Duy Huynh
TCSS 342 – Spring '15
Assignment 1 – Burger Baron
Worst Case Run-Time Analysis of changePatties

1 Introduction

This is a worst case run-time analysis of the changePatties() method in my Burger Baron assignment. For convenience, the relevant code is provided below with numbered lines:

```
1  public void changePatties(final String pattyType) {
2
3      // Don't change patties if it's already of that type!
4      if (!this.pattyType.equals(pattyType)) {
5            final MyStack<Ingredient> tempStack = new MyStack<>();
6
7            // Change the patty that is underneath the cheeses
8
9            // 1. pop off and store the cheeses:
10           for (int i = 0;i < cheeseCount;i++) {
11                 tempStack.push(botStack.pop());
12           }
13
14           // 2. Dispose the old patty
15           botStack.pop();
16
17           // 3. Push new patty:
19           botStack.push(Ingredient.getIngredient(pattyType));
20
21           // 4. Put back the cheeses
22           for (int i = 0;i < cheeseCount;i++) {
23                 botStack.push(tempStack.pop());
24           }
25
26           // Work on the patties of the other stack
27
28           // 5. Pop off old patties, if any, from top stack
29           for (int i = 0;i < pattyCount - 1;i++) {
30                 topStack.pop();
31           }
32
33           // 6. Push new patties, if any, onto top stack
34           for (int i = 0;i < pattyCount - 1;i++) {
35                 topStack.push(Ingredient.getIngredient(pattyType));
36           }
37
38           // 7. Change patty type
39           this.pattyType = pattyType;
40     }
41 }

42 /**Create a Stack. */
43 public MyStack() {
44     top = null;
45     myPointer = 0;
46 }
```

Duy Huynh
TCSS 342 – Spring '15
Assignment 1 – Burger Baron
Worst Case Run-Time Analysis of changePatties

```
47 public void push(final T element) {
48
49    if (top == null) {
50          top = new Node(element, null);
51    } else {
52          top = new Node(element, top);
53    }
54    myPointer++;
55
56 }
```

```
57 public T pop() {
58
59    T temp;
60    if (top == null) {
61          throw new NullPointerException("Nothing to pop off stack!");
62    } else {
63          temp = (T) top.getElement();
64          top = top.myNextNode;
65          myPointer--;
66    }
67     return temp;
68
69 }
```

```
70 public static Ingredient getIngredient(String ingredientName) {
71    for (Ingredient i : values()) {
72          if (i.getName().equalsIgnoreCase(ingredientName)) {
73                return i;
74          }
75    }
76    throw new IllegalArgumentException("Ingredient \"" + ingredientName
77          + "\" not found!");
78 }
```

```
148 private T getElement() {
149   return myElement_
150 }
```

```
151 private Node(final T theElement, final Node theNextNode) {
152   this.myElement = theElement_
153   this.myNextNode = theNextNode_
154 }
```

```
155 public String getName() {
156   return name;
157 }
```

Duy Huynh
TCSS 342 – Spring '15
Assignment 1 – Burger Baron
Worst Case Run-Time Analysis of changePatties

2 Analysis

2.1 Line-by-line breakdown:

Let CHEESE_MAX = 3, PATTY_MAX = 2, INGREDIENTS = 17 (total values contained in Ingredients enum). Let declarations, assignments, negations, checks, integer and Boolean arithmetic, and similar operations cost 1.

changePatties:

Line 4: check + negation + C_{equals} = $2 + C_{equals}$ = C_4

Line 5: declaration + assignment + $C_{MyStack}$ = 2 + $C_{MyStack}$ = 2 + 13 = 15

Line 10 & 11: declaration + $\sum_{n=1}^{CHEESE_{MAX}}(\text{check} + \text{increment} + C_{push} + C_{pop}) = 1 + CHEESE\_MAX * (2 + C_{push} + C_{pop})$

Line 15: C_{pop}

Line 19: C_{push} + $C_{getIngredient}$

Line 22 & 23: declaration + $\sum_{n=1}^{CHEESE_{MAX}}(\text{check} + \text{increment} + C_{push} + C_{pop}) = 1 + CHEESE\_MAX * (2 + C_{push} + C_{pop})$

Line 29 & 30: declaration + $\sum_{n=1}^{PATTY\_MAX-1}(\text{check} + \text{subtraction} + \text{increment} + C_{pop}) = 1 + (PATTY_{MAX} - 1) * (3 + C_{pop})$

Line 34 & 35: declaration + $\sum_{n=1}^{PATTY\_MAX-1}(C_{push} + \text{check} + \text{subtraction} + \text{increment} + C_{getIngredient}) = 1 + (PATTY\_MAX - 1) * (3 + C_{push} + C_{getIngredient})$

Line 39: assignment = 1

Total: $C_4 + 15 + 1 + 2 * CHEESE\_MAX * (2 + C_{push} + C_{pop}) + 1 + (PATTY\_MAX - 1) * (3 + C_{pop}) + 1 + PATTY\_MAX * (3 + C_{push} + C_{getIngredient})$

MyStack():

