children[2]=0;
      flip(trk,1); flip(trk,2); flip(trl,1); flip(trl,2);
    }
};
int n; Point ps[N];
void build(){
  tot_triangles = triange_pool; cin >> n;
  for(int i = 0; i < n; ++ i) scanf("%lf%lf",&ps[i].x,&ps[i].y);
  random_shuffle(ps, ps + n); Triangulation tri;
  for(int i = 0; i < n; ++ i) tri.add_point(ps[i]);
}
```

三维几何操作合并

```
struct Point3D {
  double x, y, z;
};
Point3D det(const Point3D &a, const Point3D &b) {
  return Point3D(a.y * b.z - a.z * b.y, a.z * b.x - a.x * b.z, a.x * b.y - a.y *
  ↪ b.x);
}
// 平面法向量 : 平面上两个向量叉积
// 点共平面 : 平面上一点与之的向量点积法向量为 0
// 点在线段 ( 直线 ) 上 : 共线且两边点积非正
// 点在三角形内 ( 不包含边界, 需再判断是与某条边共线 )
bool pointInTri(const Point3D &a, const Point3D &b, const Point3D &c, const Point3D
  ↪ &p) {
  return sign(det(a - b, a - c).len() - det(p - a, p - b).len() - det(p - b, p -
  ↪ c).len() - det(p - c, p - a).len()) == 0;
}
// 共平面的两点是否在这平面上一条直线的同侧
bool sameSide(const Point3D &a, const Point3D &b, const Point3D &p0, const Point3D
  ↪ &p1) {
  return sign(dot(det(a - b, p0 - b), det(a - b, p1 - b))) > 0;
}
// 两点在平面同侧 : 点积法向量符号相同
// 两直线平行 / 垂直 : 同二维
// 平面平行 / 垂直 : 判断法向量
// 线面垂直 : 法向量和直线平行
// 判断空间线段是否相交 : 四点共面两线段不平行相互在异侧
// 线段和三角形是否相交 : 线段在三角形平面不同侧
  ↪ 三角形任意两点在线段和第三点组成的平面的不同侧
```

```cpp
// 求空间直线交点
Point3D intersection(const Point3D &a0, const Point3D &b0, const Point3D &a1, const Point3D &b1) {
  double t = ((a0.x - a1.x) * (a1.y - b1.y) - (a0.y - a1.y) * (a1.x - b1.x)) / ((a0.x - b0.x) * (a1.y - b1.y) - (a0.y - b0.y) * (a1.x - b1.x));
  return a0 + (b0 - a0) * t;
}
// 求平面和直线的交点
Point3D intersection(const Point3D &a, const Point3D &b, const Point3D &c, const Point3D &l0, const Point3D &l1) {
  Point3D p = pVec(a, b, c); // 平面法向量
  double t = (p.x * (a.x - l0.x) + p.y * (a.y - l0.y) + p.z * (a.z - l0.z)) / (p.x * (l1.x - l0.x) + p.y * (l1.y - l0.y) + p.z * (l1.z - l0.z));
  return l0 + (l1 - l0) * t;
}
// 求平面交线 : 取不平行的一条直线的一个交点，以及法向量叉积得到直线方向
// 点到直线距离 : 叉积得到三角形的面积除以底边
// 点到平面距离 : 点积法向量
// 直线间距离 : 平行时随便取一点求距离，否则叉积方向向量得到方向点积计算长度
// 直线夹角 : 点积 平面夹角 : 法向量点积
// 三维向量旋转操作(绕向量 s 旋转 ang 角度)，对于右手系 s 指向观察者时逆时针
// 矩阵版
void rotate(const Point3D &s, double ang) {
  double l = s.len(), x = s.x / l, y = s.y / l, z = s.z / l, sinA = sin(ang), cosA = cos(ang);
  double p[4][4]= {CosA + (1 - CosA) * x * x, (1 - CosA) * x * y - SinA * z, (1 - CosA) * x * z + SinA * y, 0,
    (1 - CosA) * y * x + SinA * z, CosA + (1 - CosA) * y * y, (1 - CosA) * y * z - SinA * x, 0,
    (1 - CosA) * z * x - SinA * y, (1 - CosA) * z * y + SinA * x, CosA + (1 - CosA) * z * z, 0,
    0, 0, 0, 1 };
}
// 计算版 : 把需要旋转的向量按照 s 分解，做二维旋转，再回到三维
```

三维凸包

```cpp
#define SIZE(X) (int(X.size()))
#define PI 3.14159265358979323846264338327950288
struct Point {
  Point cross(const Point &p) const
  { return Point(y * p.z - z * p.y, z * p.x - x * p.z, x * p.y - y * p.x); }
} info[1005];
int mark[1005][1005],n, cnt;;
double mix(const Point &a, const Point &b, const Point &c)
{ return a.dot(b.cross(c)); }
double area(int a, int b, int c)
{ return ((info[b] - info[a]).cross(info[c] - info[a])).length(); }
double volume(int a, int b, int c, int d)
{ return mix(info[b] - info[a], info[c] - info[a], info[d] - info[a]); }
struct Face {
  int a, b, c; Face() {}
  Face(int a, int b, int c): a(a), b(b), c(c) {}
  int &operator [](int k)
  { if (k == 0) return a; if (k == 1) return b; return c; }
};
vector <Face> face;
inline void insert(int a, int b, int c) { face.push_back(Face(a, b, c)); }
void add(int v) {
  vector <Face> tmp; int a, b, c; cnt++;
  for (int i = 0; i < SIZE(face); i++) {
    a = face[i][0]; b = face[i][1]; c = face[i][2];
    if (Sign(volume(v, a, b, c)) < 0)
    mark[a][b] = mark[b][a] = mark[b][c] = mark[c][b] = mark[c][a] = mark[a][c] = cnt;
    else tmp.push_back(face[i]);
  } face = tmp;
  for (int i = 0; i < SIZE(tmp); i++) {
    a = face[i][0]; b = face[i][1]; c = face[i][2];
    if (mark[a][b] == cnt) insert(b, a, v);
    if (mark[b][c] == cnt) insert(c, b, v);
    if (mark[c][a] == cnt) insert(a, c, v);
}}
int Find() {
  for (int i = 2; i < n; i++) {
    Point ndir = (info[0] - info[i]).cross(info[1] - info[i]);
    if (ndir == Point()) continue; swap(info[i], info[2]);
    for (int j = i + 1; j < n; j++) if (Sign(volume(0, 1, 2, j)) != 0) {
      swap(info[j], info[3]); insert(0, 1, 2); insert(0, 2, 1); return 1;
} } return 0; }
int main() {
  for (; scanf("%d", &n) == 1; ) {
    for (int i = 0; i < n; i++) info[i].Input();
    sort(info, info + n); n = unique(info, info + n) - info;
    face.clear(); random_shuffle(info, info + n);
    if (Find()) { memset(mark, 0, sizeof(mark)); cnt = 0;
      for (int i = 3; i < n; i++) add(i); vector<Point> Ndir;
      for (int i = 0; i < SIZE(face); ++i) {
        Point p = (info[face[i][0]] - info[face[i][1]]).cross(
            info[face[i][2]] - info[face[i][1]]);
        p = p / p.length(); Ndir.push_back(p);
```

```
      } sort(Ndir.begin(), Ndir.end());
      int ans = unique(Ndir.begin(), Ndir.end()) - Ndir.begin();
      printf("%d\n", ans);
    } else printf("1\n");
} }
// 求重心
double calcDist(const Point &p, int a, int b, int c)
{ return fabs(mix(info[a] - p, info[b] - p, info[c] - p) / area(a, b, c)); }
//compute the minimal distance of center of any faces
double findDist() { //compute center of mass
  double totalWeight = 0; Point center(.0, .0, .0);
  Point first = info[face[0][0]];
  for (int i = 0; i < SIZE(face); ++i) {
    Point p = (info[face[i][0]]+info[face[i][1]]+info[face[i][2]]+first)*.25;
    double weight = mix(info[face[i][0]] - first, info[face[i][1]]
        - first, info[face[i][2]] - first);
    totalWeight += weight; center = center + p * weight;
  } center = center / totalWeight;
  double res = 1e100; //compute distance
  for (int i = 0; i < SIZE(face); ++i)
    res = min(res, calcDist(center, face[i][0], face[i][1], face[i][2]));
    return res; }
```

凸包上快速询问

```
/*
   给定凸包，$\log n$ 内完成各种询问，具体操作有 :
   1. 判定一个点是否在凸包内
   2. 询问凸包外的点到凸包的两个切点
   3. 询问一个向量关于凸包的切点
   4. 询问一条直线和凸包的交点
   INF 为坐标范围，需要定义点类大于号
   改成实数只需修改 sign 函数，以及把 long long 改为 double 即可
   构造函数时传入凸包要求无重点，面积非空，以及 pair(x,y) 的最小点放在第一个
*/
const int INF = 1000000000;
struct Convex
{
  int n;
  vector<Point> a, upper, lower;
  Convex(vector<Point> _a) : a(_a) {
    n = a.size();
    int ptr = 0;
    for(int i = 1; i < n; ++ i) if (a[ptr] < a[i]) ptr = i;
    for(int i = 0; i <= ptr; ++ i) lower.push_back(a[i]);
    for(int i = ptr; i < n; ++ i) upper.push_back(a[i]);
    upper.push_back(a[0]);
  }
  int sign(long long x) { return x < 0 ? -1 : x > 0; }
  pair<long long, int> get_tangent(vector<Point> &convex, Point vec) {
    int l = 0, r = (int)convex.size() - 2;
    for( ; l + 1 < r; ) {
      int mid = (l + r) / 2;
      if (sign((convex[mid + 1] - convex[mid]).det(vec)) > 0) r = mid;
      else l = mid;
    }
    return max(make_pair(vec.det(convex[r]), r), make_pair(vec.det(convex[0]), 0));
  }
  void update_tangent(const Point &p, int id, int &i0, int &i1) {
    if ((a[i0] - p).det(a[id] - p) > 0) i0 = id;
    if ((a[i1] - p).det(a[id] - p) < 0) i1 = id;
  }
  void binary_search(int l, int r, Point p, int &i0, int &i1) {
    if (l == r) return;
    update_tangent(p, l % n, i0, i1);
    int sl = sign((a[l % n] - p).det(a[(l + 1) % n] - p));
    for( ; l + 1 < r; ) {
      int mid = (l + r) / 2;
      int smid = sign((a[mid % n] - p).det(a[(mid + 1) % n] - p));
      if (smid == sl) l = mid;
      else r = mid;
    }
    update_tangent(p, r % n, i0, i1);
  }
  int binary_search(Point u, Point v, int l, int r) {
    int sl = sign((v - u).det(a[l % n] - u));
    for( ; l + 1 < r; ) {
      int mid = (l + r) / 2;
      int smid = sign((v - u).det(a[mid % n] - u));
      if (smid == sl) l = mid;
      else r = mid;
    }
    return l % n;
  }
  // 判定点是否在凸包内，在边界返回 true
  bool contain(Point p) {
    if (p.x < lower[0].x || p.x > lower.back().x) return false;
    int id = lower_bound(lower.begin(), lower.end(), Point(p.x, -INF)) -
    ↪ lower.begin();
    if (lower[id].x == p.x) {
      if (lower[id].y > p.y) return false;
```

