



Set Theory

Part 1



What is a Set?

Organizing Information

What is a Set?

- A *set* is an unordered collection of “objects”
- The collection objects are also called “members” or “elements”
- One of the most fundamental structures in mathematics



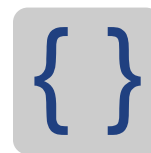
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Set Notation

- We typically denote a set name using capital letter
- Members are separated with commas and encapsulated within curly brackets



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Standard Sets

Letter	Name	Members
Z	Integers	..., -2, -1, 0, 1, 2, 3, ...
N	Natural Numbers	1, 2, 3, 4, ...
Q	Rational Numbers	a/b where both a and b are integers and b is not 0

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Standard Sets

Letter	Name	Members
R	Real Numbers	All non-imaginary numbers. e.g. 1, 2.5, 3.1415....
U	Universal Set	All values of potential interest (U depends on context)

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Set Notation: Membership

- Set notation uses a special symbol to denote if an object is a member of a set
- Below, the set V contains vegetables

`potato ∈ V`

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Set Notation: Membership

- This is read as "potato is an **element** of V "
- ...or "potato is a **member** of V "

`potato ∈ V`

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Set Notation: Not a Member

- There is another special symbol that denotes an object is **not** a member of a set
- In the example below, the set F contains fluffy animals

`lizard ∉ F`

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Defining Sets

How to specify items

Defining Sets

- Sets can be defined a number of different ways
- Each competing notation has advantages & disadvantages – depending on what you are defining



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Set Notation: Explicit

- We can **explicitly** define this by listing each element
- For example, we can define a set S for members of the Three Stooges

`S = {moe, larry, curly, shemp}`

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Set Notation: Pattern

- We can also specify a set by using a *pattern*.
- In the example below we are define a set of integers between 0 and 9.

```
A = {0, 1, 2, ... 9}
```

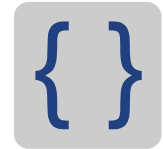
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Set Builder Notation

- A set can also be defined using *set builder notation*
- Consists of a variable name, a pipe symbol, and an true/false expression



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By Characteristic

- The most basic form consists of a variable and an true/false statement
- In this example, everything that satisfies "x is an even integer" will be the set

```
{x | x is a even integer}
```

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By Characteristic Examples

Expression	Result
{ x x is an integer }	{ ..., -1, 0, 1, 2, 3, ... }
{ x x is an even integer }	{ ..., -2, 0, 2, 4, 6, ... }
{ x x is odd natural number }	{ 1, 3, 5, 7, 9, ... }

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Characteristic with Restriction

- Definitions can also be restricted by another set
- There are two different notations that *mean the same thing*

```
{x ∈ S | true/false expression on x}
{x | x ∈ S and true/false expression on x}
```

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Characteristic Example

- Remember, Z is the set of all integers
- It reads: "All x where x is in Z and x is even"

```
A = {x | x ∈ Z and x is even}
```

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By Characteristic Examples

Expression	Result
$\{x \in \mathbb{Z} \mid 0 < x < 5\}$	$\{1, 2, 3, 4\}$
$\{x \mid x \in \mathbb{N} \text{ and } x < 7\}$	$\{1, 2, 3, 4, 5, 6\}$

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Characteristic with Structure

- The left-hand-side (before the pipe) doesn't have to be a simple variable name
- It can also be any mathematical expression

$\{f(x) \mid \text{true/false expression using } x\}$

$\{y \mid y = f(x) \text{ and true/false using } x\}$

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Let's Try One...

- The second part of the notation must always be a true/false expression
- So, how do we create a set that contains:

<input type="radio"/>	
<input type="radio"/>	$\{2, 4, 6, 8, 10, \dots\}$
<input type="radio"/>	

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Let's Try One...

First approach:

$A = \{x \mid x \in \mathbb{N} \text{ and } x \text{ is even}\}$

Second approach:

$A = \{2x \mid x \in \mathbb{N}\}$

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How Does It Evaluate?

- Basically, when you look at something like: $\{2x \mid x \in \mathbb{N}\}$, you should do the following
- Steps:
 1. Identify which variables make the **right-hand-side** true
 2. Plug them into the **left-hand-side**. These are the values in the set.

