

Equivalent definitions of Euler's number

Prove that the following are equivalent:

(1) $e = \lim_{n \rightarrow \infty} \left(1 + \frac{1}{n}\right)^n$

(2) e is the unique number such that $1 = \lim_{h \rightarrow 0} \frac{e^h - 1}{h}$