```
    } else if ((lower[id - 1] - p).det(lower[id] - p) < 0) return false;
    id = lower_bound(upper.begin(), upper.end(), Point(p.x, INF), greater<Point>()) - upper.begin();
    if (upper[id].x == p.x) {
      if (upper[id].y < p.y) return false;
    } else if ((upper[id - 1] - p).det(upper[id] - p) < 0) return false;
    return true;
  }
  // 求点 p 关于凸包的两个切点，如果在凸包外则有序返回编号，多解返回任意一个，否则返回 false
  bool get_tangent(Point p, int &i0, int &i1) {
    if (contain(p)) return false;
    i0 = i1 = 0;
    int id = lower_bound(lower.begin(), lower.end(), p) - lower.begin();
    binary_search(0, id, p, i0, i1);
    binary_search(id, (int)lower.size(), p, i0, i1);
    id = lower_bound(upper.begin(), upper.end(), p, greater<Point>()) - upper.begin();
    binary_search((int)lower.size() - 1, (int)lower.size() - 1 + id, p, i0, i1);
    binary_search((int)lower.size() - 1 + id, (int)lower.size() - 1 + (int)upper.size(), p, i0, i1);
    return true;
  }
  // 求凸包上和向量 vec 叉积最大的点，返回编号，有多个返回任意一个
  int get_tangent(Point vec) {
    pair<long long, int> ret = get_tangent(upper, vec);
    ret.second = (ret.second + (int)lower.size() - 1) % n;
    ret = max(ret, get_tangent(lower, vec));
    return ret.second;
  }
  // 求凸包和直线 u,v 的交点，如果无严格相交返回 false 。如果有则是和 (i,next(i)) 的交点，两个点无序，交在点上不确定返回两条线段之一。
  bool get_intersection(Point u, Point v, int &i0, int &i1) {
    int p0 = get_tangent(u - v), p1 = get_tangent(v - u);
    if (sign((v - u).det(a[p0] - u)) * sign((v - u).det(a[p1] - u)) < 0) {
      if (p0 > p1) swap(p0, p1);
      i0 = binary_search(u, v, p0, p1);
      i1 = binary_search(u, v, p1, p0 + n);
      return true;
    } else {
      return false;
    }
  }
};
```

圆的面积模板 $(n^2 \log n)$

```
struct Event {
  Point p;
  double ang;
  int delta;
  Event (Point p = Point(0, 0), double ang = 0, double delta = 0) : p(p), ang(ang), delta(delta) {}
};
bool operator < (const Event &a, const Event &b) {
  return a.ang < b.ang;
}
void addEvent(const Circle &a, const Circle &b, vector<Event> &evt, int &cnt) {
  double d2 = (a.o - b.o).len2(),
       dRatio = ((a.r - b.r) * (a.r + b.r) / d2 + 1) / 2,
       pRatio = sqrt(-(d2 - sqr(a.r - b.r)) * (d2 - sqr(a.r + b.r)) / (d2 * d2 * 4));
  Point d = b.o - a.o, p = d.rotate(PI / 2),
      q0 = a.o + d * dRatio + p * pRatio,
      q1 = a.o + d * dRatio - p * pRatio;
  double ang0 = (q0 - a.o).ang(),
       ang1 = (q1 - a.o).ang();
  evt.push_back(Event(q1, ang1, 1));
  evt.push_back(Event(q0, ang0, -1));
  cnt += ang1 > ang0;
}
bool issame(const Circle &a, const Circle &b) { return sign((a.o - b.o).len()) == 0 && sign(a.r - b.r) == 0; }
bool overlap(const Circle &a, const Circle &b) { return sign(a.r - b.r - (a.o - b.o).len()) >= 0; }
bool intersect(const Circle &a, const Circle &b) { return sign((a.o - b.o).len() - a.r - b.r) < 0; }
int C;
Circle c[N];
double area[N];
void solve() {
  memset(area, 0, sizeof(double) * (C + 1));
  for (int i = 0; i < C; ++i) {
    int cnt = 1;
    vector<Event> evt;
    for (int j = 0; j < i; ++j) if (issame(c[i], c[j])) ++cnt;
    for (int j = 0; j < C; ++j) {
      if (j != i && !issame(c[i], c[j]) && overlap(c[j], c[i])) {
        ++cnt;
      }
    }
```

```
    for (int j = 0; j < C; ++j) {
      if (j != i && !overlap(c[j], c[i]) && !overlap(c[i], c[j]) && intersect(c[i],
    ↪ c[j])) {
        addEvent(c[i], c[j], evt, cnt);
      }
    }
    if (evt.size() == 0) {
      area[cnt] += PI * c[i].r * c[i].r;
    } else {
      sort(evt.begin(), evt.end());
      evt.push_back(evt.front());
      for (int j = 0; j + 1 < (int)evt.size(); ++j) {
        cnt += evt[j].delta;
        area[cnt] += det(evt[j].p, evt[j + 1].p) / 2;
        double ang = evt[j + 1].ang - evt[j].ang;
        if (ang < 0) {
          ang += PI * 2;
        }
        area[cnt] += ang * c[i].r * c[i].r / 2 - sin(ang) * c[i].r * c[i].r / 2;
}}}}
```

三角形的心

```
Point inCenter(const Point &A, const Point &B, const Point &C) { // 内心
  double a = (B - C).len(), b = (C - A).len(), c = (A - B).len(),
    s = fabs(det(B - A, C - A)),
    r = s / p;
  return (A * a + B * b + C * c) / (a + b + c);
}
Point circumCenter(const Point &a, const Point &b, const Point &c) { // 外心
  Point bb = b - a, cc = c - a;
  double db = bb.len2(), dc = cc.len2(), d = 2 * det(bb, cc);
  return a - Point(bb.y * dc - cc.y * db, cc.x * db - bb.x * dc) / d;
}
Point othroCenter(const Point &a, const Point &b, const Point &c) { // 垂心
  Point ba = b - a, ca = c - a, bc = b - c;
  double Y = ba.y * ca.y * bc.y,
       A = ca.x * ba.y - ba.x * ca.y,
       x0 = (Y + ca.x * ba.y * b.x - ba.x * ca.y * c.x) / A,
       y0 = -ba.x * (x0 - c.x) / ba.y + ca.y;
  return Point(x0, y0);
}
```

最小覆盖球

```
int nouter; Tpoint outer[4], res; double radius;
void ball() {
  Tpoint q[3]; double m[3][3], sol[3], L[3], det;
  int i,j; res.x = res.y = res.z = radius = 0;
  for (i=0; i<3; ++i) q[i]=outer[i+1]-outer[0], sol[i]=dot(q[i], q[i]);
  for (i=0;i<3;++i) for(j=0;j<3;++j) m[i][j]=dot(q[i],q[j])*2;
  det= m[0][0]*m[1][1]*m[2][2]
  + m[0][1]*m[1][2]*m[2][0]
  + m[0][2]*m[2][1]*m[1][0]
  - m[0][2]*m[1][1]*m[2][0]
  - m[0][1]*m[1][0]*m[2][2]
  - m[0][0]*m[1][2]*m[2][1];
  if ( fabs(det)<eps ) return;
  for (j=0; j<3; ++j) {
    for (i=0; i<3; ++i) m[i][j]=sol[i];
    L[j]=( m[0][0]*m[1][1]*m[2][2]
    + m[0][1]*m[1][2]*m[2][0]
    + m[0][2]*m[2][1]*m[1][0]
    - m[0][2]*m[1][1]*m[2][0]
    - m[0][1]*m[1][0]*m[2][2]
    - m[0][0]*m[1][2]*m[2][1]
    ) / det;
    for (i=0; i<3; ++i) m[i][j]=dot(q[i], q[j])*2;
  } res=outer[0];
  for (i=0; i<3; ++i ) res = res + q[i] * L[i];
  radius=dist2(res, outer[0]);
}
```

经纬度求球面最短距离

```
double sphereDis(double lon1, double lat1, double lon2, double lat2, double R) {
  return R * acos(cos(lat1) * cos(lat2) * cos(lon1 - lon2) + sin(lat1) * sin(lat2));
}
```

长方体表面两点最短距离

```
int r;
void turn(int i, int j, int x, int y, int z,int x0, int y0, int L, int W, int H) {
  if (z==0) { int R = x*x+y*y; if (R<r) r=R;
  } else {
    if(i>=0 && i< 2) turn(i+1, j, x0+L+z, y, x0+L-x, x0+L, y0, H, W, L);
    if(j>=0 && j< 2) turn(i, j+1, x, y0+W+z, y0+W-y, x0, y0+W, L, H, W);
    if(i<=0 && i>-2) turn(i-1, j, x0-z, y, x-x0, x0-H, y0, H, W, L);
    if(j<=0 && j>-2) turn(i, j-1, x, y0-z, y-y0, x0, y0-H, L, H, W);
}}
int main(){
  int L, H, W, x1, y1, z1, x2, y2, z2;
  cin >> L >> W >> H >> x1 >> y1 >> z1 >> x2 >> y2 >> z2;
```

```
  if (z1!=0 && z1!=H) if (y1==0 || y1==W)
       swap(y1,z1), std::swap(y2,z2), std::swap(W,H);
  else swap(x1,z1), std::swap(x2,z2), std::swap(L,H);
  if (z1==H) z1=0, z2=H-z2;
  r=0x3fffffff; turn(0,0,x2-x1,y2-y1,z2,-x1,-y1,L,W,H);
  cout<<r<<endl; return 0;
}
```

最大团

