Dysfunctional Programmer's ICPC Notebook

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1	Tricks
1.1	 Runtime Error Checklist Did you check for formatting errors? Are you using long longs? Did you check for stack overflow? Does the recursive function have a Base case? Are you dividing by zero? Is there enough memory?
1.2	2 Makefile
OFI .PH	FLAGS:=-std=c++14 -g -Wall -Wno-parentheses -Wextra -Winline -fsanitize=address,undefined LES:=\$(subst .cpp,,\$(wildcard *.cpp)) IONY: all : \$(OFILES)
1.3	3 Printing Floats
voi	<pre>d print_fixed(double x, int pr) { cout.precision(pr); cout << fixed << x;</pre>
1.4	4 Python tester
#!/	/usr/bin/env python3
	m random import randint m subprocess import Popen, PIPE
whi	<pre>le True: N = 10 mountains = [randint(0, 10) for i in range(N)] instring = ' '.join(str(x) for x in [N] + mountains).encode('utf-8')</pre>

```
p1 = Popen('./mountains', stdin=PIPE, stdout=PIPE)
output1 = p1.communicate(instring)
p2 = Popen('./mountains.3', stdin=PIPE, stdout=PIPE)
output2 = p2.communicate(instring)
if output1 != output2:
    print(instring)
    break
else:
    print('YES')
```

2 Segment Trees

2.1 Eager

```
#include <bits/stdc++.h>
using namespace std;
struct node {
    int i;
    node() {
        i = 0;
    node(int i) {
        this->i = i;
    node operator+(node other) {
       return node(i + other.i);
};
struct sgt {
    int n;
    vector<node> a;
    sgt(int n) {
        this->n = n;
        a.resize(n<<1);
    }
    void assign(int i, node value) {
        a[n+i] = value;
    void build() {
        for (int i = n - 1; i > 0; --i) a[i] = a[i << 1] + a[i << 1 | 1];
    void update(int i, node value) {
        for (a[i += n] = value; i > 1; i >>=1) a[i>>1] = a[i] + a[i^1];
    node query(int 1, int r) {
        node ret;
        for (1 += n, r += n; 1 < r; 1 >>= 1, r >>= 1) {
            if (1\&1) ret = ret + a[1++];
            if (r\&1) ret = ret + a[--r];
        return ret;
   }
};
```

```
int main() {
   sgt s(5);
   s.assign(0, node(3));
   s.assign(1, node(4));
   s.assign(2, node(2));
   s.assign(3, node(5));
   s.assign(4, node(11));
   s.build();
    cout << s.query(0,3).i << endl;</pre>
    cout << s.query(2,4).i << endl;</pre>
   s.update(2,node(-1));
   cout << s.query(0,3).i << endl;</pre>
   return 0;
2.2
     Lazy
#include <bits/stdc++.h>
using namespace std;
using ll = long long;
int pow2(int x) {
    int 1 = 1;
   while (1 < x) 1 <<= 1;
   return 1;
template<typename T, typename U>
struct lazy_sgt {
   using op = T (*)(T, T);
    struct node {
        T val;
        bool ovr = false;
        U upd;
   using ov = void (*)(node &, U, int);
   const int n;
   vector<node> tree;
    const T id;
    const op merge;
    const ov overwrite;
   lazy_sgt(int n, T id, op m, ov o)
        : n\{pow2(n)\}, tree{2 * this->n + 1}, id{id}, merge{m}, overwrite{o} {}}
    // updates [a, b) with val
    void update(int a, int b, U upd) {
        update(1, a, b, upd, 0, n);
    // queries [a, b)
   T query(int a, int b) {
        return query(1, a, b, 0, n);
    void update(int i, int a, int b, U upd, int left, int right) {
        if (b <= left || a >= right) return; // doesn't intersect
        if (right - left == 1) overwrite(tree[i], upd, right - left);
        else if (a <= left && right <= b) { // wholly contained
            overwrite(tree[i], upd, right - left);
        } else { // intersects
            int mid = left + (right - left) / 2;
            if (tree[i].ovr == true) {
                overwrite(tree[2 * i], tree[i].upd, mid - left);
                overwrite(tree[2 * i + 1], tree[i].upd, right - mid);
                tree[i].ovr = false;
            }
```

```
update(2 * i, a, b, upd, left, mid);
            update(2 * i + 1, a, b, upd, mid, right);