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More Examples

Expression	Result
$\{2x + 1 \mid x \in \mathbb{Z}\}$	$\{\dots, -3, -1, 1, 3, 5, \dots\}$
$\{x \in \mathbb{Z} \mid \text{sqrt}(x) \in \mathbb{Z}\}$	$\{0, 1, 4, 9, 16, 25, \dots\}$

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Empty Set

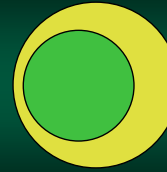
- An *empty set* contains no elements
- Can be represented with two curly-brackets (nothing in between)
- There is also a special symbol for empty sets

$A = \{ \}$
 $A = \emptyset$

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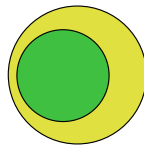


Subsets

Set Your Sets to Fun

Subsets

- Commonly, sets are compared to one another using set relationship operators
- Basically, sets are defined on elements which they may have in common



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Subsets

- Set A is considered a subset of set B if all the members of A are also members of B
- The subset operator is similar looking to the member operator

$\{ 1, 4 \} \subseteq \{ 1, 3, 4, 5 \}$

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Subsets

- A set A is not a subset of B if A contains an element not found in B

$\{ 3, 5 \} \not\subseteq \{ 3, 7 \}$

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Null is Always a Subset

- A null set contains no elements
- Hence, the null set is always a subset

$\emptyset \subseteq \{ 2, 3 \}$
 $\{ \} \subseteq \{ 2, 3 \}$

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Proper Subsets

- Set A is a *proper subset* of B if A is a subset of B , but not equal to B
- Note: the notation lacks the underline – it is consistent with other operators like $<$ and \leq

$\{ 3, 5 \} \subset \{ 3, 5, 7 \}$
 $\{ 1, 2 \} \not\subset \{ 1, 2 \}$

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Equality

- Sets A and B are considered equal if-and-only-if...

for every $x \in A$ it is also true $x \in B$
 for every $x \in B$ it is also true $x \in A$

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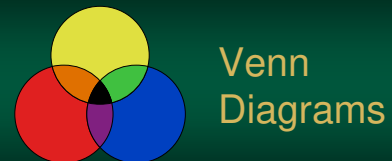
Equality

- So, are $\{ 1, 2, 3 \}$ and $\{ 2, 1, 3 \}$ equal?
- How about $\{ 1, 1, 2, 3, 3 \}$ and $\{ 3, 2, 1 \}$?
- Answer is *yes!*
 - order does not matter in a set
 - multiple occurrences does not change if an element is a member

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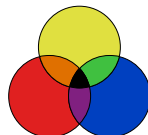
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Graphically Representing Sets

Venn Diagrams

- Sets can also be abstractly representing graphically using Venn Diagrams
- Each set is represented by circle
- Overlaps between each set can show logical relations with set members

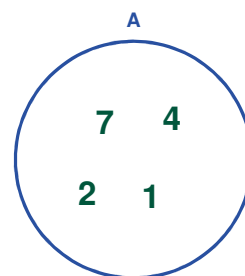


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Example: $A = \{ 2, 7, 1, 4 \}$