```
// Super Fast Maximum Clique
// To Build Graph: Maxclique(Edges, Number of Nodes)
// To Get Answer: mcqdyn(AnswerNodes Index Array, AnswserLength)
typedef bool BB[N];
struct Maxclique {
  const BB* e; int pk, level; const float Tlimit;
  struct Vertex{ int i, d; Vertex(int i):i(i),d(0){} };
  typedef vector<Vertex> Vertices; typedef vector<int> ColorClass;
  Vertices V; vector<ColorClass> C; ColorClass QMAX, Q;
  static bool desc_degree(const Vertex &vi, const Vertex &vj){
    return vi.d > vj.d;
  }
  void init_colors(Vertices &v){
    const int max_degree = v[0].d;
    for(int i = 0; i < (int)v.size(); i++) v[i].d = min(i, max_degree) + 1;
  }
  void set_degrees(Vertices &v){
    for(int i = 0, j; i < (int)v.size(); i++)
      for(v[i].d = j = 0; j < int(v.size()); j++)
        v[i].d += e[v[i].i][v[j].i];
  }
  struct StepCount{ int i1, i2; StepCount():i1(0),i2(0){} };
  vector<StepCount> S;
  bool cut1(const int pi, const ColorClass &A){
    for(int i = 0; i < (int)A.size(); i++) if (e[pi][A[i]]) return true;
    return false;
  }
  void cut2(const Vertices &A, Vertices &B){
    for(int i = 0; i < (int)A.size() - 1; i++)
      if(e[A.back().i][A[i].i])
        B.push_back(A[i].i);
  }
  void color_sort(Vertices &R){
    int j = 0, maxno = 1, min_k = max((int)QMAX.size() - (int)Q.size() + 1, 1);
    C[1].clear(), C[2].clear();
    for(int i = 0; i < (int)R.size(); i++) {
      int pi = R[i].i, k = 1;
      while(cut1(pi, C[k])) k++;
      if(k > maxno) maxno = k, C[maxno + 1].clear();
      C[k].push_back(pi);
      if(k < min_k) R[j++].i = pi;
    }
    if(j > 0) R[j - 1].d = 0;
    for(int k = min_k; k <= maxno; k++)
      for(int i = 0; i < (int)C[k].size(); i++)
        R[j].i = C[k][i], R[j++].d = k;
  }
  void expand_dyn(Vertices &R){// diff -> diff with no dyn
    S[level].i1 = S[level].i1 + S[level - 1].i1 - S[level].i2;//diff
    S[level].i2 = S[level - 1].i1;//diff
    while((int)R.size()) {
      if((int)Q.size() + R.back().d > (int)QMAX.size()){
        Q.push_back(R.back().i); Vertices Rp; cut2(R, Rp);
        if((int)Rp.size()){
          if((float)S[level].i1 / ++pk < Tlimit) degree_sort(Rp);//diff
          color_sort(Rp);
          S[level].i1++, level++;//diff
          expand_dyn(Rp);
          level--;//diff
        }
        else if((int)Q.size() > (int)QMAX.size()) QMAX = Q;
        Q.pop_back();
      }
      else return;
      R.pop_back();
    }
  }
  void mcqdyn(int* maxclique, int &sz){
    set_degrees(V); sort(V.begin(),V.end(), desc_degree); init_colors(V);
    for(int i = 0; i < (int)V.size() + 1; i++) S[i].i1 = S[i].i2 = 0;
    expand_dyn(V); sz = (int)QMAX.size();
    for(int i = 0; i < (int)QMAX.size(); i++) maxclique[i] = QMAX[i];
  }
  void degree_sort(Vertices &R){
    set_degrees(R); sort(R.begin(), R.end(), desc_degree);
  }
  Maxclique(const BB* conn, const int sz, const float tt = 0.025) \
   : pk(0), level(1), Tlimit(tt){
    for(int i = 0; i < sz; i++) V.push_back(Vertex(i));
    e = conn, C.resize(sz + 1), S.resize(sz + 1);
  }
```

```
};
```

KM

```
// 最小匹配，自带初始化 n <= m 方案存在 p[] 中
const int N = 105;
const int INF = 1000000000; // 严格大于最大边权
int n, m, a[N][N];
int u[N], v[N], p[N], fa[N], minv[N];
bool used[N];
int km() {
  memset(u, 0, sizeof(int) * n);
  for (int i = 0; i <= m; ++i) v[i] = 0, p[i] = n;
  for (int i = 0; i < n; ++i) {
    p[m] = i;
    int j0 = m;
    for (int j = 0; j <= m; ++j) minv[j] = INF, used[j] = false;
    do {
      used[j0] = true;
      int i0 = p[j0], delta = INF, j1;
      for (int j = 0; j < m; ++j) {
        if (!used[j]) {
          int cur = a[i0][j] - u[i0] - v[j];
          if (cur < minv[j]) minv[j] = cur, fa[j] = j0;
          if (minv[j] < delta) delta = minv[j], j1 = j;
        }
      }
      for (int j = 0; j <= m; ++j) {
        if (used[j]) {
          u[p[j]] += delta, v[j] -= delta;
        } else {
          minv[j] -= delta;
        }
      }
      j0 = j1;
    } while (p[j0] != n);
    do {
      int j1 = fa[j0];
      p[j0] = p[j1];
      j0 = j1;
    } while (j0 != m);
  }
  return -v[m];
}
```

最小树形图

```
const int MAXN,INF;// INF >= sum( W_ij )
int from[MAXN + 10][MAXN * 2 + 10],n,m,edge[MAXN + 10][MAXN * 2 + 10];
int sel[MAXN * 2 + 10],fa[MAXN * 2 + 10],vis[MAXN * 2 + 10];
int getfa(int x){if(x == fa[x]) return x; return fa[x] = getfa(fa[x]);}
void liuzhu(){ // 1-base: root is 1, answer = (sel[i], i) for i in [2..n]
  fa[1] = 1;
  for(int i = 2; i <= n; ++i){
    sel[i] = 1; fa[i] = i;
    for(int j = 1; j <= n; ++j) if(fa[j] != i)
      if(from[j][i] = i, edge[sel[i]][i] > edge[j][i]) sel[i] = j;
  }
  int limit = n;
  while(1){
    int prelimit = limit; memset(vis, 0, sizeof(vis)); vis[1] = 1;
    for(int i = 2; i <= prelimit; ++i) if(fa[i] == i && !vis[i]){
      int j = i; while(!vis[j]) vis[j] = i, j = getfa(sel[j]);
      if(j == 1 || vis[j] != i) continue; vector<int> C; int k = j;
      do C.push_back(k), k = getfa(sel[k]); while(k != j);
      ++limit;
      for(int i = 1; i <= n; ++i){
        edge[i][limit] = INF, from[i][limit] = limit;
      }
      fa[limit] = vis[limit] = limit;
      for(int i = 0; i < int(C.size()); ++i){
        int x = C[i], fa[x] = limit;
        for(int j = 1; j <= n; ++j)
          if(edge[j][x] != INF && edge[j][limit] > edge[j][x] - edge[sel[x]][x]){
            edge[j][limit] = edge[j][x] - edge[sel[x]][x];
            from[j][limit] = x;
          }
      }
      for(int j=1;j<=n;++j) if(getfa(j)==limit) edge[j][limit] = INF;
      sel[limit] = 1;
      for(int j = 1; j <= n; ++j)
        if(edge[sel[limit]][limit] > edge[j][limit]) sel[limit] = j;
    }
    if(prelimit == limit) break;
  }
  for(int i = limit; i > 1; --i) sel[from[sel[i]][i]] = sel[i];
}
```

无向图最小割

```
int cost[maxn][maxn],seq[maxn],len[maxn],n,m,pop,ans;
bool used[maxn];
```

```
void Init(){
  int i,j,a,b,c;
  for(i=0;i<n;i++) for(j=0;j<n;j++) cost[i][j]=0;
  for(i=0;i<m;i++){
    scanf("%d %d %d",&a,&b,&c); cost[a][b]+=c; cost[b][a]+=c;
  }
  pop=n; for(i=0;i<n;i++) seq[i]=i;
}
void Work(){
  ans=inf; int i,j,k,l,mm,sum,pk;
  while(pop > 1){
    for(i=1;i<pop;i++) used[seq[i]]=0; used[seq[0]]=1;
    for(i=1;i<pop;i++) len[seq[i]]=cost[seq[0]][seq[i]];
    pk=0; mm=-inf; k=-1;
    for(i=1;i<pop;i++) if(len[seq[i]] > mm){ mm=len[seq[i]]; k=i; }
    for(i=1;i<pop;i++){
      used[seq[l=k]]=1;
      if(i==pop-2) pk=k;
      if(i==pop-1) break;
      mm=-inf;
      for(j=1;j<pop;j++) if(!used[seq[j]])
        if((len[seq[j]]+=cost[seq[l]][seq[j]]) > mm)
          mm=len[seq[j]], k=j;
    }
    sum=0;
    for(i=0;i<pop;i++) if(i != k) sum+=cost[seq[k]][seq[i]];
    ans=min(ans,sum);
    for(i=0;i<pop;i++)
      cost[seq[k]][seq[i]]=cost[seq[i]][seq[k]]+=cost[seq[pk]][seq[i]];
    seq[pk]=seq[--pop];
  }
  printf("%d\n",ans);
}
```

带花树

