

Chapter 6

INTERNAL SORTING



Each record contains a field called the key.

Linear order: comparison.

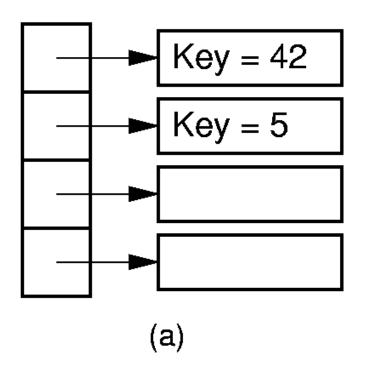
Measures of cost:

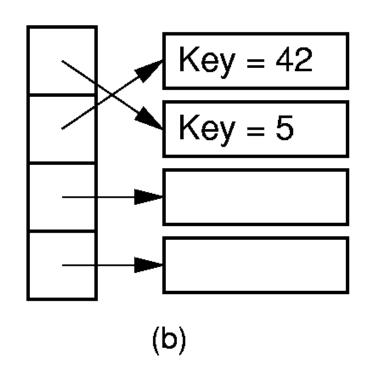
- Comparisons
- Swaps





Pointer Swapping









swap function

```
void swap(int *A, int i, int j)
  int temp;
  temp=A[i];
  A[i] = A[j];
  A[j] = temp;
```





Insertion Sort (1)

i=1	2	3	4	5	6	7
20	17	13	13	13	13	13
42	20	17	17	14	14_	14
17 —	42	20	20	17	17	15
13	13—	42	28	20	20	17
28	28	28	42	28	23	20
14	14	14	14—	42	28	23
23	23	23	23	23	42	28
15	15	15	15	15	15	42
	20 42 17 13 28 14 23	20 17 20 42 13 13 13 28 28 14 14 23 23	20 17 13 42 20 17 17 42 20 13 13 42 28 28 28 14 14 14 23 23 23	20 17 13 13 42 20 17 17 17 42 20 20 13 13 42 28 28 28 28 42 14 14 14 14 23 23 23 23	20 17 13 13 13 42 20 17 17 14 17 42 20 20 17 13 13 42 28 20 28 28 42 28 20 28 28 42 28 28 14 14 14 14 42 23 23 23 23 23	20 17 13 13 13 13 42 20 17 17 14 14 17 42 20 20 17 17 13 13 42 28 20 20 28 28 28 42 28 23 14 14 14 14 42 28 23 23 23 23 23 42





Insertion Sort (2)

```
void inssort(int* A, int N)
{
   int i,j,temp;
   for ( i = 1; i < N; i++)
   {
       j = i - 1;
       temp = A[i];
       while (j >= 0 && A[j] > temp)
       {
            swap(A, j, j+1);
            j--;
       }
    }
}
```

Best Case: O(n)

Worst Case: O(n²)

Average Case: O(n²)





Selection Sort (1)

	i=0	1	2	3	4	5	6
42◀┐	13	13	13	13	13	13	13
20	20 ◀	14	14	14	14	14	14
17	17	17 ⊸	15	15	15	15	15
13-	42	42	42 ◀┐	17	17	17	17
28	28	28	28	28 ←	20	20	20
14	14-	20	20	20 🚤	28 ◀	23	23
23	23	23	23	23	23 🕶	28 ←	28
15	15	15◀	17◀	42	42	42	42





Selection Sort (2)

Best Case: O(n²)

Worst Case: O(n²)

Average Case: O(n²)





Bubble Sort (1)

	i=0	1	2	3	4	5	6
42	13	13	13	13	13	13	13
20	42	14	14	14	14	14	14
17	20	42	15	15	15	15	15
13—	17	20	42	17	17	17	17
28	14—	17	20	42	20	20	20
14—	28	15 —	17 —	20 —	42	23	23
23	15—	28	23	23	23 —	42	28
15—	23	23 —	28	28	28	28 —	42





Bubble Sort (2)

```
void bubsort(int* A, int N)
{
    int i,j;
    for ( i = 0; i < N-1; i++)
        for ( j = 0; j < N-i-1; j++)
        if (A[j] > A[j+1] )
            swap(A, j, j+1);
}
```

Best Case: O(n²)

Worst Case: O(n²)

Average Case: O(n²)





Summary

	Insertion	Bubble	Selection
Comparisons:			
Best Case	$\Theta(n)$	$\Theta(n^2)$	$\Theta(n^2)$
Average Case	$\Theta(n^2)$	$\Theta(n^2)$	$\Theta(n^2)$
Worst Case	$\Theta(n^2)$	$\Theta(n^2)$	$\Theta(n^2)$
Swaps			
Best Case	0	0	$\Theta(n)$
Average Case	$\Theta(n^2)$	$\Theta(n^2)$	$\Theta(n)$
Worst Case	$\Theta(n^2)$	$\Theta(n^2)$	$\Theta(n)$





Exchange Sorting

All of the sorts so far rely on exchanges of adjacent records.

