



# Cascading behavior in networks



- Choices made by individuals with reference to the previous choices made by everyone else.
  - information cascades
  - network effects
  - rich-get-richer dynamics
- Structure of the network and how individuals are influenced by their particular network neighbors.
  - Cascade behavior in networks



# Diffusion of Innovations

- The diffusion of innovations
  - informational effects
  - direct-benefit effects
- Why an innovation can fail to spread through a population, even when it has significant relative advantage compared to existing practices ?
  - homophily
  - barrier to diffusion



# Diffusion of Innovations

- In Ryan and Gross's study,
  - interviewed farmers to determine how and when they decided to begin using hybrid seed corn.
  - Most of the farmers in their study first learned about hybrid seed corn from salesmen,
  - but most were first convinced to try using it based on the **experience of neighbors** in their community.





# Diffusion of Innovations

- Why an innovation can fail to spread through a population ?
  - It can be difficult for these innovations to make their way into a **tightly-knit social community**;
  - even when it is has significant **relative advantage** compared to existing practices;
  - **complexity** for people to understand and implement;
  - its **observability**; people can become aware that others are using it;
  - **trialability**, people can mitigate its risks by adopting it gradually and incrementally;
  - **compatibility** with the social system that it is entering.



# Modeling Diffusion through a Network

- individuals make decisions based on the choices of their neighbors
  - informational effects
  - direct-benefit effects



# A Coordination Game

- Nodes  $v$  and  $w$
- Two behaviors : **A** and **B**
- If  $v$  and  $w$  are linked, an incentive for them to have their behaviors match

		$w$	
		A	B
$v$	A	$a, a$	0,0
	B	0,0	$b, b$

- If  $v$  and  $w$  adopt behavior **A**, they each get a payoff  $a > 0$



- If they adopt behavior **B**, they each get a payoff  $b > 0$



- If they adopt opposite behavior, they each get a payoff 0



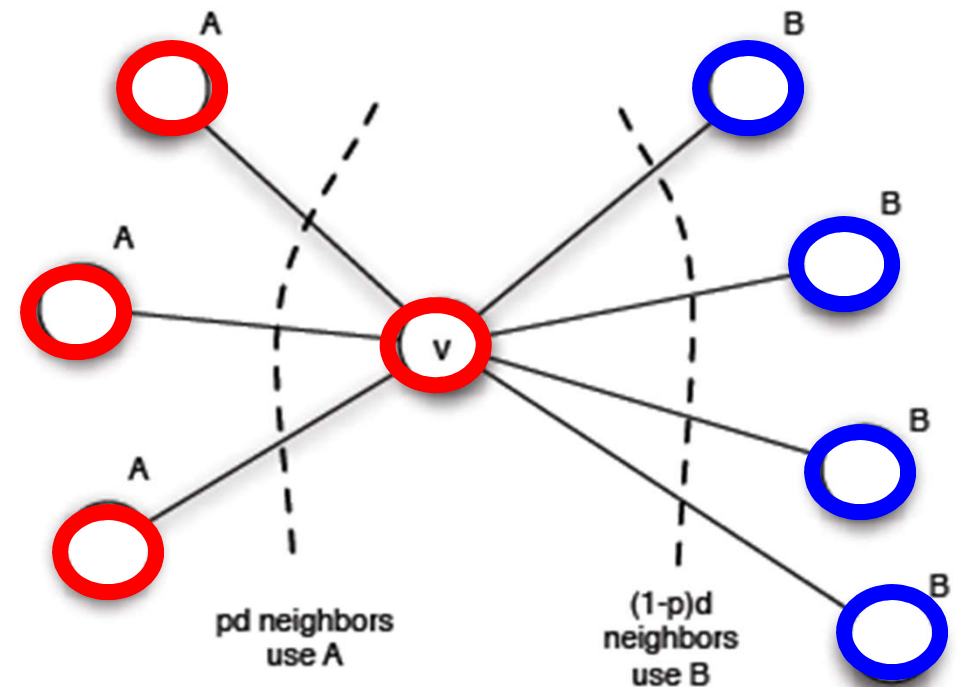


# A Networked Coordination Game

- Each node is playing this game with each of its neighbors and the payoff is the sum of all payoffs

- $v$  has  $d$  neighbors
- $p$  fraction of  $v$ 's neighbors is A
- $1-p$  fraction of  $v$ 's neighbors is B
- If  $v$  chooses A, payoff =  $pda$
- If  $v$  chooses B, payoff =  $(1-p)db$
- A is better if

$$pda \geq (1-p)db \quad \text{or} \quad p \geq \frac{b}{a+b} = q$$

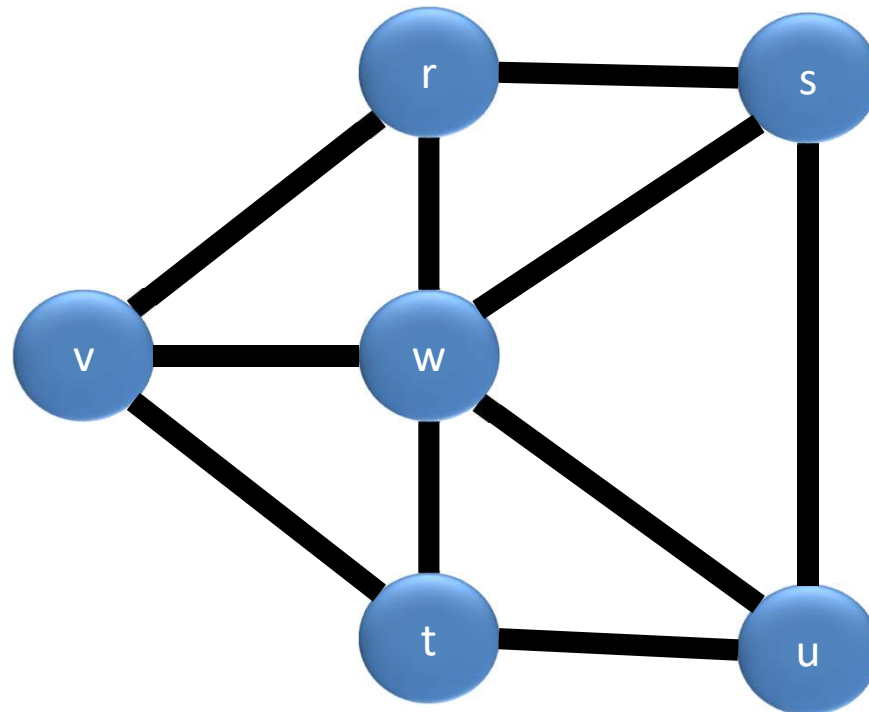






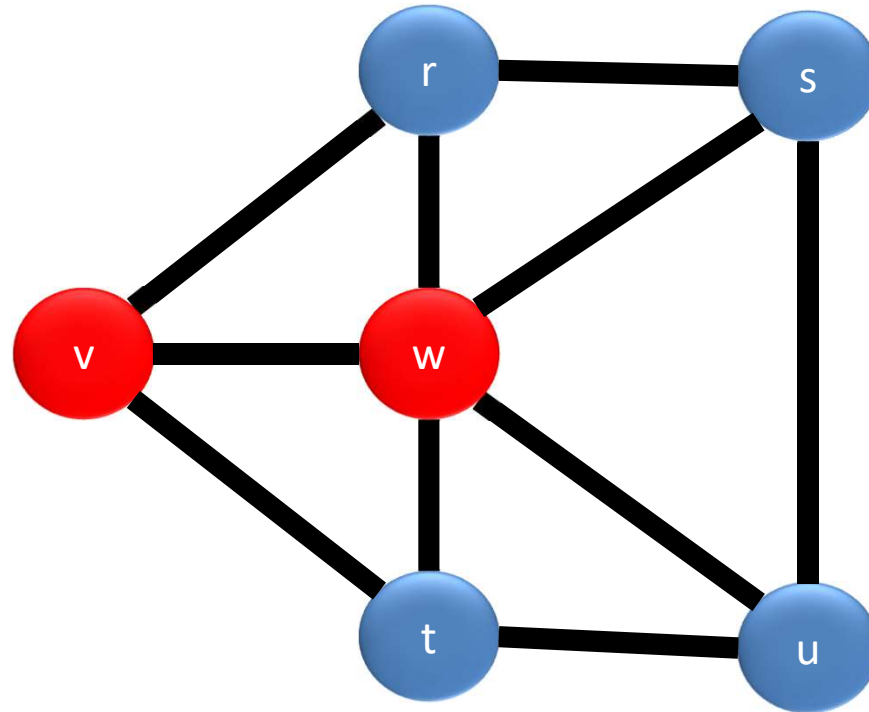
- $a = 3, b = 2$

- $q = \frac{b}{a+b} = \frac{2}{5}$





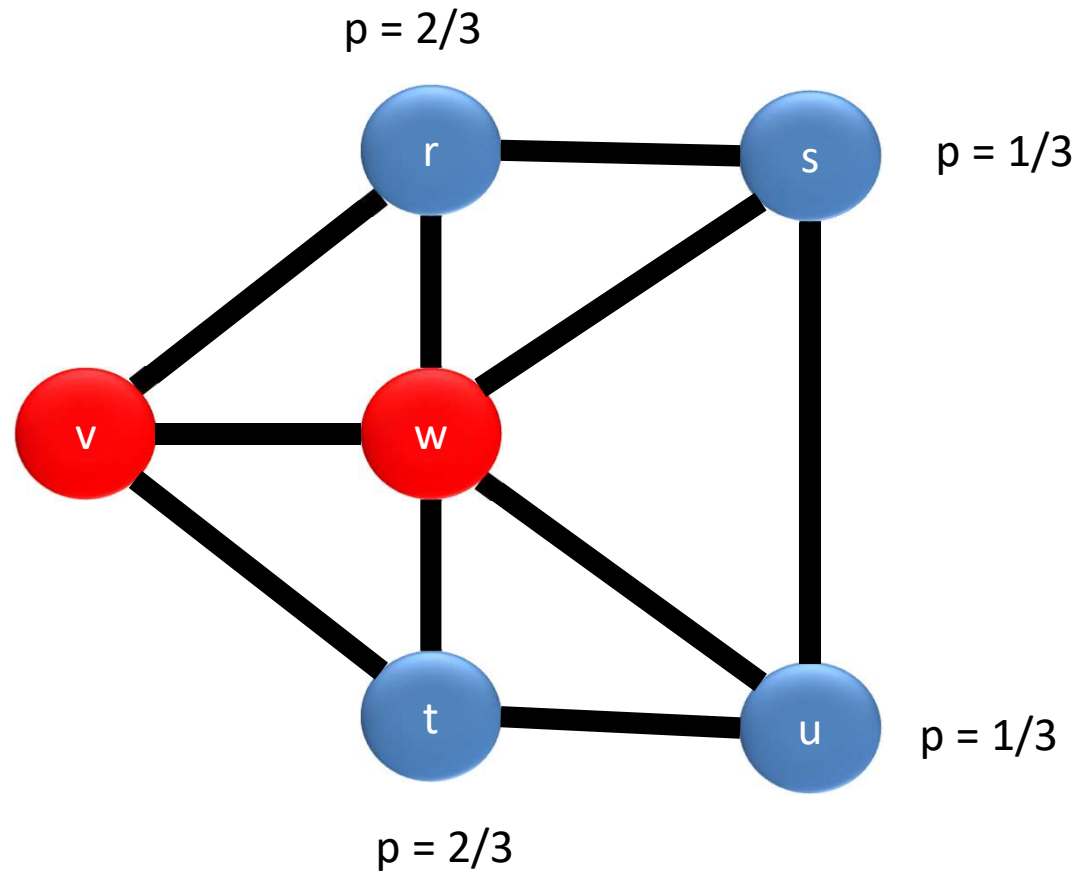
- $a = 3, b = 2$
- $q = \frac{b}{a+b} = \frac{2}{5}$
- v and w are initial adopters