```
vector<int> link[maxn];
int n,match[maxn],Queue[maxn],head,tail;
int pred[maxn],base[maxn],start,finish,newbase;
bool InQueue[maxn],InBlossom[maxn];
void push(int u){ Queue[tail++]=u;InQueue[u]=true; }
int pop(){ return Queue[head++]; }
int FindCommonAncestor(int u,int v){
  bool InPath[maxn];
  for(int i=0;i<n;i++) InPath[i]=0;
  while(true){ u=base[u];InPath[u]=true;if(u==start) break;u=pred[match[u]]; }
  while(true){ v=base[v];if(InPath[v]) break;v=pred[match[v]]; }
  return v;
}
void ResetTrace(int u){
  int v;
  while(base[u]!=newbase){
    v=match[u];
    InBlossom[base[u]]=InBlossom[base[v]]=true;
    u=pred[v];
    if(base[u]!=newbase) pred[u]=v;
  }
}
void BlossomContract(int u,int v){
  newbase=FindCommonAncestor(u,v);
  for (int i=0;i<n;i++)
  InBlossom[i]=0;
  ResetTrace(u);ResetTrace(v);
  if(base[u]!=newbase) pred[u]=v;
  if(base[v]!=newbase) pred[v]=u;
  for(int i=0;i<n;++i)
  if(InBlossom[base[i]]){
    base[i]=newbase;
    if(!InQueue[i]) push(i);
  }
}
bool FindAugmentingPath(int u){
  bool found=false;
  for(int i=0;i<n;++i) pred[i]=-1,base[i]=i;
  for (int i=0;i<n;i++) InQueue[i]=0;
  start=u;finish=-1; head=tail=0; push(start);
  while(head<tail){
    int u=pop();
    for(int i=link[u].size()-1;i>=0;i--){
      int v=link[u][i];
      if(base[u]!=base[v]&&match[u]!=v)
        if(v==start||(match[v]>=0&&pred[match[v]]>=0))
          BlossomContract(u,v);
        else if(pred[v]==-1){
          pred[v]=u;
          if(match[v]>=0) push(match[v]);
          else{ finish=v; return true; }
        }
    }
  }
  return found;
```

```
}
void AugmentPath(){
  int u=finish,v,w;
  while(u>=0){ v=pred[u];w=match[v];match[v]=u;match[u]=v;u=w; }
}
void FindMaxMatching(){
  for(int i=0;i<n;++i) match[i]=-1;
  for(int i=0;i<n;++i) if(match[i]==-1) if(FindAugmentingPath(i)) AugmentPath();
}
```

Hopcroft

```
// 左侧 N 个点, 右侧 K 个点 , 1-based, 初始化将 matx[],maty[] 都置为 0
int N, K;
int que[N], dx[N], dy[N], matx[N], maty[N];
int BFS()
{
  int flag = 0, qt = 0, qh = 0;
  for(int i = 1; i <= K; ++ i) dy[i] = 0;
  for(int i = 1; i <= N; ++ i) {
    dx[i] = 0;
    if (! matx[i]) que[qt ++] = i;
  }
  while (qh < qt) {
    int u = que[qh ++];
    for(Edge *e = E[u]; e; e = e->n)
      if (! dy[e->t]) {
        dy[e->t] = dx[u] + 1;
        if (! maty[e->t]) flag = true;
        else {
          dx[maty[e->t]] = dx[u] + 2;
          que[qt ++] = maty[e->t];
        }
      }
  }
  return flag;
}
int DFS(int u)
{
  for(Edge *e = E[u]; e; e = e->n)
    if (dy[e->t] == dx[u] + 1) {
      dy[e->t] = 0;
      if (! maty[e->t] || DFS(maty[e->t])) {
        matx[u] = e->t; maty[e->t] = u;
        return true;
      }
    }
  return false;
}
void Hopcroft()
{
  while (BFS()) for(int i = 1; i <= N; ++ i) if (! matx[i]) DFS(i);
}
```

素数判定

```
int strong_pseudo_primetest(long long n,int base) {
    long long n2=n-1,res;
    int s=0;
    while(n2%2==0) n2>>=1,s++;
    res=powmod(base,n2,n);
    if((res==1)||(res==n-1)) return 1;
    s--;
    while(s>=0) {
        res=mulmod(res,res,n);
        if(res==n-1) return 1;
        s--;
    }
    return 0; // n is not a strong pseudo prime
}
int isprime(long long n) {
  static LL testNum[]={2,3,5,7,11,13,17,19,23,29,31,37};
  static LL lim[]={4,0,1373653LL,25326001LL,25000000000LL,2152302898747LL, \
  3474749660383LL,341550071728321LL,0,0,0,0};
  if(n<2||n==3215031751LL) return 0;
  for(int i=0;i<12;++i){
    if(n<lim[i]) return 1;
    if(strong_pseudo_primetest(n,testNum[i])==0) return 0;
  }
  return 1;
}
```

启发式分解

```
int ansn; LL ans[1000];
LL func(LL x,LL n){ return(mod_mul(x,x,n)+1)%n; }
LL Pollard(LL n){
  LL i,x,y,p;
  if(Rabin_Miller(n)) return n;
  if(!(n&1)) return 2;
  for(i=1;i<20;i++){
    x=i; y=func(x,n); p=gcd(y-x,n);
```

```
    while(p==1) {x=func(x,n); y=func(func(y,n),n); p=gcd((y-x+n)%n,n)%n;}
    if(p==0||p==n) continue;
    return p;
  }
}
void factor(LL n){
  LL x;
  x=Pollard(n);
  if(x==n){ ans[ansn++]=x; return; }
  factor(x), factor(n/x);
}
```

二次剩余

```
void calcH(int &t, int &h, const int p) {
  int tmp = p - 1; for (t = 0; (tmp & 1) == 0; tmp /= 2) t++; h = tmp;
}
// solve equation x^2 mod p = a
bool solve(int a, int p, int &x, int &y) {
  srand(19920225);
  if (p == 2) { x = y = 1; return true; }
  int p2 = p / 2, tmp = power(a, p2, p);
  if (tmp == p - 1) return false;
  if ((p + 1) % 4 == 0) {
    x = power(a, (p + 1) / 4, p); y = p - x; return true;
  } else {
    int t, h, b, pb; calcH(t, h, p);
    if (t >= 2) {
      do {b = rand() % (p - 2) + 2;
      } while (power(b, p / 2, p) != p - 1);
      pb = power(b, h, p);
    } int s = power(a, h / 2, p);
    for (int step = 2; step <= t; step++) {
      int ss = (((long long)(s * s) % p) * a) % p;
      for (int i = 0; i < t - step; i++) ss = ((long long)ss * ss) % p;
      if (ss + 1 == p) s = (s * pb) % p; pb = ((long long)pb * pb) % p;
    } x = ((long long)s * a) % p; y = p - x;
  } return true;
}
```

Pell 方程

```
ULL A,B,p[maxn],q[maxn],a[maxn],g[maxn],h[maxn];
int main() {
  for (int test=1, n;scanf("%d",&n) && n;++test) {
    printf("Case %d: ",test);
    if (fabs(sqrt(n)-floor(sqrt(n)+1e-7))<=1e-7)   {
      int a=(int)(floor(sqrt(n)+1e-7)); printf("%d %d\n",a,1);
    } else {
      // 求 x^2 - ny^2 = 1 的最小正整数根，n 不是完全平方数
      p[1]=q[0]=h[1]=1;p[0]=q[1]=g[1]=0;
      a[2]=(int)(floor(sqrt(n)+1e-7));
      for (int i=2;i;++i) {
        g[i]=-g[i-1]+a[i]*h[i-1]; h[i]=(n-sqr(g[i]))/h[i-1];
        a[i+1]=(g[i]+a[2])/h[i]; p[i]=a[i]*p[i-1]+p[i-2];
        q[i]=a[i]*q[i-1]+q[i-2];
        if (sqr((ULL)(p[i]))-n*sqr((ULL)(q[i]))==1){
          A=p[i];B=q[i];break; }
      } cout << A << ' ' << B <<endl;
    }}}
```

日期公式

```
int zeller(int y,int m,int d) {
  if (m<=2) y--,m+=12; int c=y/100; y%=100;
  int w=((c>>2)-(c<<1)+y+(y>>2)+(13*(m+1)/5)+d-1)%7;
  if (w<0) w+=7; return(w);
}
int getId(int y, int m, int d) {
  if (m < 3) {y --; m += 12};
  return 365 * y + y / 4 - y / 100 + y / 400 + (153 * m + 2) / 5 + d;
}
```

Schreier-Sims

```
struct Permutation{
  vector<int> P;Permutation(){} Permutation(int n){ P.resize(n); }
  Permutation inv()const{
    Permutation ret(P.size());
    for(int i = 0; i < int(P.size()); ++i) ret.P[P[i]] = i;
    return ret;
  }
  int &operator [](const int &dn){ return P[dn]; }
  void resize(const size_t &sz){ P.resize(sz); }
  size_t size()const{ return P.size(); }
  const int &operator [](const int &dn)const{ return P[dn]; }
};
Permutation operator *(const Permutation &a, const Permutation &b){
  Permutation ret(a.size());
  for(int i = 0; i < (int)a.size(); ++i) ret[i] = b[a[i]];
  return ret;
}
typedef vector<Permutation> Bucket;
```

```
typedef vector<int> Table; typedef pair<int,int> pii;
int n, m;
vector<Bucket> buckets, bucketsInv; vector<Table> lookupTable;
int fastFilter(const Permutation &g, bool addToGroup = true){
  int n = buckets.size();
  Permutation p;
  for(int i = 0; i < n; ++i){
    int res = lookupTable[i][p[i]];
    if(res == -1){
      if(addToGroup){
        buckets[i].push_back(p); bucketsInv[i].push_back(p.inv());
        lookupTable[i][p[i]] = (int)buckets[i].size() - 1;
      }
      return i;
    }
    p = p * bucketsInv[i][res]; swap(i1,i2);
  }
  return -1;
}
long long calcTotalSize(){
  long long ret = 1;
  for(int i = 0; i < n; ++i) ret *= buckets[i].size();
  return ret;
}
bool inGroup(const Permutation &g){ return fastFilter(g, false) == -1; }
void solve(const Bucket &gen,int _n){// m perm[0..n - 1]s
  n = _n, m = gen.size();
  {//clear all
    vector<Bucket> _buckets(n); swap(buckets, _buckets);
    vector<Bucket> _bucketsInv(n); swap(bucketsInv, _bucketsInv);
    vector<Table> _lookupTable(n); swap(lookupTable, _lookupTable);
  }
  for(int i = 0; i < n; ++i){
    lookupTable[i].resize(n);
    fill(lookupTable[i].begin(), lookupTable[i].end(), -1);
  }
  Permutation id(n);
  for(int i = 0; i < n; ++i) id[i] = i;
  for(int i = 0; i < n; ++i){
    buckets[i].push_back(id); bucketsInv[i].push_back(id);
    lookupTable[i][i] = 0;
  }
  for(int i = 0; i < m; ++i) fastFilter(gen[i]);
  queue<pair<point,point> > toUpdate;
  for(int i = 0; i < n; ++i)
    for(int j = i; j < n; ++j)
      for(int k = 0; k < (int)buckets[i].size(); ++k)
        for(int l = 0; l < (int)buckets[j].size(); ++l)
          toUpdate.push(make_pair(pii(i,k), pii(j,l)));
  while(!toUpdate.empty()){
    pii a = toUpdate.front().first, b = toUpdate.front().second;
    toUpdate.pop();
    int res=fastFilter(buckets[a.first][a.second]*buckets[b.first][b.second]);
    if(res==-1) continue;
    pii newPair(res, (int)buckets[res].size() - 1);
    for(int i = 0; i < n; ++i)
      for(int j = 0; j < (int)buckets[i].size(); ++j){
        if(i <= res) toUpdate.push(make_pair(pii(i, j), newPair));
        if(res <= i) toUpdate.push(make_pair(newPair, pii(i, j)));
      }
  }
}
```

线性规划