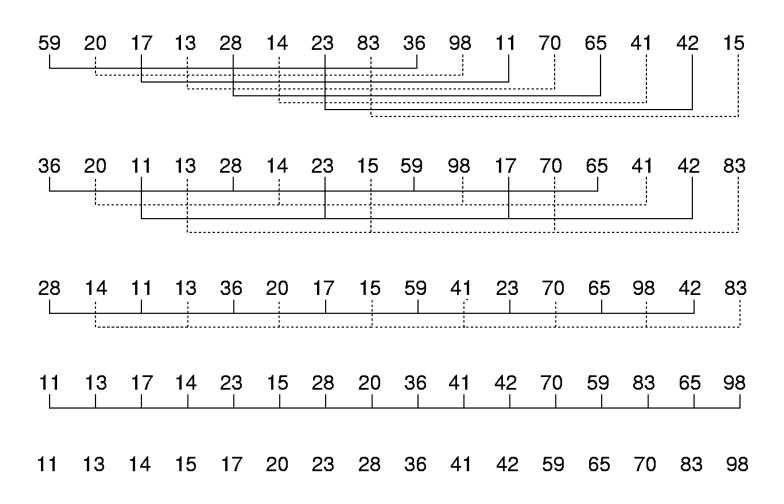
What is the average number of exchanges required?

- There are n! permutations
- Consider permuation X and its reverse, X'
- Together, every pair requires n(n-1)/2 exchanges.





Shellsort





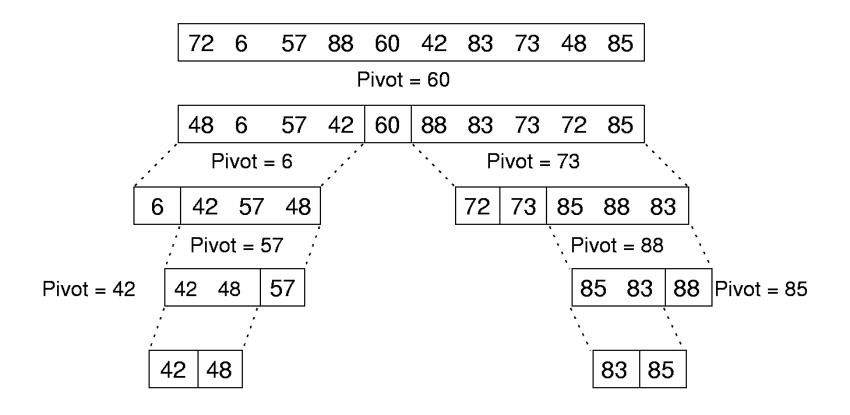


Shellsort





Quicksort Example



6 42 48 57 60 72 73 83 85 88

Final Sorted Array





Quicksort

```
void quisort(int* A, int start, int end)
{
    int i;
    if( end > start )
        {
            i = partition( A, start, end);
            quisort( A, start, i - 1 );
            quisort( A, i + 1, end );
        }
}
```



Quicksort Partition (different elements)

```
int partition(int* A, int left, int right)
     int i,j;
     int pivo = A[ (left+right)/2 ];
i = left; j = right;
     while (1)
        while( A[ i ] < pivo ) { i++; }
while( A[ j ] > pivo ) { j--; }
if ( i < j )</pre>
            swap(A, i, j);
         else
                  break:
     return i;
```

The cost for partition is $\Theta(n)$.





Partition Example

Initial	I	72	6	57	88	85	42	83	73	48	60 r
Pass 1		72 	6	57	88	85	42	83	73	48 r	60
Swap 1		48 I	6	57	88	85	42	83	73	72 r	60
Pass 2		48	6	57	88 	85	42 r	83	73	72	60
Swap 2		48	6	57	42 	85	88 r	83	73	72	60
Pass 3		48	6	57	42 r	85 I	88	83	73	72	60





Best case: Always partition in half.

Worst case: Bad partition.

Average case:

$$T(n) = cn + 1/n \sum_{k=0}^{\infty} (T(k) + T(n-k))$$

Optimizations for Quicksort:

- Better Pivot
- Better algorithm for small sublists
- Eliminate recursion