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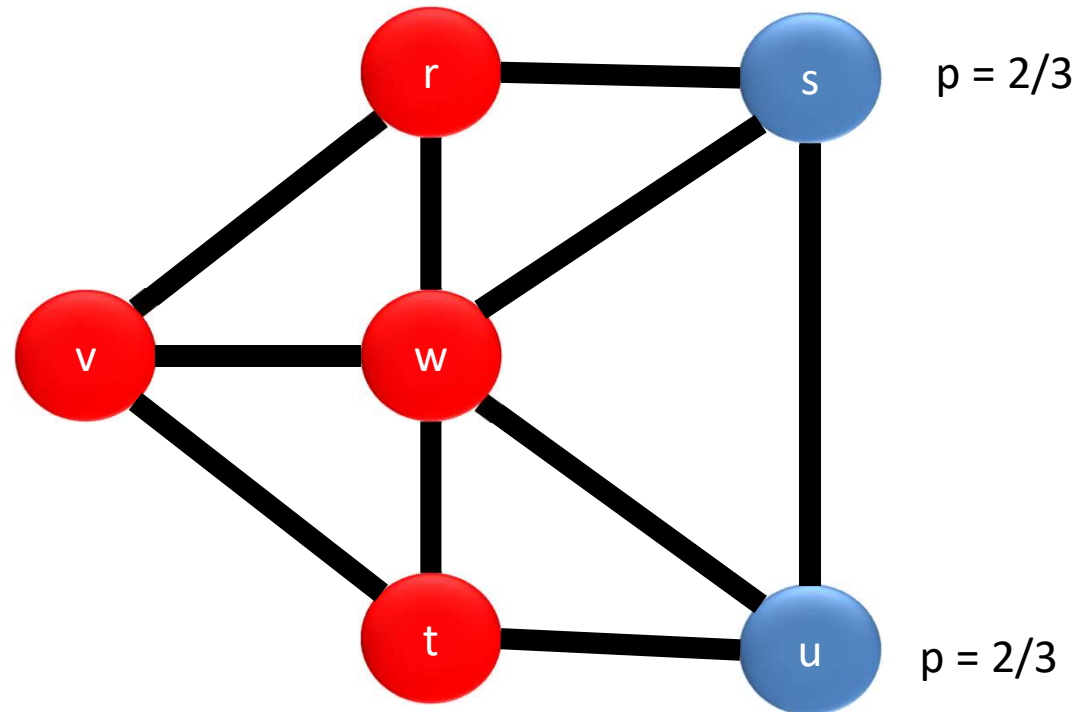
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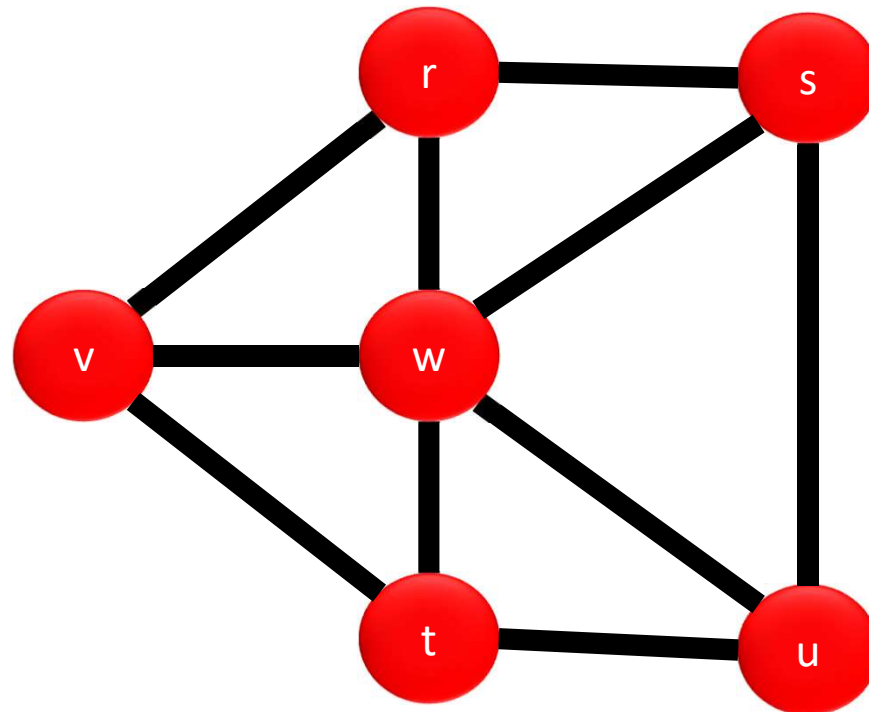
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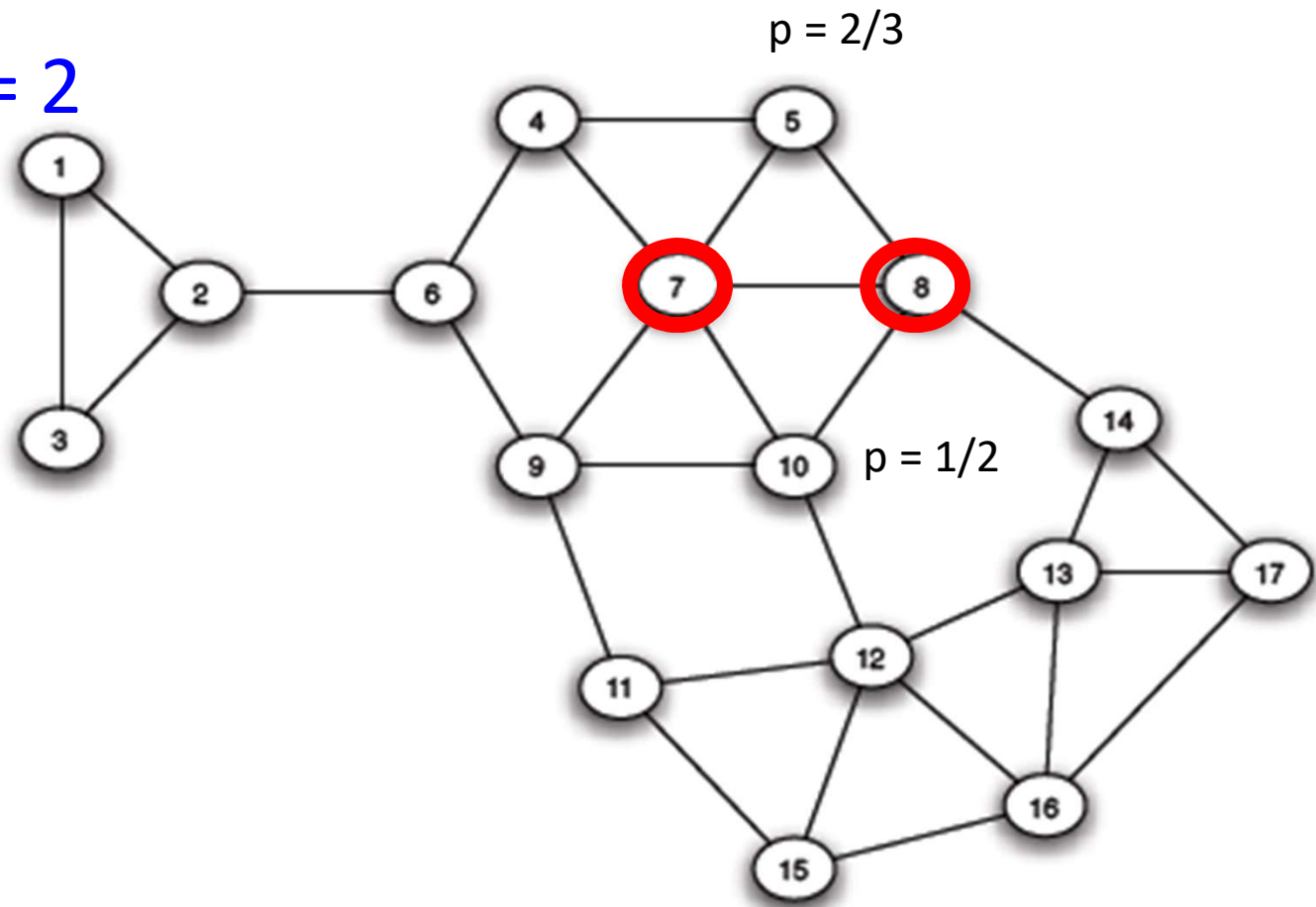
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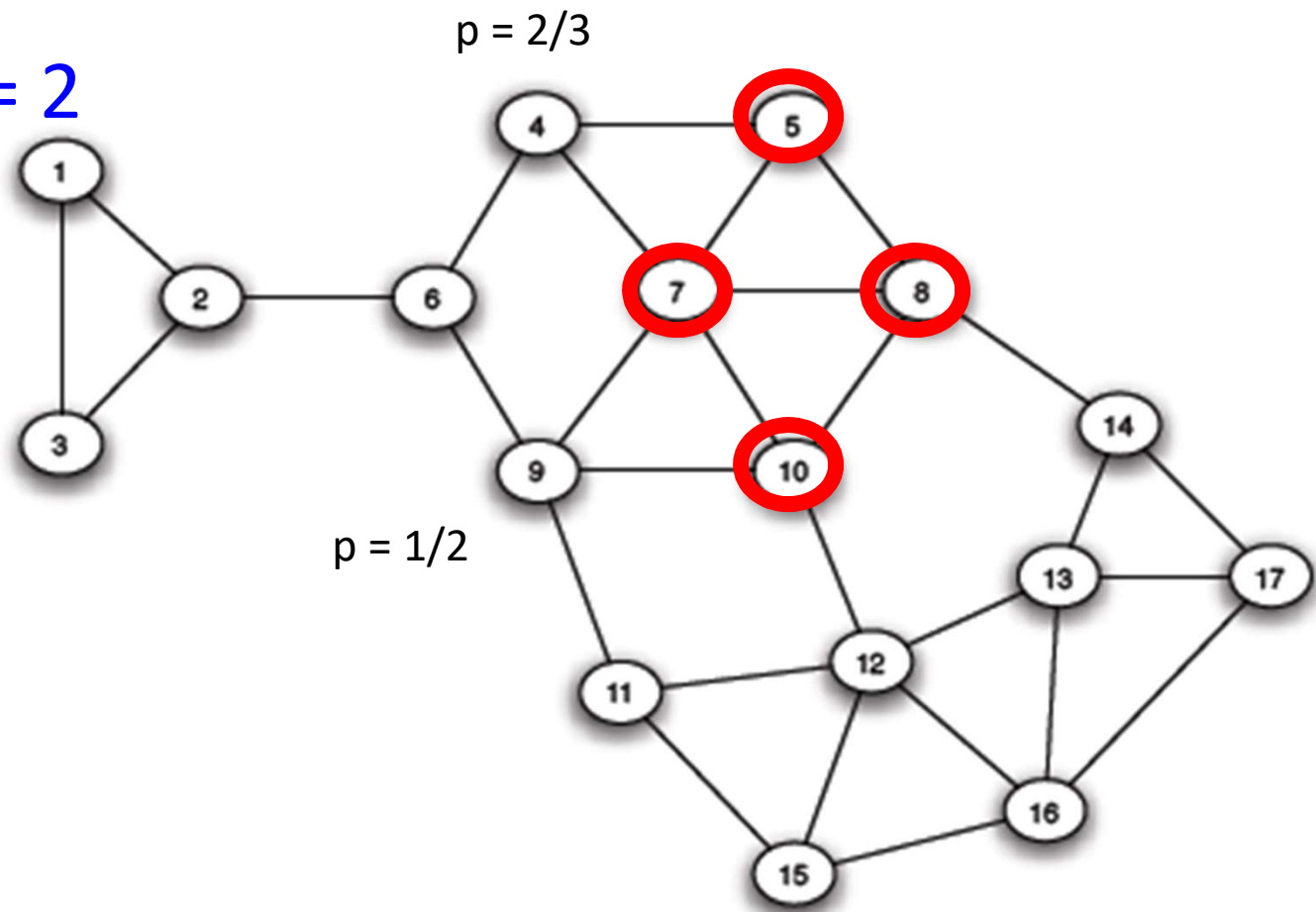
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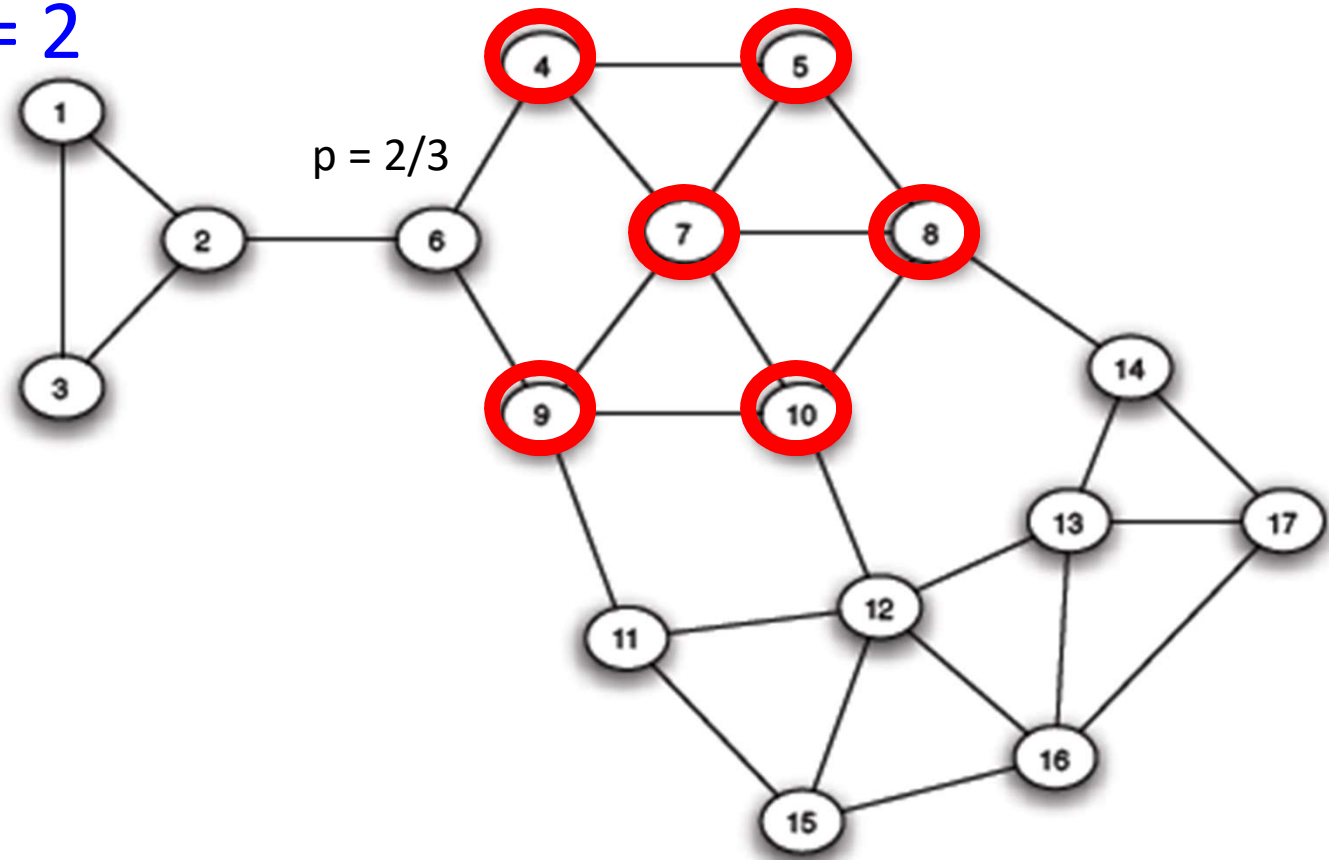
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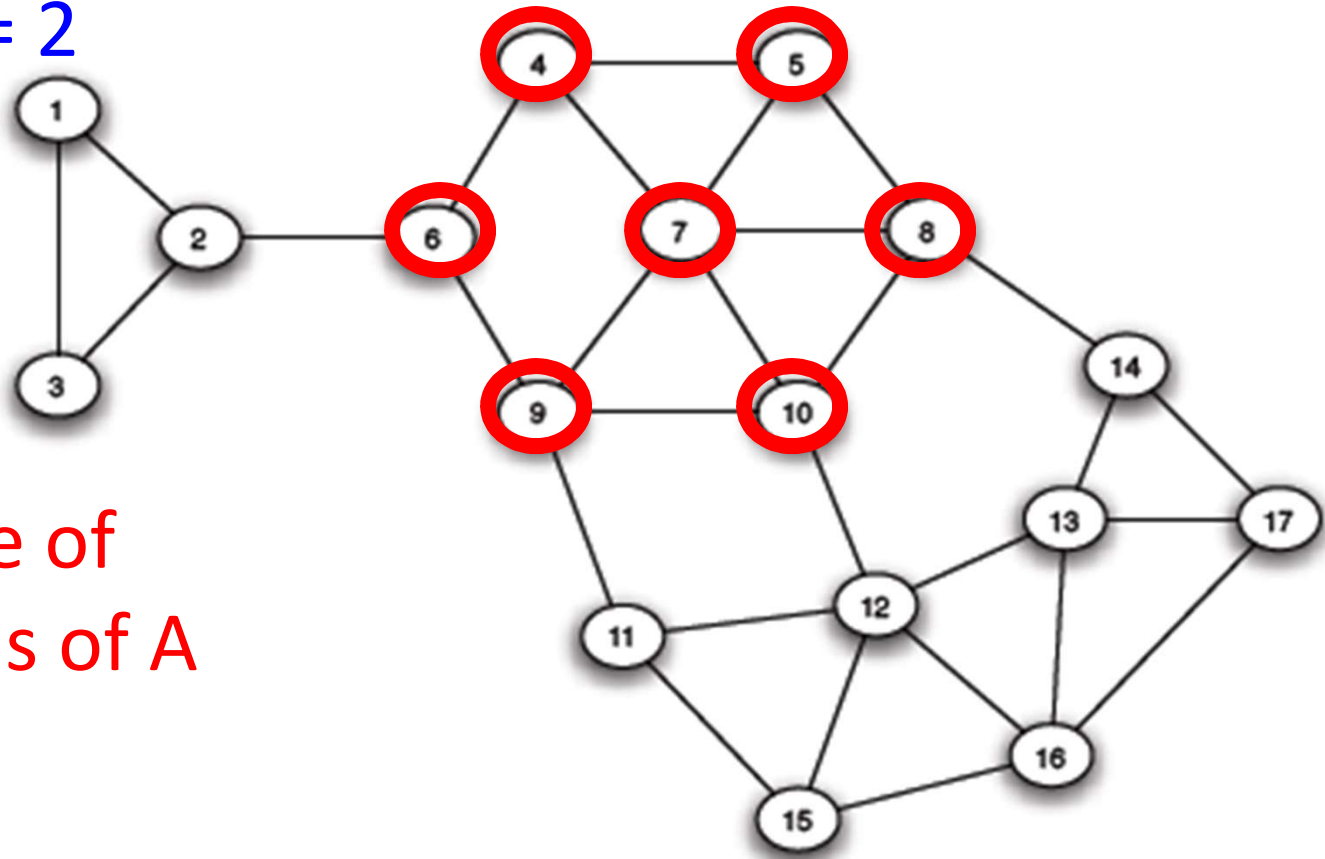