```
// 求max{cx | Ax ≤ b, x ≥ 0}的解
typedef vector<double> VD;
VD simplex(vector<VD> A, VD b, VD c) {
  int n = A.size(), m = A[0].size() + 1, r = n, s = m - 1;
  vector<VD> D(n + 2, VD(m + 1, 0)); vector<int> ix(n + m);
  for (int i = 0; i < n + m; ++ i) ix[i] = i;
  for (int i = 0; i < n; ++ i) {
    for (int j = 0; j < m - 1; ++ j) D[i][j] = -A[i][j];
    D[i][m - 1] = 1; D[i][m] = b[i];
    if (D[r][m] > D[i][m]) r = i;
  }
  for (int j = 0; j < m - 1; ++ j) D[n][j] = c[j];
  D[n + 1][m - 1] = -1;
  for (double d; ; ) {
    if (r < n) {
      int t = ix[s]; ix[s] = ix[r + m]; ix[r + m] = t;
      D[r][s] = 1.0 / D[r][s]; vector<int> speedUp;
      for (int j = 0; j <= m; ++ j) if (j != s) {
        D[r][j] *= -D[r][s];
        if(D[r][j]) speedUp.push_back(j);
      }
      for (int i = 0; i <= n + 1; ++ i) if (i != r) {
        for(int j = 0; j < speedUp.size(); ++ j)
        D[i][speedUp[j]] += D[r][speedUp[j]] * D[i][s];
        D[i][s] *= D[r][s];
    }} r = -1; s = -1;
```

```
    for (int j = 0; j < m; ++ j) if (s < 0 || ix[s] > ix[j])
      if (D[n + 1][j] > EPS || (D[n + 1][j] > -EPS && D[n][j] > EPS)) s = j;
    if (s < 0) break;
    for (int i = 0; i < n; ++ i) if (D[i][s] < -EPS)
      if (r < 0 || (d = D[r][m] / D[r][s] - D[i][m] / D[i][s]) < -EPS
          || (d < EPS && ix[r + m] > ix[i + m])) r = i;
    if (r < 0) return VD(); // 无边界
  }
  if (D[n + 1][m] < -EPS) return VD(); // 无解
  VD x(m - 1);
  for (int i = m; i < n + m; ++ i) if (ix[i] < m - 1) x[ix[i]] = D[i - m][m];
  return x; // 最优值在 D[n][m]
}
```

FFT

```
// double 精度对10^9 + 7 取模最多可以做到2^20
const int MOD = 1000003;
const double PI = acos(-1);
typedef complex<double> Complex;
const int N = 65536, L = 15, MASK = (1 << L) - 1;
Complex w[N];
void FFTInit() {
  for (int i = 0; i < N; ++i) {
    w[i] = Complex(cos(2 * i * PI / N), sin(2 * i * PI / N));
  }
}
void FFT(Complex p[], int n) {
  for (int i = 1, j = 0; i < n - 1; ++i) {
    for (int s = n; j ^= s >>= 1, ~j & s;);
    if (i < j) {
      swap(p[i], p[j]);
    }
  }
  for (int d = 0; (1 << d) < n; ++d) {
    int m = 1 << d, m2 = m * 2, rm = n >> (d + 1);
    for (int i = 0; i < n; i += m2) {
      for (int j = 0; j < m; ++j) {
        Complex &p1 = p[i + j + m], &p2 = p[i + j];
        Complex t = w[rm * j] * p1;
        p1 = p2 - t;
        p2 = p2 + t;
}}}}
Complex A[N], B[N], C[N], D[N];
void mul(int a[N], int b[N]) {
  for (int i = 0; i < N; ++i) {
    A[i] = Complex(a[i] >> L, a[i] & MASK);
    B[i] = Complex(b[i] >> L, b[i] & MASK);
  }
  FFT(A, N), FFT(B, N);
  for (int i = 0; i < N; ++i) {
    int j = (N - i) % N;
    Complex da = (A[i] - conj(A[j])) * Complex(0, -0.5),
        db = (A[i] + conj(A[j])) * Complex(0.5, 0),
        dc = (B[i] - conj(B[j])) * Complex(0, -0.5),
        dd = (B[i] + conj(B[j])) * Complex(0.5, 0);
    C[j] = da * dd + da * dc * Complex(0, 1);
    D[j] = db * dd + db * dc * Complex(0, 1);
  }
  FFT(C, N), FFT(D, N);
  for (int i = 0; i < N; ++i) {
    long long da = (long long)(C[i].imag() / N + 0.5) % MOD,
          db = (long long)(C[i].real() / N + 0.5) % MOD,
          dc = (long long)(D[i].imag() / N + 0.5) % MOD,
          dd = (long long)(D[i].real() / N + 0.5) % MOD;
    a[i] = ((dd << (L * 2)) + ((db + dc) << L) + da) % MOD;
  }
}
```

Manacher/ 扩展 KMP

```
void Manacher(char text[], int n, int palindrome[]) {
  palindrome[0] = 1;
  for (int i = 1, j = 0, i < (n << 1) - 1; ++ i) {
    int p = i >> 1;
    int q = i - p;
    int r = (j + 1 >> 1) + palindrome[j] - 1;
    palindrome[i] = r < q ? 0 : min(r - q + 1, palindrome[(j << 1) - i]);
    while (0 <= p - palindrome[i] && q + palindrome[i] < n && text[p -
    ↪ palindrome[i]] == text[q + palindrome[i]]) {
      palindrome[i] ++;
    }
    if (q + palindrome[i] - 1 > r) {
      j = i;
    }
  }
}
void ExtendedKMP(char *a, char *b, int M, int N, int *Next, int *ret) {// a ->
  ↪ 模式串 b -> 匹配串
  int i, j, k;
  for (j = 0; 1 + j < M && a[j] == a[1 + j]; j++); Next[1] = j;
  k = 1;
```

```
  for (i = 2; i < M; i++) {
    int Len = k + Next[k], L = Next[i - k];
    if (L < Len - i) {
      Next[i] = L;
    } else {
      for (j = max(0, Len - i); i + j < M && a[j] == a[i + j]; j++);
      Next[i] = j;
      k = i;
    }
  }
  for (j = 0; j < N && j < M && a[j] == b[j]; j++);
  ret[0] = j;
  k = 0;
  for (i = 1; i < N; i++) {
    int Len = k + ret[k], L = Next[i - k];
    if (L < Len - i) {
      ret[i] = L;
    } else {
      for (j = max(0, Len - i); j < M && i + j < N && a[j] == b[i + j]; j++);
      ret[i] = j;
      k = i;
    }
  }
}
```

后缀数组（倍增）

```
int rank[MAX_N],height[MAX_N];
int cmp(int *x,int a,int b,int d){
  return x[a]==x[b]&&x[a+d]==x[b+d];
}
void doubling(int *a,int N,int M){
  static int sRank[MAX_N],tmpA[MAX_N],tmpB[MAX_N];
  int *x=tmpA,*y=tmpB;
  for(int i=0;i<M;++i) sRank[i]=0;
  for(int i=0;i<N;++i) ++sRank[x[i]=a[i]];
  for(int i=1;i<M;++i) sRank[i]+=sRank[i-1];
  for(int i=N-1;i>=0;--i) sa[--sRank[x[i]]]=i;
  for(int d=1,p=0;p<N;M=p,d<<=1){
    p=0; for(int i=N-d;i<N;++i) y[p++]=i;
    for(int i=0;i<N;++i) if(sa[i]>=d) y[p++]=sa[i]-d;
    for(int i=0;i<M;++i) sRank[i]=0;
    for(int i=0;i<N;++i) ++sRank[x[i]];
    for(int i=1;i<M;++i) sRank[i]+=sRank[i-1];
    for(int i=N-1;i>=0;--i) sa[--sRank[x[y[i]]]]=y[i];
    swap(x,y); x[sa[0]]=0; p=1;
    for(int i=1;i<N;++i) x[sa[i]]=cmp(y,sa[i],sa[i-1],d)?p-1:p++;
  }
}
void calcHeight(){
  for(int i=0;i<N;++i) rank[sa[i]]=i;
  int cur=0; for(int i=0;i<N;++i)
  if(rank[i]){
    if(cur) cur--;
    for(;a[i+cur]==a[sa[rank[i]-1]+cur];++cur);
    height[rank[i]]=cur;
  }
}
```

后缀自动机

```
struct State {
  int length;
  State *parent,*go[C];
  State(int length = 0):length(length),parent(NULL){
    memset(go,0,sizeof(go));
  }
  State* extend(State*, int token);
} node_pool[V], *tot_node;
State* State::extend(State *start,int token){
  State *p=this;
  State *np=new(tot_node++) State(this->length+1);
  while(p!=NULL&&p->go[token]==NULL)
    p->go[token]=np, p=p->parent;
  if(p==NULL) np->parent=start;
  else{
    State *q=p->go[token];
    if(p->length+1==q->length) np->parent=q;
    else{
      State *nq=new(tot_node++) State(p->length+1);
      memcpy(nq->go,q->go,sizeof(q->go));
      nq->parent=q->parent;
      np->parent=q->parent=nq;
      while(p!=NULL&&p->go[token]==q)
        p->go[token]=nq, p=p->parent;
    }
  }
  return np;
}
```

后缀树 (With Pop Front)

