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## Mini-math Div 3/4: Friday, April 7, 2023 (25 minutes)

1. (3 points) The series  $\sum_{n=1}^{\infty} \frac{(-1)^n}{n}$  converges to S. If  $S_n$  is used to approximate S, what is the least value of n for which the alternating series error bound guarantees an error to strictly within 0.01?

2. (3 points) Let P(x) be the fifth-degree Taylor Polynomial for a function f about x = 1. Information about the maximum of the absolute value of selected derivatives of f over various intervals is given below.

$$\max_{0 \le x \le 1.5} |f^{(4)}(x)| = 4.6, \quad \max_{0 \le x \le 1.5} |f^{(5)}(x)| = 7.2, \quad \max_{0 \le x \le 1.5} |f^{(6)}(x)| = 6.8,$$

$$\max_{1 \le x \le 1.5} |f^{(4)}(x)| = 3.2, \quad \max_{1 \le x \le 1.5} |f^{(5)}(x)| = 4.7, \quad \max_{1 \le x \le 1.5} |f^{(6)}(x)| = 5.1$$

Find the smallest value of k for which the Lagrange error bound guarantees that

$$|f(1.5) - P(1.5)| \le k$$

3. (4 points) Find the interval of convergence for the series  $\sum_{n=1}^{\infty} \frac{(-1)^n (x-3)^n}{n2^n}$ 

4. (3 points) What is the Maclaurin series for  $\frac{\cos x - 1}{x}$ ? (You may, but are not required to, express your answer in summation notation.)

5. (4 points) Let f be a function with f(0) = 2 and  $f'(x) = \arctan x$ . Write the first three non-zero terms of the Maclaurin series for f.