ReinforcedLearningClass

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Preface

This is a Quarto book.

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1 Tarea 1 (Fecha de Entrega 20 Septiembre 2024 12:00:00)

Read (Sec 1.1, pp 1-2 Sutton and Barto 2018) and answer the following. Explain why Reinforcement Learning differs for supervised and unsupervised.

See the first Brunton's youtube about Reinforced Learning. Then acordingly to its presentation explain what is the meaning of the following expression.

$$V_\pi(s) = E\left(\sum_t \gamma^t r_t \mid s_0 = s\right)$$

Form (see Sutton and Barto 2018, sec. 1.7) obtain a time line pear year from 1950 to 2012.

Consider the following comsuption-saving problem with dynamics

$$x_{k+1} = (1+r)(x_k - a_k), k = 0, 1, \dots, N-1$$

and utility function

$$\beta^N (x_N)^{1-\gamma} + \sum_{k=0}^{N-1} \beta^k (a_k)^{1-\gamma}.$$

Show that the value functions of the DP alghorithm the form

$$J_k(x) = A_k k \beta^k x^{1-\gamma},$$

where $A_N = 1$ and for $k = N-1, \dots, 0$,

$$A_k = \left[1 + \left((1+r)\beta A_{k+1}\right)^{1/\gamma}\right]^\gamma.$$

Show also that the optimal policies are $h_k(x) = A^{-1/\gamma} x$, for $k = N-1, \dots, 0$.

Consider now the infinite-horizon version of the above compsumption problem.

1. Write down the associated Bellman equation.
2. Argue why a solution to the Bellman equation should be the form

$$v(x) = cx^{1-\gamma},$$

where c is constant. Find the constant c and the stationary optimal policy.

Let $\{\xi_k\}$ be a dynamics of iid random variables such that $E[\xi] = 0$ and $E[\xi^2] = d$. Consider the dynamics

$$x_{k+1} = x_k + a_k + \xi_k, k = 0, 1, 2, \dots,$$

and the discounted cost

$$E\left[\sum \beta^k \left(a_k^2 + x_k^2\right)\right]$$

1. Write down the associated Bellman equation.
2. Conjecture that the solution to the Bellman equation takes the form $v(x) = ax^2 + b$, where a and b are constant.
3. Determine the constants a and b.
4. Conjecture that the solution to the Bellman equation takes the form $v(x) = ax^2 + b$, where a and b are constant. Determine the constants a and b.

2 Tarea 2

References