```
int pos, text[N];
struct Node {
  int l, r;
  Node *suf, *ch[C];
  int dgr;
  Node *fa;
  Node (int l = -1, int r = INF) : l(l), r(r) {
    suf = fa = NULL;
    memset(ch, 0, sizeof(ch));
    dgr = 0;
  }
  Node* addEdge(Node *t) {
    int c = text[t->l];
    dgr += !ch[c];
    ch[c] = t;
    t->fa = this;
    return t;
  }
  int len() {
    return min(r, pos + 1) - l;
  }
};

int top;
Node pool[N << 1], *root, *nxtSuf, *cur;
int remCnt, curP, curLen;
long long size;
queue<Node*> leaves;
void init() {
  top = 0, pos = -1;
  remCnt = 0, curP = 0, curLen = 0;
  nxtSuf = NULL;
  root = cur = new(pool + (top++)) Node(-1, -1);
  size = 0;
  while (leaves.size()) leaves.pop();
}
void link(Node *u) {
  if (nxtSuf) nxtSuf->suf = u;
  nxtSuf = u;
}
bool walk(Node *u) {
  int len = u->len();
  if (curLen >= len) {
    curP += len, curLen -= len, cur = u;
    return true;
  }
  return false;
}
void extend(int c) {
  text[++pos] = c;
  nxtSuf = NULL;
  ++remCnt;
  while (remCnt) {
    curP = curLen ? curP : pos;
    int curE = text[curP];
    if (!cur->ch[curE]) {
      leaves.push(cur->addEdge(new(pool + (top++)) Node(pos)));
      link(cur);
    } else {
      Node *nxt = cur->ch[curE];
      if (walk(nxt)) continue;
      if (text[nxt->l + curLen] == c) {
        ++curLen;
        link(cur);
        break;
      }
      Node *split = new(pool + (top++)) Node(nxt->l, nxt->l + curLen);
      cur->addEdge(split);
      leaves.push(split->addEdge(new(pool + (top++)) Node(pos)));
      nxt->l += curLen;
      split->addEdge(nxt);
      link(split);
    }
    --remCnt;
    if (cur == root && curLen > 0) {
      curP = pos - (--curLen);
    } else {
      cur = cur->suf ? cur->suf : root;
    }
  }
  size += leaves.size();
}
void finish() {
  nxtSuf = NULL;
  for (int i = 0; i < top; ++i) if (pool[i].r == INF) link(pool + i);
  while (remCnt > 0) {
    if (curLen) {
      int curE = text[curP];
      Node *nxt = cur->ch[curE];
```

```
      if (walk(nxt)) continue;
      Node *split = new(pool + (top++)) Node(nxt->l, nxt->l + curLen);
      leaves.push(cur->addEdge(split));
      nxt->l += curLen;
      split->addEdge(nxt);
      link(split);
    } else {
      leaves.push(cur);
      link(cur);
    }
    --remCnt;
    if (cur == root && curLen > 0) {
      --curLen;
      curP = pos - remCnt + 1;
    } else {
      cur = cur->suf ? cur->suf : root;
    }
  }
  if (nxtSuf != root) link(root);
}
void eraseUp(Node *&u) {
  size -= u->len();
  int ch = text[u->l];
  u = u->fa;
  u->ch[ch] = NULL;
  --(u->dgr);
}
void erase() {
  Node *u = leaves.front();
  leaves.pop();
  while (u->dgr == 0 && u != cur) eraseUp(u);
  if (u == cur) {
    if (cur->dgr == 0 && curLen == 0) {
      int len = u->len();
      curLen = len;
      curP = pos - len + 1;
      cur = cur->fa;
      eraseUp(u);
    }
    if (curLen) {
      int curE = text[curP];
      if (!cur->ch[curE]) {
        Node *leaf = new(pool + (top++)) Node(pos - curLen + 1);
        leaves.push(cur->addEdge(leaf));
        size += leaf->len();
        --remCnt;
        if (cur == root && curLen > 0) {
          curP = pos - (--curLen) + 1;
        } else {
          cur = cur->suf ? cur->suf : root;
        }
        while (curLen && walk(cur->ch[text[curP]])) continue;
}}}}}
int n;
char s[N], buf[N];
int ord[N], stop, sord[N << 1];
void dfs(Node *u) {
  sord[u - pool] = stop++;
  for (int i = 0; i < C; ++i) {
    if (u->ch[i]) {
      dfs(u->ch[i]);
    }
  }
}
void getOrd() {
  init();
  for (int i = 0; i < n; ++i) extend(s[i] - 'a');
  finish();
  stop = 0;
  dfs(root);
  int i = 0;
  while (leaves.size()) {
    ord[i++] = sord[leaves.front() - pool];
    leaves.pop();
  }
}
```

字符串最小表示

```
std::string find(std::string s) {
  int i,j,k,l,N=s.length(); s+=s;
  for(i=0,j=1;j<N;){
    for(k=0;k<N&&s[i+k]==s[j+k];k++);
    if(k>=N) break;
    if(s[i+k]<s[j+k]) j+=k+1;
    else l=i+k,i=j,j=max(l,j)+1;
  }
  return s.substr(i,N);
}
```

轻重链剖分

```
struct Tree(){}*root[N];
int father[N],size[N],depth[N];
int bfsOrd[N],pathId[N],ordInPath[N],sqn[N];
void doBfs(int s){
  int qh=0,qt=0,*que=bfsOrd; father[s]=-1; depth[s]=0;
  for(que[qt++]=s;qh<qt;){
    int u=que[qh++];
    foreach(iter,adj[u]){
      int v=*iter; if(v==father[u]) continue;
      father[v]=u; depth[v]=depth[u]+1; que[qt++]=v;
    }
  }
}
void doSplit(){
  for(int i=N-1;i>=0;--i){
    int u=bfsOrd[i]; size[u]=1;
    foreach(iter,adj[u]){
      int v=*iter; if(v==father[u]) continue; size[u]+=size[v];
    }
  }
  memset(pathId,-1,sizeof pathId);
  for(int i=0;i<N;++i){
    int top=bfsOrd[i],cnt=0;
    if(pathId[top]!=-1) continue;
    for(int next,u=top;u!=-1;u=next){
      sqn[cnt]=val[u]; ordInPath[u]=cnt; pathId[u]=top; ++cnt;
      next=-1;
      foreach(iter,adj[u]){
        int v=*iter; if(v==father[u]) continue;
        if(next<0||size[next]<size[v]) next=v;
      }
    }
    root[top]=new Tree(0,cnt,sqn);
  }
}
void prepare(){ doBfs(0); doSplit(); }
```

Splay Tree

```
// 注意初始化内存池和 null 节点
struct Node{
  int rev,size; Node *ch[2],*p;
  void set(Node*,int); int dir(); void update(); void relax(); void appRev();
} nodePool[MAX_NODE],*curNode,*null;
Node *newNode(){
  Node *t=curNode++; t->rev=0, t->size=1;
  t->ch[0]=t->ch[1]=t->p=null; return t;
}
struct Splay{
  Node *root;
  Splay(){ root=newNode(); root->set(newNode(),0); root->update(); }
  void rot(Node *t){
    Node *p=t->p; int d=t->dir();
    p->relax(); t->relax();
    if(p==root) root=t;
    p->set(t->ch[!d],d); p->p->set(t,p->dir()); t->set(p,!d);
    p->update();
  }
  void splay(Node *t,Node *f=null){
    for(t->relax();t->p!=f;)
      if(t->p->p==f) rot(t);
      else t->dir()==t->p->dir()?(rot(t->p),rot(t)):(rot(t),rot(t));
    t->update();
  }
};
void initNull(){ curNode=nodePool;null=curNode++;null->size=0; }
void Node::set(Node *t,int _d){ ch[_d]=t; t->p=this; }
int Node::dir(){ return this==p->ch[1]; }
void Node::update(){ size=ch[0]->size+ch[1]->size+1;}
void Node::relax(){ if(rev) ch[0]->appRev(), ch[1]->appRev(), rev=false; }
void Node::appRev(){ if(this==null) return; rev^=true; swap(ch[0],ch[1]); }
```

Link Cut Tree

```
// 注意初始化 null 节点，单点的 is_root 初始为 true
struct Node{
  Node *ch[2], *p;
  int is_root, rev;
  bool dir();
  void set(Node*, bool);
  void update();
  void relax();
  void app_rev();
} *null;
void rot(Node *t){
  Node *p=t->p; bool d=t->dir();
  p->relax(); t->relax(); p->set(t->ch[!d],d);
  if(p->is_root) t->p=p->p,swap(p->is_root,t->is_root);
  else p->p->set(t,p->dir());
  t->set(p,!d); p->update();
```

```
}
void splay(Node *t){
  for(t->relax();!t->is_root;)
    if(t->p->is_root) rot(t);
    else t->dir()==t->p->dir() ?(rot(t->p),rot(t)) :(rot(t),rot(t));
  t->update();
}
void access(Node *t){
  for(Node *s=null; t!=null; s=t,t=t->p){
    splay(t);
    if (t->p == null) { /*TODO*/ }
    t->ch[1]->is_root=true; s->is_root=false;
    t->ch[1]=s; t->update();
  }
}
bool Node::dir(){ return this==p->ch[1]; }
void Node::set(Node *t,bool _d){ ch[_d]=t; t->p=this; }
void Node::update(){ }
void Node::app_rev(){ if (this == null) return; rev ^= true; swap(ch[0], ch[1]); }
void Node::relax() { if(this==null) return; if (rev) { ch[0]->app_rev();
  ↪ ch[1]->app_rev(); rev = false; } }
void make_root(Node *u) { access(u); splay(u); u->app_rev(); }
```

Dominator Tree

```
vector<int> prec[N], succ[N];
vector<int> ord;
int stamp, vis[N];
int num[N];
int fa[N];
void dfs(int u) {
  vis[u] = stamp;
  num[u] = ord.size();
  ord.push_back(u);
  for (int i = 0; i < (int)succ[u].size(); ++i) {
    int v = succ[u][i];
    if (vis[v] != stamp) {
      fa[v] = u;
      dfs(v);
    }
  }
}
int fs[N], mins[N], dom[N], sem[N];
int find(int u) {
  if (u != fs[u]) {
    int v = fs[u];
    fs[u] = find(fs[u]);
    if (mins[v] != -1 && num[sem[mins[v]]] < num[sem[mins[u]]]) {
      mins[u] = mins[v];
    }
  }
  return fs[u];
}
void merge(int u, int v) { fs[u] = v; }
vector<int> buf[N];
int buf2[N];
void mark(int source) {
  ord.clear();
  ++stamp;
  dfs(source);
  for (int i = 0; i < (int)ord.size(); ++i) {
    int u = ord[i];
    fs[u] = u, mins[u] = -1, buf2[u] = -1;
  }
  for (int i = (int)ord.size() - 1; i > 0; --i) {
    int u = ord[i], p = fa[u];
    sem[u] = p;
    for (int j = 0; j < (int)prec[u].size(); ++j) {
      int v = prec[u][j];
      if (use[v] != stamp) continue;
      if (num[v] > num[u]) {
        find(v); v = sem[mins[v]];
      }
      if (num[v] < num[sem[u]]) {
        sem[u] = v;
      }
    }
    buf[sem[u]].push_back(u);
    mins[u] = u;
    merge(u, p);
    while (buf[p].size()) {
      int v = buf[p].back();
      buf[p].pop_back();
      find(v);
      if (sem[v] == sem[mins[v]]) {
        dom[v] = sem[v];
      } else {
        buf2[v] = mins[v];
      }
    }
  }
```

