

The ratio of girls to boys at a party was 27:31. After 9 boys arrived, the ratio of girls to boys at the party was 27:32. Find the number of boys at the start.

$$\begin{array}{rcl}
 \begin{array}{l} \text{girls} \\ 27 \square \end{array} & \begin{array}{l} \text{boys} \\ 31 \square \\ + 9 \\ 32 \square \end{array} & \left. \vphantom{\begin{array}{l} \text{girls} \\ 27 \square \end{array}} \right\} \square = 9 \\
 27 \square & & 31 \times 9 = 279
 \end{array}$$

The ratio of girls to boys at a party was 13:10. After 3 girls left and 3 boys arrived, the ratio of girls to boys at the party was 38:31. Find the number of girls at the start.

What is staying the same? girls, boys, or total

$$\begin{array}{rcl}
 \text{start:} & 13:10 & 13\Delta:10\Delta \quad \text{total: } 23\Delta \\
 \text{end:} & 38:31 & 38\boxplus:31\boxplus \quad \text{total: } 69\boxplus
 \end{array}
 \left. \vphantom{\begin{array}{rcl} \text{start:} & 13:10 & 13\Delta:10\Delta \end{array}} \right\} \begin{array}{l} \text{should be equal} \\ \Delta = 3\boxplus \end{array}$$

$$\begin{array}{rcl}
 \text{start:} & 39\square:30\square & \left. \vphantom{\begin{array}{rcl} \text{start:} & 39\square:30\square \end{array}} \right\} \text{difference: } \square \\
 \text{end:} & 38\square:31\square & \square = 3
 \end{array}$$

Start with $39\square = 39 \times 3 = 117$

The ratio of girls to boys at a party was 3:4. After 12 girls arrived, the ratio of girls to boys became 3:2. How many children are there in total at the end?

① Identify what is not changing: boys

$$\begin{array}{rcl}
 3:4 & & \left. \vphantom{\begin{array}{rcl} 3:4 \\ 6:4 \end{array}} \right\} \begin{array}{l} 3\square = 12 \\ \square = 4 \end{array} \\
 \downarrow & \text{becomes} & \\
 3:2 & & \underline{6:4}
 \end{array}$$

Total: $10\square = 10 \times 4 = 40$

The ratio of girls to boys at a party was 3:4. After 510 girls arrive and 510 boys leave, the ratio becomes 5:1. How many girls at the end?

The total # of children is staying the same

| | | | | | |
|------------|----------|------------|-------|------|-------------|
| Start: 3:4 | total: 7 | $\times 6$ | 18:24 | | 18□:24□ |
| End: 5:1 | total: 6 | $\times 7$ | 35:7 | +17□ | 35□:7□ -17□ |

$$\Rightarrow 17\square = 510$$

$$\square = 30$$

$$35\square = 1050$$