

1. Consider differentiable functions  $f(x)$  and  $g(x)$  which have the following values and derivatives:

$x$	-3	0	1	4	5
$f(x)$	-3	-3	-4	1	-3
$g(x)$	-3	1	3	-4	2
$f'(x)$	4	-3	-3	-4	2
$g'(x)$	-2	-1	-1	1	4

Based on the table above, find the following, if possible:

- (a) (2 points)  $(f + g)'(1)$

**Solution:** -4

- (b) (2 points)  $(f - g)'(1)$

**Solution:** -2

- (c) (2 points)  $(fg)'(-3)$

**Solution:** -6

- (d) (2 points)  $(f/g)'(0)$

**Solution:** -6

- (e) (2 points)  $(g/f)'(0)$

**Solution:**  $\frac{2}{3}$

- (f) (2 points) The average value of  $f$  on  $[-3, 5]$

**Solution:** 0

2. Consider differentiable functions  $f(x)$  and  $g(x)$  which have the following values and derivatives:

$x$	-2	0	1	4	5
$f(x)$	-1	2	1	-4	4
$g(x)$	-4	-1	4	4	-4
$f'(x)$	3	-4	2	3	-3
$g'(x)$	1	1	-3	4	-4

Based on the table above, find the following, if possible:

- (a) (2 points)  $(f + g)'(4)$

**Solution:** 7

- (b) (2 points)  $(f - g)'(5)$

**Solution:** 1

- (c) (2 points)  $(fg)'(1)$

**Solution:** 5

- (d) (2 points)  $(f/g)'(0)$

**Solution:** 2

- (e) (2 points)  $(g/f)'(0)$

**Solution:**  $-\frac{1}{2}$

- (f) (2 points) The average value of  $f$  on  $[-2, 5]$

**Solution:**  $\frac{5}{7}$

3. Consider differentiable functions  $f(x)$  and  $g(x)$  which have the following values and derivatives:

$x$	-3	-2	0	2	6
$f(x)$	3	4	3	4	2
$g(x)$	-2	-3	-3	3	2
$f'(x)$	-1	-2	-3	3	-1
$g'(x)$	4	4	3	-1	-3

Based on the table above, find the following, if possible:

- (a) (2 points)  $(f + g)'(2)$

**Solution:** 2

- (b) (2 points)  $(f - g)'(0)$

**Solution:** -6

- (c) (2 points)  $(fg)'(2)$

**Solution:** 5

- (d) (2 points)  $(f/g)'(2)$

**Solution:**  $\frac{13}{9}$

- (e) (2 points)  $(g/f)'(-3)$

**Solution:**  $\frac{10}{9}$

- (f) (2 points) The average value of  $f$  on  $[-3, 6]$

**Solution:**  $\frac{-1}{9}$

4. Consider differentiable functions  $f(x)$  and  $g(x)$  which have the following values and derivatives:

$x$	-2	-1	2	3	6
$f(x)$	3	3	-2	-1	-1
$g(x)$	-4	-1	-3	-3	-1
$f'(x)$	-1	0	4	1	-2
$g'(x)$	2	3	-4	1	0

Based on the table above, find the following, if possible:

- (a) (2 points)  $(f + g)'(-1)$

**Solution:** 3

- (b) (2 points)  $(f - g)'(-1)$

**Solution:** -3

- (c) (2 points)  $(fg)'(3)$

**Solution:** -4

- (d) (2 points)  $(f/g)'(-1)$

**Solution:** -9

- (e) (2 points)  $(g/f)'(2)$

**Solution:** 5

- (f) (2 points) The average value of  $f$  on  $[-2, 6]$

**Solution:**  $-\frac{1}{2}$

5. Consider differentiable functions  $f(x)$  and  $g(x)$  which have the following values and derivatives:

$x$	-2	0	1	4	5
$f(x)$	-1	-4	2	-2	2
$g(x)$	-4	-4	-3	-4	1
$f'(x)$	-4	-2	-3	-4	0
$g'(x)$	-4	-2	-1	0	4

Based on the table above, find the following, if possible:

- (a) (2 points)  $(f + g)'(0)$

**Solution:** -4

- (b) (2 points)  $(f - g)'(0)$

**Solution:** 0

- (c) (2 points)  $(fg)'(-2)$

**Solution:** 20

- (d) (2 points)  $(f/g)'(4)$

**Solution:** 1

- (e) (2 points)  $(g/f)'(1)$

**Solution:**  $-\frac{11}{4}$

- (f) (2 points) The average value of  $f$  on  $[-2, 5]$

**Solution:**  $\frac{3}{7}$

6. Consider differentiable functions  $f(x)$  and  $g(x)$  which have the following values and derivatives:

$x$	-3	0	2	3	4
$f(x)$	-1	3	0	-3	2
$g(x)$	3	4	-4	-3	-4
$f'(x)$	1	-1	-2	-3	-3
$g'(x)$	0	4	-1	2	3

