



Introduction to Computing Using Java

Primitive Data Type Boolean and Related Operators





Boolean/Truth/Logic Processing

- ★ 布林 (布爾) / 真值 / 邏輯運算
- ★ A proposition may be true, false or undetermined, e.g.
 - true/false questions in examinations
 - You are a boy
 - Peter is 21 years old
 - Principal of no less than HK\$30,000
 - It will rain tomorrow?



Boolean Values



```
int    moneyAtHand    = 3000;  
boolean noMoneyAtHand = false;
```



```
accountMichael.deposit(3000);  
moneyAtHand    = moneyAtHand - 3000;
```



```
noMoneyAtHand = true;  
noMoneyAtHand = moneyAtHand <= 0;
```

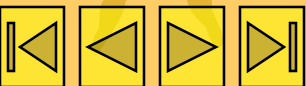
- ★ The only values a boolean type field can take is either true or false.



Expressions



- Up to now we have seen
 - *arithmetic expressions* that use the operators
`+` `-` `*` `/` `%` `++` `--`
 - *assignment expressions* that use the operators
`=` `+=` `-=` ...
 - **Boolean expressions** use *relational* and *logical* operators.
 - The **result** of a Boolean expression is either `true` or `false`.
 - Boolean expressions allow us to write programs that decide whether to execute some code or not.
 - These decisions changes the *flow* of the program execution.





Relational Operators

- **Relational operators** compare two **arithmetic expressions** and evaluate to a **boolean** result.

★ ==

LHS is equal to RHS

★ !=

LHS is not equal to RHS

★ >

LHS is greater than RHS

★ <

LHS is less than RHS

★ >=

LHS is greater than or equal to RHS

★ <=

LHS is less than or equal to RHS

★ =

Assignment/Storage Operation! LHS is a locker!

This is
NOT a
relational
operator!





Relational Operators

★ How do they look like?

- For numerics:

`3 > 7`

`-1 != 1`

`oldWeight + oldHeight >= 190.34 * newHeight`

`18 == Age`

- For characters:

`'Z' > 'A'`

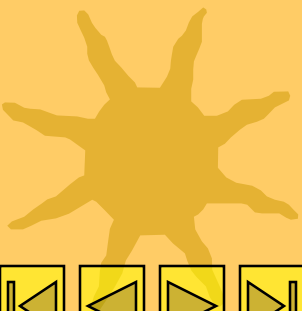
`'A' > '0' ??? true ???`

`'a' > 'A' ??? true ???`

★ Result must be **true** or **false**



Relational operators



- These relational operators have **lower precedence** than the arithmetic operators.
 - Thus, arithmetic expressions are evaluated first, then the resulting Boolean expressions.
 - That is, Java does the “math” first, then the comparison.





Relational operators

Examples:

```
int x = 15;
```

```
int y = 100;
```

```
System.out.println(x > y);
```

```
System.out.println(x < 15);
```

```
System.out.println(x <= 15);
```

```
System.out.println(x == y);
```

```
System.out.println(x != 5);
```

```
System.out.println(x * -y > 0);
```

```
boolean isBigger = x > y;
```

**Calculate
firstly**





Floating point comparison

- ★ True or false? (inexact bit storage)

- `0.7 * 0.7 == 0.49` ??? **false** ???

- ★ Why false?

- Numerical error

- ★ How to compare floating point?

- `Math.abs(f1-f2) < threshold` (e.g. `0.0000001`)

- Threshold: a very small value



Logical operators

- **Logical operators** combine `boolean` values and evaluate to a `boolean` result.

Operator	Name	Example	Result
<code>!</code>	Logical NOT	<code>!a</code>	<code>true</code> if <code>a</code> is false, <code>false</code> if <code>a</code> is true
<code>&&</code>	Logical AND	<code>a && b</code>	<code>true</code> if both <code>a</code> and <code>b</code> are true, <code>false</code> otherwise
<code> </code>	Logical OR	<code>a b</code>	<code>true</code> if <code>a</code> or <code>b</code> , or both are true, <code>false</code> otherwise



Boolean Expression



```
boolean iAmDry;
```

```
/*
```

```
 * sunnyDay and noSweat → iAmDry
```

```
*/
```

```
iAmDry = sunnyDay && noSweat;
```

```
--- 8< -----
```