            tree[i].val = merge(tree[2 * i].val, tree[2 * i + 1].val);
        }
    }
    T query(int i, int a, int b, int left, int right) {
        if (b <= left || a >= right) {return id;} // doesn't intersect
        if (right - left == 1) { return tree[i].val;}
        else if (a <= left && right <= b) { // wholly contained
            return tree[i].val;
        } else {
            int mid = left + (right - left) / 2;
            if (tree[i].ovr == true) {
                overwrite(tree[2 * i], tree[i].upd, mid - left);
                overwrite(tree[2 * i + 1], tree[i].upd, right - mid);
                tree[i].ovr = false;
            }
            T l = query(2 * i, a, b, left, mid);
            T r = query(2 * i + 1, a, b, mid, right);
            return merge(1, r);
        }
    }
};
int main() {
    ios::sync_with_stdio(false);
    // Solution to https://www.spoj.com/problems/HORRIBLE/
    using lsgt = lazy_sgt<ll, ll>;
    lsgt::op plus =
        [] (ll a, ll b) {
            return a + b;
        };
    lsgt::ov upd =
        [] (lsgt::node &a, ll u, int width) {
            a.val += u * width;
            if (a.ovr == false) {
                a.upd = u;
            } else {
                a.upd += u;
            a.ovr = true;
        };
    int T;
    cin >> T;
    for (int testcase = 0; testcase < T; ++testcase) {</pre>
        int N, C;
        cin >> N >> C;
        lsgt tree(N, 011, plus, upd);
        for (int i = 0; i < C; ++i) {
            int c, a, b, v;
            cin >> c >> a >> b;
            if (c == 0) \{
                cin >> v;
                tree.update(a - 1, b, (11)v);
            } else {
                cout << tree.query(a - 1, b) << "\n";
        }
    }
    return 0;
}
```

3 Numerical Integration

```
#include <bits/stdc++.h>
using namespace std;
double f(double x) {
        return pow(M_E, -x * x); // dummy
}
// error = -(b - a)^3/(12N^2) * f''(c) for some c in [a, b].
double integrate(double a, double b, int n) {
        double res = 0.5 * f(a) + 0.5 * f(b);
        for (int i = 1; i < n; ++i) {
                res += f(a + (b - a) * i / n);
        return res * (b - a) / n;
}
int main() {
        cout << fixed << setprecision(10) << integrate(-10,10,10000) << '\n';</pre>
        cout << fixed << setprecision(10) << integrate(-10,10,1000) << '\n';</pre>
        cout << fixed << setprecision(10) << integrate(-10,10,100) << '\n';</pre>
        cout << fixed << setprecision(10) << integrate(-10,10,10) << '\n';</pre>
}
     Geometry
4
// Mostly copied from standford ICPC notebook
#include <bits/stdc++.h>
using ll = long long;
using namespace std;
// If the algorithm is exact ll is used. If it is inexact double is used.
// If it is both then T is used.
// Tips for geometry
// 1 Remember special cases
// 1.1 coincident (e.g. point on line)
// 1.2 colinear
// 1.3 Paralell lines (no intersection or gradient, division by zero)
// 2. Remember when multiplying inequalities about possibilites of negatives
// 3. Use <= for EPS to allow EPS to be 0.
// 4. Avoid gradient use cross product instead
// BEGIN TESTED GEOMETRY
// If dealing with integers make EPS 0
#define EPS 0
#define EPSD 1e-12
#define INF LLONG_MAX
// b in [a, c).
template<typename T> bool between(T a, T b, T c) { return a <= b && b < c; }
// b in [a, c].
template<typename T> bool betweenincl(T a, T b, T c) { return a <= b && b <= c; }
// b in [a, c] or [c, a]
template<typename T> bool betweeneither(T a, T b, T c) { return between(a, b, c) || between(c, b, a); }
// On complex number we already have
// abs, norm, arg, conj and polar
template<typename T> using pt = complex<T>;
```

```
const pt<double> Idb = pt<double>(0.0, 1.0);
const pt<11> Ill = pt<11>(011, 111);
// standards compliant magic!
