

- Ejercicios Tema 1:

$$1. \left\{ \begin{array}{l} \text{Gasto eléctrico: } 56800 \text{ €} \\ \text{Gasto medio: } 55300 \text{ €} \\ \text{Desv. típica: } 2100 \text{ €} \end{array} \right\} \Rightarrow X: \text{Gasto de cada una} \\ [N \sim (55300, 2100^2)]$$

$$a) P[X < 56800] = P\left[Z < \frac{56800 - 55300}{2100}\right]$$

$P[Z < 0.7142] \Rightarrow$ Si buscamos en la tabla $N(0,1)$ tenemos $0.71 \Rightarrow \boxed{0.7611}$



$$P_{86} \Rightarrow Z_{0.86} \Rightarrow 1.08\%$$

$$X = \mu + Z\sigma;$$

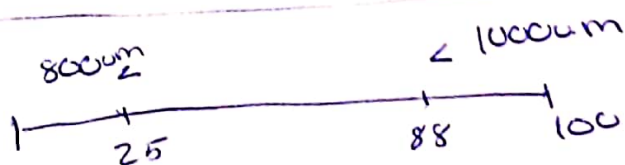
$$P_{86} = 55300 + 1.08 \cdot 2100 = 57568 \text{ €};$$

* No pertenece

$$c) P_{25} = Z_{0.25} = -0.67$$

$$P_{25} = 55300 - 0.67 \cdot 2100 = 53843 \text{ €}$$

$$56800 - 53843 = \underline{2957 \text{ €}} \text{ tendría que reducir}$$



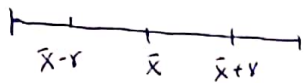
$$\left. \begin{array}{l} 800 = \mu - 0.67\sigma; \\ 1000 = \mu + 1.175\sigma; \end{array} \right\} \begin{array}{l} -800 = -\mu + 0.67\sigma \\ 1000 = \mu + 1.175\sigma \end{array}$$

$$2000 = 1.845\sigma; \quad \sigma = \boxed{1081.4010}$$

$$\mu = 800 + 0.67 \cdot 1081.4010 \Rightarrow \boxed{872.62}$$

3. a) Desigualdad [Chebyshev]

$$P(\bar{x} - r < x < \bar{x} + r) \geq \frac{1 - \text{var}(x)}{r^2}$$



$$\left\{ \begin{array}{l} \text{var} = 64 \text{ €}^2 \\ r = 20; \end{array} \right\}$$

$$1 - \frac{64}{20^2} \Rightarrow \frac{1}{0.84}$$

$P \Rightarrow 0.16 \Rightarrow \text{Probabilidad}$

$P \Rightarrow 0.84 \Rightarrow \text{Probabilidad}$

b) $S^2 = 64$; $S = 8$; Media $\Rightarrow 200 \text{ €}$

$$180 = 200 + 8\alpha_1 \Rightarrow \alpha_1 = -2.5$$

$$220 = 200 + 8\alpha_2 \Rightarrow \alpha_2 = 2.5$$

$$-2.5 \leq p \leq 2.5$$

• Resamos a distribución Normal:

$$Z_{-2.5} = 0.0062$$

$$Z_{2.5} = 0.9938$$

$$0.0062 < p < 0.9938$$

Cota;

$$0.9938 - 0.0062 \Rightarrow 0.9876$$

\Rightarrow Probabilidad;

$$4. B\left(\overset{n}{1200}, \overset{p}{0.05}\right) \left\{ \begin{array}{l} \mu = n \cdot p \Rightarrow 1200 \cdot 0.05 \Rightarrow 60 \\ \sigma^2 = 60 \cdot (1 - 0.05) = 57; \sigma = \sqrt{57} = 7.5498 \end{array} \right\}$$

$$X \sim N(60, 7.5498);$$

* Convertimos

$$P[X > 45] = 1 - P[X \leq 45] = 1 - (-1.9868) \Rightarrow 1 - 0.0233 = 0.9767$$

$$B(100, 0.05) \Rightarrow \left\{ \begin{array}{l} \mu = n \cdot p = 100 \cdot 0.05 = 5 \\ \sigma^2 = 5 \cdot (1 - 0.05) = 4.75 \Rightarrow \sigma = \sqrt{4.75} = 2.1794 \end{array} \right\}$$

$$X \sim N(5, 2.1794)$$

$$P[X < 0] \Rightarrow \frac{0 - 5}{2.1794} = -2.29 \Rightarrow 0.011$$

\hookrightarrow * Probabilidad de que acepte.