Based on the table above, find the following, if possible:

- (a) (2 points)  $(f + g)'(0)$

**Solution:** 3

- (b) (2 points)  $(f - g)'(-3)$

**Solution:** 1

- (c) (2 points)  $(fg)'(2)$

**Solution:** 8

- (d) (2 points)  $(f/g)'(-3)$

**Solution:**  $\frac{1}{3}$

- (e) (2 points)  $(g/f)'(-3)$

**Solution:** -3

- (f) (2 points) The average value of  $f$  on  $[-3, 4]$

**Solution:**  $\frac{3}{7}$

7. Consider differentiable functions  $f(x)$  and  $g(x)$  which have the following values and derivatives:

$x$	-4	-1	2	3	4
$f(x)$	-3	-2	-1	1	3
$g(x)$	-2	-2	-1	-1	0
$f'(x)$	-3	1	-1	-1	4
$g'(x)$	4	0	4	-4	1

Based on the table above, find the following, if possible:

- (a) (2 points)  $(f + g)'(2)$

**Solution:** 3

- (b) (2 points)  $(f - g)'(-4)$

**Solution:** -7

- (c) (2 points)  $(fg)'(4)$

**Solution:** 3

- (d) (2 points)  $(f/g)'(-4)$

**Solution:**  $\frac{9}{2}$

- (e) (2 points)  $(g/f)'(-1)$

**Solution:**  $\frac{1}{2}$

- (f) (2 points) The average value of  $f$  on  $[-4, 4]$

**Solution:**  $\frac{3}{4}$

8. Consider differentiable functions  $f(x)$  and  $g(x)$  which have the following values and derivatives:

$x$	-4	-3	-1	4	6
$f(x)$	1	-4	-4	0	1
$g(x)$	2	-2	-2	-4	2
$f'(x)$	1	-3	-2	-4	-3
$g'(x)$	2	1	3	4	2

Based on the table above, find the following, if possible:

- (a) (2 points)  $(f + g)'(6)$

**Solution:** -1

- (b) (2 points)  $(f - g)'(-4)$

**Solution:** -1

- (c) (2 points)  $(fg)'(-1)$

**Solution:** -8

- (d) (2 points)  $(f/g)'(4)$

**Solution:** 1

- (e) (2 points)  $(g/f)'(-1)$

**Solution:** -1

- (f) (2 points) The average value of  $f$  on  $[-4, 6]$

**Solution:** 0



9. Consider differentiable functions  $f(x)$  and  $g(x)$  which have the following values and derivatives:

$x$	-4	-3	-1	3	6
$f(x)$	-2	-1	2	2	-1
$g(x)$	2	3	0	2	1
$f'(x)$	-1	1	-2	-3	-3
$g'(x)$	0	-2	4	-2	3

Based on the table above, find the following, if possible:

- (a) (2 points)  $(f + g)'(-1)$

**Solution:** 2

- (b) (2 points)  $(f - g)'(-3)$

**Solution:** 3

- (c) (2 points)  $(fg)'(-3)$

**Solution:** 5

- (d) (2 points)  $(f/g)'(3)$

**Solution:**  $-\frac{1}{2}$

- (e) (2 points)  $(g/f)'(-4)$

**Solution:**  $\frac{1}{2}$

- (f) (2 points) The average value of  $f$  on  $[-4, 6]$

**Solution:**  $\frac{1}{10}$

10. Consider differentiable functions  $f(x)$  and  $g(x)$  which have the following values and derivatives:

$x$	-2	-1	2	3	5
$f(x)$	-4	-3	0	3	3
$g(x)$	-3	3	1	0	3
$f'(x)$	4	-2	3	3	3
$g'(x)$	-1	-2	-1	0	4

Based on the table above, find the following, if possible:

(a) (2 points)  $(f + g)'(-1)$

**Solution:** -4

(b) (2 points)  $(f - g)'(5)$

**Solution:** -1

(c) (2 points)  $(fg)'(5)$

**Solution:** 21

(d) (2 points)  $(f/g)'(3)$

**Solution:** Does not exist

(e) (2 points)  $(g/f)'(3)$

**Solution:** 0

(f) (2 points) The average value of  $f$  on  $[-2, 5]$

**Solution:** 1