template<typename T> T& x(pt<T> &p) {
    return reinterpret_cast<T*>(&p)[0];
template<typename T > T % y(pt < T > %p) {
    return reinterpret_cast<T*>(&p)[1];
template<typename T> T dot(const pt<T> a, const pt<T> b) {
    return real(conj(a) * b);
template<typename T> T cross(pt<T> a, pt<T> b) {
    return imag(conj(a) * b);
// returns true if p is strictly inside the rectangle with corners a and b
// returns false if p is strictly outside
// returns true or false otherwise
template<typename T> bool pt_in_rect(pt<T> p, pt<T> a, pt<T> b) {
    return betweeneither(x(a), x(p), x(b)) && betweeneither(y(a), y(p), y(b));
// determine if lines from a to b and c to d are parallel or collinear
// n^2 overflow
\label{template} $$\text{template < typename T> bool lines_parallel(pt < T> a, pt < T> b, pt < T> c, pt < T> d) $$\{$
    return abs(cross(b-a, c-d)) <= EPS;
// determine if point is in a possibly non-convex polygon (by William Randolph
// Franklin modified by Yaseen Mowzer); returns true for strictly interior
// points, false for strictly exterior points, and false or true for the
// remaining points.
// n^2 overflow
template<typename T>
bool pt_in_pgon(pt<T> q, vector<pt<T>> &p) {
    bool c = false;
    for (int i = 0; i < (int) p.size(); i++) {
        pt < T > a = p[i], b = p[(i + 1) \% p.size()];
        if (y(a) > y(b)) swap(a, b);
        pt < T > d = b - a;
        if (between(y(a), y(q), y(b))
            && x(q) * y(d) < x(a) * y(d) + x(d) * (y(q) - y(a))) {
        }
    }
    return c;
// determine if point is on the boundary of a polygon
// n^2 overflow
bool pt_on_pgon(pt<ll> q, vector<pt<ll>> &p) {
    for (int i = 0; i < (int) p.size(); i++) {
        pt<ll> a = p[i], b = p[(i + 1) % p.size()];
        if (norm(a - q) <= EPS) return true; // Coincident with a
        if (x(a) < x(b)) swap(a, b);
        if (pt_in_rect(q, a, b)) {
            if (lines_parallel(a, b, a, q)) {
                return true;
        }
    }
    return false;
}
int other_main()
{
```

```
ios::sync_with_stdio(false);
    vector<pt<double>> points {{-1, -1}, {1, -2}, {2, 0}, {2, 2}, {-1, 1}};
    assert(pt_in_pgon({0, 0}, points) == true);
    assert(pt_in_pgon({-2, 0}, points) == false);
    assert(pt_in_pgon({0, 2}, points) == false);
    assert(pt_in_pgon({0, -2}, points) == false);
    // https://codeforces.com/contest/1030/problem/B
    int N, D, M;
    cin >> N >> D;
    vector<pt<11>> rect {{0, D}, {D, 0}, {N, N - D}, {N - D, N}};
    cin >> M;
    for (int i = 0; i < M; ++i) {
        pt<11> p;
        cin >> x(p) >> y(p);
        \verb|cout| << ((pt_on_pgon(p, rect) || pt_in_pgon(p, rect)) ? "YES\n" : "NO\n");
    return 0;
}
// END TESTED GEOMETRY
// project point z onto line through a and b
// assuming a != b (if a == b division by zero will occur).
pt < double > \ proj_pt_on_line(pt < double > \ a, \ pt < double > \ b, \ pt < double > \ z) \ \{
    return a + (b-a)*dot(z-a, b-a)/dot(b-a, b-a);
// project point c onto line segment through a and b
pt<double> proj_pt_on_seg(pt<double> a, pt<double> b, pt<double> c) {
    double r = dot(b-a,b-a);
  if (fabs(r) < EPS) return a;</pre>
  r = dot(c-a, b-a)/r;
  if (r < 0) return a;
  if (r > 1) return b;
  return a + (b-a)*r;
// compute distance between point (x,y,z) and plane ax+by+cz=d
