

# VISVESVARAYA TECHNOLOGICAL UNIVERSITY

“JnanaSangama”, Belgaum -590014, Karnataka.



## LAB REPORT

on

## Artificial Intelligence (23CS5PCAIN)

Submitted by

Dyuthi (1BM23CS097)

*in partial fulfillment for the award of the degree of*  
**BACHELOR OF ENGINEERING**  
*in*

## COMPUTER SCIENCE AND ENGINEERING



**B.M.S. COLLEGE OF ENGINEERING**

(Autonomous Institution under VTU)

**BENGALURU-560019**

**Aug 2025 to Dec 2025**

**B.M.S. College of Engineering,**  
**Bull Temple Road, Bangalore 560019**  
(Affiliated To Visvesvaraya Technological University, Belgaum)  
**Department of Computer Science and Engineering**



**CERTIFICATE**

This is to certify that the Lab work entitled “Artificial Intelligence (23CS5PCAIN)” carried out by **Dyuthi (1BM23CS097)**, who is bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements in respect of an Artificial Intelligence (23CS5PCAIN) work prescribed for the said degree.

Swathi Sridharan Assistant Professor Department of CSE, BMSCE	Dr. Kavitha Sooda Professor & HOD Department of CSE, BMSCE
---	--

# Index

<b>Sl. No.</b>	<b>Date</b>	<b>Experiment Title</b>	<b>Page No.</b>
1	21-08-2025	Implement Tic – Tac – Toe Game Implement vacuum cleaner agent	4-13
2	28-08-2025	Implement 8 puzzle problems using Depth First Search (DFS) Implement Iterative deepening search algorithm	14-23
3	09-10-2025	Implement A* search algorithm	24-31
4	09-10-2025	Implement Hill Climbing search algorithm to solve N-Queens problem	32-38
5	09-10-2025	Simulated Annealing to Solve 8-Queens problem	39-42
6	16-10-2025	Create a knowledge base using propositional logic and show that the given query entails the knowledge base or not.	43-48
7	30-10-2025	Implement unification in first order logic	49-52
8	30-10-2025	Create a knowledge base consisting of first order logic statements and prove the given query using forward reasoning.	53-58
9	13-11-2025	Create a knowledge base consisting of first order logic statements and prove the given query using Resolution	59-62
10	20-11-2025	Implement Alpha-Beta Pruning.	63-67

Github Link:

<https://github.com/GayathriS-CSE/AI-LAB>

## Program 1

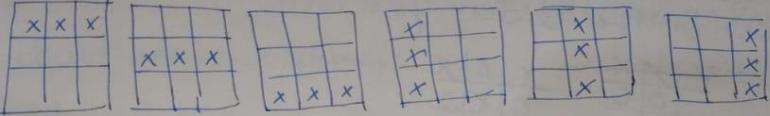
Implement Tic-Tac-Toe Game Implement  
vacuum cleaner agent

Algorithm:

21.08'25.

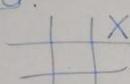
Tic Tac Toe game.

8 ways to win the game.

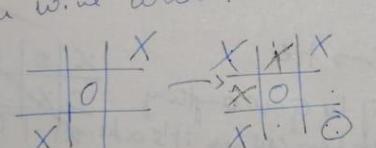


The game has only two players.  
O X.

=> Step 1:- Place your symbol in any corner of the board.

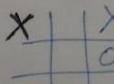


Step 2:- if Opponents places their symbol in the center of the board. You will have to wait till they make a mistake to win. If they Continue to play correctly, there is high chances of tie.  
→ we can win when.

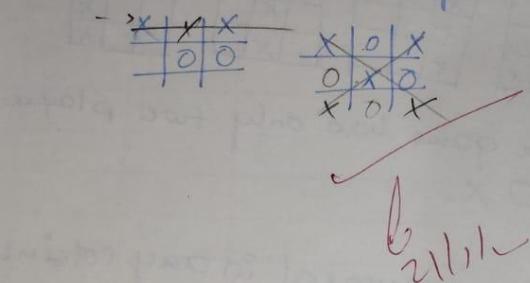


If they place their second O in any of two other corners you can win by placing your next symbol in opposite corner.