- $a = 3, b = 2$

- $q = \frac{b}{a+b} = \frac{2}{5}$

a cascade of  
adoptions of A





# Cascading Behavior

- At least two equilibria to the network coordination game :
  - all **A** or
  - all **B**.
  - Are there other equilibria ?
- Is it easy to "tip" from one equilibrium to another one ?
- Can we change from all **B** to all **A** with some **initial adopters** ?



# cascade of adoptions of A

- 2 possible outcomes
  - the cascade stops when there are **some B nodes**
  - **all nodes switch to A** : a complete cascade



## a complete cascade

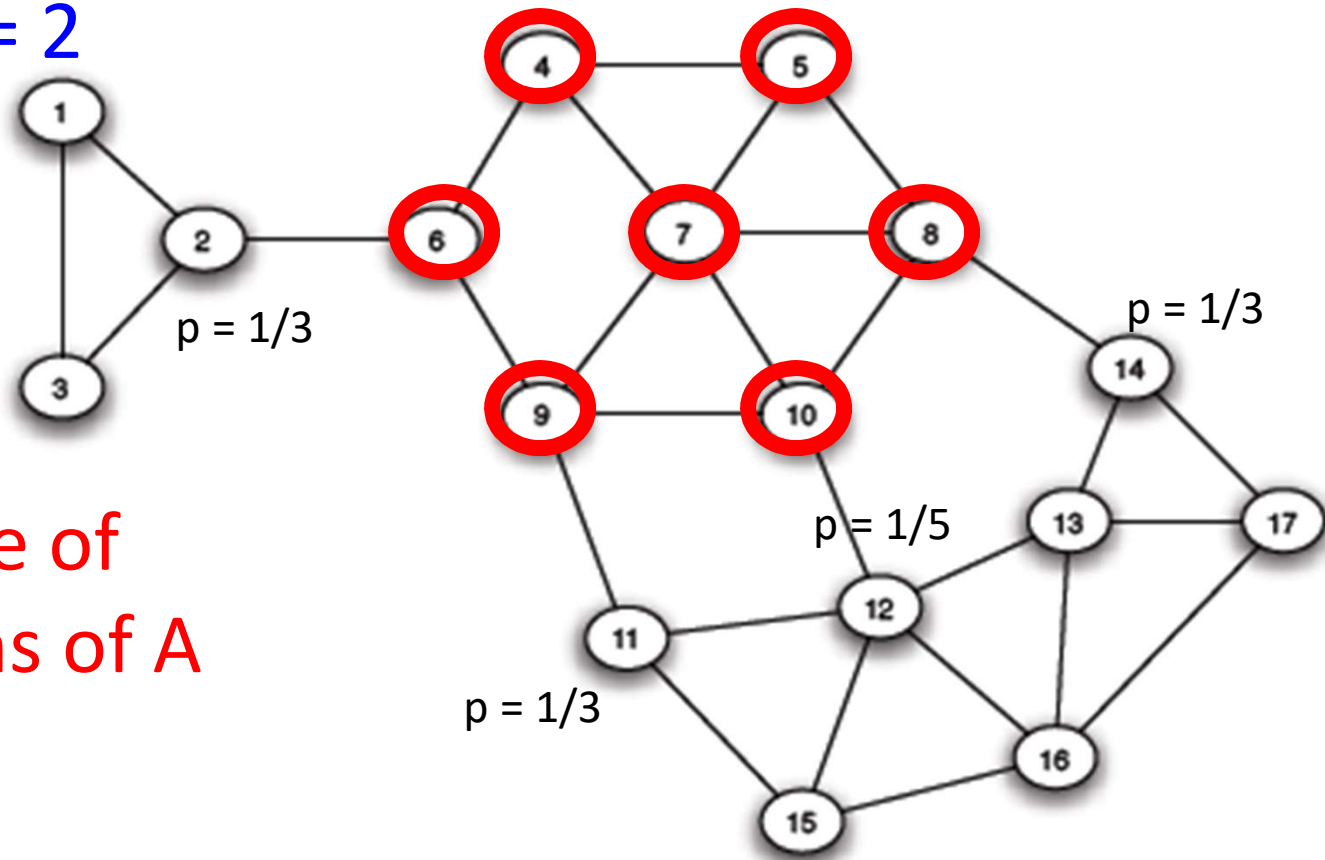
- Consider a set of initial adopters who start with a new behavior **A**, while every other node starts with behavior **B**.
- Nodes then repeatedly evaluate the decision to switch from **B** to **A** using a threshold of  $q$ .
- If the resulting cascade of adoptions of **A** eventually causes every node to switch from **B** to **A**, then we say that **the set of initial adopters causes a complete cascade at threshold  $q$ .**



- $a = 3, b = 2$

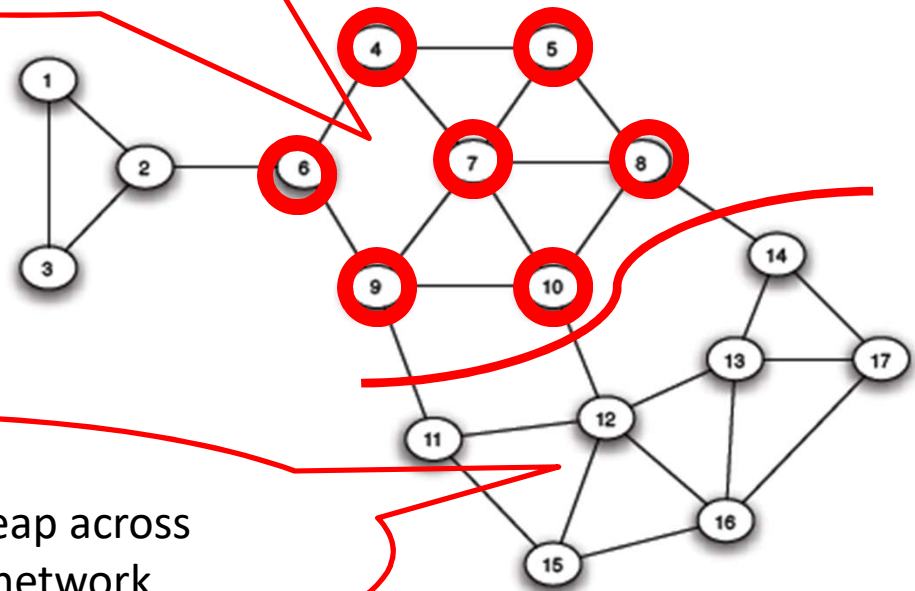
- $q = \frac{b}{a+b} = \frac{2}{5}$

a cascade of  
adoptions of A





A was able to spread to a set of nodes where there was sufficiently dense internal connectivity,



it was never able to leap across the “shores” in the network



# Cascading Behavior and Viral Marketing

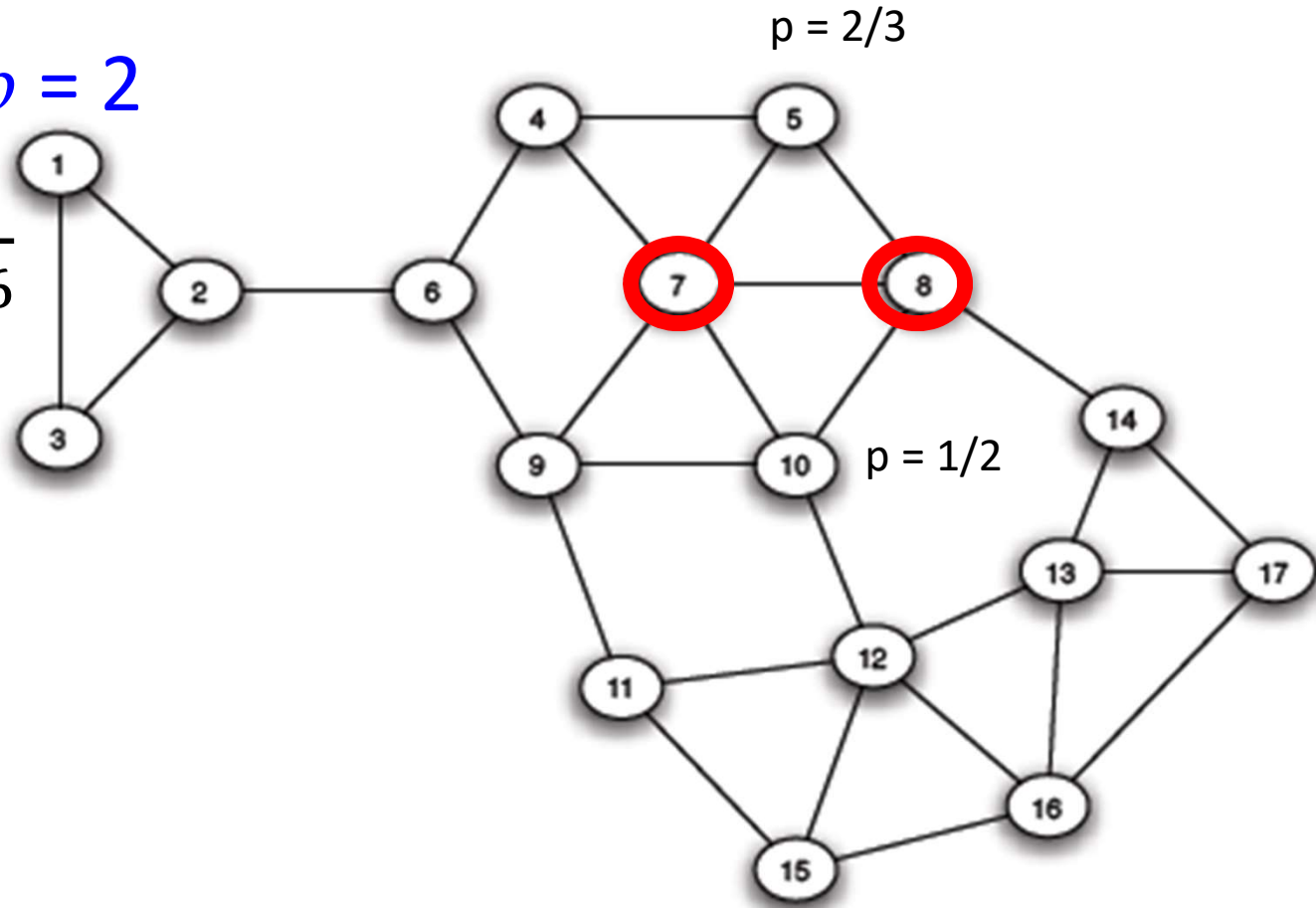
- The cascade runs for a while but stops while there are still nodes using B
  - different dominant political views between adjacent communities
  - different social-networking sites are dominated by different age groups and lifestyles even when the rest of the world are using something else
  - certain industries heavily use Apple Macintosh computers despite the general prevalence of Windows.