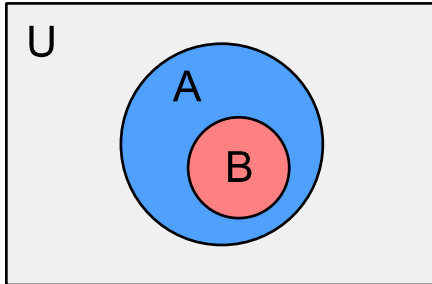


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Subset Venn Diagram

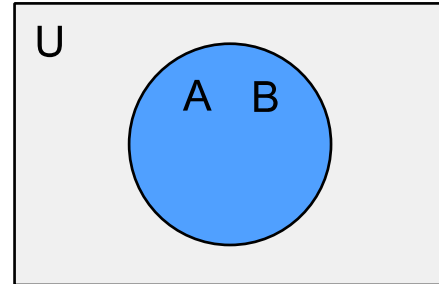


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Equality

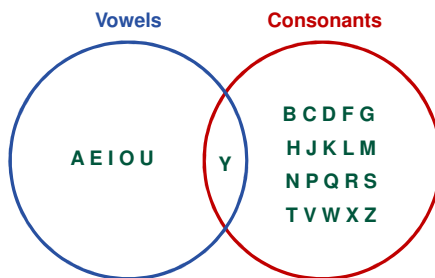


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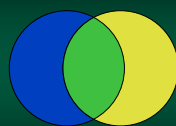
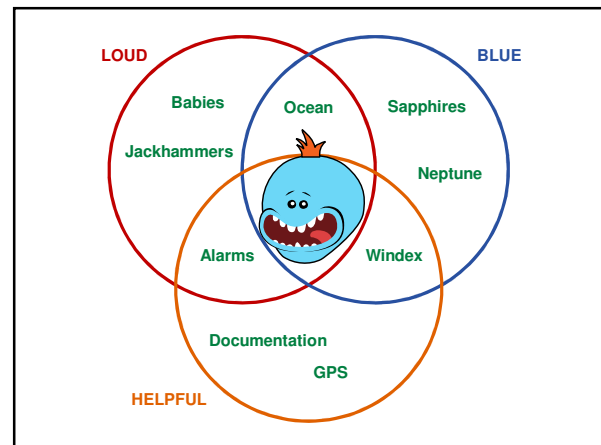
Example: Letters in English



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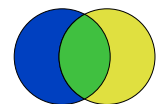


Set Operators

Defining Sets Using Sets

Operations on Sets

- New sets can be made from old sets using set operators.
- Just like new numbers can be created from old numbers: $1 + 2 = 3$
- So, for the rest of this section, let U be the universe, and let A and B be sets



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Union

- A union of two sets combines all members of each set into a new one
- So, the result is two merged sets

$$A \cup B = \{x \mid x \in A \text{ or } x \in B\}$$

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Union

- The symbol \cup looks like U
 - which is also used for the "universe set"
 - be careful not to confuse the two

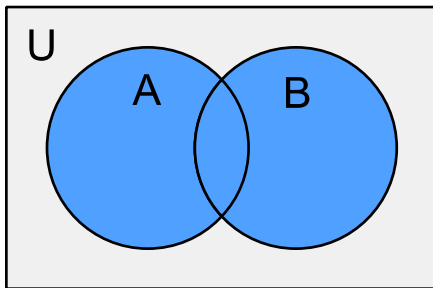
$$A \cup B = \{x \mid x \in A \text{ or } x \in B\}$$

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$A \cup B$



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Intersection

- The intersection of two sets contains only those elements that are found in both sets
- So, the result is where the two sets overlap

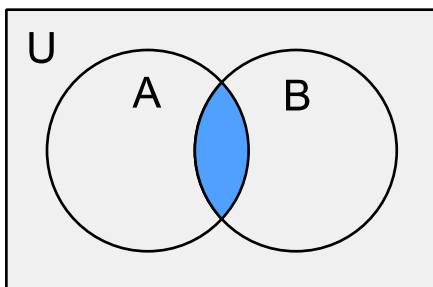
$$A \cap B = \{x \mid x \in A \text{ and } x \in B\}$$

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$A \cap B$



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Difference

- *Difference* (aka exclusion) removes all items found in set from another
- Typically, it is written as $A - B$ even though it is not the same as subtraction

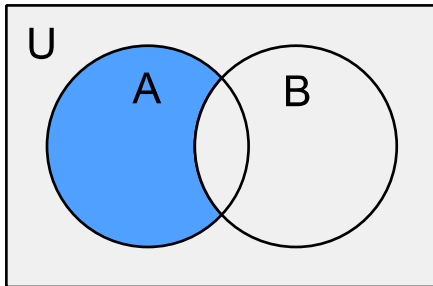
$$A - B = \{x \mid x \in A \text{ and } x \notin B\}$$

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A - B



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Difference – So Many Notations

- The notation for difference varies greatly
- Below are two different variations on the same notation

$A - B$
 $A \setminus B$

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Complement

- The *complement* of a set A , is all elements in the Universe, not in A
- Remember: what elements are in the Universe depends on the sets