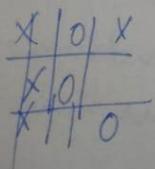
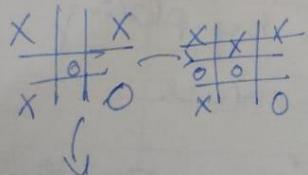
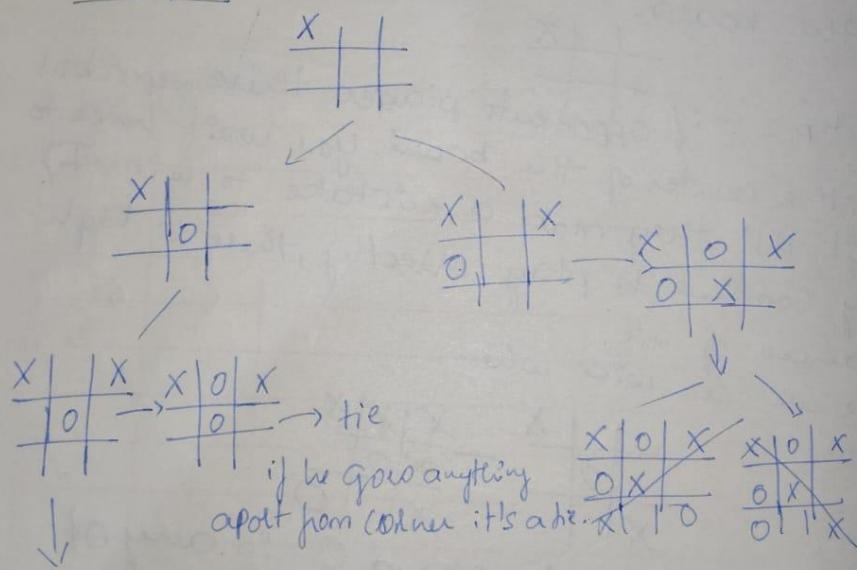
Step 3:- if opponent's first move is anythin other than center. then place you second move in the corner of you same row of your first move.



Step 4:- no matter what is your opponents second move place your third move in the center. If in case he place his second move in the center you win.



### Example



Output:-

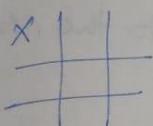
who goes first? Enter 'H' for human or 'A' for AI: h  
Tic Tac Toe: You (X) vs AI (O). You go first.

Board positions reference:

1	2	3
4	5	6
7	8	9

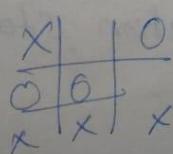
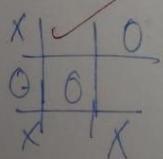
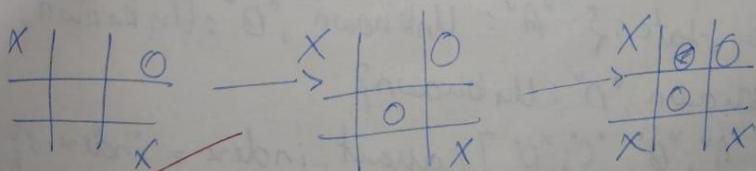
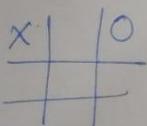
Enter your move (1-9): 1

Current board:



AI moves at position 3

Current board:



Human wins

## Vaccum cleaner Agent.

### Problems statement.

Design an Algorithm where there are 4 rooms and the vaccum cleaner should clean the room if it's dirty  $2^k = n \times n^{loc} = 4 \times 2^4$ .

Step 1: start the agent in any one of the 4 rooms  
(A, B or C, D)

Step 2: check if the current room is dirty or clean.

Step 3: If the room is Dirty then perform action such (clean the room)

Step 4: If the room is clean move to the next room for light.

If in  $A \rightarrow B$  or  $B \rightarrow C$ ,  $C \rightarrow D$ ,  $D \rightarrow A$ .

Step 5: Repeat 2-4 steps until all rooms are clean.

Step 6: stop the process.

Initialize state: { "A": Unknown, "B": Unknown, "C": Unknown, "D": Unknown }

path = [ "A", "B", "C", "D" ] current\_index = index of starting room.

function VacuumAgent [location, status]:  
state [location] = status

{ status == "Dirty";  
else ... } ...

if all room in state are "clean",  
return "Do Nothing".  
if current\_index < 3:  
    current\_index += 1  
    return "Move Right"  
else if current\_index > 0  
    current\_index -= 1  
    return "Move Left".

Code:

```
Tic - Tac - Toe Game
def print_board(board):
    for row in board:
        print(" | ".join(row))
        print("-" * 9)

def check_winner(board, player):
    # Check rows, columns and diagonals
    for i in range(3):
        if all([cell == player for cell in board[i]]) or \
            all([board[j][i] == player for j in range(3)]):
            return True

        if all([board[i][i] == player for i in range(3)]) or \
            all([board[i][2 - i] == player for i in range(3)]):
            return True

    return False

def is_full(board):
    return all(cell in ['X', 'O'] for row in board for cell in row)

def get_move(player):
    while True:
        try:
            move = input(f'Player {player}, enter your move (row and column: 1 1): ')
            row, col = map(int, move.split())
            if row in [1, 2, 3] and col in [1, 2, 3]:
                return row - 1, col - 1
            else:
                print("Invalid input. Enter numbers between 1 and 3.")
        except ValueError:
            print("Invalid input. Enter two numbers separated by space.")

def play_game():
    board = [[" " for _ in range(3)] for _ in range(3)]
    current_player = "X"

    while True:
        print_board(board)
        row, col = get_move(current_player)
```

```
if board[row][col] != " ":
    print("That spot is taken. Try again.")
    continue

board[row][col] = current_player

if check_winner(board, current_player):
    print_board(board)
    print(f"Player {current_player} wins!")
    break

if is_full(board):
    print_board(board)
    print("It's a draw!")
    break

current_player = "O" if current_player == "X" else "X"

if __name__ == "__main__":
    play_game()
```