Line 44: assignment = 1

Line 45: assignment = 1

Total: 1 + 1 = 2 = $C_{MyStack}$

push():

Line 49: check + check = 2

Line 50: assignment + C_{Node} = 1 + C_{Node} (Node has 2 assignments, so it costs 2). = 3

Line 51: assignment + C_{Node} = 1 + C_{Node} = 3

Line 54: increment = 1

Total: $7 + 2 * C_{Node} = 7 + 2 * 3 = 13 = C_{push}$

pop():

Line 59: declaration = 1

Line 60: check + check = 2

Line 63: assignment + C_{cast} + $C_{getElement}$ = 1 + C_{cast} + $C_{getElement}$ (getElement() has one return statement = 1)

Line 67: return statement = 1

Total: 4 + C_{cast} + $C_{getElement}$ = 5 + C_{cast} = C_{pop}

getIngredient():

Line 71: declaration + C_{values} = 1 + C_{values}

Line 72 & 73: $\sum_{n=1}^{INGREDIENTS}(\text{check} + C_{getName} + C_{equalsIgnoreCase}) = INGREDIENTS * (1 + C_{getName} + C_{equalsIgnoreCase})$

Total: 1 + C_{values} + $C_{getName}$ + $C_{equalsIgnoreCase}$ = $C_{getIngredient}$

Duy Huynh
TCSS 342 – Spring '15
Assignment 1 – Burger Baron
Worst Case Run-Time Analysis of changePatties

2.2 For-loop breakdowns:

In changePatties(), there are 4 for-loops.

2.2.1: The for-loop on line 10 is responsible for taking off the cheeses that are present in the current Burger. This loop has a worst case run-time scenario when cheeseCount is at the maximum, which is 3 pieces of cheese:

$$\sum_{n=1}^{CHEESE_{MAX}} (\text{check} + \text{increment} + \text{C}_{push} + \text{C}_{pop}) = CHEESE\_MAX * (2 + C_{push} + C_{pop})$$

2.2.2: The for-loop on line 22 is responsible for putting back on the cheeses after the new patty has been put on. This loop, similar to the previous, has worst case run-time scenario when cheeseCount is at the maximum, which is 3:

$$\sum_{n=1}^{CHEESE_{MAX}} (\text{check} + \text{increment} + \text{C}_{push} + \text{C}_{pop}) = CHEESE\_MAX * (2 + C_{push} + C_{pop})$$

2.2.3: The for-loop on line 29 is responsible for removing any old existing patties that sit on top of the cheeses. This loop has a worst case run-time scenario when the patty count that sit on top of the cheeses is maxed out at 2 patties:

$$\sum_{n=1}^{PATTY\_MAX-1} (\text{check} + \text{subtraction} + \text{increment} + \text{C}_{pop}) = (PATTY\_MAX - 1) * (3 + \text{C}_{pop})$$

2.2.4: The for-loop on line 34 is responsible for pushing new patties onto the stack to match the new patty type. This loop has a worst case run-time scenario when there is a change of 2 patties max that sit on top of the cheeses. It is also interesting to note that the getIngredient() method called in this loop is also a for-loop that searches through all the values of my Ingredient enumeration which has 17 values:

$$\sum_{n=1}^{INGREDIENTS} (\text{check} + C_{getName} + \text{C}_{equalsIgnoreCase}) = INGREDIENTS * (1 + C_{getName} + \text{C}_{equalsIgnoreCase})$$

2.3 Total method cost:

The total summation of the line-by-line cost *c(n)* for changePatties() is:

$$c(n) = C_4 + 15 + 1 + 2 * CHEESE\_MAX * (2 + C_{push} + C_{pop}) + 1 + (PATTY\_MAX - 1) * (3 + \text{C}_{pop}) + 1 + PATTY\_MAX * (3 + \text{C}_{push} + \text{C}_{getIngredient})$$

$$c(n) = C_4 + 18 + 2 * CHEESE\_MAX * (2 + C_{push} + C_{pop}) + (PATTY\_MAX - 1) * (6 + \text{C}_{pop} + \text{C}_{push} + \text{C}_{getIngredient})$$

$$c(n) = C_4 + 18 + 2 * 3 * (2 + C_{push} + C_{pop}) + 2 * (6 + \text{C}_{pop} + \text{C}_{push} + \text{C}_{getIngredient})$$

$$c(n) = C_4 + 18 + 6 * (2 + C_{push} + C_{pop}) + 2 * (6 + \text{C}_{pop} + \text{C}_{push} + \text{C}_{getIngredient})$$

$$c(n) = C_4 + 18 + 12 + 6 * C_{push} + 6 * C_{pop} + 12 + 2 * \text{C}_{pop} + 2 * \text{C}_{push} + 2 * \text{C}_{getIngredient}$$

$$c(n) = C_4 + 42 + 8 * C_{push} + 8 * C_{pop} + 2 * \text{C}_{getIngredient}$$

$$c(n) = C_4 + 8 * (C_{push} + C_{pop}) + 2 * \text{C}_{getIngredient} + 42 = C_{totalSum}$$

Conclusion: $c(n) \in O(n)$