An improper integral

Does
$$\int_0^\infty \sin x \sin x^2 dx$$
 converge? Why or why not?