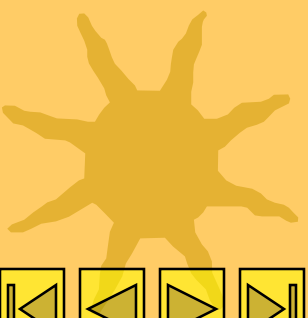
What if it's NOT sunny? [iAmDry=false]

What if I DO sweat? [iAmDry=false]





Boolean AND (&)

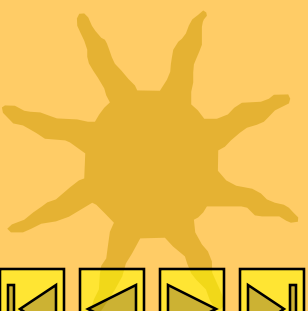


iAmDry	noSweat		
sunnyDay	and (&)	true	false
	true	true	false
	false	false	false





Boolean OR (/)

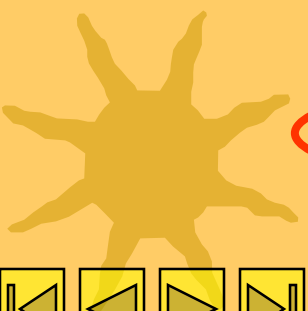


phoneRing	callComing		
	or ()	true	false
lowBattery	true	true	true
	false	true	false





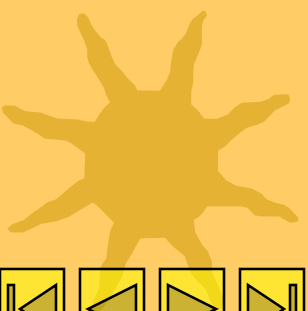
Short Circuit (AND)



iAmDry	noSweat		
	and (&&)	true	false
	true	true	false
	false	false	false
sunnyDay	false	false	false



Short Circuit (OR)



phoneRing	callComing		
	or ()	true	false
lowBattery	true	true	true
	false	true	false





Short Circuit Boolean Operators

(`&&` `||`)



```
iAmDry = sunnyDay && noSweat
```

- ★ If **sunnyDay** is false, Java will not check the truth value of **noSweat** as the result must be false.



```
phoneRing = lowBattery || callComing;
```

- ★ If **lowBattery** is true, Java will not check the truth value of **callComing** as the result must be true.



- ★ This is called *short circuit* boolean evaluation.





Other Boolean Operators

- ★ The *not* (!) operator gives you the negation (反話).

```
iAmCareless = !iAmCareful;
```

- ★ The *xor* (^) exclusive-or operator gives you false when the truth values of both operands are equal, true otherwise.

```
normalDay = workingDay ^ HOLIDAY;
```

```
true <- false ^ true
```

```
true <- true ^ false
```

```
false <- false ^ false
```

```
false <- true ^ true
```



Truth Tables

- **Truth tables** list all possible combination of values for the variables in an expression.

a	b	a && b	a b	!a
true	true	true	true	false
true	false	false	true	false
false	true	false	true	true
false	false	false	false	true



Logical operators

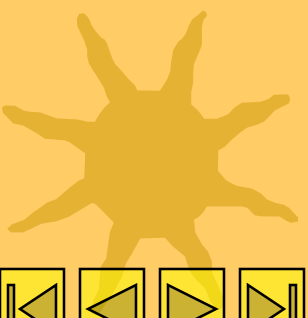


Example:

age > 26	hasLicense	(age > 26) && hasLicense



```
boolean canRentCar = (age > 26) && hasLicense;
```





Logical operators

Example:

<code>age > 26</code>	<code>hasLicense</code>	<code>(age > 26) && hasLicense</code>
true	true	true
true	false	false
false	true	false
false	false	false

```
int age = 16;  
boolean hasLicense = true;  
boolean canRentCar = (age > 26) && hasLicense;
```



Logical operators: Exercise 1

- It is time to buy a Iphone X when at least one of the following situations occurs:
 - the phone breaks
 - the phone is at least 3 years old

```
int phoneAge;           // in years
boolean isBroken;
...                      // code initializes variables

boolean needPhone = _____;
```



