

Name: \_\_\_\_\_

Mark: \_\_\_\_\_

**Mini-math Div 3/4: Friday, February 8, 2023 (20 minutes)**

**Calculator active**

1. (4 points) At time  $t \geq 0$ , a particle moving in the  $xy$ -plane has velocity vector given by  $v(t) = \langle \sin(t^2), 2\sqrt{t} \rangle$ . If the particle is at point  $(-3, 1)$  at time  $t = 0$ , how far is the particle from the origin at time  $t = 3$ ?
2. (4 points) Where does the graph  $r = 1 - \sin \theta$ ,  $0 \leq \theta \leq 2\pi$ , have a vertical tangent?

3. (4 points) Find the area of the inner loop of  $r = 4\sqrt{3} - 8\cos\theta$

4. (4 points) Find the area of the region common to  $r = 1 - \sin\theta$  and  $r = 2\sin\theta$ .