Mini-math Div 3/4: Monday, November 30, 2020 (12 minutes)

Find the optimizing function (in terms of a single variable) for the following optimization problems. You do not need to simplify the function, nor do you need to solve the optimization question.

1. (2 points) Find the largest value of (x+2)(y-3) if 2x+3y=4

2. (2 points) What is the shortest distance between the point (3,1) and the curve $y = x^2 + 2$

3. $(2 \text{ points}) 2500 \text{ cm}^2$ of material is available to make a cylindrical can with an open top. Find the largest possible volume of the can.

4. (2 points) A cable television company is laying cable in an area with underground utilities. Two subdivisions are located on opposite sides of Terren Creek, which is 88 m wide. The company has to connect points P and Q with cable, where P is on the south bank while Q is 120 m downstream from P, on the opposite shore. It costs \$35/m to lay the cable underground and \$65/m to lay the cable underwater. At what point should the company lay the point to on the opposite shore in order to minimize the cost of the cable?