Mini-math Div 3/4: Monday, September 21, 2020

- (1) True or false: The value of $\lim_{x\to a} f(x)$ is f(a), assuming f(a) is defined.
- (2) True or false: $\lim_{x\to a} f(x)$ can only exist if the left and right limits exist are are equal.
- (3) What method would you use to solve

$$\lim_{h \to 0} \frac{(2+h)^2 - 4}{h}?$$

For an extra half point, what is the limit?

(4) What method would you use to solve

$$\lim_{x\to 9} \frac{\sqrt{x}-3}{x-9}?$$

For an extra half point, what is the limit?

(5) What method would you use to solve

$$\lim_{x \to 2} \frac{x^2 + x + 1}{3x^2 + 1}?$$

For an extra half point, what is the limit?

(6) What method would you use to solve

$$\lim_{x \to 2} \frac{|x-2|}{x-2}?$$

For an extra half point, what is the limit?

(7) Where is the following function discontinuous? Identify the type of discontinuity, if any.

$$f(x) = \begin{cases} 0 & \text{if } x \le 0 \\ x & \text{if } 0 < x < 2 \\ 1 & \text{if } x \ge 2 \end{cases}$$

- (8) If s(t) represents the position of a particle at time t, write an expression which represents the velocity of the particle at time t = a.
- (9) What method would you use to solve

$$\lim_{n \to \infty} \frac{3n^2 + 1}{2n^2 - 4n + 1}?$$

For an extra half point, what is the limit?

(10) Find the sum of

$$\sum_{n=2}^{\infty} 2 \cdot \frac{1}{3^n}$$

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