Output:

```
| |
-----
| |
-----
| |
-----
Player X, enter your move (row and column: 1 1): 1 1
X | |
-----
| |
-----
| |
-----
Player O, enter your move (row and column: 1 1): 1 2
X | O |
-----
| |
-----
| |
-----
Player X, enter your move (row and column: 1 1): 1 3
X | O | X
-----
| |
-----
| |
-----
Player O, enter your move (row and column: 1 1): 2 2
X | O | X
-----
| O |
-----
| |
-----
Player X, enter your move (row and column: 1 1): 3 3
X | O | X
-----
| O |
-----
| | X
-----
Player O, enter your move (row and column: 1 1): 3 1
X | O | X
-----
| O |
-----
O |   | X
-----
Player X, enter your move (row and column: 1 1): 2 3
X | O | X
-----
| O | X
-----
O |   | X
-----
Player X wins!
```

Vacuum Cleaner

```
def vacuum_simulation():
    cost = 0

    # Get initial states and location
    state_A = int(input("Enter state of A (0 for clean, 1 for dirty): "))
    state_B = int(input("Enter state of B (0 for clean, 1 for dirty): "))
    location = input("Enter location (A or B): ").upper()

    # Vacuum operation loop
    while True:
        if location == 'A':
            if state_A == 1:
                print("Cleaning A.")
                state_A = 0
                cost += 1
            elif state_B == 1:
                print("Moving vacuum right")
                location = 'B'
                cost += 1
            else:
                print("Turning vacuum off")
                break
        elif location == 'B':
            if state_B == 1:
                print("Cleaning B.")
                state_B = 0
                cost += 1
```

```
elif state_A == 1:  
    print("Moving vacuum left")  
    location = 'A'  
    cost += 1  
  
else:  
    print("Turning vacuum off")  
    break  
  
print(f"Cost: {cost}")  
print(f"{{'A': {state_A}, 'B': {state_B}}}")
```

```
vacuum_simulation()
```

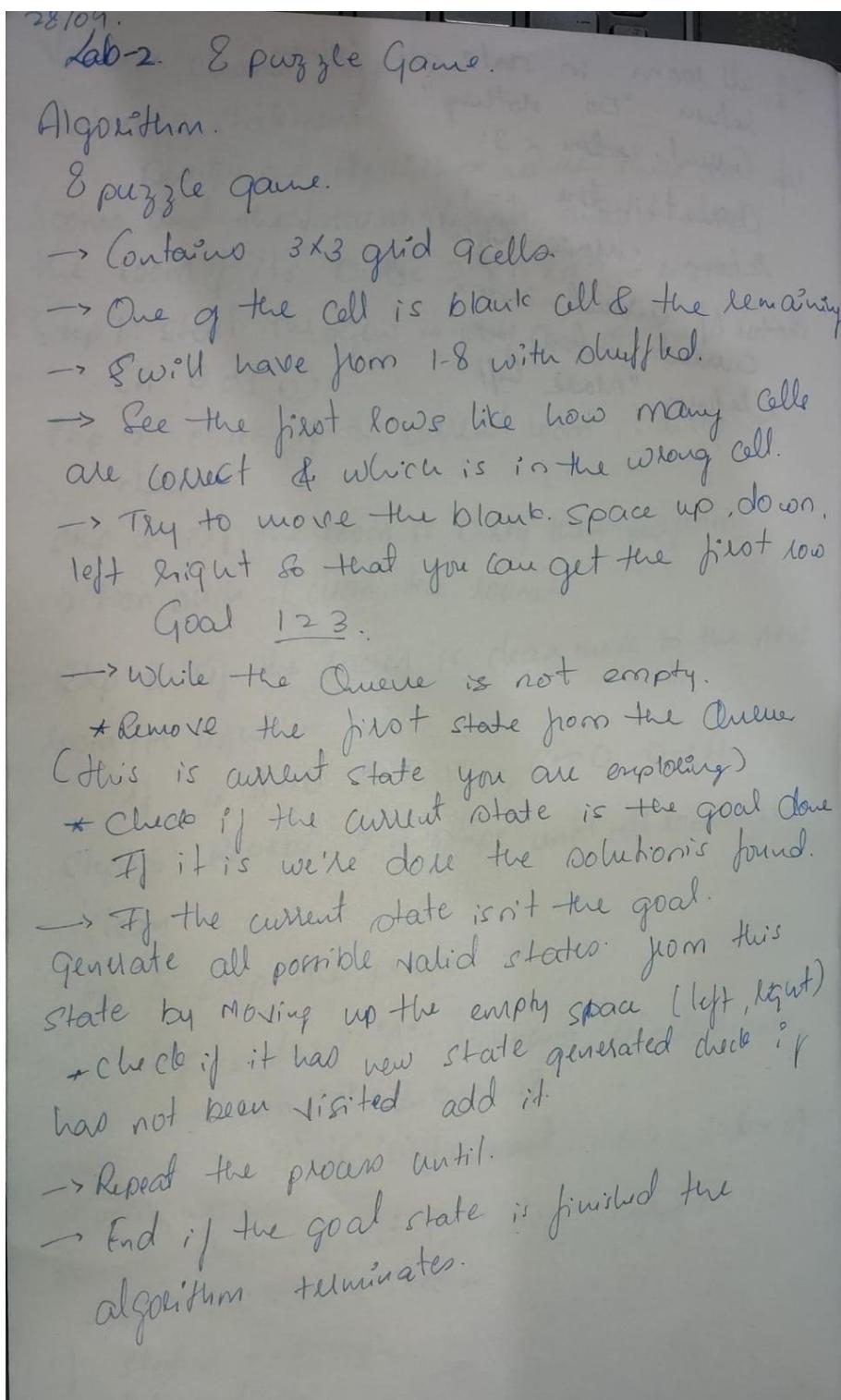
OUTPUT

```
Enter state of A (0 for clean, 1 for dirty): 1  
Enter state of B (0 for clean, 1 for dirty): 0  
Enter location (A or B): A  
Cleaning A.  
Turning vacuum off  
Cost: 1  
{'A': 0, 'B': 0}
```