Logical operators: Exercise 1

- It is time to buy a new phone when at least one of the following situations occurs:
 - the phone breaks
 - the phone is at least 3 years old

```
int phoneAge;           // in years
boolean isBroken;
...                     // code initializes variables

boolean needPhone = (isBroken == true)
                    || (phoneAge >= 3);
```





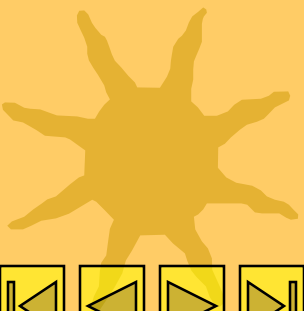
Logical Operators: Exercise 2

- Assume `x`, `y`, and `z` are `int` variables that have been initialized.

```
boolean areAllEqual = _____;
```



Logical Operators: Exercise 2



- Assume `x`, `y`, and `z` are `int` variables that have been initialized.

```
boolean areAllEqual = (x == y) && (y == z);
```




Logical operators

Examples:

```
int x = 15;
```

```
int y = 100;
```

```
System.out.println(x > y && x >= 15);
```

```
System.out.println(x < 15 || x > 15);
```

```
System.out.println(x == y && y == 100);
```

```
System.out.println(x != 5 && x < y);
```

```
System.out.println(x + y > 100 || y <= 10);
```

&& is evaluated after relational operators.

|| is evaluated after &&.



Complex Boolean Expression

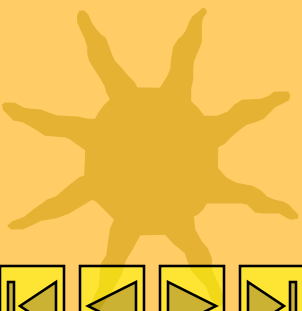


```
iAmDry          = sunnyDay && noSweat;  
phoneSilent     = lowBattery && callForwarded;  
badMood        = !(iAmDry && phoneSilent);  
/* by De Morgan's Law:  $\& \leftrightarrow |$  */  
badMood        = !iAmDry || !phoneSilent;  
/* in expanded form: */  
badMood = ! (sunnyDay && noSweat) |  
          ! (lowBattery && callForwarded);
```





Boolean Algebra



- Double negative: $!!a \equiv a$

- de Morgan's Law:

$$!(a \ \&\& \ b) \equiv !a \ || \ !b$$

$$!(a \ || \ b) \equiv !a \ \&\& \ !b$$



de Morgan's Law (version 1)



Truth table: Consider all possible combinations of values of boolean **a** and **b**.

$$\neg(a \ \&\& \ b) == (\neg a \ || \ \neg b)$$



a	b	a && b	!(a && b)	!a	!b	!a !b
T	T					
T	F					
F	T					
F	F					





de Morgan's Law (version 1)

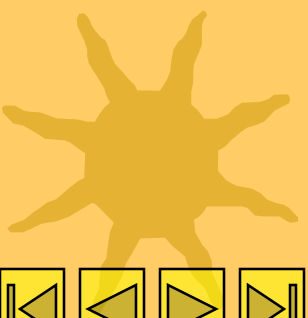


Truth table: Consider all possible combinations of values of boolean `a` and `b`.

$$\text{!(a \&\& b) == (!a || !b)}$$

equal

a	b	a && b	!(a && b)	!a	!b	!a !b
T	T	T	F	F	F	F
T	F	F	T	F	T	T
F	T	F	T	T	F	T
F	F	F	T	T	T	T





de Morgan's Law (version 2)

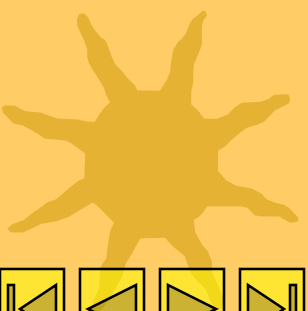
Truth table: Consider all possible combinations of values of boolean **a** and **b**.

$$\neg(a \vee b) == (\neg a \wedge \neg b)$$

a	b	$a \vee b$	$\neg(a \vee b)$	$\neg a$	$\neg b$	$\neg a \wedge \neg b$
T	T					
T	F					
F	T					
F	F					



de Morgan's Law (version 2)