# complete cascade (lower threshold)

- $a = 3$ ,  $b = 2$

$$q = \frac{b}{a+b} = \frac{2}{56} = \frac{1}{3}$$

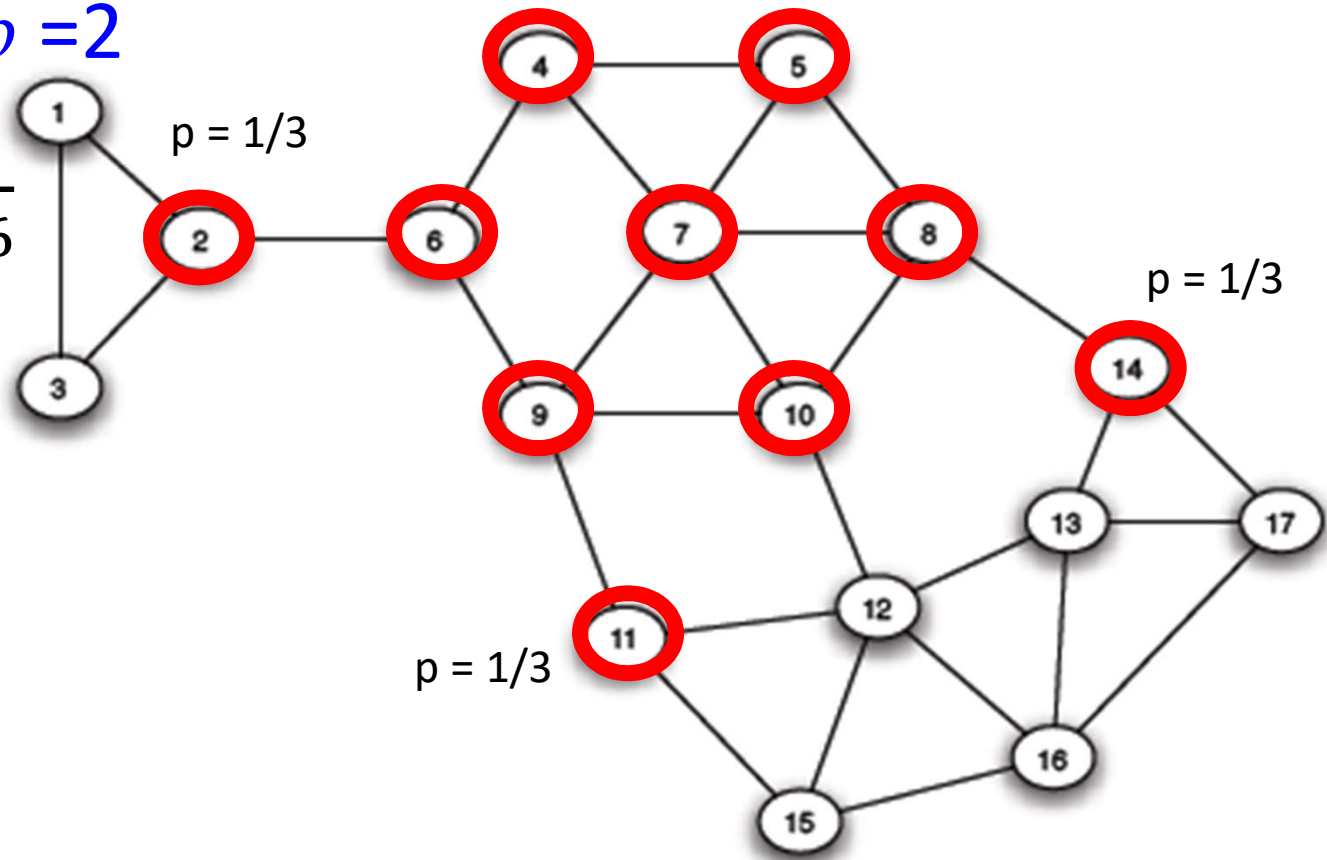






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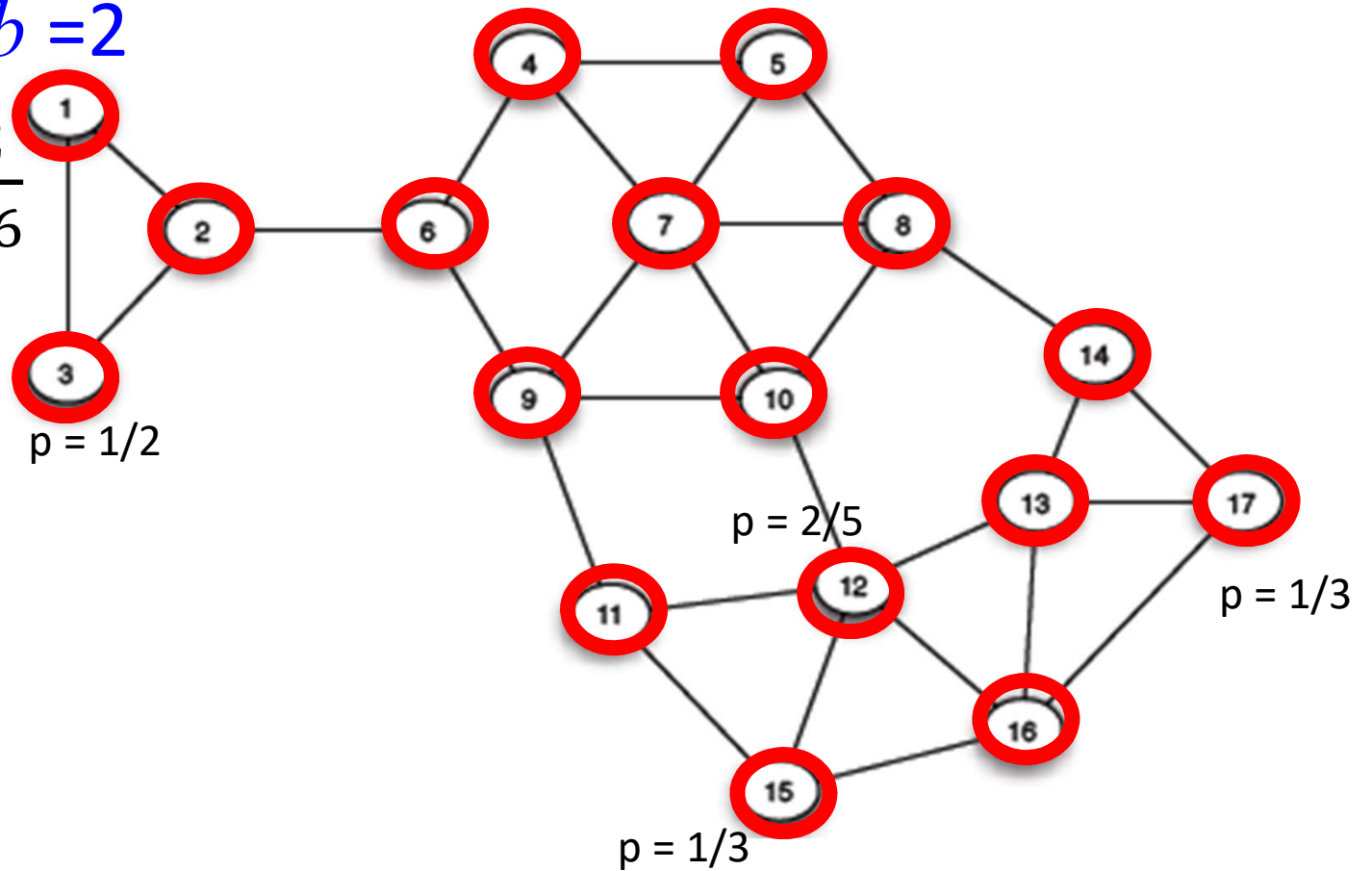




- $a = 3$ ,  $b = 2$

$$q = \frac{b}{a+b} = \frac{2}{56}$$

$$= \frac{1}{3}$$

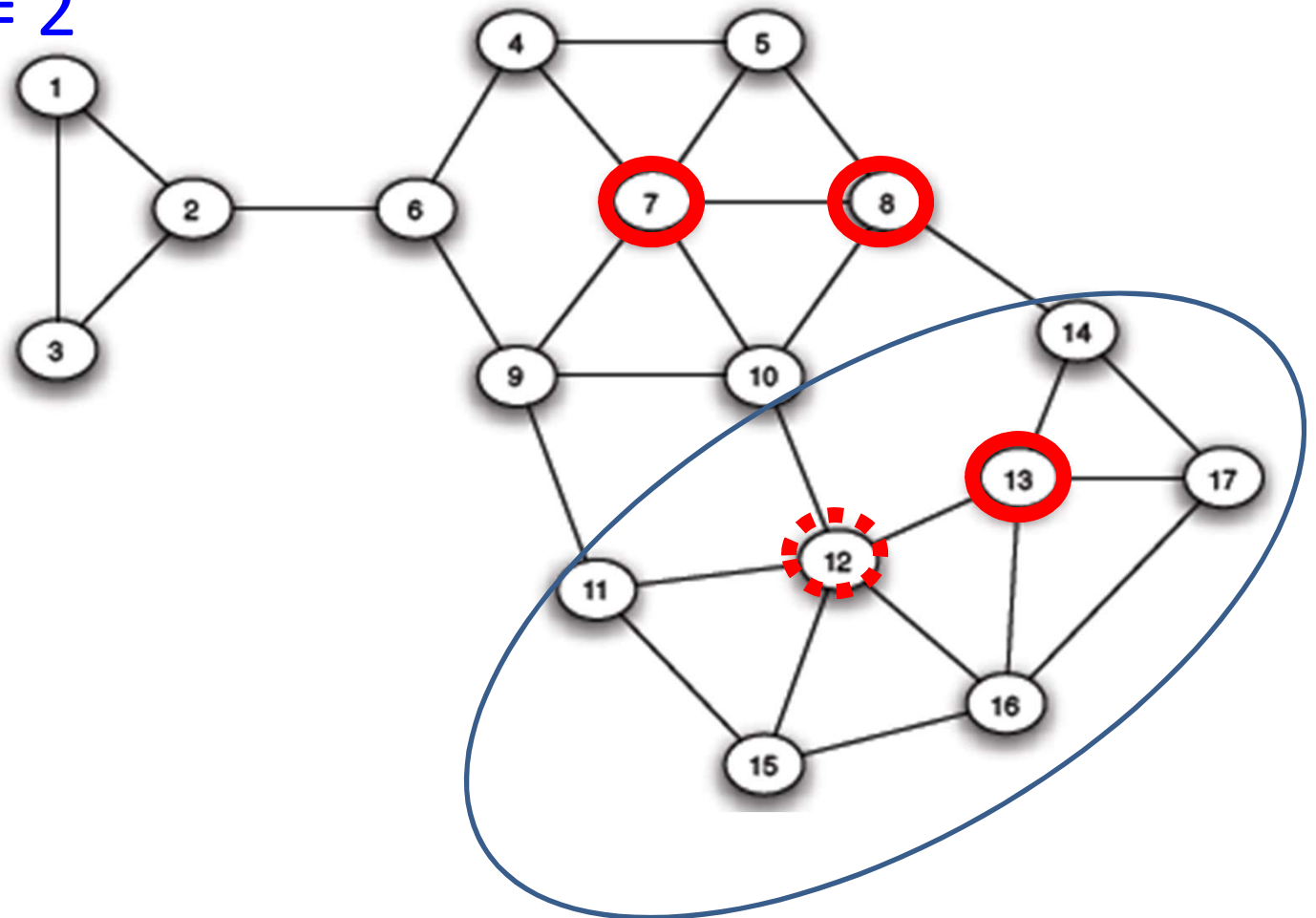




# complete cascade (choosing key nodes)

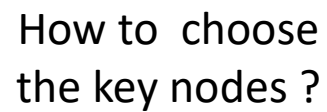
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- $$q = \frac{b}{a+b} = \frac{2}{5}$$



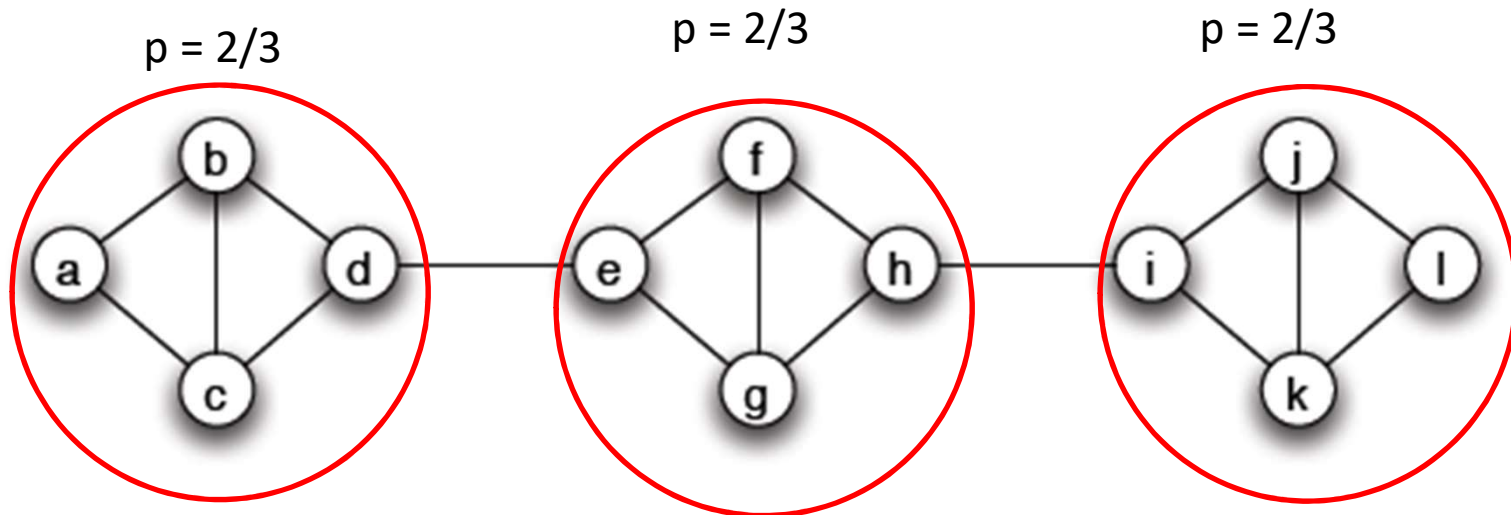


- Population-level model
  - Adoption decisions are evaluated based on the **fraction** of the entire population.
  - It can be very hard for a new technology to get started, even when it is an improvement on the status quo.
- Network-level model
  - People only care about what the immediate **neighbors** are doing.
  - It's possible for a small set of initial adopters to essentially start a long fuse running that eventually spreads the innovation globally.



## a cluster of density $p$

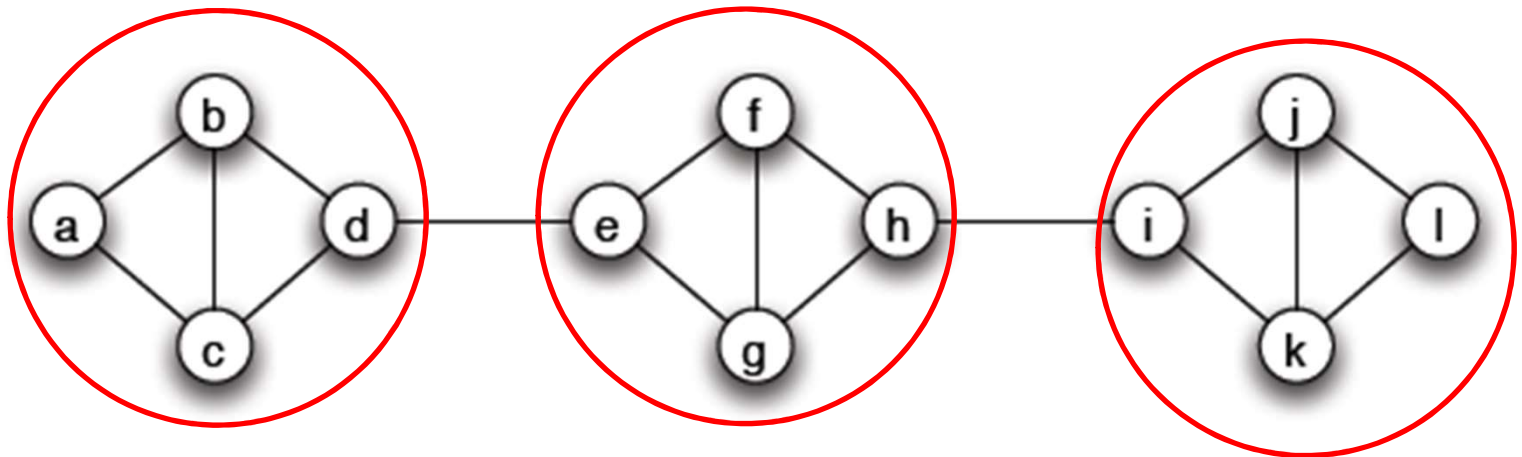
- a **cluster of density  $p$**  = a set of nodes such that each node in the set has at least a  $p$  fraction of its network neighbors in the set.





