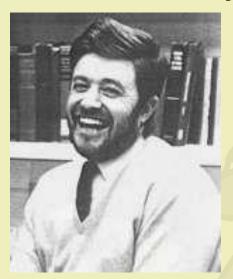


Array Oriented Functional Programming With Dyalog APL

Jay Foad Morten Kromberg Roger Hui



History of APL



Kenneth E. Iverson 1920-2004

- Canadian of Norwegian Descent
- Born on a small farm in Alberta (Canada)
- Finished one-room school after 9th grade and worked on the farm
- Army 1942, Flight Engineer in Air Force from 1943
 - Almost finished High School in the service
 - Promised his officers and mates that he would pursue an academic career after the war
- B.A. from Queens University, Kingston Ontario
 - Ken didn't know there was such a thing as University before he joined the army!



History of APL, continued



- Doctoral work at Harvard with Aiken and Leontief
- Taught at Harvard for 6 years,
 - frustrated with inadequacies of mathematical notation
 - Developed "Iverson Notation" in response
 - Published "A Programming Language" in 1962

ACM Turing award in 1979:

"For his pioneering effort in programming languages and mathematical notation resulting in what the computing field now knows as APL, for his contributions to the implementation of interactive systems, to educational uses of APL, and to programming language theory and practice."

Syntaxes of Mathematics

a b

 $Mat1 \cdot Mat2$

Problems:

- Wide variety of syntactical forms
- Strange and inconsistent precedence rules
- Things get worse when you deal with matrices

See http://www.jsoftware.com/papers/EvalOrder.htm

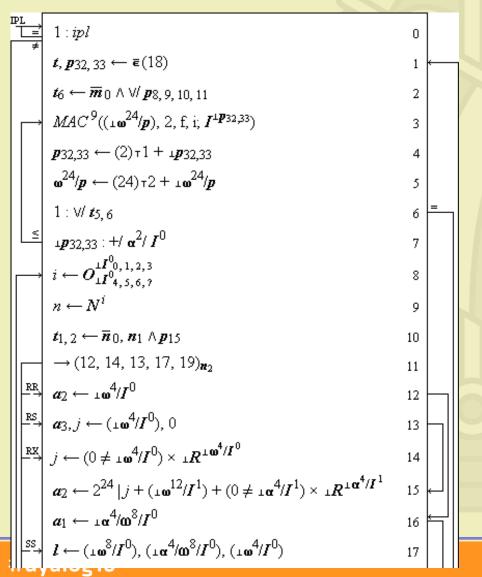
$$\sum_{n=1}^{\infty} 4n$$

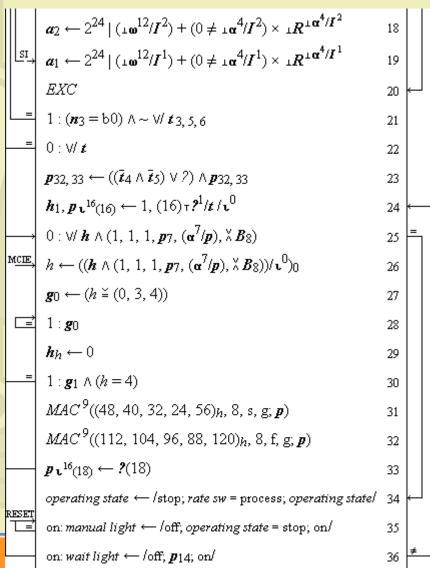
$$\prod_{i=1}^{5} 4i$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$



Iverson Notation: Description of IBM\360





A Programming Language

• The book, 1962

```
Quotient z \leftarrow x \div y z is the quotient of x and y

Absolute value z \leftarrow |x| z = x \times [(x > 0) - (x < 0)]

Floor k \leftarrow \lfloor x \rfloor k \le x < k + 1

Ceiling k \leftarrow \lceil x \rceil k \ge x > k - 1

j-Residue mod k \leftarrow h|_j i i = hq + k; j \le k < j + h; and q is integral.
```

Linearization => APL\360

 The 5: Ken Iverson, Adin Falkoff, Larry Breed, Dick Lathwell, Roger Moore. Operated by "Quaker Consensus".

```
Quotient z \leftarrow x \div y z is the quotient of x and y

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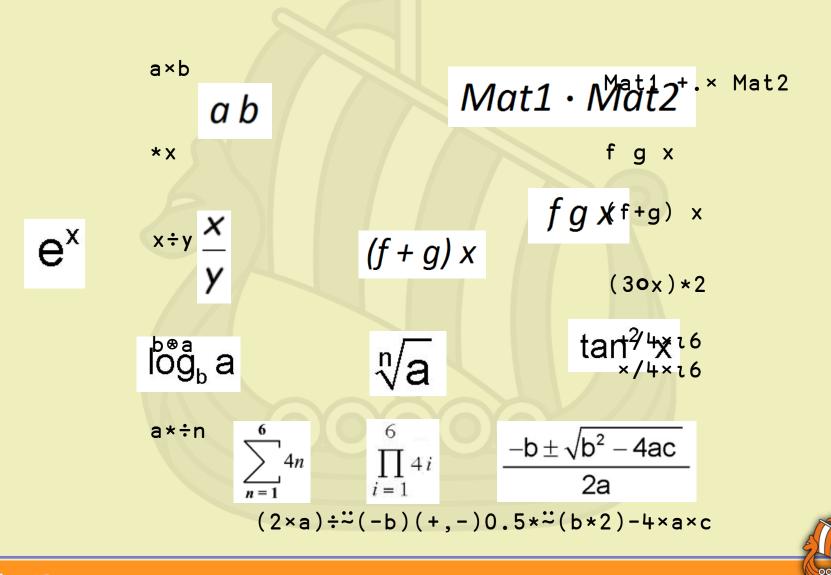
The first saved workspace:

)LOAD 1 CLEARSPACE SAVED 1966-11-27 15.53.59 (GMT-7)



A Programming Language

(for Mathematics)



Saving Your Work

- Historically, APL users have saved workspaces containing code and data as a single file
 - Similar to an Excel Spreadsheet
 - Takes a "snapshot of the VM"
 - Beware: also saves the execution stack if there is one
- Save your work using)save /path/mywsname[.dws]
- Load it again with) load /path/mywsname
- You can extract named objects from a workspace:
 -)copy /path/mywsname foo goo x y
- Saved workspaces can have a "latent expression"

 LX, which is executed when the workspace is loaded, unless you
 -)xload /path/mywsname



Saving Your Work, continued

- In the last few years, it has become more popular to use Unicode text files (and SVN/GIT), especially for source code
- You can save a fn/var, namespace or class using]save (]save is a "user command" - written in APL):

