# Course at a Glance

#### Plan

The Course at a Glance provides a useful visual organization of the AP Calculus AB and AP Calculus BC curricular components, including:

- Sequence of units, along with approximate weighting and suggested pacing.
   Please note, pacing is based on 45-minute class periods, meeting five days each week for a full academic year.
- Progression of topics within each unit.
- Spiraling of the big ideas and mathematical practices across units.

#### Teach

#### MATHEMATICAL PRACTICES

Mathematical practices spiral throughout the course.

- Implementing
  Mathematical
  Processes
- Justification
   Communication
   and Notation
- 2 Connecting Representations

#### **BIG IDEAS**

Big ideas spiral across topics and units.

- CHA Change
- FUN Analysis of Functions

#### **BC ONLY**

The purple shading represents BC only content.

#### **Assess**

Assign the Personal Progress Checks—either as homework or in class—for each unit. Each Personal Progress Check contains formative multiple-choice and free-response questions. The feedback from the Personal Progress Checks shows students the areas where they need to focus.



### Limits and Continuity

AP EXAM WEIGHTING

10-12% AB 4-7% BC

CLASS PERIODS ~22-23 AB ~13-14 BC

| СНА | Introducing Calculus:           |
|-----|---------------------------------|
| 2   | Can Change Occur at an Instant? |
|     | <br>D C : T: '/ 1               |

- 1.2 Defining Limits and Using Limit Notation
- 1.3 Estimating Limit
  Values from Graphs
- 1.4 Estimating Limit
  Values from Tables
- 1.5 Determining Limits
  Using Algebraic
  Properties of Limits
- 1.6 Determining Limits
  Using Algebraic
  Manipulation
- 1.7 Selecting Procedures for Determining Limits
- 1.8 Determining Limits
  Using the Squeeze
  Theorem
- 1.9 Connecting Multiple
  Representations
  of Limits
- 1.10 Exploring Types of Discontinuities
- 1.11 Defining Continuity at a Point
- 1.12 Confirming Continuity over an Interval
- 1.13 Removing
  Discontinuities
- 1.14 Connecting Infinite
  Limits and Vertical
  Asymptotes
- 2 1.15 Connecting Limits at Infinity and Horizontal Asymptotes
- 1.16 Working with the
  Intermediate Value
  Theorem (IVT)

# UNIT 2

Differentiation: Definition and Basic Derivative Rules

AP EXAM WEIGHTING

10-12% AB 4-7% BC

CLASS PERIODS ~13-14 AB ~9-10 BC

| CHA<br>2        | 2.1  | Defining Average and<br>Instantaneous Rates of<br>Change at a Point                           |
|-----------------|------|---|
| CHA<br>1<br>4   | 2.2  | Defining the Derivative of a Function and Using Derivative Notation                           |
| CHA<br>1        | 2.3  | Estimating Derivatives of a Function at a Point   |
| FUN<br>3        | 2.4  | Connecting Differentiability and Continuity: Determining When Derivatives Do and Do Not Exist |
| FUN<br>1        | 2.5  | Applying the Power Rule   |
| FUN<br>1        | 2.6  | Derivative Rules:<br>Constant, Sum,<br>Difference, and<br>Constant Multiple                   |
| FUN<br>LIM<br>1 | 2.7  | Derivatives of $\cos x$ , $\sin x$ , $e^x$ , and $\ln x$                                      |
| FUN<br>1        | 2.8  | The Product Rule  |
| FUN<br>1        | 2.9  | The Quotient Rule   |
| FUN<br>1        | 2.10 | Finding the Derivatives<br>of Tangent, Cotangent,<br>Secant, and/or<br>Cosecant Functions     |

#### Personal Progress Check 1

Multiple-choice: ~45 questions Free-response: 3 questions (partial)

#### Personal Progress Check 2

Multiple-choice: ~30 questions Free-response: 3 questions (partial)

**NOTE:** Partial versions of the free-response questions are provided to prepare students for more complex, full questions that they will encounter on the AP Exam.