```
  dom[ord[0]] = ord[0];
  for (int i = 0; i < (int)ord.size(); ++i) {
    int u = ord[i];
    if (~buf2[u]) {
      dom[u] = dom[buf2[u]];
    }
  }
}
```

DancingLinks

```
struct node{
  node *left,*right,*up,*down,*col; int row,cnt;
}*head,*col[MAXC],Node[MAXNODE],*ans[MAXNODE];
int totNode;
void insert(const std::vector<int> &V,int rownum){
  std::vector<node*> N;
  for(int i=0;i<int(V.size());++i){
    node* now=Node+(totNode++); now->row=rownum;
    now->col=now->up=col[V[i]], now->down=col[V[i]]->down;
    now->up->down=now, now->down->up=now;
    now->col->cnt++; N.push_back(now);
  }
  for(int i=0;i<int(V.size());++i)
    N[i]->right=N[(i+1)%V.size()], N[i]->left=N[(i-1+V.size())%V.size()];
}
void Remove(node *x){
  x->left->right=x->right, x->right->left=x->left;
  for(node *i=x->down;i!=x;i=i->down)
    for(node *j=i->right;j!=i;j=j->right)
      j->up->down=j->down, j->down->up=j->up, --(j->col->cnt);
}
void Resume(node *x){
  for(node *i=x->up;i!=x;i=i->up)
    for(node *j=i->left;j!=i;j=j->left)
      j->up->down=j->down->up=j, ++(j->col->cnt);
  x->left->right=x, x->right->left=x;
}
bool search(int tot){
  if(head->right==head) return true;
  node *choose=NULL;
  for(node *i=head->right;i!=head;i=i->right){
    if(choose==NULL||choose->cnt>i->cnt) choose=i;
    if(choose->cnt<2) break;
  }
  Remove(choose);
  for(node *i=choose->down;i!=choose;i=i->down){
    for(node *j=i->right;j!=i;j=j->right) Remove(j->col);
    ans[tot]=i;
    if(search(tot+1)) return true;
    ans[tot]=NULL;
    for(node *j=i->left;j!=i;j=j->left) Resume(j->col);
  }
  Resume(choose);
  return false;
}
void prepare(int totC){
  head=Node+totC;
  for(int i=0;i<totC;++i) col[i]=Node+i;
  totNode=totC+1;
  for(int i=0;i<=totC;++i){
    (Node+i)->right=Node+(i+1)%(totC+1);
    (Node+i)->left=Node+(i+totC)%(totC+1);
    (Node+i)->up=(Node+i)->down=Node+i;
  }
}
```

环状最长公共子序列

```
int n, a[N << 1], b[N << 1];
bool has(int i, int j) { return a[(i - 1) % n] == b[(j - 1) % n];}
const int DELTA[3][2] = {{0, -1}, {-1, -1}, {-1, 0}};
int from[N][N];
int solve() {
  memset(from, 0, sizeof(from));
  int ret = 0;
  for (int i = 1; i <= 2 * n; ++ i) {
    from[i][0] = 2;
    int left = 0, up = 0;
    for (int j = 1; j <= n; ++ j) {
      int upleft = up + 1 + !!from[i - 1][j];
      if (!has(i, j)) upleft = INT_MIN;
      int max = std::max(left, std::max(upleft, up));
      if (left == max) {
        from[i][j] = 0;
      } else if (upleft == max) {
        from[i][j] = 1;
      } else {
        from[i][j] = 2;
      }
      left = max;
    }
```

```
    if (i >= n) {
      int count = 0;
      for (int x = i, y = n; y;) {
        int t = from[x][y];
        count += t == 1;
        x += DELTA[t][0];
        y += DELTA[t][1];
      }
      ret = std::max(ret, count);
      int x = i - n + 1, y = 0;
      from[x][0] = 0;
      while (y <= n && from[x][y] == 0) y++;
      for (; x <= i; ++ x) {
        from[x][y] = 0;
        if (x == i) break;
        for (; y <= n; ++ y) {
          if (from[x + 1][y] == 2) break;
          if (y + 1 <= n && from[x + 1][y + 1] == 1) {
            y ++;
            break;
  }}}}}
  return ret;
}
```

直线下有多少个格点

```
LL solve(LL n,LL a,LL b,LL m){
  // 计算 for (int i=0;i<n;++i) s+=floor((a+b*i)/m)
  //n,m,a,b>0
  if(b==0) return n*(a/m);
  if(a>=m) return n*(a/m)+solve(n,a%m,b,m);
  if(b>=m) return (n-1)*n/2*(b/m)+solve(n,a,b%m,m);
  return solve((a+b*n)/m,(a+b*n)%m,m,b);
}
```

费用流