## Program 2

Implement 8 puzzle problems using Depth First Search (DFS)  
Implement Iterative deepening search algorithm

Algorithm:



Initial state

1 2 3

4 0 6

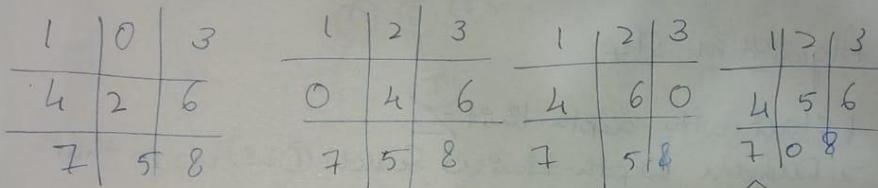
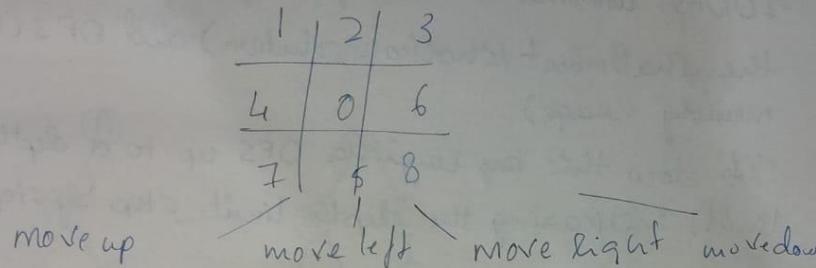
7 5 8

goal state

1 2 3

4 5 6

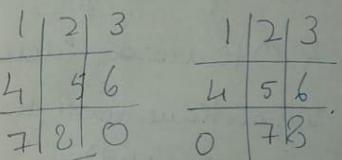
7 8 0.



Best: When the puzzle can be solved in minimal

Steps  $\rightarrow$  no. of moves  $\rightarrow$  Best case

move up



Worst: 150 move when the

input matrix.  $\begin{bmatrix} 8 & 6 & 7 \\ 2 & 5 & 4 \\ 3 & 0 & 1 \end{bmatrix}$

Average:

$\begin{bmatrix} 2 & 8 & 3 \\ 1 & 6 & 4 \\ 2 & 0 & 5 \end{bmatrix} \rightarrow 65$  moves

Lab-3.

IDDFS Algorithm.

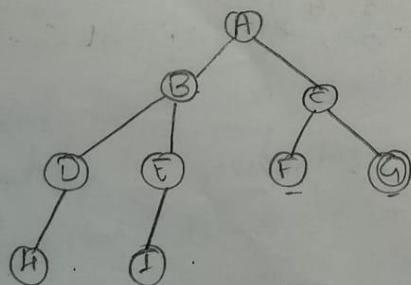
Iterative Deepening Depth First Search.

IDDFS combines the benefits of BFS (finds the shallowest/shortest solution) and DFS (low memory usage).