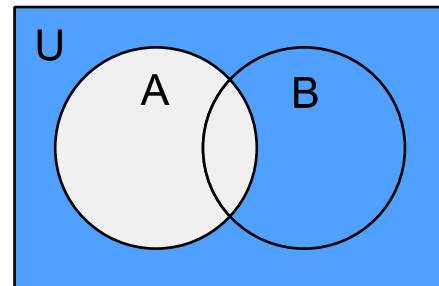
$$A' = \{x \mid x \notin A\}$$

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A'



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Different Notations Used

- Single postfix apostrophe
- An "over bar" (which is underlining on top)
- Superscript "c" for complement

$$A' \equiv \overline{A} \equiv A^c$$

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Complement Example

- If set A is a subset of a set B , then the complement of A is all elements not in A but still in B
- Look at the following:

$A \subset B$
 $A = \{1, 2, 3\}$
 $B = \{1, 2, \dots, 10\}$

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Complement Example

- Set **A** is a subset of a set **B**
- Therefore its "universe" is defined as the set of **B**

Therefore...

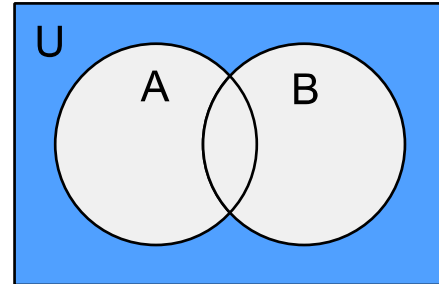
$$A' = \{4, 5, 6, 7, 8, 9, 10\}$$

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$(A \cup B)'$

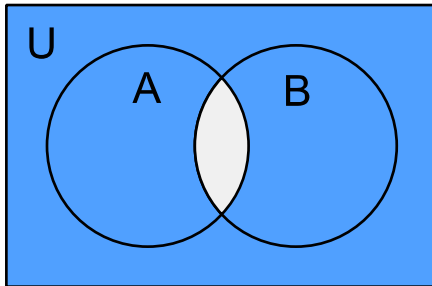


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$(A \cap B)'$



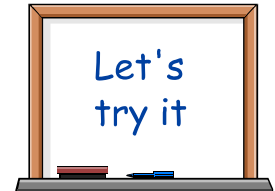
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Let's Draw Some...

- Let's draw some Venn Diagrams using a several sets
- Using set operators we can highlight any area we want



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Let's Draw Some

$$U = \{a, b, c, d, e, f\}$$

$$A = \{a, b, c\}$$

$$B = \{b, c, d, e\}$$



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Let's Draw Some

Two sets:

In **A** but not in **B**: $\{a\}$

In **B** but not in **A**: $\{d, e\}$

In both **A** and **B**: $\{b, c\}$

In neither **A** nor **B**: $\{f\}$

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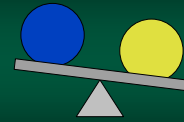
Reasoning with Venn Diagrams

- Say 100 people receive a questionnaire with two questions (1) Do you program Java?, (2) Do you program C# ?
- If 65 said 'yes' to Java, 40 said 'yes' to **both**. How many program just program C#?
-

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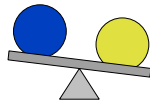


Cardinality

Counting Sets

Cardinality of a Set

- The *cardinality* of a set is the number of *distinct* elements
- This information is used in counting – the classification of the set's contents



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Different Notations Used

- There are two different notations used
- The most common is the | pipe delimiters
- Alternatively, the "n" function is used

$$|\mathbf{A}| \equiv n(\mathbf{A})$$

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Examples

$$\mathbf{A} = \{1, 3, 5, 7\}$$

$$|\mathbf{A}| = 4$$

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Examples

$$\mathbf{B} = \{1, 2, 3, 3, 3, 4\}$$

$$|\mathbf{B}| = 4$$

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Counting

- If the set contains a finite number of elements, it is said to be *countable* – i.e. the cardinality is knowable
- If the set is infinitely large, *but* the elements can be uniquely identified, then it is *countably infinite*
- Otherwise it is said to be *uncountable*

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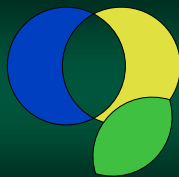
Countable Examples

Set	Result
$\{x \mid x \in \mathbb{N} \text{ and } x \leq 100\}$	Countable
$\{2x \mid x \in \mathbb{N}\}$	Countably Infinite
$\{x \mid x \in \mathbb{R} \text{ and } 0 < x < 1\}$	Uncountable

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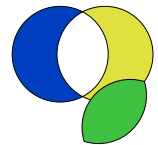


Inclusion-Exclusion

Counting by Subtracting!