## Some properties

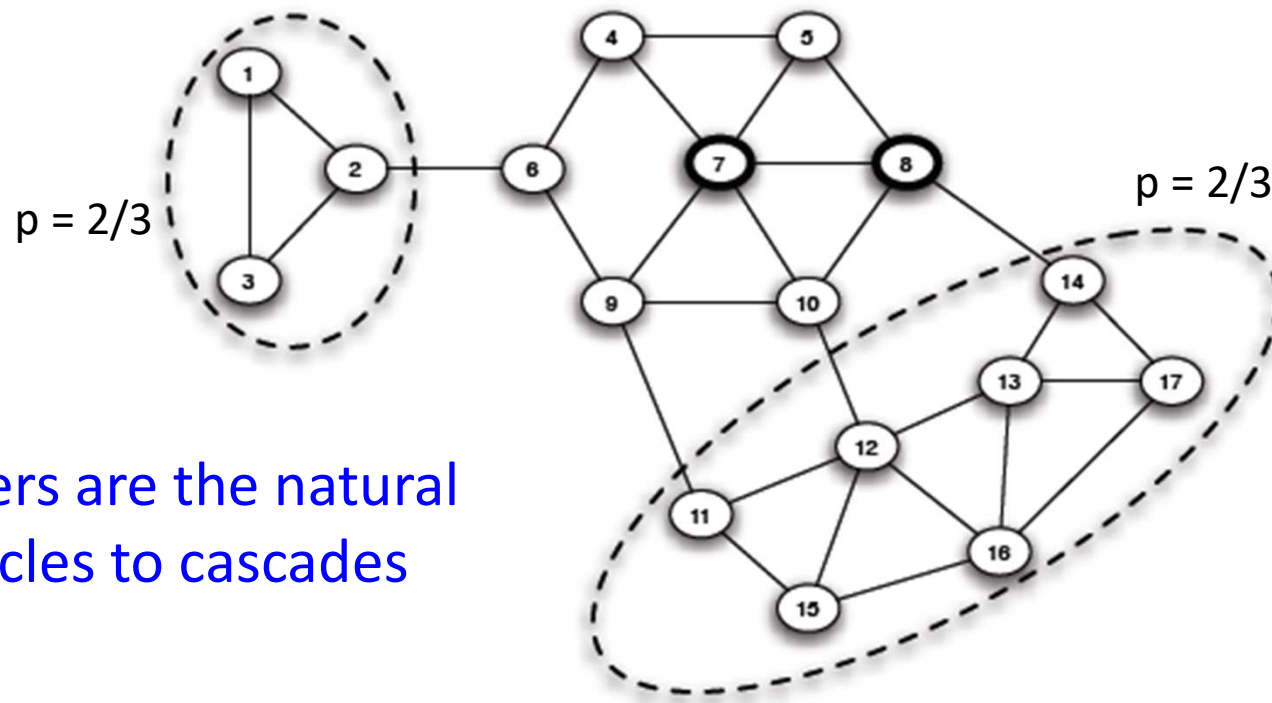
- The set of all nodes is always a cluster of density 1.
- The union of two clusters of density  $p$  is also a cluster of density  $p$ .





# Two clusters of density $p = 2/3$

Threshold  $q = \frac{2}{5}$



Clusters are the natural  
obstacles to cascades





# The Relationship between Clusters and Cascades

Claim: Consider a set of initial adopters of behavior A, with a threshold of  $q$  for nodes in the remaining network to adopt behavior A.

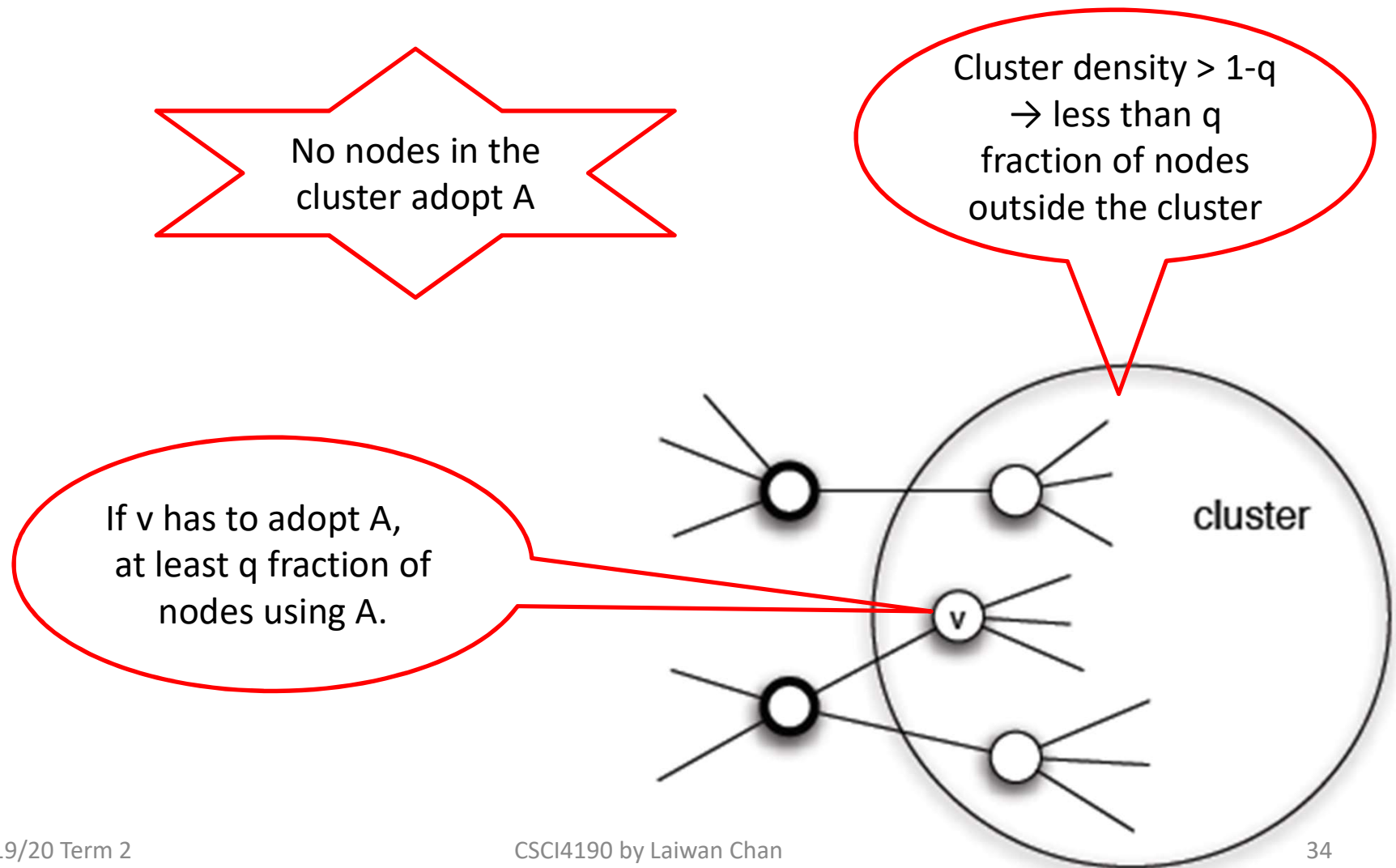
Clusters are Obstacles to Cascades

- (i) If the remaining network contains a **cluster of density greater than  $1 - q$** , then the set of initial adopters will **not cause a complete cascade**.
- (ii) Moreover, whenever a set of initial adopters **does not cause a complete cascade** with threshold  $q$ , the remaining network must contain **a cluster of density greater than  $1 - q$** .

Clusters are the only Obstacles to Cascades

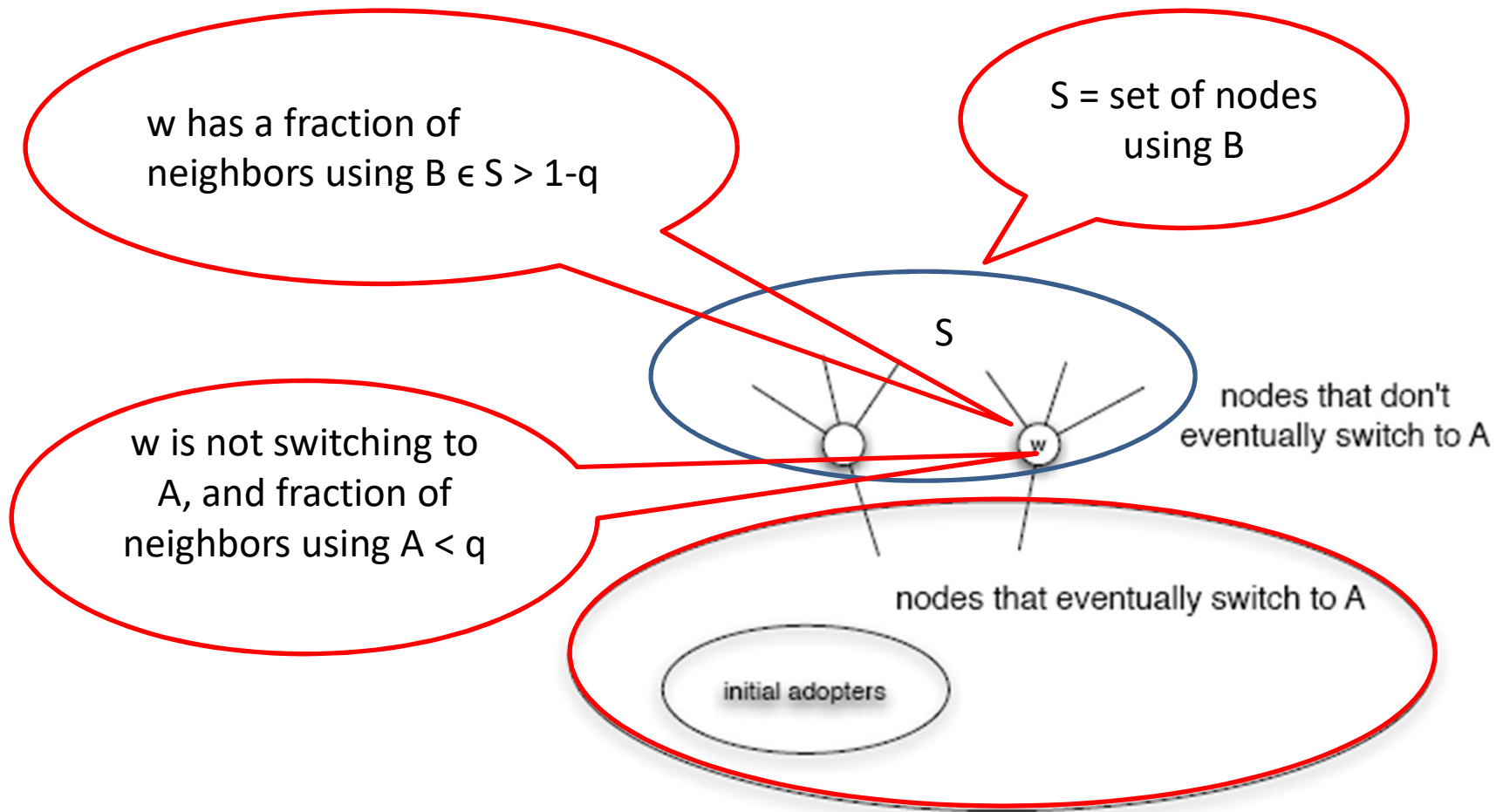


## (i) Clusters are Obstacles to Cascades



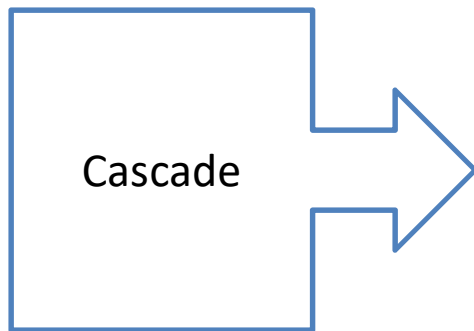


## (ii) Clusters are the only Obstacles to Cascades



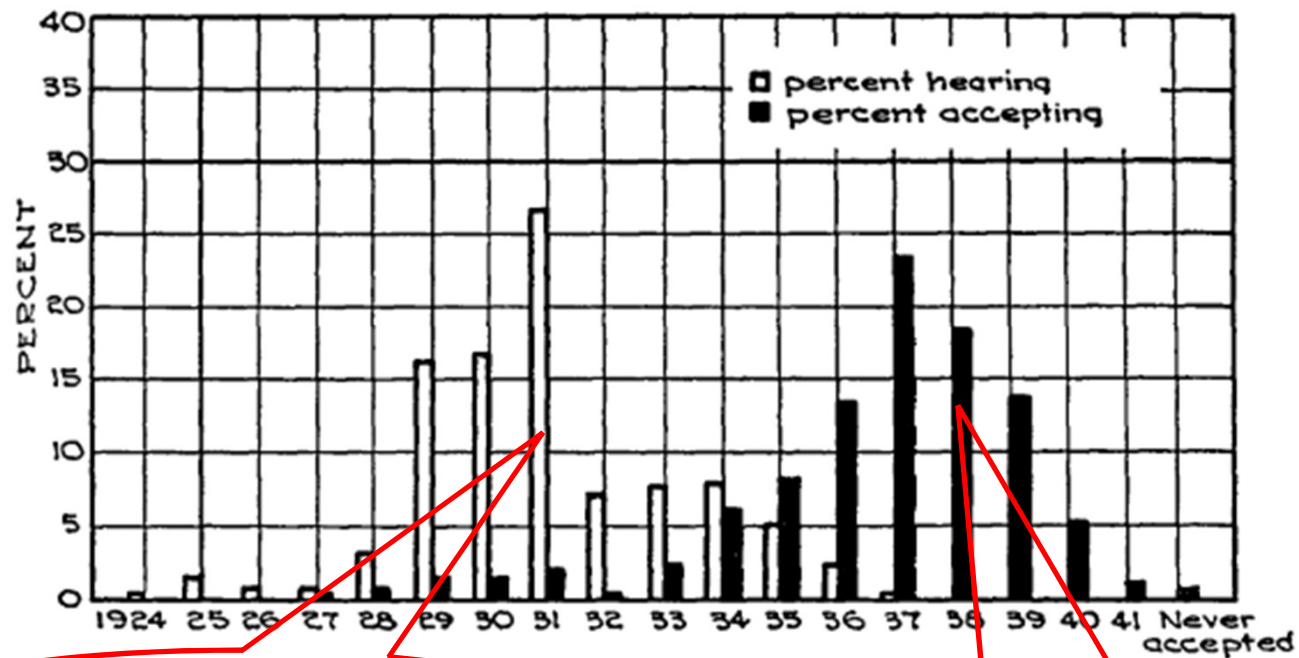


- Clusters block the spread of cascades
- When a cascade comes to a stop, there's a cluster !!