```
// Q is a priority_queue<PII, vector<PII>, greater<PII> >
// for an edge(s, t): u is the capacity, v is the cost, nxt is the next edge,
// op is the opposite edge
// this code can not deal with negative cycles
typedef pair<int,int> PII;
struct edge{ int t,u,v; edge *nxt,*op; }E[MAXE],*V[MAXV];
int D[MAXN], dist[MAXN], maxflow, mincost; bool in[MAXN];
bool modlabel(){
  while(!Q.empty()) Q.pop();
  for(int i=S;i<=T;++i) if(in[i]) D[i]=0,Q.push(PII(0,i)); else D[i]=inf;
  while(!Q.empty()){
    int x=Q.top().first,y=Q.top().second; Q.pop();
    if(y==T) break; if(D[y]<x) continue;
    for(edge *ii=V[y];ii;ii=ii->nxt) if(ii->u)
      if(x+(ii->v+dist[ii->t]-dist[y])<D[ii->t]){
        D[ii->t]=x+(ii->v+dist[ii->t]-dist[y]);
        Q.push(PII(D[ii->t],ii->t));
      }
  }
  if(D[T]==inf) return false;
  for(int i=S;i<=T;++i) if(D[i]>D[T]) dist[i]+=D[T]-D[i];
  return true;
}
int aug(int p,int limit){
  if(p==T) return maxflow+=limit,mincost+=limit*dist[S],limit;
  in[p]=1; int kk,ll=limit;
  for(edge *ii=V[p];ii;ii=ii->nxt) if(ii->u){
    if(!in[ii->t]&&dist[ii->t]+ii->v==dist[p]){
      kk=aug(ii->t,min(ii->u,ll)); ll-=kk,ii->u-=kk,ii->op->u+=kk;
      if(!ll) return in[p]=0,limit;
    }
  }
  return limit-ll;
}
PII mincostFlow(){
  for(int i=S;i<=T;++i) dist[i]=i==T?inf:0;
  while(!Q.empty()) Q.pop(); Q.push(PII(0,T));
  while(!Q.empty()){
    int x=Q.top().first,y=Q.top().second; Q.pop(); if(dist[y]<x) continue;
    for(edge *ii=V[y];ii;ii=ii->nxt) if(ii->op->u&&ii->v+x<dist[ii->t]
      dist[ii->t]=ii->v+x,Q.push(PII(dist[ii->t],ii->t));
  }
  maxflow=mincost=0;
  do{
    do{
      memset(in,0,sizeof(in));
    }while(aug(S,maxflow));
  }while(modlabel());
  return PII(maxflow,mincost);
}
```

积分表

Integrals of Rational Functions

$\int \frac{1}{1+x^2}dx = \tan^{-1}x$ $\int \frac{1}{a^2+x^2}dx = \frac{1}{a}\tan^{-1}\frac{x}{a}$ $\int \frac{x}{a^2+x^2}dx = \frac{1}{2}\ln|a^2+x^2|$ $\int \frac{x^2}{a^2+x^2}dx = x - a\tan^{-1}\frac{x}{a}$ $\int \frac{x^3}{a^2+x^2}dx = \frac{1}{2}x^2 - \frac{1}{2}a^2\ln|a^2+x^2|$

$\int \frac{1}{ax^2+bx+c}dx = \frac{2}{\sqrt{4ac-b^2}}\tan^{-1}\frac{2ax+b}{\sqrt{4ac-b^2}}$ $\int \frac{1}{(x+a)(x+b)}dx = \frac{1}{b-a}\ln\frac{a+x}{b+x},\ a \neq b$ $\int \frac{x}{(x+a)^2}dx = \frac{a}{a+x} + \ln|a+x|$ $\int \frac{x}{ax^2+bx+c}dx = \frac{1}{2a}\ln|ax^2+bx+c| - \frac{b}{a\sqrt{4ac-b^2}}\tan^{-1}\frac{2ax+b}{\sqrt{4ac-b^2}}$

Integrals with Roots

$\int \frac{x}{\sqrt{x\pm a}}dx = \frac{2}{3}(x \mp 2a)\sqrt{x \pm a}$ $\int \sqrt{\frac{x}{a-x}}dx = -\sqrt{x(a-x)} - a\tan^{-1}\frac{\sqrt{x(a-x)}}{x-a}$ $\int \sqrt{\frac{x}{a+x}}dx = \sqrt{x(a+x)} - a\ln\left[\sqrt{x}+\sqrt{x+a}\right]$ $\int x\sqrt{x^2\pm a^2}dx = \frac{1}{3}\left(x^2\pm a^2\right)^{3/2}$

$\int x\sqrt{ax+b}dx = \frac{2}{15a^2}(-2b^2+abx+3a^2x^2)\sqrt{ax+b}$ $\int \sqrt{x(ax+b)}dx = \frac{1}{4a^{3/2}}\left[(2ax+b)\sqrt{ax(ax+b)}\ -b^2\ln\left|a\sqrt{x}+\sqrt{a(ax+b)}\right|\right]$ $\int \sqrt{x^2\pm a^2}dx = \frac{1}{2}x\sqrt{x^2\pm a^2} \pm \frac{1}{2}a^2\ln\left|x+\sqrt{x^2\pm a^2}\right|$

$\int \sqrt{x^3(ax+b)}dx = \left[\frac{b}{12a} - \frac{b^2}{8a^2x} + \frac{x}{3}\right]\sqrt{x^3(ax+b)} + \frac{b^3}{8a^{5/2}}\ln\left|a\sqrt{x}+\sqrt{a(ax+b)}\right|$ $\int \sqrt{a^2-x^2}dx = \frac{1}{2}x\sqrt{a^2-x^2} + \frac{1}{2}a^2\tan^{-1}\frac{x}{\sqrt{a^2-x^2}}$ $\int \frac{x^2}{\sqrt{x^2\pm a^2}}dx = \frac{1}{2}x\sqrt{x^2\pm a^2} \mp \frac{1}{2}a^2\ln\left|x+\sqrt{x^2\pm a^2}\right|$

$\int \frac{1}{\sqrt{x^2\pm a^2}}dx = \ln\left|x+\sqrt{x^2\pm a^2}\right|$ $\int \frac{1}{\sqrt{a^2-x^2}}dx = \sin^{-1}\frac{x}{a}$ $\int \frac{x}{\sqrt{x^2\pm a^2}}dx = \sqrt{x^2\pm a^2}$ $\int \frac{x}{\sqrt{a^2-x^2}}dx = -\sqrt{a^2-x^2}$ $\int \sqrt{ax^2+bx+c}dx = \frac{b+2ax}{4a}\sqrt{ax^2+bx+c} + \frac{4ac-b^2}{8a^{3/2}}\ln\left|2ax+b+2\sqrt{a(ax^2+bx+c)}\right|$

$\int x\sqrt{ax^2+bx+c} = \frac{1}{48a^{5/2}}\left(2\sqrt{a}\sqrt{ax^2+bx+c}\ \times\left(-3b^2+2abx+8a(c+ax^2)\right)\ +3(b^3-4abc)\ln\left|b+2ax+2\sqrt{a}\sqrt{ax^2+bx+c}\right|\right)$ $\int \frac{1}{\sqrt{ax^2+bx+c}}dx = \frac{1}{\sqrt{a}}\ln\left|2ax+b+2\sqrt{a(ax^2+bx+c)}\right|$

$\int \frac{x}{\sqrt{ax^2+bx+c}}dx = \frac{1}{a}\sqrt{ax^2+bx+c} - \frac{b}{2a^{3/2}}\ln\left|2ax+b+2\sqrt{a(ax^2+bx+c)}\right|$ $\int \frac{dx}{(a^2+x^2)^{3/2}} = \frac{x}{a^2\sqrt{a^2+x^2}}$

Integrals with Logarithms

$\int \ln(ax+b)dx = \left(x+\frac{b}{a}\right)\ln(ax+b) - x, a \neq 0$

$\int \frac{\ln ax}{x}dx = \frac{1}{2}(\ln ax)^2$ $\int \ln(x^2+a^2)\,\mathrm{dx} = x\ln(x^2+a^2) + 2a\tan^{-1}\frac{x}{a} - 2x$ $\int \ln(x^2-a^2)\,\mathrm{dx} = x\ln(x^2-a^2) + a\ln\frac{x+a}{x-a} - 2x$ $\int x\ln(ax+b)dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2}\left(x^2-\frac{b^2}{a^2}\right)\ln(ax+b)$

$\int \ln\left(ax^2+bx+c\right)dx = \frac{1}{a}\sqrt{4ac-b^2}\tan^{-1}\frac{2ax+b}{\sqrt{4ac-b^2}} - 2x + \left(\frac{b}{2a}+x\right)\ln\left(ax^2+bx+c\right)$ $\int x\ln\left(a^2-b^2x^2\right)dx = -\frac{1}{2}x^2 + \frac{1}{2}\left(x^2-\frac{a^2}{b^2}\right)\ln\left(a^2-b^2x^2\right)$

Integrals with Exponentials

$\int x^n e^{ax}\,\mathrm{dx} = \frac{x^n e^{ax}}{a} - \frac{n}{a}\int x^{n-1}e^{ax}\,\mathrm{dx}$ $\int xe^{-ax^2}\,\mathrm{dx} = -\frac{1}{2a}e^{-ax^2}$

Integrals with Trigonometric Functions

$\int \sin^3 axdx = -\frac{3\cos ax}{4a} + \frac{\cos 3ax}{12a}$ $\int \cos^2 axdx = \frac{x}{2} + \frac{\sin 2ax}{4a}$

$\int \cos^3 axdx = \frac{3\sin ax}{4a} + \frac{\sin 3ax}{12a}$ $\int \cos ax\sin bxdx = \frac{\cos[(a-b)x]}{2(a-b)} - \frac{\cos[(a+b)x]}{2(a+b)}, a \neq b$ $\int \sin^2 ax\cos bxdx = -\frac{\sin[(2a-b)x]}{4(2a-b)} + \frac{\sin bx}{2b} - \frac{\sin[(2a+b)x]}{4(2a+b)}$ $\int \sin^2 x\cos xdx = \frac{1}{3}\sin^3 x$

$\int \cos^2 ax\sin bxdx = \frac{\cos[(2a-b)x]}{4(2a-b)} - \frac{\cos bx}{2b} - \frac{\cos[(2a+b)x]}{4(2a+b)}$ $\int \cos^2 ax\sin axdx = -\frac{1}{3a}\cos^3 ax$ $\int \sin^2 ax\cos^2 bxdx = \frac{x}{4} - \frac{\sin 2ax}{8a} - \frac{\sin[2(a-b)x]}{16(a-b)} + \frac{\sin 2bx}{8b} - \frac{\sin[2(a+b)x]}{16(a+b)}$ $\int \sin^2 ax\cos^2 axdx = \frac{x}{8} - \frac{\sin 4ax}{32a}$

$\int \tan axdx = -\frac{1}{a}\ln\cos ax$ $\int \tan^2 axdx = -x + \frac{1}{a}\tan ax$ $\int \tan^3 axdx = \frac{1}{a}\ln\cos ax + \frac{1}{2a}\sec^2 ax$ $\int \sec xdx = \ln|\sec x+\tan x| = 2\tanh^{-1}\left(\tan\frac{x}{2}\right)$ $\int \sec^2 axdx = \frac{1}{a}\tan ax$

$\int \sec^3 x\,\mathrm{dx} = \frac{1}{2}\sec x\tan x + \frac{1}{2}\ln|\sec x+\tan x|$ $\int \sec x\tan xdx = \sec x$ $\int \sec^2 x\tan xdx = \frac{1}{2}\sec^2 x$ $\int \sec^n x\tan xdx = \frac{1}{n}\sec^n x, n \neq 0$ $\int \csc xdx = \ln\left|\tan\frac{x}{2}\right| = \ln|\csc x - \cot x| + C$

$\int \csc^2 axdx = -\frac{1}{a}\cot ax$ $\int \csc^3 xdx = -\frac{1}{2}\cot x\csc x + \frac{1}{2}\ln|\csc x - \cot x|$ $\int \csc^n x\cot xdx = -\frac{1}{n}\csc^n x, n \neq 0$ $\int \sec x\csc xdx = \ln|\tan x|$

Products of Trigonometric Functions and Monomials

$\int x\cos xdx = \cos x + x\sin x$ $\int x\cos axdx = \frac{1}{a^2}\cos ax + \frac{x}{a}\sin ax$ $\int x^2\cos xdx = 2x\cos x + \left(x^2-2\right)\sin x$ $\int x^2\cos axdx = \frac{2x\cos ax}{a^2} + \frac{a^2x^2-2}{a^3}\sin ax$ $\int x\sin xdx = -x\cos x + \sin x$

$\int x\sin axdx = -\frac{x\cos ax}{a} + \frac{\sin ax}{a^2}$ $\int x^2\sin xdx = \left(2-x^2\right)\cos x + 2x\sin x$ $\int x^2\sin axdx = \frac{2-a^2x^2}{a^3}\cos ax + \frac{2x\sin ax}{a^2}$

Products of Trigonometric Functions and Exponentials

$\int e^x\sin xdx = \frac{1}{2}e^x(\sin x - \cos x)$ $\int e^{bx}\sin axdx = \frac{1}{a^2+b^2}e^{bx}(b\sin ax - a\cos ax)$ $\int e^{bx}\cos axdx = \frac{1}{a^2+b^2}e^{bx}(a\sin ax + b\cos ax)$ $\int xe^x\sin xdx = \frac{1}{2}e^x(\cos x - x\cos x + x\sin x)$

$\int xe^x\cos xdx = \frac{1}{2}e^x(x\cos x - \sin x + x\sin x)$ $\int e^x\cos xdx = \frac{1}{2}e^x(\sin x + \cos x)$

Java

```java
import java.io.*;
import java.util.*;
import java.math.*;

public class Main{
  BufferedReader reader = new BufferedReader(new InputStreamReader(System.in));
  PrintWriter writer = new PrintWriter(System.out);
  StringTokenizer tokenizer = null;

  void solve() throws Exception {
  }
  void run()throws Exception{
    try{
      while (true) {
        solve();
      }
    }
    catch(Exception e){
    }
    finally{
      reader.close();
      writer.close();
    }
  }
  String next()throws Exception{
    for(;tokenizer == null || !tokenizer.hasMoreTokens();){
      tokenizer = new StringTokenizer(reader.readLine());
```

```
    }
    return tokenizer.nextToken();
  }
  int nextInt()throws Exception{
    return Integer.parseInt(next());
  }
  double nextDouble()throws Exception{
    return Double.parseDouble(next());
  }
  BigInteger nextBigInteger()throws Exception{
    return new BigInteger(next());
  }
  public static void main(String args[])throws Exception{
    (new Main()).run();
  }
}
```

Vimrc

```
\begin{lstlisting}
set nu ai ci si mouse=a ts=4 sts=4 sw=4

nmap<C-A> ggVG
vmap<C-C> "+y

nmap<F3> : vs %<.in <CR>
nmap<F5> : !./%< <CR>
nmap<F8> : !./%< < %<.in <CR>
nmap<F9> : !g++ % -o %< -Wall <CR>

"nmap<F4> : !gedit % <CR>
"autocmd BufNewFile *.cpp 0r ~/temp.cpp
"set hlsearch incseach

"syntax on
"filetype plugin indent on
\end{lstlisting}
```