#### **Differentiation:** Composite, Implicit, and **Inverse Functions**

AP EXAM WEIGHTING

9-13% AB 4-7% BC

CLASS PERIODS

~10-11 AB ~8-9 BC

- FUN 3.1 The Chain Rule
- FUN 3.2 Implicit Differentiation
- FUN
- 3.3 Differentiating Inverse unctions
- FUN
- Differentiating nverse Trigonometric Functions
- FUN
- Selecting Procedures or Calculating **Derivatives**
- FUN
- 3.6 Calculating Higher-**Order Derivatives**



#### Contextual **Applications of** Differentiation

AP EXAM WEIGHTING

10-15% AB 6-9% BC

CLASS PERIODS

~10-11 AB ~6-7 BC

- CHA 4.1 Interpreting the Meaning of the Derivative in Context
- СНА Straight-Line Motion: Connecting Position, Velocity, and Acceleration
- CHA 4.3 Rates of Change in Applied Contexts Other Than Motion
- СНА 4.4 Introduction to Related Rates
- 4.5 Solving Related Rates **Problems**
- СНА **4.6** Approximating Values of a Function Using Local Linearity and Linearization
- LIM 4.7 Using L'Hospital's Rule for Determining Limits of Indeterminate Forms



#### **Analytical Applications of** Differentiation

AP EXAM WEIGHTING

15-18% AB 8-11% BC

CLASS PERIODS ~15-16 AB ~10-11 BC

- FUN 5.1 Using the Mean Value Theorem
- FUN 5.2 Extreme Value Theorem, Global Versus Loca Extrema, and Critical
- 5.3 Determining Intervals on Which a Function Is FUN Increasing or Decreasing
- 5.4 Using the First FUN Derivative Test to Determine Relative (Local) Extrema
- 5.5 Using the Candidates FUN Test to Determine Absolute (Global) Extrema
- **Determining Concavity** 5.6 FUN of Functions over Their Domains
- FUN 5.7 Using the Second **Derivative Test to Determine Extrema**
- FUN 5.8 Sketching Graphs of Functions and Their Derivatives
- FUN Connecting a Function, Its First Derivative, and
- 5.10 Introduction to Optimization Problems FUN
- **5.11 Solving Optimization** FUN Problems
- **5.12** Exploring Behaviors of FUN **Implicit Relations**

#### Personal Progress Check 3

Multiple-choice: ~15 questions Free-response: 3 questions (partial/full)

#### Personal Progress Check 4

Multiple-choice: ~15 questions Free-response: 3 questions

#### Personal Progress Check 5

Multiple-choice: ~35 questions Free-response: 3 questions

## UNIT 6

## Integration and Accumulation of Change

AP EXAM WEIGHTING 17-20% AB 17-20% BC CLASS PERIODS ~18-20 AB ~15-16 BC

|          |      | 10 20 AB 10 10 B0   |
|----------|------|---|
| CHA<br>4 | 6.1  | Exploring Accumulations of Change   |
| LIM<br>1 | 6.2  | Approximating Areas with Riemann Sums   |
| LIM<br>2 | 6.3  | Riemann Sums, Summation Notation, and Definite Integral Notation                    |
| FUN<br>1 | 6.4  | The Fundamental Theorem of Calculus and Accumulation Functions                      |
| FUN<br>2 | 6.5  | Interpreting the Behavior of Accumulation Functions Involving Area                  |
| FUN<br>3 | 6.6  | Applying Properties of Definite Integrals   |
| FUN<br>3 | 6.7  | The Fundamental Theorem of Calculus and Definite Integrals                          |
| FUN<br>4 | 6.8  | Finding Antiderivatives<br>and Indefinite<br>Integrals: Basic Rules<br>and Notation |
| FUN<br>1 | 6.9  | Integrating Using Substitution  |
| FUN<br>1 | 6.10 | Integrating Functions Using Long Division and Completing the Square                 |
| FUN<br>1 | 6.11 | Integrating Using<br>Integration by Parts<br>BC ONLY                                |
| FUN<br>1 | 6.12 | Using Linear Partial Fractions BC ONLY  |
| LIM<br>1 | 6.13 | Evaluating Improper<br>Integrals BC ONLY  |
| FUN<br>1 | 6.14 | Selecting Techniques for Antidifferentiation  |



### Differential Equations

AP EXAM WEIGHTING 6-12% AB 6-9% BC

CLASS PERIODS ~8-9 AB ~9-10 BC

| CLASSI   | LINIOD | 3 ~6-9 AB ~9-10 BC   |
|----------|--------|--|
| FUN<br>2 | 7.1    | Modeling Situations with Differential Equations  |
| FUN<br>3 | 7.2    | Verifying Solutions for<br>Differential Equations  |
| FUN<br>2 | 7.3    | Sketching Slope Fields   |
| FUN<br>4 | 7.4    | Reasoning Using Slope<br>Fields  |
| FUN 1    | 7.5    | Approximating Solutions Using Euler's Method BC ONLY                                       |
| FUN<br>1 | 7.6    | Finding General<br>Solutions Using<br>Separation of Variables                              |
| FUN<br>1 | 7.7    | Finding Particular<br>Solutions Using<br>Initial Conditions and<br>Separation of Variables |
| FUN<br>3 | 7.8    | Exponential Models with Differential Equations   |
| FUN<br>3 | 7.9    | Logistic Models with<br>Differential Equations<br>BC ONLY                                  |