double dist_pt_plane(double x, double y, double z,
                      double a, double b, double c, double d)
  return fabs(a*x+b*y+c*z-d)/sqrt(a*a+b*b+c*c);
}
template<typename T> bool lines_collinear(pt<T> a, pt<T> b, pt<T> c, pt<T> d) {
    return lines_parallel(a, b, c, d)
        && fabs(cross(a-b, a-c)) <= EPS
        && fabs(cross(c-d, c-a)) <= EPS;
// determine if line segment from a to b intersects with
// line segment from c to d
template<typename T>
bool seg_intersect(pt<T> a, pt<T> b, pt<T> c, pt<T> d) {
    if (lines_collinear(a, b, c, d)) {
        if (norm(a - c) \le EPS \mid \mid norm(a - d) \le EPS \mid \mid
            norm(b - c) <= EPS || norm(b - d) <= EPS) return true;</pre>
        if (dot(c-a, c-b) > 0 \&\& dot(d-a, d-b) > 0 \&\& dot(c-b, d-b) > 0)
            return false;
        return true;
    if (cross(d-a, b-a) * cross(c-a, b-a) > 0) return false;
    if (cross(a-c, d-c) * cross(b-c, d-c) > 0) return false;
    return true;
// compute intersection of line passing through a and b
```

```
// with line passing through c and d, assuming that unique
// intersection exists; for segment intersection, check if
// segments intersect first
pt<double> line_intersection(pt<double> a, pt<double> b, pt<double> c, pt<double> d) {
    b=b-a; d=c-d; c=c-a;
    assert(dot(b, b) > EPS && dot(d, d) > EPS);
    return a + b*cross(c, d)/cross(b, d);
// compute center of circle given three points
pt<double> circle_center(pt<double> a, pt<double> b, pt<double> c) {
    b=(a+b)/2.0;
    c=(a+c)/2.0;
    return line_intersection(b, b+(a-b)*(-Idb), c, c+(a-c)*(-Idb));
}
// determine if point is on the boundary of a polygon
bool pt_on_pgon(vector<pt<double>> &p, pt<double> q) {
    for (int i = 0; i < p.size(); i++)
         \label{eq:conseq}  \mbox{if } (\mbox{norm}(\mbox{proj\_pt\_on\_seg}(\mbox{p[i]}, \mbox{ p[(i+1)\%p.size()]}, \mbox{ q) } \mbox{--} \mbox{ q) } <= \mbox{EPS) } 
            return true;
    return false;
}
// compute intersection of line through points a and b with
// circle centered at c with radius r > 0
// WARNING: FAILS TESTS!
vector<pt<double>> circle_line_intersection(pt<double> a, pt<double> b, pt<double> c, double r) {
    vector<pt<double>> ret;
    b = b-a;
    a = a-c;
    double A = dot(b, b);
    double B = dot(a, b);
    double C = dot(a, a) - r*r;
    double D = B*B - A*C;
    if (D < -EPSD) return ret;
    ret.push_back(c+a+b*(-B+sqrt(D+EPSD))/A);
    if (D > EPSD)
        ret.push_back(c+a+b*(-B-sqrt(D))/A);
    return ret;
}
// compute intersection of circle centered at a with radius r
// with circle centered at b with radius R
vector<pt<double>> circle_circle_intersection(pt<double> a, pt<double> b, double r, double R) {
    vector<pt<double>> ret;
    double d = sqrt(norm(a - b));
    if (d > r+R \mid \mid d+min(r, R) < max(r, R)) return ret;
    double x = (d*d-R*R+r*r)/(2*d);
    double y = sqrt(r*r-x*x);
    pt < double > v = (b-a)/d;
    ret.push_back(a+v*x + v*Idb*y);
    if (y > 0)
        ret.push_back(a+v*x - v*Idb*y);
    return ret;
}
// This code computes the area or centroid of a (possibly nonconvex)
// polygon, assuming that the coordinates are listed in a clockwise or
// counterclockwise fashion. Note that the centroid is often known as
// the "center of gravity" or "center of mass".