# Ryan-Gross : hybrid seed corn



Awareness of innovation

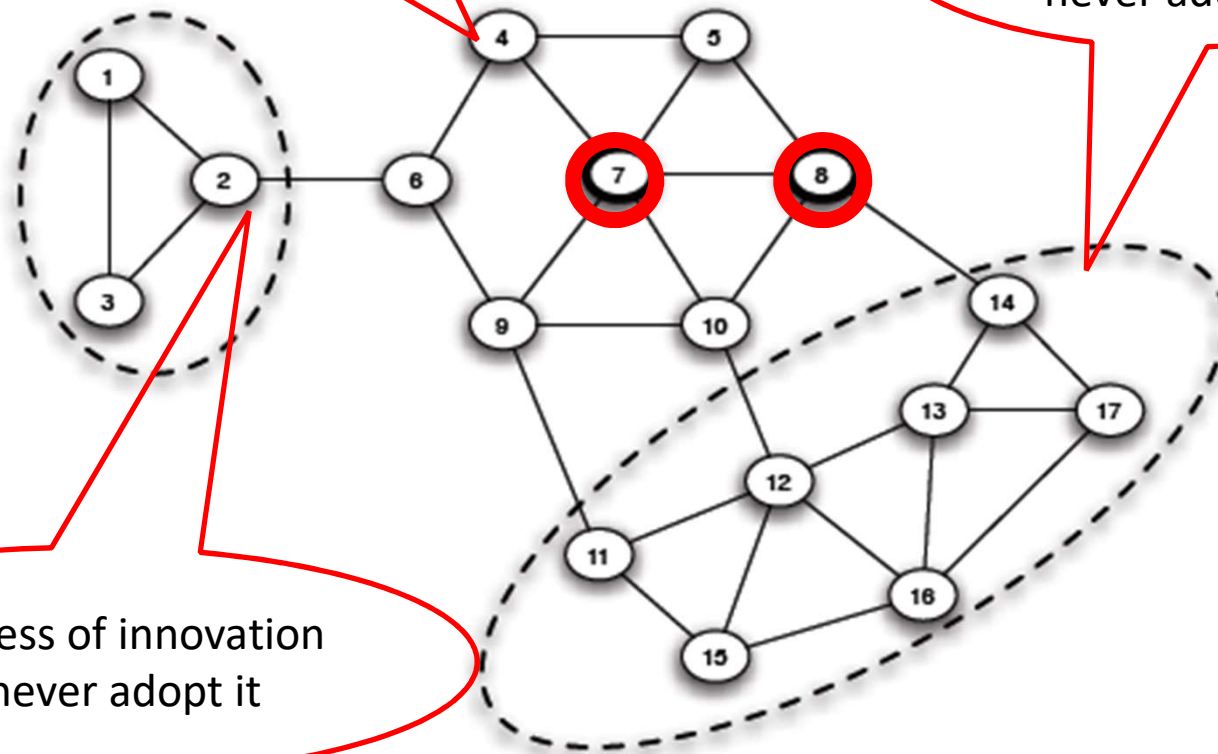
Adoption of innovation



Awareness of innovation  
but adopt it later when  
neighbors have adopted it

Awareness of  
innovation but  
never adopt it

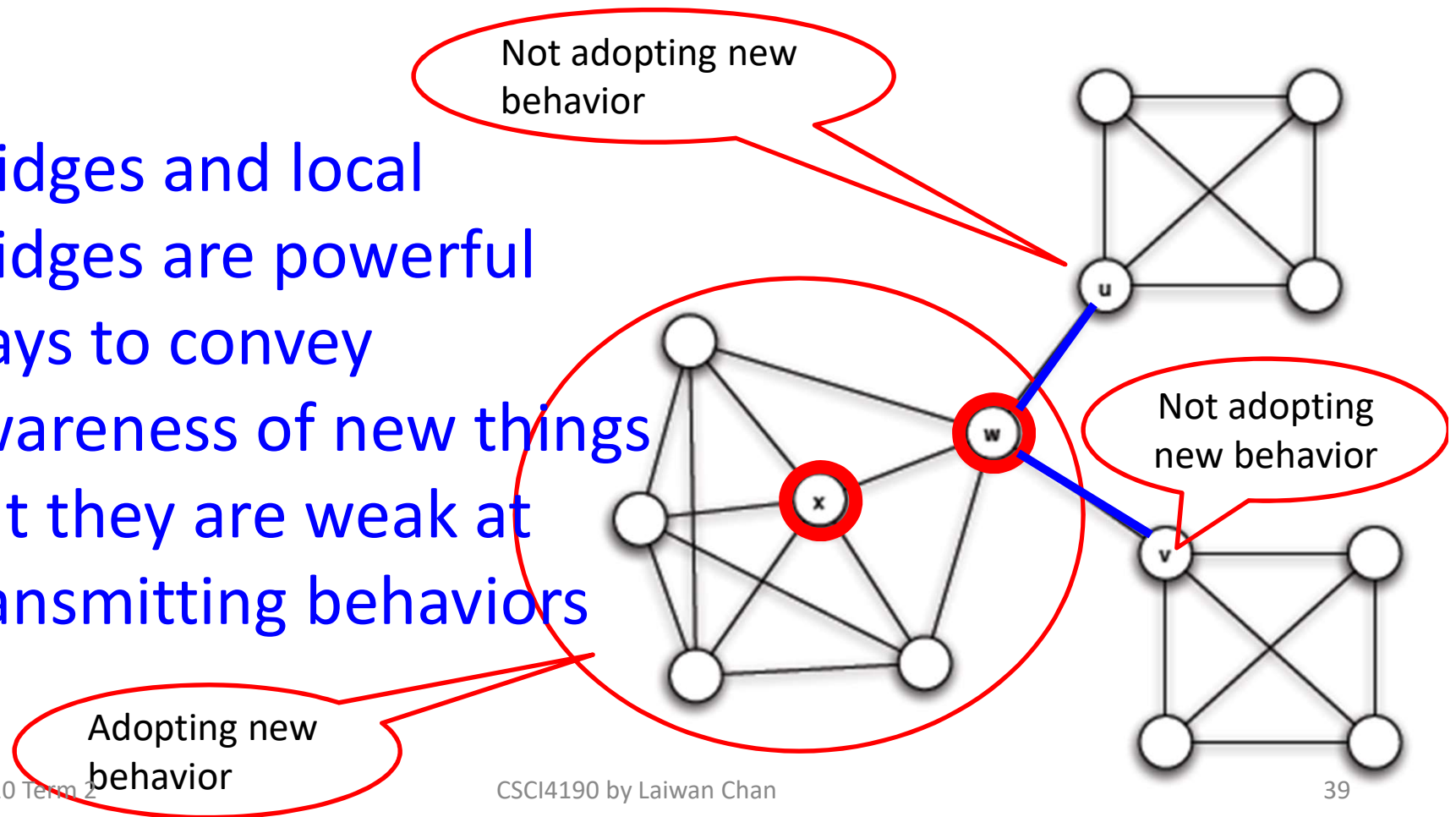
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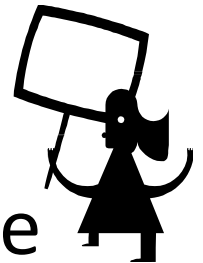
- x and w are the initial adopters of a new behavior with a threshold of  $1/2$ .

- Bridges and local bridges are powerful ways to convey awareness of new things but they are weak at transmitting behaviors





- A world-spanning system of weak ties in the global friendship network is able to **spread awareness** of a joke or an on-line video with remarkable speed.
- Political mobilization moves more sluggishly, needing to gain momentum within neighborhoods and small communities. Strong ties, rather than weak ties, played the more significant role in **social movements**.







# Extensions of the Basic Cascade Model

- **Heterogeneous Thresholds**

- each node has a specific payoff and hence threshold

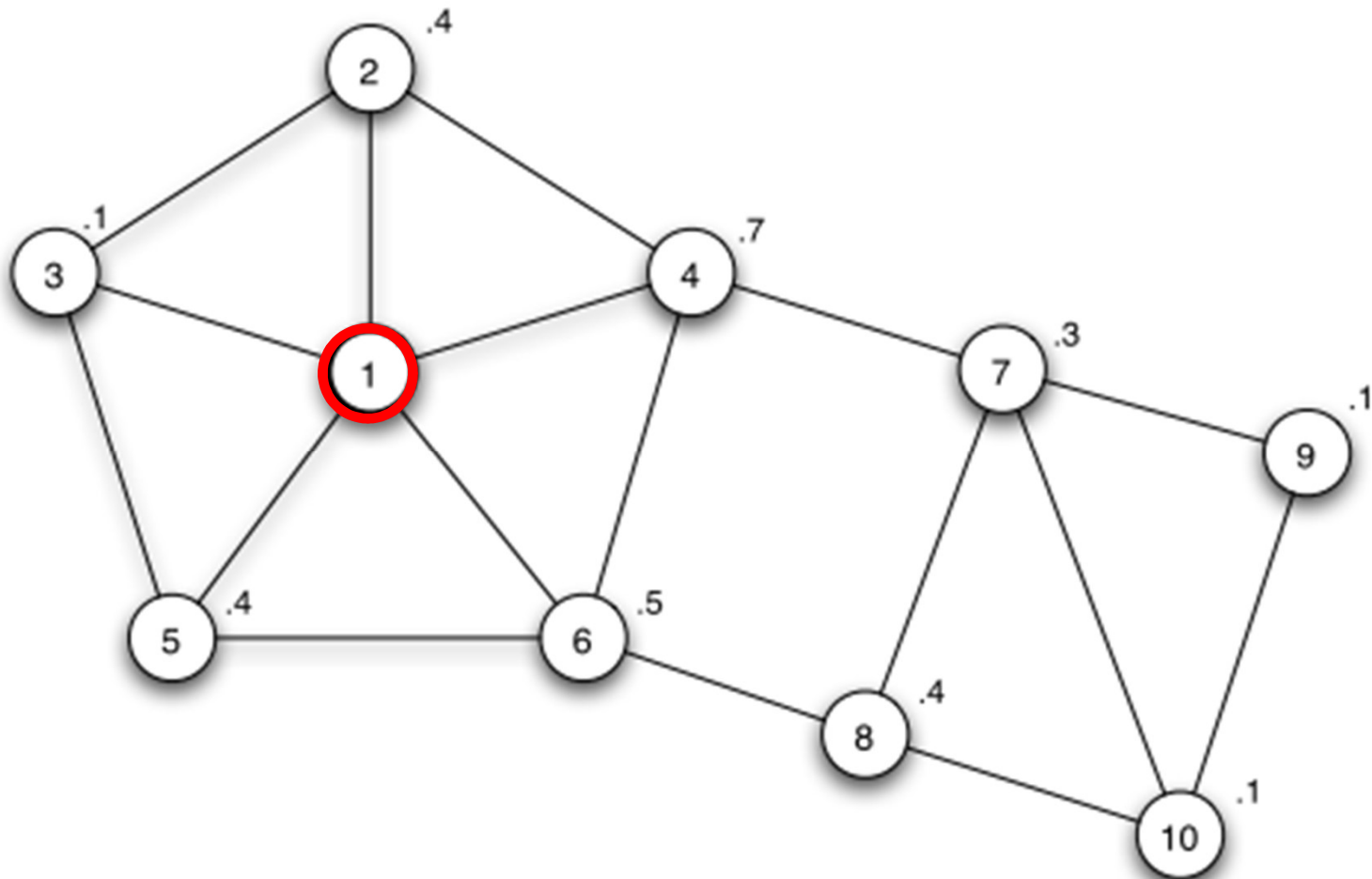
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- If  $v$  chooses A, payoff =  $pda_v$
- If  $v$  chooses B, payoff =  $(1-p)db_v$
- A is better if

$$pda_v \geq (1-p)db_v \quad \text{or} \quad p \geq \frac{b_v}{a_v + b_v} = q_v$$

