

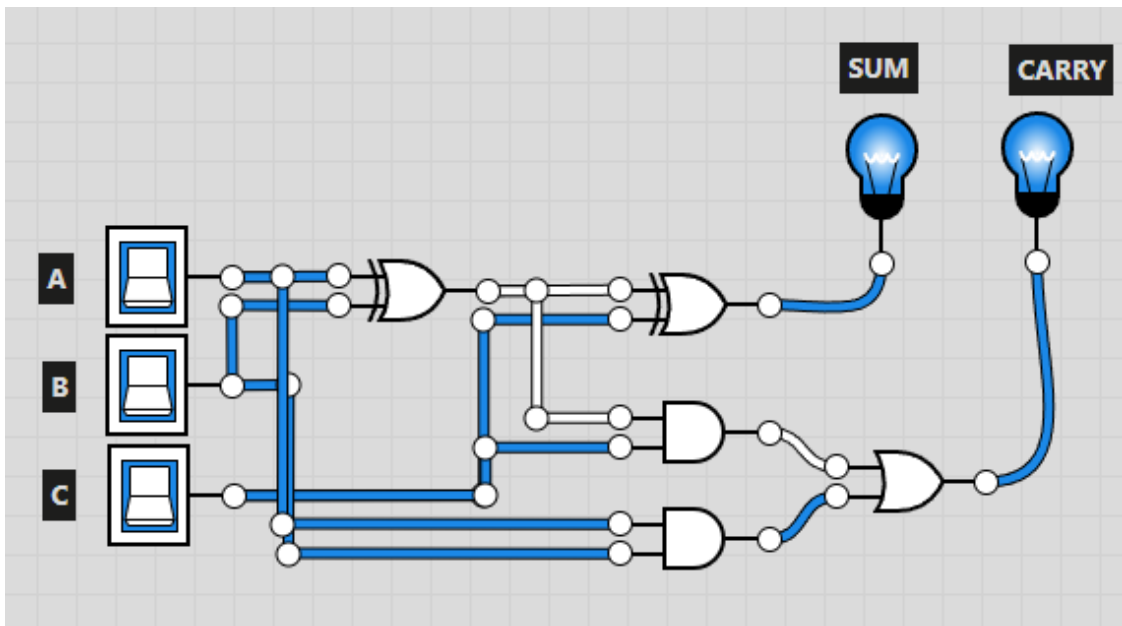
Grade Compensation

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- 1 Give the logical structure of a 1-bit Full Adder with its functional description and truth table. Write the VHDL code of a 1-bit Full Adder.

Logical Structure:



Functional Description:

$$\text{SUM} = (A \oplus B) \oplus C$$

$$\text{Carry} = ((A \oplus B)C) + (AB)$$

Truth Table:

A	B	C	SUM	CARRY
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

VHDL Code:

Design:

```
[ ]: library IEEE;
use IEEE.std_logic_1164.all;

-- ENTITY
entity FullAdder is
port(
    A, B, C: in std_logic;
    Sum, Carry: out std_logic);
end FullAdder;

-- ARCHITECTURE
architecture dataflow of FullAdder is
signal xor1, xor2, and1, and2, or1: std_logic;
begin
    xor1 <= A xor B;
    xor2 <= xor1 xor C;
    and1 <= xor1 and C;
    and2 <= A and B;
    or1 <= and1 or and2;
    Sum <= xor2;
    Carry <= or1;
end dataflow;
```

Test Bench:

```
[ ]: library IEEE;
use IEEE.std_logic_1164.all;

-- TESTBENCH ENTITY
entity testbench is
--empty
end testbench;
```

```

architecture tb of testbench is
-- DUT COMPONENT
component FullAdder is
port(
    A, B, C: in std_logic;
    Sum, Carry: out std_logic);
end component;

signal A_IN, B_IN, C_IN, SUM_OUT, CARRY_OUT : std_logic;

begin

-- CONNECT DUT
DUT: FullAdder port map(A_IN, B_IN, C_IN, SUM_OUT, CARRY_OUT);

    process
    begin
        A_IN <='0';
        B_IN <='0';
        C_IN <='0';
        wait for 1 ns;

        A_IN <='1';
        B_IN <='0';
        C_IN <='0';
        wait for 1 ns;

        A_IN <='0';
        B_IN <='1';
        C_IN <='0';
        wait for 1 ns;

        A_IN <='0';
        B_IN <='0';
        C_IN <='1';
        wait for 1 ns;

        A_IN <='1';
        B_IN <='1';
        C_IN <='1';
        wait for 1 ns;

        -- CLEAR INPUTS
        A_IN <='0';
        B_IN <='0';
        C_IN <='0';
        wait;
    end process;
end tb;

```

```
end process;  
end tb;
```

2 Simplify the following functional description using the algebraic method and mention the Boolean rule at each step.

$$Z(A,B,C,D) = ABCD + AB\bar{C}D + AB\bar{C}\bar{D} + A\bar{B}CD + A\bar{B}\bar{C}D + BC$$

1. Demorgan: $ABCD + A(B'+C') + A(B'+C'+D') + A'B'CD' + A'BCD + BC$
2. Absorption: $A(B'+C')D + A(B'+C'+D') + (A'+B)CD + BC$
3. Distributive: $ADB' + ADC' + AB' + AC' + AD' + (A'+B)CD + BC$
4. Absorption: $AB' + AC' + AD' + (A'+B')CD + BC$
5. Distributive: $AB' + AC' + D'(CA'+A) + CD'B' + BC$
6. Absorption: $A'B + AC' + D'(C+A) + CD'B' + BC$
7. Distributive: $AB' + AC' + D'(C+A) + C(D'B'+B)$
8. Absorption: $AB' + AC' + D'(C+A) + C(D'+B)$
9. Distributive: $AB' + AC' + D'C + D'A + CD' + CB$
10. Idempotent: $AB' + AC' + D'C + D'A + CB$
11. Consensus: $AB' + AC' + D'C + CB$

Simplified Expression: $AB' + AC' + D'C + CB$

3 Simplify the following functional description using the algebraic method and mention the Boolean rule at each step.

$$V(X,Y,Z) = X'YZ + XY + XZ$$

1. Distributive: $Y(X'Z + X) + XZ$
2. Absorption: $Y(Z + X) + XZ$
3. Distribute: $YZ + YX + XZ$

Simplified Expression: $YZ + YX + XZ$