Inclusion-Exclusion

- Sets can overlap – and can contain the same elements
- So, when counting items in sets, you *must* be careful not to count an item twice
- *Inclusion-exclusion* principle, can get the correct count



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Disjoint Set Cardinality

- If sets *A* and *B* are disjoint then they have no elements in common
- Cardinality of the union is the sum of the cardinality of both *A* and *B*

$$|A \cup B| = |A| + |B|$$

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Set Exclusion

- If sets *A* and *B* overlap they have elements in common
- The cardinality of the union is the sum of *A* and *B* excluding the intersection

$$|A \cup B| = |A| + |B| - |A \cap B|$$

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Set Exclusion

- Why?
- $|A| + |B|$ counts the intersection twice!
- So, we need to remove the duplicate count

$$|A \cup B| = |A| + |B| - |A \cap B|$$

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Set Exclusion

- Also note: this is the same equation for disjoint sets
- If disjoint, the intersection is \emptyset

$$|A \cup B| = |A| + |B| - |A \cap B|$$

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Let's look at this again...

○ Say 100 people receive a questionnaire with two questions (1) Do you program Java?, (2) Do you program C# ?

○ If 65 said 'yes' to Java and 40 say 'yes' to both. How many program just program C#?

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Using the Formula...

- The union of Java & C# contains 100
- Java set contains 65
- The intersection contains 40

$$|J \cup C| = |J| + |C| - |J \cap C|$$

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Using the Formula...

- The union of Java & C# contains 100
- Java set contains 65
- The intersection contains 40

$$100 = 65 + |C| - 40$$

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Using the Formula...


- The union of Java & C# contains 100
- Java set contains 65
- The intersection contains 40

$$\begin{aligned} |C| &= 100 - 65 + 40 \\ &= 75 \end{aligned}$$

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Partitions

Cutting a Set Into Pieces

Partitions


- A *partition* of a set A is a collection of non-empty disjoint sets whose union is A
- So, it is like the set A was "chopped", cleanly, into subsets



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Requirements

- Each subset must be mutually exclusive
- ... unless they are identical (*because duplicates don't count in sets*)



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Partition Example

- The following is a valid partition of the set $\{1, 2, 3, \dots, 9\}$

$\{ \{1\}, \{2, 3, 5, 7\}, \{4, 6\}, \{8, 9\} \}$

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Partition Example

- The following is a partition of N .

$N = \{ \{1\}, \{2, 3\}, \{4, 5, 6\}, \dots \}$

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Countable Examples

For the set $\{1, 2, 3, 4\} \dots$

Set	Partition?
$\{ \{1\}, \{2\}, \{3\}, \{4\} \}$	Yes
$\{ \{1, 2\}, \{1, 2\}, \{3, 4\} \}$	Yes. $\{1, 2\}$ is duplicate
$\{ \{1, 2, 3\}, \{2, 4\} \}$	No.

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Power Series

All the combinations

Power Series

- A *power set* of a set S is a set of all the subsets of S
- This also, obviously, contains the null set
- The notation for the power set S is $P(S)$



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Power Set Example

$$G = \{a, b\}$$

$$P(G) = \{ \emptyset, \{a\}, \{b\}, \{a,b\} \}$$

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Power Set Example 2

$$H = \{a, b, c\}$$

$$P(H) = \{ \emptyset, \{a\}, \{b\}, \{c\}, \{a,b\}, \{a,c\}, \{b,c\}, \{a,b,c\} \}$$

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Power Set Example 3

$$I = \{a, b, c, d\}$$

$$P(I) = \{ \emptyset, \{a\}, \{b\}, \{c\}, \{d\}, \{a,b\}, \{a,c\}, \{a,d\}, \{b,c\}, \{b,d\}, \{c,d\}, \{a,b,c\}, \{a,b,d\}, \{b,c,d\}, \{a,c,d\}, \{a,b,c,d\} \}$$

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Cardinality of Power Sets



- What is the cardinality of power sets?
- Is it possible to determine $|P(S)|$ if we know $|S|$?
- This will be important later...