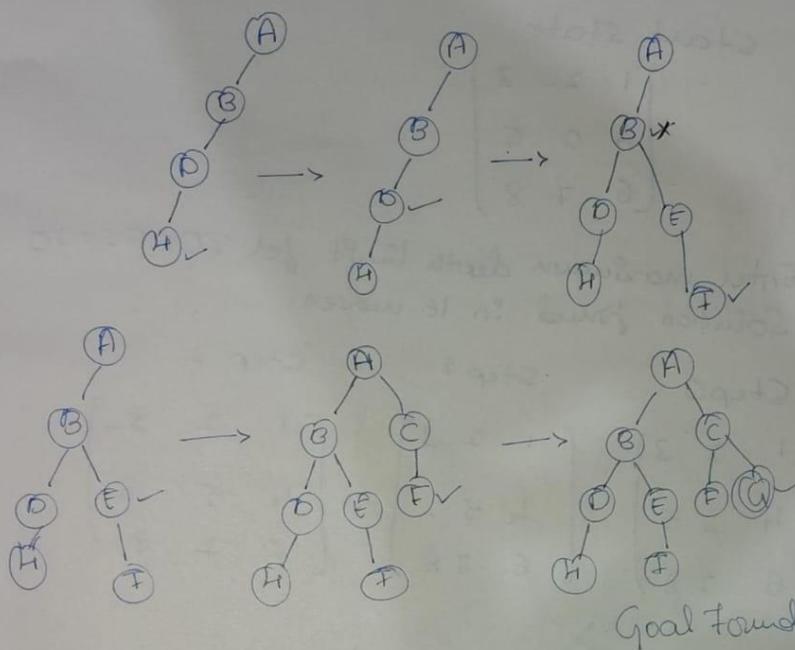
It does this by running DFS up to a depth limit, increasing the depth limit step by step.

Algorithm Step

1. Start with depth limit = 0.
2. Perform Depth-Limited Search (DLS) up to that depth.
3. If the goal is found  $\rightarrow$  stop.
4. Otherwise, increase the depth limit and repeat.
5. Continue until the goal is found (all nodes are explored).

Example.

Max depth = 3



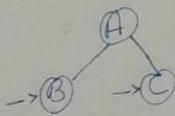
Path → H O I E F G X

Depth 0:



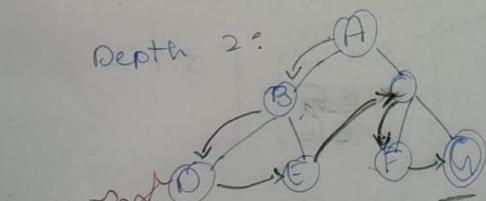
A

Depth 1:



A  
B C

Depth 2:



A  
B C  
D E F G

Goal Found.

~~S purple~~  
O/P Jem

Start State

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 0 & 6 \\ 7 & 5 & 8 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 3 \\ 4 & 2 & 6 \\ 7 & 5 & 8 \end{bmatrix} \quad \begin{bmatrix} 1 & 2 & 3 \\ 0 & 4 & 6 \\ 7 & 5 & 8 \end{bmatrix} \quad \begin{bmatrix} 1 & 2 & 3 \\ 4 & 6 & 0 \\ 7 & 5 & 8 \end{bmatrix} \quad \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 0 & 8 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 0 & 8 & 0 \end{bmatrix} \quad \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 0 & 7 & 8 \end{bmatrix} \quad \begin{bmatrix} 1 & 2 & 3 \\ 4 & 0 & 6 \\ 7 & 5 & 8 \end{bmatrix}$$

~~Q~~

Code:

```
Usig DFS 8 puzzel without heuristic
# Goal state
goal = ((1, 2, 3),
         (8, 0, 4),
         (7, 6, 5))

# Moves: Up, Down, Left, Right
moves = [(-1, 0), (1, 0), (0, -1), (0, 1)]

def get_neighbors(state):
    # Find the empty tile (0)
    for i in range(3):
        for j in range(3):
            if state[i][j] == 0:
                x, y = i, j
                break

    neighbors = []
    for dx, dy in moves:
        nx, ny = x + dx, y + dy
        if 0 <= nx < 3 and 0 <= ny < 3:
            # Swap empty tile with adjacent tile
            new_state = [list(row) for row in state]
            new_state[x][y], new_state[nx][ny] = new_state[nx][ny], new_state[x][y]
            neighbors.append(tuple(tuple(row) for row in new_state))
    return neighbors

def dfs_limited(start, depth_limit):
    stack = [(start, [start])]
    visited = set([start])

    while stack:
        current, path = stack.pop()

        if current == goal:
            return path

        if len(path) - 1 >= depth_limit: # already reached depth limit
            continue

        for neighbor in get_neighbors(current):
            if neighbor not in visited:
                visited.add(neighbor)
                stack.append((neighbor, path + [neighbor]))

    return None
```

```

# Example start state
start = ((2, 8, 3),
          (1, 6, 4),
          (7, 0, 5))

solution_path = dfs_limited(start, depth_limit=5)

if solution_path:
    print(f"Solution found in {len(solution_path) - 1} moves:")
    for state in solution_path:
        for row in state:
            print(row)
        print()
else:
    print("No solution found within 5 moves.")

