TUTORIAL 1

CSCI3230 (2019-2020 First Term)

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Outline

- Artificial Neural Network
 - Biological Neuron vs. Artificial Neuron
 - Gradient Descent
 - Vanishing Gradient Problem

Artificial Neural Network

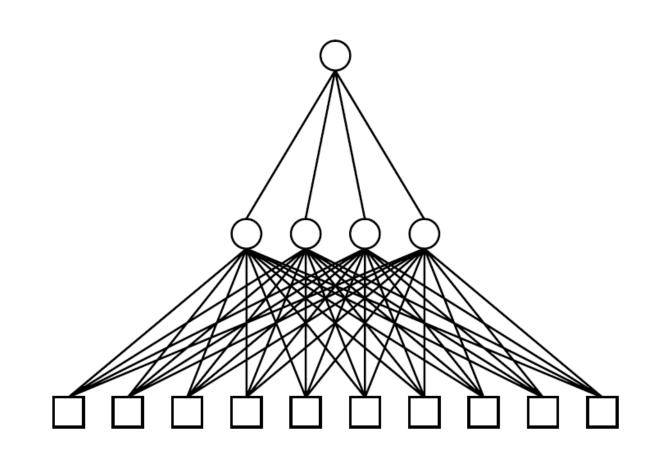
Output units O_i

 $W_{j,i}$

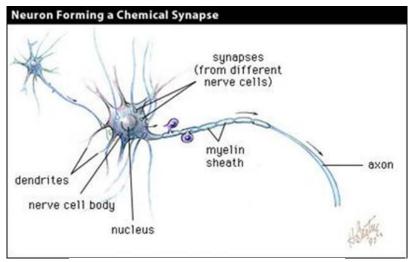
Hidden units a_j

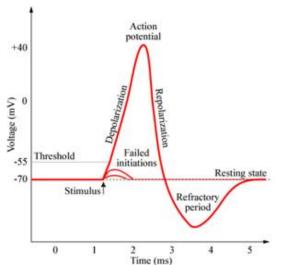
 $W_{k,j}$

Input units I_k



Biological Neuron

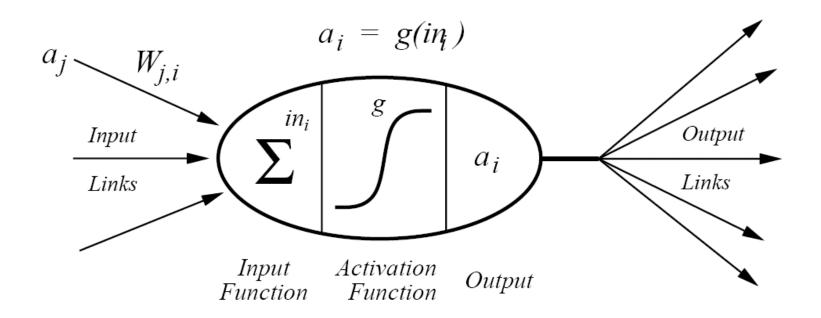




- A neuron is an electrically excitable cell that processes and transmits information through electrical and chemical signals.
- A chemical signal is transmitted via a synapse, a specialized connection with other cells.

Artificial Neuron

 An artificial neuron is a logic computing unit, conceived as a model of biological neurons.



Idea Behind ANN

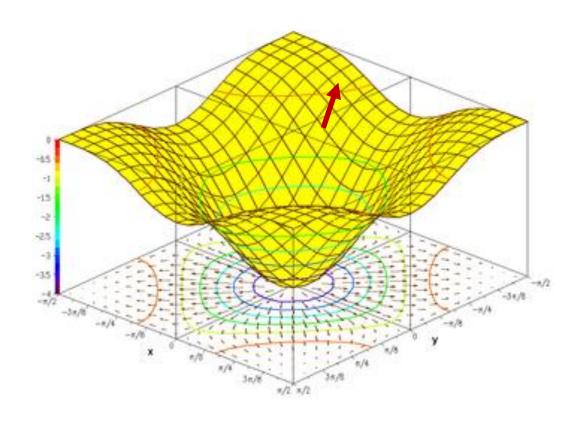
- Gradient Descent
- To find a *local* minimum of a function using gradient descent, one takes steps proportional to the *negative* of the gradient (or of the approximate gradient) of the function at the current point.
- A widely-used iterative optimization technique

For a smooth function $f(\vec{x})$,

 $\frac{\partial f}{\partial \vec{x}}$ is the direction that f increases most rapidly.

