

CSC 130
Homework 1

1. For the table below, compare pairs of functions $f(n)$ (rows) and $g(n)$ (columns). For each cell, fill in the tightest and strongest true relationship between f and g :

O if $f(n)$ is $O(g(n))$
 Ω if $f(n)$ is $\Omega(g(n))$
 Θ if $f(n)$ is $\Theta(g(n))$
 – if none of the above.

If there is a * in the box, then also give a short explanation of why that relationship holds.

| | 5 | n^2+3 | $n \log n^5$ | 5^n |
|----------|---|---------|--------------|-------|
| n^2 | | | | |
| $\log n$ | | | | |
| 100 | | | | |

2. True or False:

- $f(n)$ is $\Theta(g(n))$ implies $f(n)$ is $O(g(n))$
- $f(n)$ is $\Theta(g(n))$ implies $g(n)$ is $\Theta(f(n))$
- $f(n)$ is $\Omega(g(n))$ implies $f(n)$ is $O(g(n))$

3. What's the $O()$ – Big “Oh” runtime of the code fragment in terms of n :

- a. `int x = 0;`
`for(int i = n; i >= 0; i--)`
 `if((i % 3) == 0) break;`
 `else x += n;`
- b. `int x = 0;`
`for(int i = 0; i < n; i++)`
 `for(int j = 0; j < (n * n / 3); j++)`
 `x += j;`
- c. `int x = 0;`
`for(int i = 0; i <= n; i++)`
 `for(int j = 0; j < (i * i); j++)`
 `x += j;`