

Homework 1

Microprocessor System Design- ELEN 120

Due 9/25/2023

34 points

These problems are to be solved without a calculator or computer. There is a table of powers of 2 in decimal at the end that may be helpful.

Binary number representations:

- 1) Without using a calculator or computer, properly represent each of the numbers in column 1 as a **16-bit unsigned binary** number in column 2 and as a **16-bit unsigned hexadecimal** number in column 3. (2 points each)

Decimal	16-bit unsigned binary	16-bit unsigned hexadecimal
(Example) 1	0000000000000001	0x0001
127	0000000011111111	0x007F
4097	0001000000000001	0x1001
60000	1110101001100000	0xEA60

four
2010s

- 2) Without using a calculator or computer, properly represent each of the hexadecimal numbers in column 1 as a **decimal number** in column 2. (2 points each)

16-bit unsigned hexadecimal	Decimal
(Example) 0x0001	1
0x0111	273
0xffff	4095
0x1023	4131

$$0000 \quad 0001 \quad 0001 \quad 0001$$

$$2^8 \quad 2^4$$

$$256 + 16 + 1$$

$$0fff = 2^{12} - 1 = 4095$$

$$00010000 \quad 0010 \quad 0011$$

$$2^{12} + 2^5 + 2^1 + 2^0$$

$$4096 + 32 + 2 + 1$$

$$4131$$

$$\begin{array}{r} 32768 \\ 16384 \\ \hline 49152 \\ 49152 \\ \hline 8192 \\ 57344 \\ \hline 2048 \\ 59392 \\ \hline 512 \\ 59904 \\ \hline 96 \\ 60000 \end{array}$$

$$\begin{array}{r} 016 \\ \downarrow \\ 64 + 32 \\ 2^6 + 2^5 \end{array}$$

- 3) Without using a calculator or computer, properly represent each of the numbers in column 1 as a **32-bit signed hexadecimal** number in column 2. (2 points each)

Decimal	32-bit signed hexadecimal
(Example) 1	0x00000001
100	0x00000064
-100	0xFFFFF9C
-2	0xFFFFFEE
8,388,607	0x007FFFFF
-2,147,483,648	0x80000000

$$100 = 01100100 = 64$$

$$-100 = 10011100 = 9C$$

$$\begin{array}{c} 0 \\ \wedge \\ 00 \dots 0111 \dots 111 \\ 2^{31} \quad 2^2 \quad 2^0 \end{array}$$

range
-2147,483,648
to
2147,483,647

100... to 0111... plus 1 forces carry all the way to the front so 2147483648 unsigned \Rightarrow 2147483648 signed

- 4) Without using a calculator or computer, properly represent each of the **32-bit signed hexadecimal** numbers in column 1 as a **decimal** number in column 2. (2 points each)

32-bit signed hexadecimal	Decimal
(Example) 0xFFFFFFFF	-1
0xFFFFFFF	-3
0x00080000	524,288
0xE0000000	-536,870,912

1 1 2 1 2 1
2147483648
1073741824
536870912

3758096384

$$E \Rightarrow \boxed{1110} 00000000$$

$$\begin{array}{c} 8 \\ \hline 000,1000,0000 \\ \hline 524,288 \end{array}$$

signed

$$\begin{array}{c} 0001 \text{ FFFFFFFF} + 1 \\ \hline 0001 00000000 = -536,870,912 \end{array}$$