```
]save name /path/name[.dyalog]
(it is customary to use the same name for the file)
```

- If you edit objects that were] loaded, the system will offer to update the file each time you make a change
- From version 15.0, the interpreter (editor) knows how to open and view source files without user commands.

Indexing and Partial Assignment

]demo indexing.txt



Reading APL

$$CB \leftarrow \{\omega[1+(\rho\omega)|X\circ.+X\leftarrow(\iota\alpha)-1]\}$$

Imagine arguments:



Reading APL

```
life \{ \uparrow 1 \ \omega \lor . \land 3 \ 4 = +/, \ 1 \ 0 \ 1 \circ . \ominus \ 1 \ 0 \ 1 \circ . \varphi \subset \omega \}
```

http://dfns.dyalog.com/n life.htm
http://www.youtube.com/watch?v=a9xAKttWgP4

- Try it out in small chunks, starting from the right.
- Know what's a function and what's an operator.
- Note the creative use of inner product.
- Finally try reading it from left to right.



Quirks that you may notice:

- Some APL programmers like to avoid parentheses, to reduce the cognitive load!
- Hence, put simple argument on left: 1+...
- Or, use Commute: 2 * [□]...
- N.B. game of life has no parentheses, partly because (some) primitives (e.g. Residue) were carefully designed to be most useful with a simple constant on the *left*.



Or:

Reading APL

What does this function do?

```
{(~R∈R∘.×R)/R←1↓ιω}
{{(~ω∈ω∘.×ω)/ω}1↓ιω}
```



"Procedures"

- Before dfns, APL had an imperative form now known as "tradfns"
- The only control flow was → (goto)
- Control structures (: If etc) arrived in the late 1980's
- Within "tradfns", names have dynamic scope



Procedures / Tradfns

Monadic:

Dyadic:

```
∇ R←A MatMult B
[1] R←A+.×B
```

Niladic:



Procedures / Tradfns

"Ambi-valent" (+ use a control structure)



Procedures / Tradfns

Name Elements of Right Argument

- + Local Variable
- + Class / DotNet declarations



Errors

```
1 2 3÷4 5
LENGTH ERROR
      1 2 3÷4 5
     ۸
      □EN
5
      1÷0
DOMAIN ERROR: Divide by zero
      1÷0
      □EN (□EM 11)
 11
    DOMAIN ERROR
      DMX.Message
Divide by zero
```



Errors

- 1 WS FULL
- 2 SYNTAX ERROR
- 3 INDEX ERROR
- 4 RANK ERROR
- 5 LENGTH ERROR
- 6 VALUE ERROR
- 7 FORMAT ERROR
- 10 LIMIT ERROR
- 11 DOMAIN ERROR
- 12 HOLD ERROR
- 13 OPTION ERROR
- 15 LST FULL
- 16 NONCE ERROR
- 17 ACCESS ERROR

- 18 FILE TIE ERROR
- 19 FILE ACCESS ERROR
- 20 FILE INDEX ERROR
- 21 FILE FULL
- 22 FILE NAME ERROR
- 23 FILE DAMAGED
- 24 FILE TIED
- 25 FILE TIED REMOTELY
- 26 FILE SYSTEM ERROR
- 28 FILE SYSTEM NOT AVAILABLE
- 30 FILE SYSTEM TIES USED UP
- 31 FILE TIE QUOTA USED UP
- 32 FILE NAME QUOTA USED UP
- 34 FILE SYSTEM NO SPACE
- 35 FILE ACCESS ERROR CONVERTING FILE
- 36 INCOMPATIBLE ARRAY
- 38 FILE COMPONENT DAMAGED



Error Trapping: Dfns

```
div+{0::'Something Else is Wrong'
          11::0 A DOMAIN error: return 0
          α÷ω}
          3 div 0
0
          1 2 3 div 4 5
Something Else is Wrong
```



Error Trapping: Tradfns

Using: Trap



Error Trapping: Tradfns

Using **TRAP**



System Functions

(built-in library functions)

]demo sysfns.txt



Building Applications

Delivery Mechanisms:

- Saved Workspace
- Workspace Bound with Interpreter as an .exe
- COM Server
- Microsoft.Net Assembly
 - ASP.Net scripting language, Web Services, SharePoint Web Parts,
 WCF, etc etc etc
- "Stand Alone" Web Server, Web Service