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Let's Look at the Examples

$$G = \{a, b\}$$

$$P(G) = \{ \emptyset, \{a\}, \{b\}, \{a,b\} \}$$

$$|G| = 2$$

$$|P(G)| = 4$$

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Power Set Example 2

$$H = \{a, b, c\}$$

$$P(H) = \{ \emptyset, \{a\}, \{b\}, \{c\}, \{a,b\}, \{a,c\}, \{b,c\}, \{a,b,c\} \}$$

$$|H| = 3$$

$$|P(H)| = 8$$

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Power Set Example 3

$$I = \{a, b, c, d\}$$

$$P(I) = \{ \emptyset, \{a\}, \{b\}, \{c\}, \{d\}, \{a,b\}, \{a,c\}, \{a,d\}, \{b,c\}, \{b,d\}, \{c,d\}, \{a,b,c\}, \{a,b,d\}, \{b,c,d\}, \{a,c,d\}, \{a,b,c,d\} \}$$

$$|I| = 4$$

$$|P(I)| = 16$$

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Cardinality of Power Set

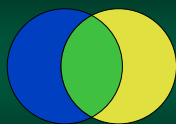
- The cardinality of a power set is 2^n where n is the cardinality of the original set
- This is used in statistics... covered later

$$|P(S)| = 2^{|S|}$$

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Set Algebra

Just a preview...

Let's Look at These...

- Let's see if the following are the same:

$$A \cup (B \cap C)$$

$$(A \cup B) \cap (A \cup C)$$

Let's try it

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Set Algebra

- We will cover more of this later, but set algebra shares the same principles as basic math
- You can visually treat the union as a “+” and the intersection as a “*”
- You can then factor out sets

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Another Look

$$\begin{aligned}
 & (A \cup B) \cap (A \cup C) \\
 & \rightarrow (A * B) + (A * C) \\
 & = A * (B + C) \\
 & A \cup (B \cap C)
 \end{aligned}$$

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Tuples

Order is Important

Tuples & Sets

- To denote sets, we delimit the list of members with curly brackets
- For example, the prime numbers between 1 and 10 is {2, 3, 5, 7}
- Order does not matter, so {2, 3, 5, 7} = {7, 5, 3, 2}



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Tuples

- However, in many cases the *order is important*
- These are called *n-tuples* where “n” is the number of elements
- 2-tuples are also called *ordered pairs*



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Tuple Notation

- To denote a tuple – we delimit the elements by either parenthesis, angle brackets or square brackets
- Curly-brackets are never used to avoid obvious confusion

$$\begin{aligned}
 & (1, 2, 3) \\
 & < 1, 2, 3 > \\
 & [1, 2, 3]
 \end{aligned}$$

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Tuple Examples

- Order is important, so any element out of position will cause inequality

$(1, 2, 3) \neq (3, 2, 1)$

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Tuple Examples

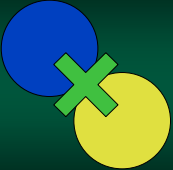
- Logic generally applies to algorithms since, in procedural programming, order is important
- The following is a tuple of events in California History

$(\text{Sutter's Fort Built}, \text{Bear Flag Revolt}, \text{Gold Rush}, \text{California Joins Union})$

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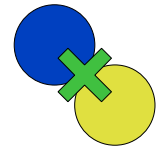


Cross Products

Databases use this...

Products

- Sets can be multiplied, which will result in a set of tuples
- Well, a set of ordered pairs, to be more specific
- $A \times B = \{ (x, y) \mid x \in A \text{ and } y \in B \}$



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Example Product

Given:

$A = \{1, 2\}$

$B = \{x, y\}$

$A \times B = \{ (1, x), (2, x), (1, y), (2, y) \}$

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