```

## OUTPUT

```

Solution found in 5 moves:
(2, 8, 3)
(1, 6, 4)
(7, 0, 5)

(2, 8, 3)
(1, 0, 4)
(7, 6, 5)

(2, 0, 3)
(1, 8, 4)
(7, 6, 5)

(0, 2, 3)
(1, 8, 4)
(7, 6, 5)

(1, 2, 3)
(0, 8, 4)
(7, 6, 5)

(1, 2, 3)
(8, 0, 4)
(7, 6, 5)

```

Iterative Deepening Search(IDS) or Iterative Deepening Depth First Search(IDDFS)

```
from copy import deepcopy
GOAL_STATE = [
    [1, 2, 3],
    [4, 5, 0],
    [6, 7, 8]
]

# Possible moves of the blank (0) tile: up, down, left, right
MOVES = [(-1, 0), (1, 0), (0, -1), (0, 1)]

def find_blank(state):
    for i in range(3):
        for j in range(3):
            if state[i][j] == 0:
                return i, j

def is_goal(state):
    return state == GOAL_STATE

def get_neighbors(state):
    neighbors = []
    x, y = find_blank(state)

    for dx, dy in MOVES:
        nx, ny = x + dx, y + dy
        if 0 <= nx < 3 and 0 <= ny < 3:
            new_state = deepcopy(state)
            # Swap blank with neighbor
            new_state[x][y], new_state[nx][ny] = new_state[nx][ny], new_state[x][y]
            neighbors.append(new_state)

    return neighbors
```

```

neighbors.append(new_state)

return neighbors

def dfs(state, depth, limit, path, visited):
    if is_goal(state):
        return path + [state]
    if depth == limit:
        return None

    for neighbor in get_neighbors(state):
        # To avoid cycles, do not revisit states in current path
        if neighbor not in visited:
            result = dfs(neighbor, depth + 1, limit, path + [state], visited + [neighbor])
            if result is not None:
                return result
    return None

def iterative_deepening_search(initial_state, max_depth=50):
    for depth_limit in range(max_depth):
        print(f"Searching with depth limit = {depth_limit}")
        result = dfs(initial_state, 0, depth_limit, [], [initial_state])
        if result is not None:
            return result
    return None

def print_state(state):
    for row in state:
        print(' '.join(str(x) for x in row))
    print()

```

```

if __name__ == "__main__":
    initial_state = [
        [1, 2, 3],
        [4, 0, 5],
        [6, 7, 8]
    ]

    solution = iterative_deepening_search(initial_state)

    if solution:
        print(f"Solution found in {len(solution)-1} moves!")
        for step, state in enumerate(solution):
            print(f"Step {step}:")
            print_state(state)
    else:
        print("No solution found.")

```

## OUTPUT

```

Searching with depth limit = 0
Searching with depth limit = 1
Solution found in 1 moves!
Step 0:
1 2 3
4 0 5
6 7 8

Step 1:
1 2 3
4 5 0
6 7 8

```

### Program 3

Implement A\* search algorithm

Algorithm:

=> A\* using 8 puzzle.

```

A-star(start, goal):
    open-set = {start}
    g-score[start] = 0
    f-score[start] = heuristic(start, goal)

    while open-set is not empty:
        current = node in open-set with
        lowest f-score
        if current == goal:
            return reconstruct_path(current)
        open-set.remove(current)

        for each neighbor of current:
            tentative_g-score = g-score[current]
            + distance(current, neighbor)
            if tentative_g-score < g-score[
                neighbor]:
                came-from[neighbor] = current
                g-score[neighbor] = current
                g-score[neighbor] = tentative_g-
                score
                f-score[neighbor] = tentative_g-
                score + heuristic(current, goal)
                if neighbor not in open-set:
                    open-set.add(neighbor)
    return failure

```

Output:-  
Solution path.

Initial

$$\begin{bmatrix} 1 & 2 & 3 \\ 0 & 4 & 6 \\ 7 & 5 & 8 \end{bmatrix}$$

①

$$\begin{bmatrix} 1 & 2 & 3 \\ 0 & 4 & 6 \\ 7 & 5 & 8 \end{bmatrix}$$

②

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 0 & 6 \\ 7 & 5 & 8 \end{bmatrix}$$

