

PROBLEM No. 1

a. 0.5p

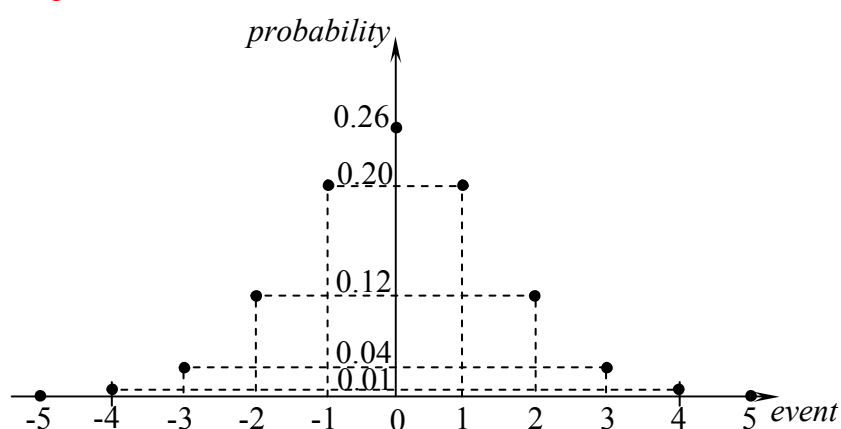
$$[f]_{\text{SI}} = \text{m}^{-1}\text{s}$$

b. 0.5p

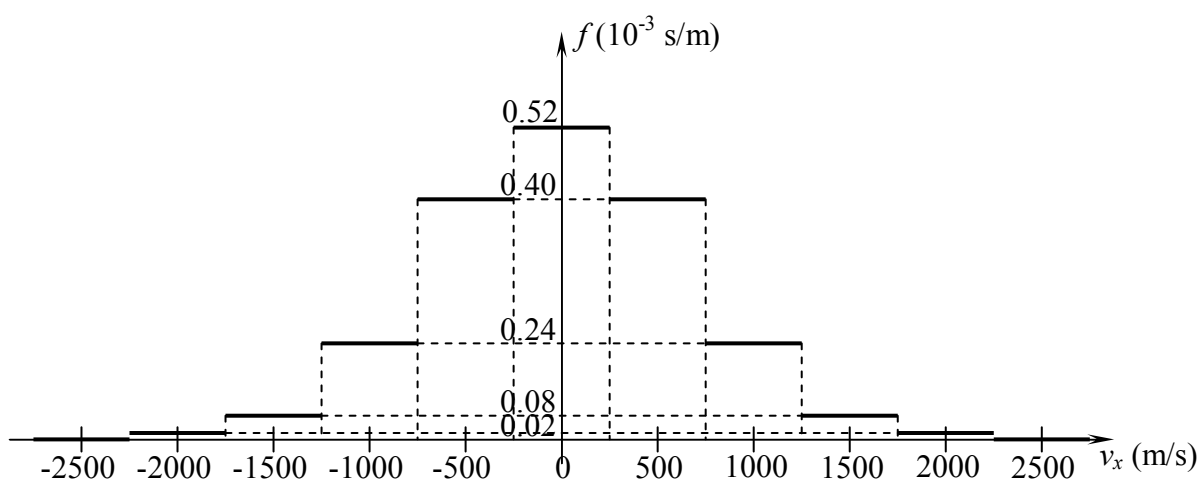
$$e^{-\frac{\mu v_{x\text{max}}^2}{2RT}} = 0.01 \Rightarrow -\frac{\mu v_{x\text{max}}^2}{2RT} = \ln \frac{1}{100} \Rightarrow v_{x\text{max}} = \sqrt{\frac{4RT \ln 10}{\mu}} = \sqrt{\frac{4 \cdot 8.31 \frac{\text{J}}{\text{molK}} \cdot 300\text{K} \cdot 2.5}{4 \cdot 10^{-3} \frac{\text{kg}}{\text{mol}}}}$$

$$v_{x\text{max}} = 2500 \text{ m/s}$$

c. 2p



d. 2p



e. 0.5p

$$\eta = 0.13$$

f. 0.5p

$$\eta = 0.0022$$

g. 0.5p

$$\left(v^2 e^{-\frac{\mu v^2}{2RT}} \right)' = 0 \Rightarrow 2v e^{-\frac{\mu v^2}{2RT}} = v^2 \frac{2\mu v}{2RT} e^{-\frac{\mu v^2}{2RT}} \Rightarrow v^2 = \frac{2RT}{\mu}$$

$$v_p = \sqrt{\frac{2RT}{\mu}} = \sqrt{\frac{2 \cdot 8.31 \frac{\text{J}}{\text{molK}} \cdot 300\text{K}}{4 \cdot 10^{-3} \frac{\text{kg}}{\text{mol}}}} \approx 1125 \frac{\text{m}}{\text{s}}$$

$$v \in [1000 ; 1250] \frac{\text{m}}{\text{s}}$$

h. 0.5p

$$P(0,0,0) = 0.0022$$

i. 2p

| <i>magnitude of the velocity component (m/s)</i> | <i>magnitude of the velocity component (m/s)</i> | <i>magnitude of the velocity component (m/s)</i> | <i>number of occurrences</i> | <i>P</i> |
|--|--|--|------------------------------|----------|
| 0 | 0 | 1000 | 6 | 0.00100 |
| 0 | 0 | 1250 | 6 | 0.00068 |
| 0 | 250 | 1000 | 24 | 0.00090 |
| 0 | 500 | 1000 | 24 | 0.00078 |
| 0 | 750 | 750 | 12 | 0.00083 |
| 0 | 750 | 1000 | 24 | 0.00062 |
| 250 | 250 | 1000 | 24 | 0.00079 |
| 250 | 500 | 1000 | 48 | 0.00069 |
| 250 | 750 | 750 | 24 | 0.00074 |
| 500 | 500 | 750 | 24 | 0.00080 |
| 500 | 500 | 1000 | 24 | 0.00060 |

j. 1p

$$\eta = 0.17868$$