

Collaborative Design:

Pro-functors, categorification, and Monoidal categories:

Takeaway: Understanding Mathematical theory of co-design (collaborative design) and hence understanding constructs like profunctors, monoidal categories and categorifying.

→ Understanding collaborative design:

codesign: A design hierarchical design process where each a large-scale system is divided into sub-group (& further sub-sub-groups), each group working on a sub project.

co-design diagram:

- The small boxes can be considered as sub-projects (groups)
- The wires connecting to the L.H.S of the boxes are requirements and the ones on the R.H.S are produces

And if box A produces requires a resource that box B produces, then A's requirements must be less-than-or-equal-to B's production.

- The box marked Σ correspond to summing inputs.

Ex: 4.1

Formalizing:

Each of the boxes in a co-design diagram correspond to a feasibility relation (giving an idea about feasibility of a sub-project based on produce & requirements)

P is the preorder of resources to be produced
 R is the resources to be required.

Feasibility relation hence defines

The Box says "yes, I can provide p given r " (true)
or "No, I can't provide p given r " (false)

$$(p, r) \in P \times R$$

Feasibility relation hence define a function $\phi: P \times R \rightarrow \text{Bool.}$
with two conditions (to make sense)

(a) If $\phi(p, r) = \text{true}$ and $p' \leq p$, then $\phi(p', r) = \text{true}$

(b) If $\phi(p, r) = \text{true}$ and $r \leq r'$, then $\phi(p, r') = \text{true}$