

AP CALCULUS BC	YouTube Live Virtual Lessons	Mr. Bryan Passwater Mr. Anthony Record
Topic: All Units	Free Response Question Stem Types  Verbal Interpretations, Explanations & Reasoning	Date: April 30, 2020

## Free Response Questions Stem Types: Verbal 2020 FRQ Practice Problem BC1

$t$ (minutes)	0	1	4	6	10
$E'(t)$ (students/minute)	21	18	8	3	1

**BC1:** When Mr. Passwater starts his live online help session for his AP Calculus students, there are 25 students in the session. For  $0 \leq t \leq 10$  minutes, students enter the online session at a rate modeled by the differentiable function,  $E'(t)$ , where  $E'(t)$  is decreasing and measured in students per minute.

(a) Use the data in the table to approximate  $E''(5)$ . Using correct units, interpret the meaning of  $E''(5)$  in the context of the problem.

(b) Is there a time  $t$ ,  $0 < t < 10$ , at which  $E''(t) = -2$ ? Justify your answer.

The problem has been restated.

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$E'(t)$ (students/minute)	21	18	8	3	1

**BC1:** When Mr. Passwater starts his live online help session for his AP Calculus students, there are 25 students in the session. For  $0 \leq t \leq 10$  minutes, students enter the online session at a rate modeled by the differentiable function,  $E'(t)$ , where  $E'(t)$  is decreasing and measured in students per minute.

(c) Using correct units, explain the meaning of  $\int_0^{10} E'(t) dt$  in the context of the problem. Use a right

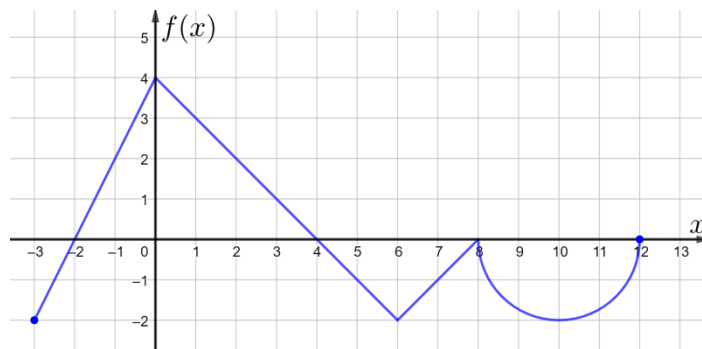
Riemann with the four subintervals indicated in the table to estimate  $\int_0^{10} E'(t) dt$ .

(d) Is the approximation in part (b) an overestimate or underestimate of  $\int_0^{10} E'(t) dt$ ? Give a reason for your answer.

(e) A tangent line to the graph of  $y = E(t)$  at  $t = 0$  is used to approximate  $E(1)$ . Does this approximation overestimate or underestimate  $E(1)$ ? Give a reason for your answer.

# Free Response Questions Stem Types: Verbal

## 2020 FRQ Practice Problem BC2



**BC2:** The function  $f$  is defined on the closed interval  $[-3, 12]$ . The graph of  $f$ , shown in the figure above, consists of three line segments and a semicircle centered at  $(10, 0)$ . Let  $g$  be the function defined by

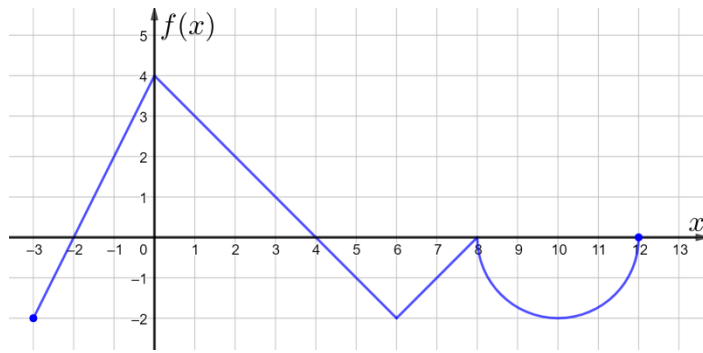
$$g(x) = \int_4^x f(t) dt.$$

(a) Find all value(s) of  $x$  on the open interval  $-3 < x < 12$  for which the function  $g$  has a local maximum. Justify your answer.

(b) On what open intervals contained in  $-3 < x < 12$  is the graph of  $g$  both concave up and decreasing? Explain your reasoning.

(c) For  $-3 < x < 12$ , find all values of  $x$  for which the graph of  $g$  has a point of inflection. Explain your reasoning.

The problem has been restated.



**BC2:** The function  $f$  is defined on the closed interval  $[-3, 12]$ . The graph of  $f$ , shown in the figure above, consists of three line segments and a semicircle centered at  $(10, 0)$ . Let  $g$  be the function defined by

$$g(x) = \int_4^x f(t) dt.$$

(d) Determine the minimum value of  $g$  on the closed interval  $[-3, 12]$ . Justify your answer.

(e) Find  $\lim_{x \rightarrow 3} \frac{g(2x) + x - 1}{1 - e^{f(x+1)}}$ .

(f) Let  $H(x) = \begin{cases} \frac{x}{g(x)} & x < 8 \\ -2\ln|e + f(x)| & x \geq 8 \end{cases}$ . Is  $H(x)$  continuous at  $x = 8$ ? Why or why not?