So
$$\vec{x}_{t+1} = \vec{x}_t - \eta \frac{\partial f}{\partial \vec{x}} \Big|_{\vec{x} = \vec{x}_t}$$
 until \vec{x} converges

Visualization of Gradient



Gradient Descent Method

- Let E be the loss function of some model
- Gradient

$$\nabla E[\vec{w}] \equiv \left[\frac{\partial E}{\partial w_0}, \frac{\partial E}{\partial w_1}, \cdots \frac{\partial E}{\partial w_n} \right]$$

Training Rule

$$w_i \leftarrow w_i + \Delta w_i$$

with

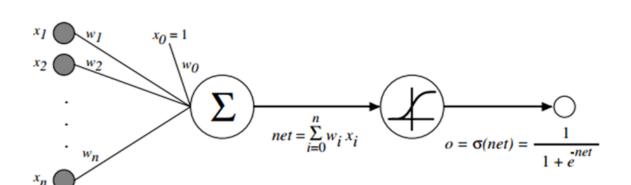
$$\Delta \vec{w} = -\eta \nabla E[\vec{w}]$$

i.e.

$$\Delta w_i = -\eta \frac{\partial E}{\partial w_i}$$

Partial Derivatives and Chain Rule are the keys

Chain Rule



$$\frac{dz}{dx} = \frac{dz}{dy} \cdot \frac{dy}{dx}$$

Input
$$x \longrightarrow net = \sum w_i x_i \longrightarrow o = \frac{1}{1 + e^{-net}} \longrightarrow Error E = \frac{1}{2}(t - o)^2$$

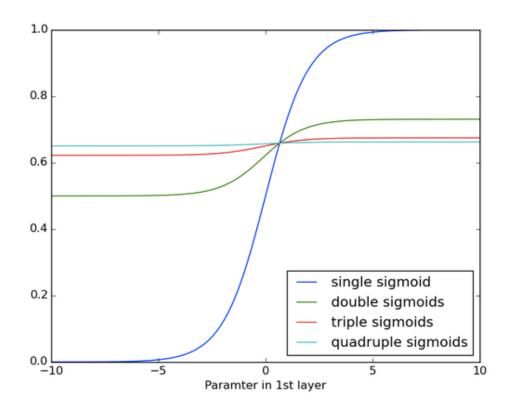
$$\frac{\partial E}{\partial w_i} = \frac{\partial E}{\partial o} * \frac{\partial o}{\partial net} * \frac{\partial net}{\partial w_i}$$

Training via Gradient Descent

```
function Back-Prop-Update(network, examples, \alpha) returns a network with modified weights
inputs: network, a multilayer network
          examples, a set of input/output pairs
         \alpha, the learning rate
repeat
  for each e in examples do
     /* Compute the output for this example */
      O \leftarrow \text{Run-Network}(network, I^e)
     /* Compute the error and \Delta for units in the output layer */
     Err^e \leftarrow T^e - O
     /* Update the weights leading to the output layer */
      W_{i,i} \leftarrow W_{i,i} + \alpha \times a_i \times Err^e_i \times g'(in_i)
                                                   /* Err^{e}_{i} \times g'(in_{i}) = \Delta_{i} */
      for each subsequent layer in network do
                                                                             Output units O_i
        /* Compute the error at each node */
        \Delta_i \leftarrow g'(in_i) \Sigma_i W_{i,i} \Delta_i
                                                                                              W_{i,i}
        /* Update the weights leading into the layer */
        W_{k,i} \leftarrow W_{k,i} + \alpha \times I_k \times \Delta_i
                                                                              Hidden units a_i
      end
    end
                                                                                              W_{k,i}
until network has converged
return network
                                                                              Input units
```

Limitation of ANN

- Vanishing Gradient Problem
- Activation function becomes flatter with more layers of neurons, so the network cannot go too deep



What if

- Generally speaking, the power of neural networks increase with more layers
- Bottleneck: vanishing gradient
- What if we can overcome this problem?
- Answer: Deep Neural Network