Mean, median, mode puzzle

Create a list of non-negative integers (i.e. whole numbers) such that the mean, median, and mode are are single, integer values, and which satisfy:

(1) Mean < Median < Mode

(2) Mean < Mode < Median

(3) Median < Mean < Mode

(4) Median < Mode < Mean

(5) Mode < Mean < Median

(6) Mode < Median < Mean

Your score for each of the 6 challenges is the largest number you used in your list of numbers. Your goal is to have the smallest score possible.

For example, consider the list $1, 1, 2, 2, 6, 6, 7, 7, 7, 11$. This has mean $50/10 = 5$, median of $(6 + 6)/2 = 6$, and mode 7. This satisfies challenge (1), with a score of 11 (this is not a good score).