③

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 0 & 8 \end{bmatrix}$$

④

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 0 \end{bmatrix}$$

Solved in 3 moves

Code:  
Misplace Tiles  
import heapq

```
# Goal state
goal = ((1, 2, 3),
         (8, 0, 4),
         (7, 6, 5))

# Moves: Up, Down, Left, Right
moves = [(-1, 0), (1, 0), (0, -1), (0, 1)]
```

```
# Heuristic: Misplaced tiles
def misplaced_tiles(state):
    count = 0
    for i in range(3):
        for j in range(3):
            if state[i][j] != 0 and state[i][j] != goal[i][j]:
                count += 1
    return count
```

```
# Find blank position (0)
def find_blank(state):
    for i in range(3):
        for j in range(3):
            if state[i][j] == 0:
                return i, j

# Generate neighbors
def get_neighbors(state):
    neighbors = []
    x, y = find_blank(state)
```

```

for dx, dy in moves:
    nx, ny = x + dx, y + dy
    if 0 <= nx < 3 and 0 <= ny < 3:
        new_state = [list(row) for row in state]
        new_state[x][y], new_state[nx][ny] = new_state[nx][ny], new_state[x][y]
        neighbors.append(tuple(tuple(row) for row in new_state))
    return neighbors

# A* Search

def astar(start):
    pq = []
    heapq.heappush(pq, (misplaced_tiles(start), 0, start, []))
    visited = set()

    while pq:
        f, g, state, path = heapq.heappop(pq)
        if state == goal:
            return path + [state]
        if state in visited:
            continue
        visited.add(state)
        for neighbor in get_neighbors(state):
            if neighbor not in visited:
                new_g = g + 1
                new_f = new_g + misplaced_tiles(neighbor)
                heapq.heappush(pq, (new_f, new_g, neighbor, path + [state]))

    return None

# Example usage

```

```
start_state = ((2, 8, 3),  
              (1, 6, 4),  
              (7, 0, 5))
```

```
solution = astar(start_state)
```

```
# Print solution path
```

```
for step in solution:
```

```
    for row in step:
```

```
        print(row)
```

```
        print("-----")
```

OUTPUT

```
(2, 8, 3)  
(1, 6, 4)  
(7, 0, 5)  
-----  
(2, 8, 3)  
(1, 0, 4)  
(7, 6, 5)  
-----  
(2, 0, 3)  
(1, 8, 4)  
(7, 6, 5)  
-----  
(0, 2, 3)  
(1, 8, 4)  
(7, 6, 5)  
-----  
(1, 2, 3)  
(0, 8, 4)  
(7, 6, 5)  
-----  
(1, 2, 3)  
(8, 0, 4)  
(7, 6, 5)  
-----
```

Manhattan:

```
import heapq

goal = ((1, 2, 3),
        (8, 0, 4),
        (7, 6, 5))

moves = [(-1, 0), (1, 0), (0, -1), (0, 1)] # Up, Down, Left, Right

def manhattan_distance(state):
    distance = 0
    for i in range(3):
        for j in range(3):
            value = state[i][j]
            if value != 0:
                # goal position of this tile
                goal_x = (value - 1) // 3
                goal_y = (value - 1) % 3
                distance += abs(i - goal_x) + abs(j - goal_y)
    return distance

def find_blank(state):
    for i in range(3):
        for j in range(3):
            if state[i][j] == 0:
                return i, j

def get_neighbors(state):
    neighbors = []
    x, y = find_blank(state)
    for dx, dy in moves:
        nx, ny = x + dx, y + dy
        if 0 <= nx < 3 and 0 <= ny < 3:
            new_state = [list(row) for row in state]
```

```

new_state[x][y], new_state[nx][ny] = new_state[nx][ny], new_state[x][y]
neighbors.append(tuple(tuple(row) for row in new_state))

return neighbors

def astar(start):
    pq = []
    heapq.heappush(pq, (manhattan_distance(start), 0, start, [])) # (f, g, state, path)
    visited = set()
    while pq:
        f, g, state, path = heapq.heappop(pq)
        if state == goal:
            return path + [state]
        if state in visited:
            continue
        visited.add(state)
        for neighbor in get_neighbors(state):
            if neighbor not in visited:
                new_g = g + 1
                new_f = new_g + manhattan_distance(neighbor)
                heapq.heappush(pq, (new_f, new_g, neighbor, path + [state]))

    return None

start_state = ((2, 8, 3),
               (1, 6, 4),
               (7, 0, 5))
solution = astar(start_state)

if solution is None:
    print("No solution found.")
else:
    print("Solution path:")

```

```
for step in solution:
```

```
    for row in step:
```

```
        print(row)
```

```
        print("-----")
```

OUTPUT:

```
Solution path:
```

```
(2, 8, 3)
```

```
(1, 6, 4)
```

```
(7, 0, 5)
```

```
-----
```

```
(2, 8, 3)
```

```
(1, 0, 4)
```

```
(7, 6, 5)
```

```
-----
```

```
(2, 0, 3)
```

```
(1, 8, 4)
```

```
(7, 6, 5)
```

```
-----
```

```
(0, 2, 3)
```

```
(1, 8, 4)
```

```
(7, 6, 5)
```

```
-----
```

```
(1, 2, 3)
```

```
(0, 8, 4)
```

```
(7, 6, 5)
```

```
-----
```

```
(1, 2, 3)
```

```
(8, 0, 4)
```

```
(7, 6, 5)
```

```
-----
```

## Program 4

Implement Hill Climbing search algorithm to solve N-Queens problem

Algorithm:

9/10/2025

① Hill Climbing: - iteratively moves from a starting solution to a better neighboring solution until no further improvement can be made.