Truth table: Consider all possible combinations of values of boolean `a` and `b`.

$$!(a \ || \ b) == (!a \ \&\& \ !b)$$

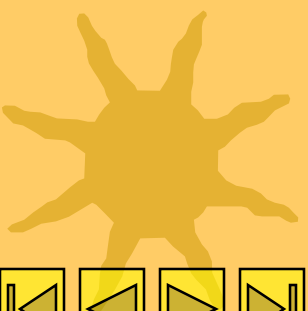
equal

a	b	a b	!(a b)	!a	!b	!a && !b
T	T	T	F	F	F	F
T	F	T	F	F	T	F
F	T	T	F	T	F	F
F	F	F	T	T	T	T





de Morgan's Law



In Java:

```
! ((age < 12) || (age >= 65))
```

In English: *It is not the case that age less than 12 or age greater than or equal to 65. !!!?*

Simplify using de Morgan's Law:

```
!(age < 12) && !(age >= 65)
```

The reverse the meaning of the relational expressions:

```
(age >= 12) && (age < 65)
```

That is, *when age is at least 12 and less than 65.*





de Morgan's Law



In English:

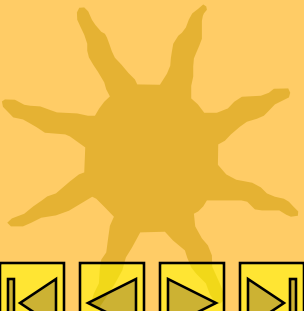
Words neither rhyme nor alliterate.



In Java:

`!wordsRhyme && !wordsAlliterate`

Words don't rhyme and they don't alliterate



Apply de Morgan's Law:

`!(wordsRhyme || wordsAlliterate)`

It's not the case words rhyme or alliterate.





Precedence



★ () [highest]

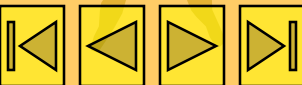
★ !

★ &

★ |

★ & &

★ | | [lowest]





More About Expression

- ★ Assignment is also an expression!

```
USdollar = (HKdollar = 123.45) * rate;  
[double = double * double]
```

- ★ Left to right evaluation

$$1 - 2 - 3 = (1 - 2) - 3 \neq 1 - (2 - 3)$$

- ★ Short forms for number types

```
Age = Age + 1;  $\equiv$  Age++;
```

```
Age = Age - 1;  $\equiv$  Age--;
```

- ★ Short forms for number types

```
Age = Age + 15;  $\equiv$  Age += 15;
```

```
USdollar = USdollar - 1.7;  $\equiv$  USdollar -= 1.7;
```





Mixing Numeric and Boolean Expressions



```
int temperature = 38;
```

```
boolean goHome = (temperature > 40) | (temperature < 0);  
System.out.println("goHome? " + goHome);
```



```
int diceOne = 5, diceTwo = 6, diceThree = 6;
```

```
boolean triple = (diceOne == diceTwo) &  
                 (diceTwo == diceThree);
```

```
boolean small  = (diceOne + diceTwo + diceThree <= 10) &  
                 ! triple;
```

```
boolean big    = (diceOne + diceTwo + diceThree >= 11) &  
                 ! triple;
```





Prime Number Checker

Get an **integer** input from user through **console** (remember how to use **Scanner**?), then check that whether this input number is a **prime number** or not?

```
boolean isPrime = true;
```

```
Scanner scan = new Scanner(System.in);
```

```
int num = scan.nextInt();
```

```
int temp = 0;
```





Prime Number Checker

```
for(int i = 2; i <= Math.floor(Math.sqrt(num)); i++)  
{  
    temp = num % i;  
    if(temp == 0)  
    {  
        isPrime = false;  
        break;  
    }  
}
```



Exercise: MPF Contribution

- ★ http://www.mpfa.org.hk/eng/mpf_system/system_features/contributions/index.jsp
- ★ Write a Java program to calculate the monthly mandatory contribution of an **employee**, given input the relevant monthly salary.



Introduction—MPF

★ Mandatory Provident Fund (強積金制度)

Relevant month salary	Monthly mandatory contribution (employee)
Less than \$7,100	No contributions required
Between \$7,100 to \$30,000	Relevant salary*5%
More than \$30,000	\$1,500