

Algorithm dySkySeq_build This procedure¹ (see Algorithm 1) takes \mathcal{D} and T as input, and returns a *seqStruct* \mathcal{F} . At the beginning, \mathcal{F} is empty. Variable i indicates the dimension the algorithm is processing and is initialized to 1. Variable *seq* is a stack structure and is used to store the sequences. The algorithm proceeds in a Depth-First fashion. It calls the recursive function *recursiveSeq* with parameters (i) i to indicate the dimension B_i , (ii) T , (iii) *seq*, and (iv) the set \mathcal{F} (line 5). Inside *recursiveSeq*, T' is filtered wrt B_i and o is pushed onto *seq* (line 3-4). If $(i < l)$, i.e. , the algorithm is not processing the last dimension, it recalls *recursiveSeq* with new parameters (line 6). Otherwise, i.e. $(i = l)$, at this step, *seq* contains l orders. Hence it computes the complementary skyline wrt T'' and inserts the pair $(seq, NSky_{\{seq\}}(T''))$ in \mathcal{F} (line 8). Finally, o is popped from the sequence (line 9).

Algorithm 1: dySkySeq_build

Input: a set of dimensions $\mathcal{D} = \{A_1, \dots, A_s, B_1, \dots, B_l\}$, a dataset T

Output: *seqStruct* \mathcal{F}

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1 Procedure recursiveSeq( $i, T', seq, \mathcal{F}$ )
2   foreach  $o \in Orders(B_i)$  in parallel do
3      $T'' \leftarrow \Pi_{[B_i|o.left]}(T') \cup \Pi_{[B_i|o.right]}(T')$ 
4     seq.push( $o$ )
5     if  $i < l$  then
6        $\text{recursiveSeq}(i + 1, T'', seq, \mathcal{F})$ 
7     else
8        $\mathcal{F} \leftarrow \mathcal{F} \cup (seq, NSky_{\{seq\}}(T''))$ 
9     seq.pop( $o$ )

1 begin
2    $\mathcal{F} \leftarrow \emptyset$ 
3    $i \leftarrow 1$ 
4   seq  $\leftarrow \emptyset$ 
5   recursiveSeq( $i, T, seq, \mathcal{F}$ )
6 return  $\mathcal{V}$ 

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¹This algorithms implementation is in <https://github.com/DynamicPartialSky/dySky/blob/master/dySky/dySky.h>