Mini-math Div 3/4: Friday, February 8, 2023 (9.6-9.9) - (24 minutes) Calculator active

1. (4 points) The velocity vector of a particle moving in the plane is given by

$$\langle 5 - 2\cos(t^2), 8\sin(t^2)\cos(e^t) \rangle$$
, for $0 \le t \le 2$

At time t = 0, the particle is at position (3, -1). Write an equation for the line tangent to the path of the particle at t = 1.

2. (4 points) Where does the graph $r = 1 - \sin \theta$, $0 \le \theta \le 2\pi$, have a vertical tangent?

3. (4 points) Find the area of the inner loop of $r=4\sqrt{3}-8\cos\theta$

4. (4 points) Find the area of the region common to $r = 1 - \sin \theta$ and $r = 2 \sin \theta$.