		$w$	
		A	B
$v$	A	$a_v, a_w$	0, 0
	B	0, 0	$b_v, b_w$

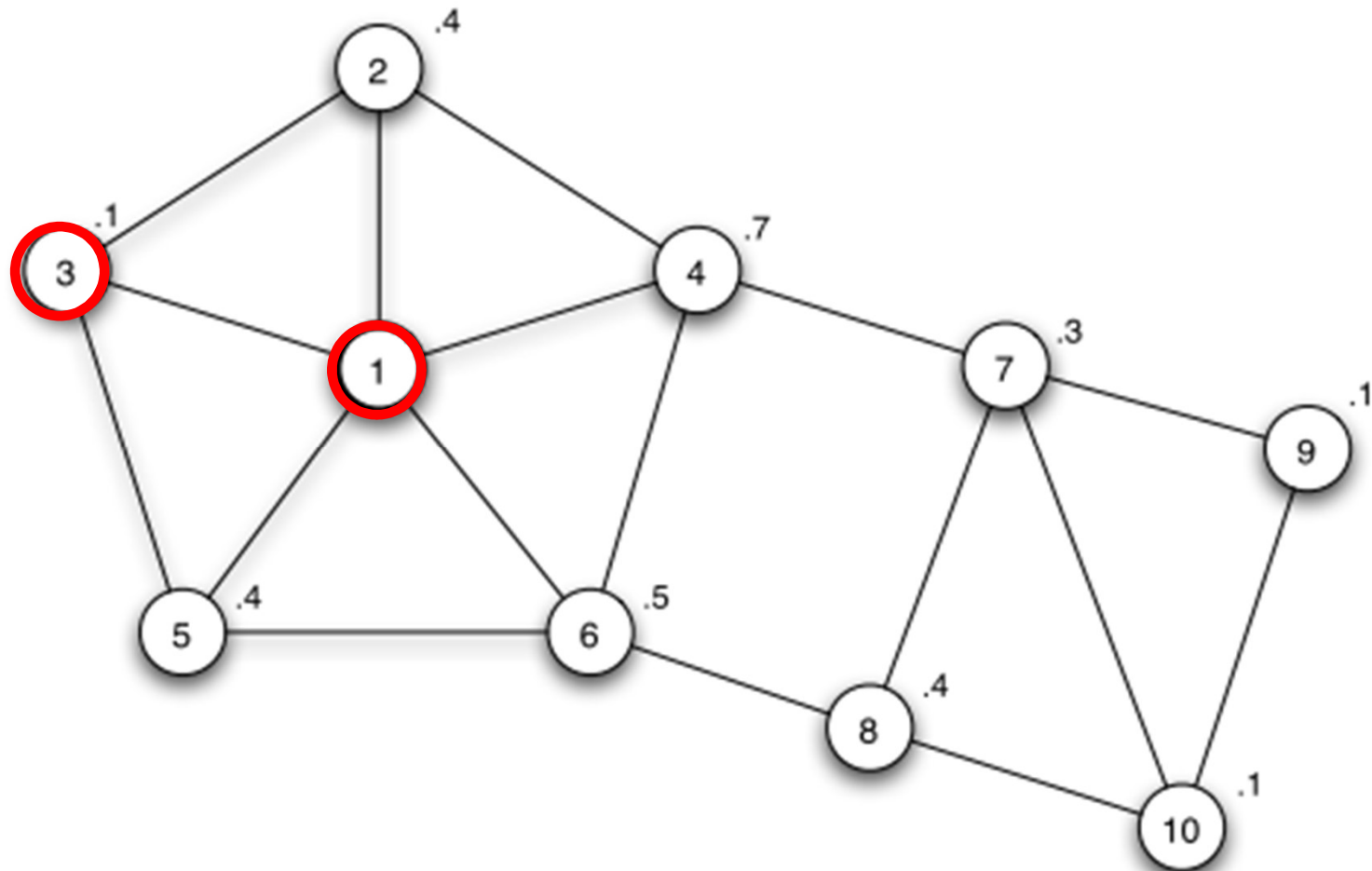


# Example of heterogeneous thresholds



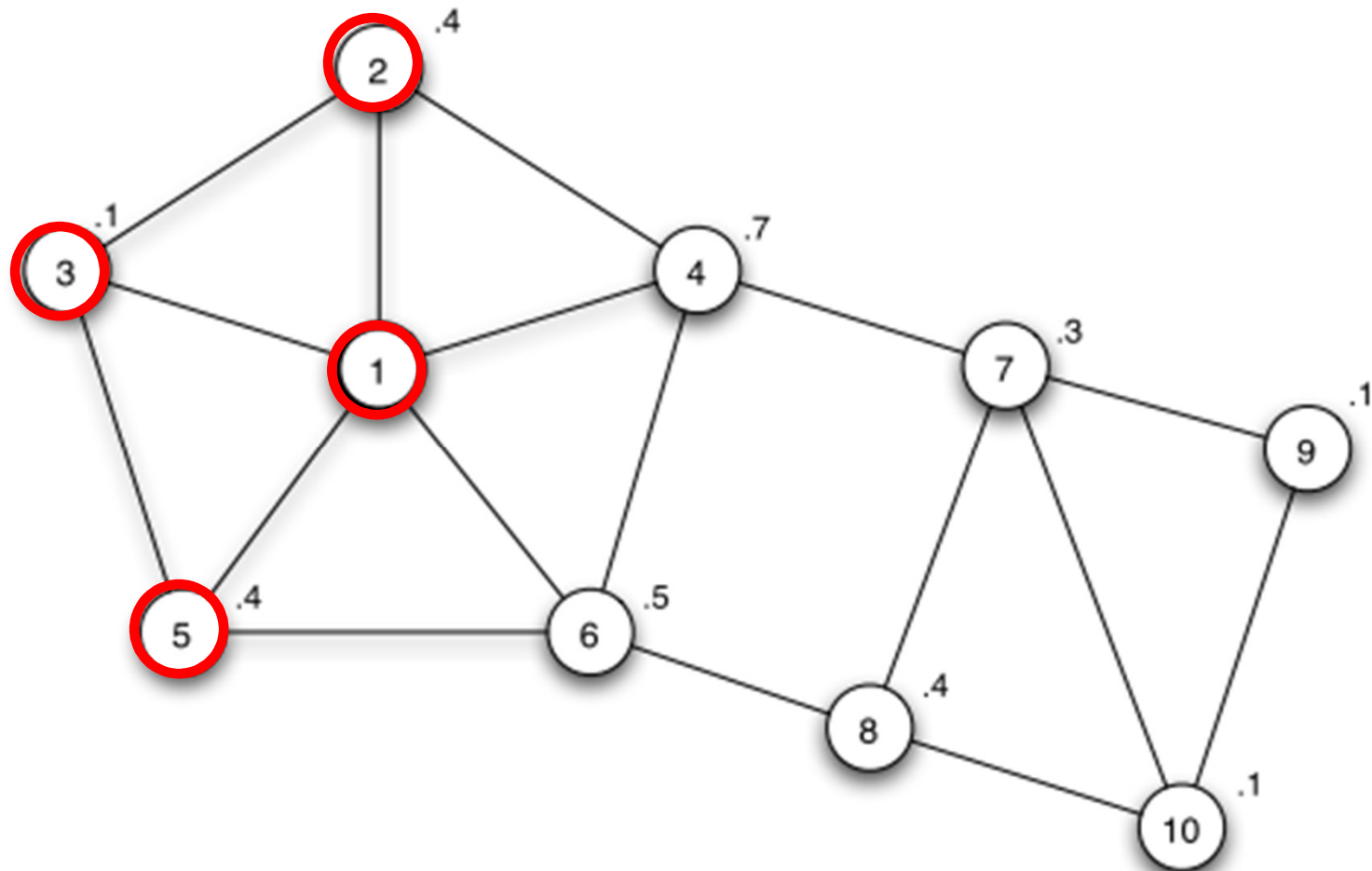


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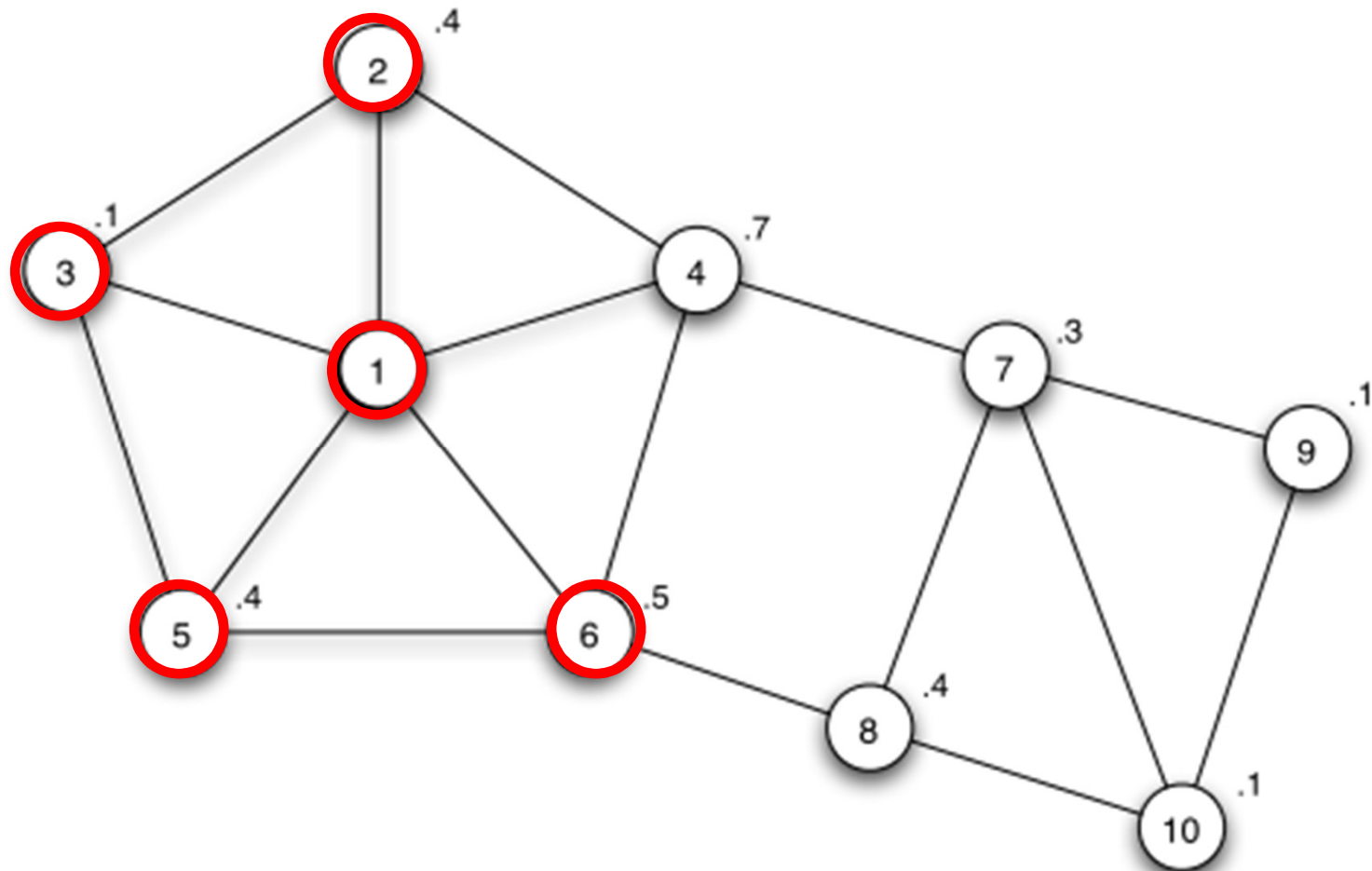


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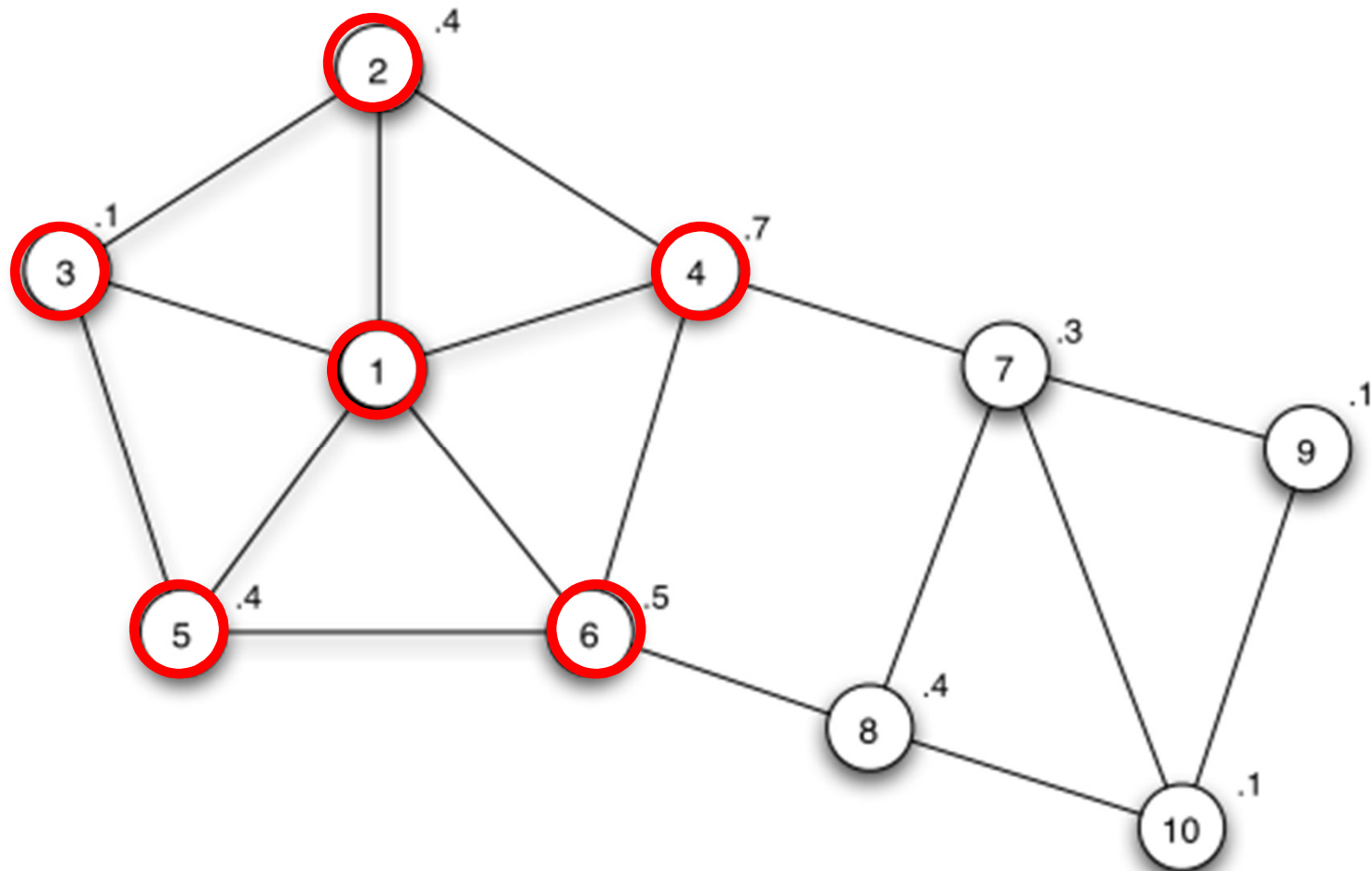