double signed_area(vector<pt<double>> &p) {
    double area = 0;
    for(int i = 0; i < p.size(); i++) {</pre>
        int j = (i + 1) % p.size();
        area += cross(p[i], p[j]);
    }
    return area / 2.0;
}
```

```
double area(vector<pt<double>> &p) {
    return fabs(signed_area(p));
pt<double> centroid(vector<pt<double>> &p) {
    pt<double> c(0.0 , 0.0);
    double scale = 6.0 * signed_area(p);
    for (int i = 0; i < p.size(); i++){
        int j = (i+1) % p.size();
        c = c + (p[i]+p[j])*cross(p[i], p[j]);
    return c / scale;
}
/\!/\ tests\ \textit{whether or not a given polygon (in CW or CCW order) is simple}
template<typename T>
bool is_simple(const vector<pt<T>> &p) {
    for (int i = 0; i < p.size(); i++) {
        for (int k = i+1; k < p.size(); k++) {</pre>
            int j = (i+1) % p.size();
            int 1 = (k+1) % p.size();
            if (i == 1 \mid \mid j == k) continue;
            if (seg_intersect(p[i], p[j], p[k], p[l]))
                 return false;
        }
    }
    return true;
int secondmain() {
    using PT = pt<double>;
    // expected: (-5,2)
    cerr << pt<11>(2,5)*Ill << endl;</pre>
    // expected: (5,-2)
    cerr << pt<11>(2,5)*(-I11) << endl;
    // expected: (-5,2)
    cerr << pt<double>(2,5) * polar<double>(1.0, M_PI/2) << endl;</pre>
    // expected: (5,2)
    cerr << proj_pt_on_line(PT(-5,-2), PT(10,4), PT(3,7)) << endl;</pre>
    // expected: (5,2) (7.5,3) (2.5,1)
    cerr << proj_pt_on_seg(PT(-5,-2), PT(10,4), PT(3,7)) << " "</pre>
         << proj_pt_on_seg(PT(7.5,3), PT(10,4), PT(3,7)) << " "</pre>
         << proj_pt_on_seg(PT(-5,-2), PT(2.5,1), PT(3,7)) << endl;</pre>
    // expected: 6.78903
    cerr << dist_pt_plane(4,-4,3,2,-2,5,-8) << endl;</pre>
    // expected: 1 0 1
    cerr << lines_parallel(PT(1,1), PT(3,5), PT(2,1), PT(4,5)) << " "</pre>
         << lines_parallel(PT(1,1), PT(3,5), PT(2,0), PT(4,5)) << " "</pre>
         << lines_parallel(PT(1,1), PT(3,5), PT(5,9), PT(7,13)) << endl;</pre>
    // expected: 0 0 1
    cerr << lines_collinear(PT(1,1), PT(3,5), PT(2,1), PT(4,5)) << " "</pre>
         << lines_collinear(PT(1,1), PT(3,5), PT(2,0), PT(4,5)) << " "
         << lines_collinear(PT(1,1), PT(3,5), PT(5,9), PT(7,13)) << endl;</pre>
    // expected: 1 1 1 0
    cerr << seg_intersect(PT(0,0), PT(2,4), PT(3,1), PT(-1,3)) << " "</pre>
         << seg_intersect(PT(0,0), PT(2,4), PT(4,3), PT(0,5)) << " "
         << seg_intersect(PT(0,0), PT(2,4), PT(2,-1), PT(-2,1)) << " "
         << seg_intersect(PT(0,0), PT(2,4), PT(5,5), PT(1,7)) << endl;</pre>
    // expected: (1,2)
```

```
cerr << line_intersection(PT(0,0), PT(2,4), PT(3,1), PT(-1,3)) << endl;</pre>
    // expected: (1,1)
    cerr << circle_center(PT(-3,4), PT(6,1), PT(4,5)) << endl;</pre>
    vector<PT> v;
    v.push_back(PT(0,0));
    v.push_back(PT(5,0));
    v.push_back(PT(5,5));
    v.push_back(PT(0,5));
    // expected: 1 1 1 0 0
    cerr << pt_in_pgon(PT(2,2), v) << " "</pre>
         << pt_in_pgon(PT(2,0), v) << " "
         << pt_in_pgon(PT(0,2), v) << " "
         << pt_in_pgon(PT(5,2), v) << " "
         << pt_in_pgon(PT(2,5), v) << endl;
    // expected: 0 1 1 1 1
    cerr << pt_on_pgon(v, PT(2,2)) << " "
         << pt_on_pgon(v, PT(2,0)) << " "
         << pt_on_pgon(v, PT(0,2)) << " "
         << pt_on_pgon(v, PT(5,2)) << " "
         << pt_on_pgon(v, PT(2,5)) << endl;</pre>
    // expected: (1,6)
    //
                 (5,4) (4,5)
    //
                 blank line
    //
                 (4,5) (5,4)
                 blank line
    //
                 (4,5) (5,4)
    vector<PT> u = circle_line_intersection(PT(0,6), PT(2,6), PT(1,1), 5);
    for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;</pre>
    u = circle_line_intersection(PT(0,9), PT(9,0), PT(1,1), 5);
    for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;</pre>
    u = circle_line_intersection(PT(1,1), PT(10,10), 5, 5);
    for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;
    u = circle_line_intersection(PT(1,1), PT(8,8), 5, 5);
    for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;
    u = circle_line_intersection(PT(1,1), PT(4.5,4.5), 10, sqrt(2.0)/2.0);
    for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;
    u = circle\_line\_intersection(PT(1,1), PT(4.5,4.5), 5, sqrt(2.0)/2.0);
    for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;
    // area should be 5.0
    // centroid should be (1.1666666, 1.166666)
    PT pa[] = { PT(0,0), PT(5,0), PT(1,1), PT(0,5) };
    vector<PT> p(pa, pa+4);
    PT c = centroid(p);
    cerr << "Area: " << area(p) << endl;</pre>
    cerr << "Centroid: " << c << endl;</pre>
    return 0;
      Convex Hull
4.1
// Mostly copied from stanford ICPC notebook
// Compute the 2D convex hull of a set of points using the monotone chain
// algorithm. Eliminate redundant points from the hull if REMOVE_REDUNDANT is
// #defined.
