Notes from bibliography

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Contents

1 Fundamental of Higher Order Neural Networks for Modeling and Simulation (Gupta and Bukovsky 2012)

1.1 Introduction

Biological neuron

1. Synaptic operation - strength (weight) is represented by previous knowledge.

2. Somatic operation

- aggregation (summing), thresholding, nonlinear activation and dynamic processing
- output after certain threshold

if neuron was only linear the complex cognition would disappear

First neuron modeled (1943)

$$u = \sum_{i=1}^{n} w_i x_i$$

1.1.1 Higher Order Terms of Neural Inputs

year 1986, 1987, 1991, 1992, 1993

$$u = \sum_{j=i}^{n} \sum_{i=1}^{n} w_{ij} x_i x_j$$

1.1.2 Activation functions

1.1.2.1 Sigmoid

$$\phi(x) = \frac{1}{1 + e^{-x}}$$

1.2 SONU/QNU

- parameter reduction using upper triangular matrix of weights

$$u = \mathbf{x}_a^T \mathbf{W}_a \mathbf{x}_a = \sum_{j=i}^{n} \sum_{i=1}^{n} w_{ij} x_i x_j$$

$$y = \phi(u)$$

if a weight is high it shows correlation between components of input patterns

Learning algorithm for second order neural units

The purpose of the neural units is to minimize the error E by adapting the weight

$$E(k) = \frac{1}{2} e(k)^2 \quad ; \quad e(k) = y(k) - y_d(k)$$

$$\mathbf{W}_a(k+1) = \mathbf{W}_a(k) + \Delta \mathbf{W}_a(k)$$

$$\Delta \mathbf{W}_a(k) = -\eta \frac{\delta E(k)}{\delta \mathbf{W}_a(k)}$$

where η is learning coefficient chain rule …

using chain rule we get changes in the weight matrix as

$$\Delta \mathbf{W}_a(k) = -\eta e(k)\phi'(u(k))\mathbf{x}_a(k)\mathbf{x}_a^T(k)$$

Table with mathemathical structure and learning rule

SONU	Math. Struct	Learning rule
Static	$y_n = \mathbf{x_a^T W x}$	Levenberg_marquard (L-M)
		Gradient descent
Dynamic	$y_n(k+n_s) = \mathbf{x_a^T W x}$	Recurrent Gradient Descent
		Backpropagation throughtime

1.2.1 Performance Assesment of SONU

1.2.1.1 XOR problem

- XOR 6params vs 9 of 3 linear units

1.3 Time Series Prediction

1.4 High order neural network units

- HONU is just a basic building block

1.4.1 Example of Cubic neural network with two inputs

1.5 Modified PNN

1.5.1 Sigma-Pi NN

1.5.2 Ridge PNN

1.6 Conclusion

- this neural network first aggregates inputs and then multiplicate

2 Nonconventional Neural Architectures and their Advantages for Technical Applications (Bukovský 2012)

2.1 Introduction

- first mathematical model of neuron 1943
- principals for modeling of dynamic systems
  - customable non-linearity
  - order of dynamics of state space representation of a neuron
  - adaptable time delays

2.1.1 HONU, HONN

- PNN - polynomial neural networks
- LNU, QNU, CNU
- linear optimization, avoidance of local minima

bio-inspired neuron, *perceptron*, *recurrent* (dynamic, hopfield)

static vs dynamic
continuous vs discrete implementation of static/dynamic HONN

2.1.2 Gradient optimization methods

- back propagation
- gradient descent rule
- Levenberg-Marquardt algorithm

2.2 RHONN

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RTRL – real time recurrent learning

- dynamic version of gradient descent

BPTT – back propagation throught time

- batch training technique can be implemented as combination of RTRL and L-M algorithm => RHONU

2.3 Weight update stability of static and dynamic version

3 Artificial High Order NN for Economics and Bussiness (Zhang 2008)

3.1 Chapter 1

- use case of HONN
- model 1, 1b, 0
  - model 1 is containing one hidden layer with linear units
  - model 1b is containing two

Polynomial HONN uses poly-func as activation function

Neural Adaptive HONN uses adaptive functions as neuron

3.1.1 Learning algorithm of HONN

3.1.2 PHONN

3.1.3 Trigonometric HONN

- uses trigonometric functions as activation functions

3.1.4 Ultra high frequency cosine and sine HONN

3.1.5 SINC and Sine Polynomial HONN

3.2 Chapter 3

- HONN first introduced in (Giles, Maxwell 1987)
- hyperbolic tangent function

$$S(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$

3.3 Chapter 5

- info about “High order Flexibel Neural Tree”

Chapter 6 - most basic motivation of stock forecasting is financial gain - motivation behind recurrent is that patterns may repeat in time

3.3.1 Background HONN

3.3.2 HONN structure

3.4 Chapter 7

Problems of ANNs - long convergence time - can be stuck in local minima - unable to handle high-frequency, non-linear and discontinuous data - black box

HONN can be considered as “open box”

3.5 Chapter 8

4 Adaptive control with RHONN (Rovithakis and Christodoulou 2000)

4.1 Introduction

- for training model uses current and previous inputs, as well as the previous outputs
- in discrete outputs we need to discretized the model
- model is trained to identify the inverse dynamics of the plant instead of the forward dynamics
- by connecting the past neural output as input we make dynamic network that is highly nonlinear

Problem with dynamic neural networks that are based on static multilayer networks is that criterial functions possesses many local minima.

4.1.1 Book goals

Chapter 2 introduces RHONN
Chapter 3 online identification

4.2 Identification using RHONN

4.2.1 Model description

$$\dot{x}_i = -a_i x_i + b_i \left[\sum_{k=1}^{L} w_{ik} z_k \right]$$

4.2.2 Learning algorithms

5 Discrete-time HONN (Sanchez, Alanís, and Loukianov 2008)

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