A continuous, non-differentiable function

(EXTREMELY HARD) Does there exist a function $f: \mathbb{R} \to \mathbb{R}$ (i.e., the domain is the real numbers and every value is a real number) such that f(x) is continuous everywhere and differentiable nowhere?