// Running time: O(n log n)
             a vector of input points, unordered.
     INPUT:
     OUTPUT: a vector of points in the convex hull, counterclockwise, starting
              with bottommost/leftmost point
```

//

// //

//

//

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#include <bits/stdc++.h>
#include "geom.cpp"
using namespace std;
using PT = pt<double>;
//#define REMOVE_REDUNDANT
double area2(PT a, PT b, PT c) {
         vector < PT > s = \{a, b, c\};
         return signed_area(s);
}
bool operator<(PT a, PT b) {</pre>
         return make_pair(y(a), x(a)) < make_pair(y(b), x(b));
}
bool operator<=(PT a, PT b) {</pre>
         return make_pair(y(a), x(a)) <= make_pair(y(b), x(b));</pre>
#ifdef REMOVE_REDUNDANT
template <typename T> bool between(PT a, PT b, PT c) {
          \text{return } (fabs(area2(a,b,c)) <= EPS \ \&\& \ (x(a)-x(b))*(x(c)-x(b)) <= 0 \ \&\& \ (y(a)-y(b))*(y(c)-y(b)) <= 0); \\  (x(a)-x(b))*(x(c)-x(b)) <= 0 \ \&\& \ (x(a)-x(b))*(x(a)-x(b)) <= 0 \ \&\& \ (x(a)-x(b))*(x(a)-x(
}
#endif
void ConvexHull(vector<PT> &pts) {
         sort(pts.begin(), pts.end(), [] (PT a, PT b) {return a < b;});</pre>
         pts.erase(unique(pts.begin(), pts.end()), pts.end());
         vector<PT> up, dn;
         for (int i = 0; i < pts.size(); i++) {</pre>
                  up.push_back(pts[i]);
                  dn.push_back(pts[i]);
         }
         pts = dn;
         for (int i = (int) up.size() - 2; i >= 1; i--) pts.push_back(up[i]);
\#ifdef\ REMOVE\_REDUNDANT
         if (pts.size() <= 2) return;</pre>
         dn.clear();
         dn.push_back(pts[0]);
         dn.push_back(pts[1]);
         for (int i = 2; i < pts.size(); i++) {</pre>
                   \  \  \text{if (between(dn[dn.size()-2], dn[dn.size()-1], pts[i])) dn.pop\_back();} \\
                  dn.push_back(pts[i]);
         }
         if (dn.size() \ge 3 \&\& between(dn.back(), dn[0], dn[1])) {
                  dn[0] = dn.back();
                  dn.pop_back();
         }
         pts = dn;
#endif
}
// BEGIN CUT
// The following code solves SPOJ problem #26: Build the Fence (BSHEEP)
struct cmp {
         bool operator()(PT a, PT b) {
                  return a < b;
         }
};
int main() {
         int t;
         scanf("%d", &t);
```

```
for (int caseno = 0; caseno < t; caseno++) {</pre>
         int n;
         scanf("%d", &n);
         vector<PT> v(n);
        for (int i = 0; i < n; i++) scanf("%lf%lf", &x(v[i]), &y(v[i]));
         vector<PT> h(v);
        map<PT, int, cmp> index;
         for (int i = n-1; i >= 0; i--) index[v[i]] = i+1;
         ConvexHull(h);
         double len = 0;
         for (int i = 0; i < h.size(); i++) {</pre>
             double dx = x(h[i]) - x(h[(i+1)%h.size()]);
double dy = y(h[i]) - y(h[(i+1)%h.size()]);
             len += sqrt(dx*dx+dy*dy);
         }
         if (caseno > 0) printf("\n");
         printf("%.2f\n", len);
         for (int i = 0; i < h.size(); i++) {</pre>
             if (i > 0) printf(" ");
             printf("%d", index[h[i]]);
        printf("\n");
    }
}
// END CUT
```

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