

Name: \_\_\_\_\_

Mark: \_\_\_\_\_

**Mini-math Div 3/4: Monday, February 1, 2021 (15 minutes)**

1. (2 points) Let  $f$  be a differentiable function such that:

$$f(4) = 6, \quad f(8) = 4, \quad f'(4) = -3, \quad f'(8) = -5.$$

Suppose the function  $g(x) = f^{-1}(x)$  is differentiable for all  $x$ . What is  $g'(4)$ ?

2. (4 points) Find the equation of the line tangent to the given curve at the given point.

$$e^x + \ln(x + y) = x + 1, \quad \text{at } (0, 1)$$

3. (2 points) Find  $f(t)$  if  $f(t) = 2^{3^x}$ .

4. Find the derivative of  $y$  with respect to  $x$  in each of the following.

(a) (2 points)  $y = \ln |x^4 - 4|$

(b) (2 points)  $y = \log_2 \left( \frac{\sin x}{2^x} \right)$

5. (4 points) Find the derivative of  $y$  with respect to  $x$  in the following via logarithmic differentiation. **You do not need to simplify your final expression, and may express your answer in terms of both  $y$  and  $x$ .**

$$y = \sqrt{\frac{(x+1)^2(2x-1)^3}{x}}$$