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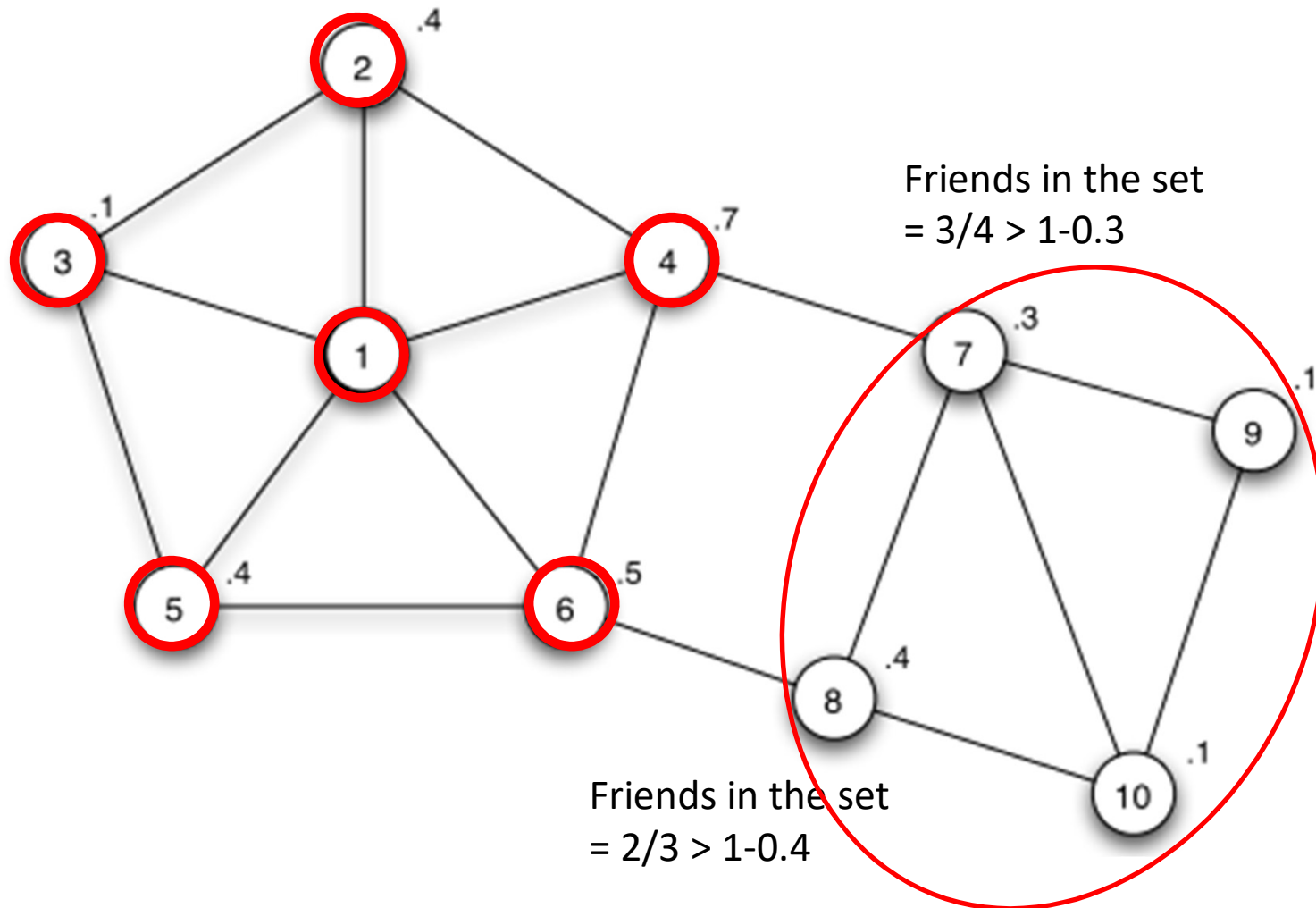




- Given a set of node thresholds
- A **blocking cluster** in the network is a set of nodes for which each node  $v$  has more than a  $1 - q_v$  fraction of its friends also in the set.
- It can be shown that a set of initial adopters will cause a complete cascade — with a given set of node thresholds — if and only if the remaining network does not contain a blocking cluster.



# Example of heterogeneous thresholds







# Knowledge, Thresholds, and Collective Action



Integrating network effects at both the population level and the local network level.

- There is a public demonstration against the government tomorrow.
  - If an enormous number of people show up, the government will have to address the issue and everyone will benefit.
  - If only a few hundred show up, the demonstrators will be arrested.
  - What would you do ?






# Knowledge, Thresholds, and Collective Action

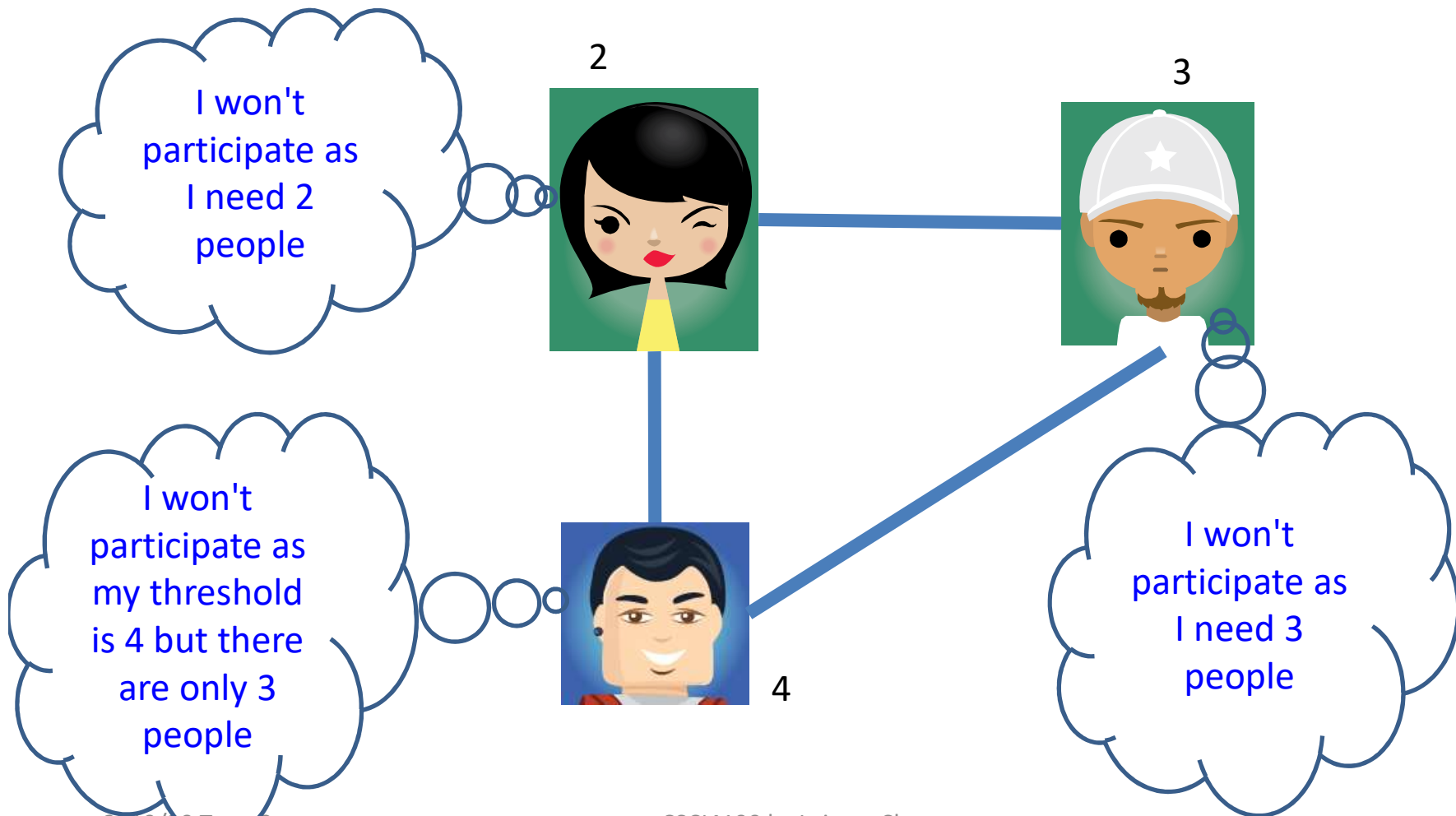
- We consider situations where coordination across a large segment of the population is important, and the underlying social network is serving to transmit information about people's willingness to participate.
- **Collective action problem**: A positive payoff if a lot of people participate, a negative payoff if only a few participate (e.g. protest under a repressive regime).
- **Pluralistic ignorance**: People have wildly erroneous estimates about the prevalence of certain opinions in the population at large.

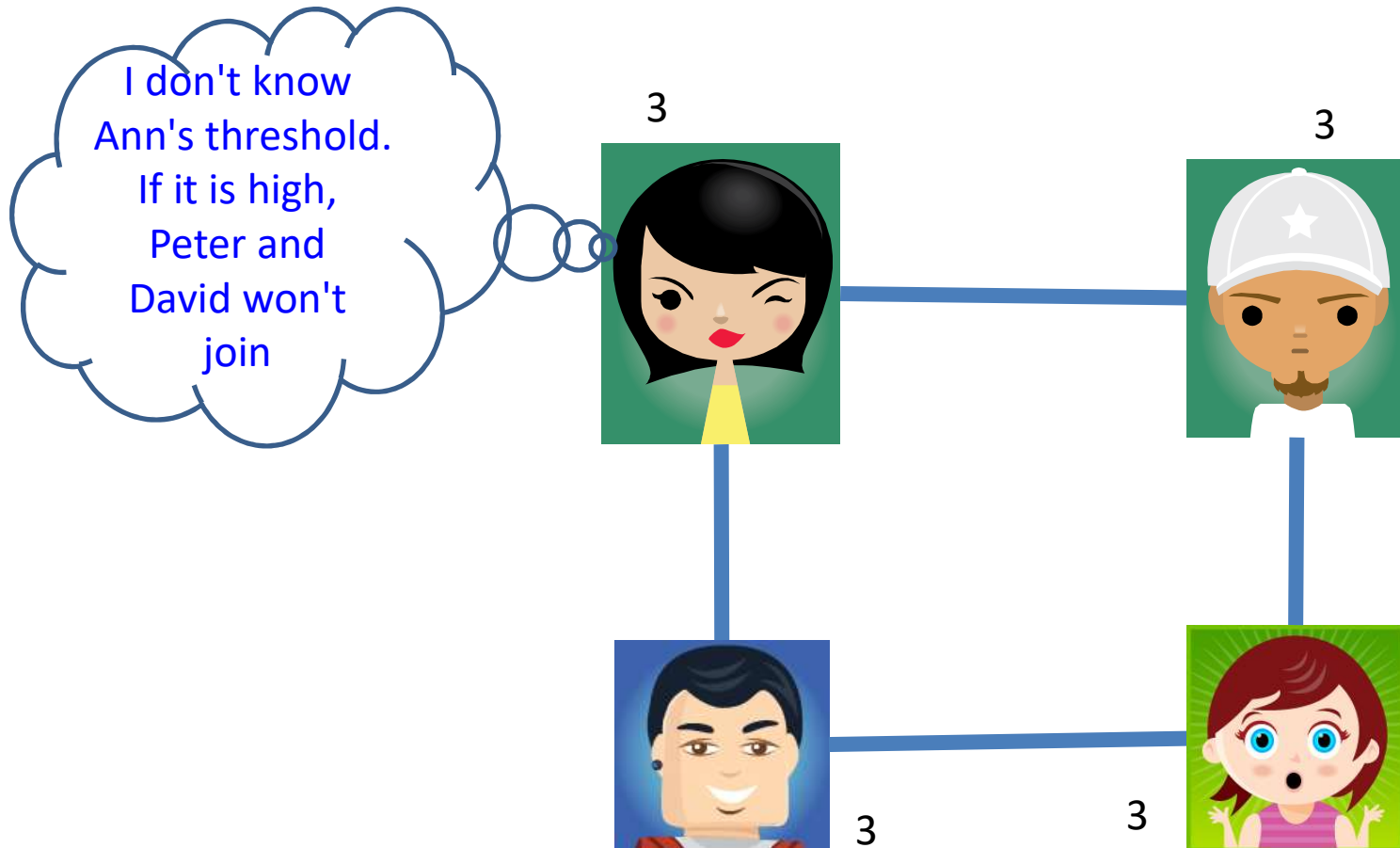




# A Model for the Effect of Knowledge on Collective Action

- 
- Each person in the network knows the thresholds of all her neighbors in the network.
- Each does not know the thresholds of anyone else.
- What is likely to happen?

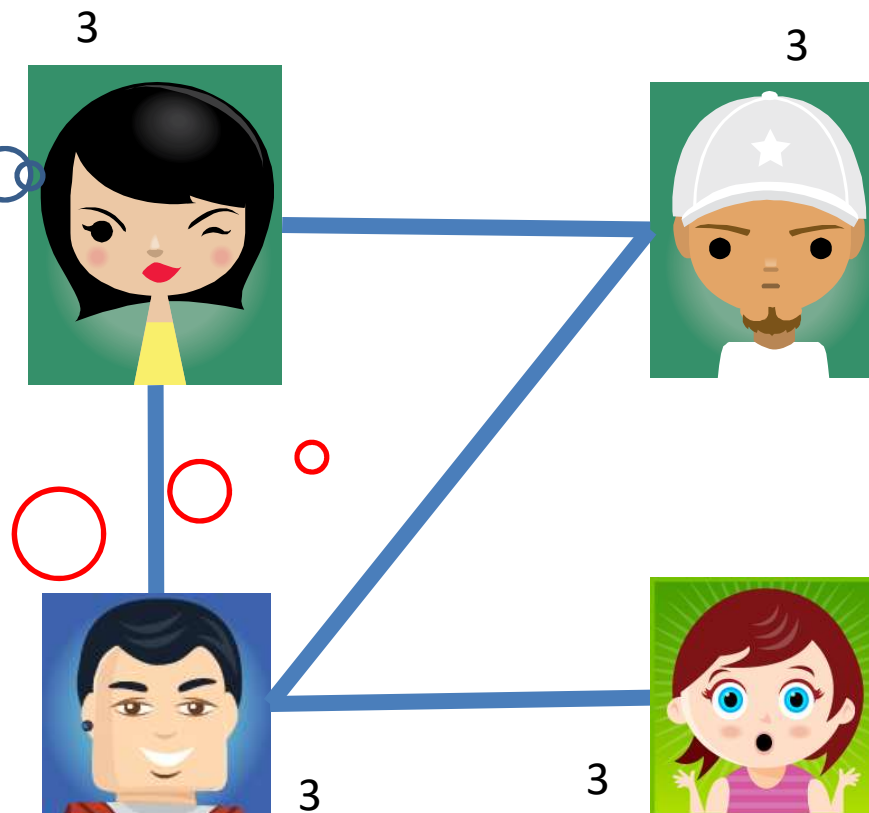






All three of us  
have threshold  
of 3, so let's  
join !!!!!

Strong ties and  
tightly-knit  
communities give  
us common  
knowledge →  
collective actions





# Common Knowledge and Social Institutions

- generators of common knowledge
  - A widely-publicized speech, or
  - an article in a high-circulation newspaper
  - freedom of the press and freedom of assembly
  - advertise products where there are strong network effects (telling each viewer that many other viewers were informed about the product)
- social networks
  - allow for interaction,
  - the flow of information,
  - allow individuals to base decisions on what others know, and on how they expect others to behave as a result.