## **Applications** of Integration

AP EXAM WEIGHTING 10-15% AB 6-9% BC CLASS PERIODS ~19-20 AB ~13-14 BC

|          |      | 10 20 AD 10 14 BC  |
|----------|------|--|
| CHA<br>1 | 8.1  | Finding the Average<br>Value of a Function on<br>an Interval                       |
| CHA<br>1 | 8.2  | Connecting Position, Velocity, and Acceleration of Functions Using Integrals       |
| CHA<br>3 | 8.3  | Using Accumulation<br>Functions and Definite<br>Integrals in Applied<br>Contexts   |
| CHA<br>4 | 8.4  | Finding the Area<br>Between Curves<br>Expressed as<br>Functions of <i>x</i>        |
| CHA<br>1 | 8.5  | Finding the Area<br>Between Curves<br>Expressed as<br>Functions of y               |
| CHA<br>2 | 8.6  | Finding the Area<br>Between Curves That<br>Intersect at More Than<br>Two Points    |
| CHA<br>3 | 8.7  | Volumes with Cross<br>Sections: Squares and<br>Rectangles                          |
| CHA<br>3 | 8.8  | Volumes with Cross<br>Sections: Triangles and<br>Semicircles                       |
| CHA<br>3 | 8.9  | Volume with Disc<br>Method: Revolving<br>Around the <i>x</i> - or <i>y</i> -Axis   |
| CHA<br>2 | 8.10 | Volume with Disc<br>Method: Revolving<br>Around Other Axes                         |
| CHA<br>4 | 8.11 | Volume with Washer<br>Method: Revolving<br>Around the <i>x</i> - or <i>y</i> -Axis |
| CHA<br>2 | 8.12 | Volume with Washer<br>Method: Revolving<br>Around Other Axes                       |
| СНА<br>3 | 8.13 | The Arc Length of a Smooth, Planar Curve and Distance Traveled BC ONLY             |

#### Personal Progress Check 6

#### Multiple-choice:

- ~25 questions (AB)
- ~35 questions (BC)

Free-response: 3 questions

#### Personal Progress Check 7

#### Multiple-choice:

- ~15 questions (AB)
- ~20 questions (BC)

Free-response: 3 questions

#### Personal Progress Check 8

Multiple-choice: ~30 questions Free-response: 3 questions



Parametric Equations, Polar Coordinates, and **Vector-Valued** Functions BC ONLY

AP EXAM WEIGHTING

N/A AB

11-12% BC

CLASS PERIODS N/A AB

~10-11 BC

- 9.1 Defining and **Differentiating Parametric Equations**
- CHA 9.2 Second Derivatives of Parametric **Equations**
- 9.3 Finding Arc Lengths of Curves Given by Parametric **Equations**
- CHA 9.4 Defining and **Differentiating Vector-Valued Functions**
- FUN 9.5 Integrating Vector-Valued Functions
- FUN 9.6 Solving Motion **Problems Using** Parametric and Vector-**Valued Functions**
- FUN 9.7 Defining Polar Coordinates and Differentiating in **Polar Form**
- CHA 9.8 Find the Area of a Polar Region or the Area Bounded by a Single **Polar Curve**
- CHA 9.9 Finding the Area of the Region Bounded by Two Polar Curves

#### **Infinite** UNIT Sequences and 10 Series BC ONLY

AP EXAM WEIGHTING

N/A AB

17-18% BC

CLASS PERIODS

N/A AB

~17-18 BC

- 10.1 Defining Convergent and Divergent Infinite Series
- LIM 10.2 Working with **Geometric Series**
- LIM 10.3 The *n*th Term Test for Divergence
- LIM 10.4 Integral Test for Convergence
- LIM 10.5 Harmonic Series and p-Series
- LIM 10.6 Comparison Tests for Convergence
- LIM 10.7 Alternating Series Test for Convergence 3
- LIM 10.8 Ratio Test for Convergence
- LIM 10.9 Determining Absolute or Conditional Convergence
- LIM 10.10 Alternating Series **Error Bound**
- 10.11 Finding Taylor Polynomial Approximations of Functions
- 10.12 Lagrange Error Bound
- 10.13 Radius and Interval of Convergence of **Power Series**
- LIM 10.14 Finding Taylor or **Maclaurin Series for** a Function
- 10.15 Representing Functions as **Power Series**

#### Personal Progress Check 9

Multiple-choice: ~25 questions Free-response: 3 questions

Personal Progress Check 10

Multiple-choice: ~45 questions Free-response: 3 questions