1. Start: Begin with an initial solution.
2. Evaluate Neighbors: Evaluate all the neighboring solutions to the current solution.
3. Choose Best Neighbor: Select the neighbor that provides the greatest improvement.
4. Move: Move to the chosen best neighbor making towards a better  $\chi$  if the new current solution.
5. Repeat: Continue 2-4 steps, always moving towards a better state.
6. Stop: The algorithm stops when it reaches a point where no neighbor offers a better value, indicating a local maximum.

② Pseudocode:

```
FUNCTION HillClimbing(problem):
    current_state = INITIAL_STATE(problem)
    Loop Forever:
        neighbors = GENERATE_NEIGHBORS
                    (current_state)
        IF neighbors is empty:
            RETURN current_state.
        best_neighbor = SELECT_BEST_NEIGH
                        -BOR(neighbors,
                            current_state, problem.EVALUATE_FUNC)
```

IF EVALUATE (best-neighbor)

RETURN current-state

current-state = best-neighbor

→ Output for N-Queens using  
Hill climbing

Initial state (Step 0):

Q ... .

Q ... .

Q ... .

Q ... .

①

. Q ..	.. Q ..	.. Q ..	.. Q ..	... Q ..
Q .. .	Q .. .	Q .. .	Q .. .	Q .. .
Q .. .	Q .. .	Q .. .	Q .. .	Q .. .
Q .. .	Q .. .	Q .. .	Q .. .	Q .. .

②

Q ... .	Q ... .	Q ... .	Q ... .	... Q ..
. Q .. .	Q .. .			
Q .. .				
Q .. .				

Selected

③ Q... Q... Q... Q...  
Q... Q... Q... Q...  
Q... Q... Q... Q...  
Q... Q... Q... Q...  
Q... Q... Q... Q... Q

④ Q... Q... Q... Q...  
Q... Q... Q... Q...  
Q... Q... Q... Q...  
Q... Q... Q... Q...  
Q... Q... Q... Q... Q

Step 1.

① Q... Q... Q... Q...  
Q... Q... Q... Q...  
Q... Q... Q... Q...  
Q... Q... Q... Q...  
Q... Q... Q... Q... *Method*

② Q... Q... Q... Q...  
Q... Q... Q... Q...  
Q... Q... Q... Q...  
Q... Q... Q... Q...  
Q... Q... Q... Q...

③ Q... Q... Q... Q...  
Q... Q... Q... Q...  
Q... Q... Q... Q...  
Q... Q... Q... Q... Q

Step 2

① Q... Q... Q... Q...  
Q... Q... Q... Q...  
Q... Q... Q... Q...  
Q... Q... Q... Q...  
Q... Q... Q... Q...

② Q... Q... Q... Q...  
Q... Q... Q... Q...  
Q... Q... Q... Q...  
Q... Q... Q... Q... *Best Solution* ~~Q~~

Code:

```
import random
```

```
def compute_cost(state):
    n = len(state)
    cost = 0
    for i in range(n):
        for j in range(i + 1, n):
            if state[i] == state[j]:          # same row
                cost += 1
            elif abs(state[i] - state[j]) == abs(i - j): # same diagonal
                cost += 1
    return cost
```

```
def get_neighbors(state):
    neighbors = []
    n = len(state)
    for col in range(n):      # pick a column
        for row in range(n):  # try moving queen in this column to another row
            if row != state[col]:
                new_state = state.copy()
                new_state[col] = row
                neighbors.append(new_state)
    return neighbors
```

```
def print_board(state):
```

```
    n = len(state)
```

```

for r in range(n):
    line = ""
    for c in range(n):
        line += "Q " if state[c] == r else ". "
    print(line)
print("")

def hill_climb(initial_state, max_sideways=50):
    current = initial_state
    current_cost = compute_cost(current)
    steps = 0
    sideways_moves = 0

    print("Initial State (cost={}):".format(current_cost))
    print_board(current)

    while True:
        neighbors = get_neighbors(current)
        costs = [compute_cost(n) for n in neighbors]
        min_cost = min(costs)

        if min_cost > current_cost:
            # no better neighbor -> stop
            break

        # pick one of the best neighbors randomly
        best_neighbors = [n for n, c in zip(neighbors, costs) if c == min_cost]
        next_state = random.choice(best_neighbors)
        next_cost = compute_cost(next_state)

```

```

# handle sideways moves

if next_cost == current_cost:
    if sideways_moves >= max_sideways:
        break
    else:
        sideways_moves += 1
else:
    sideways_moves = 0

current = next_state
current_cost = next_cost
steps += 1

print("Step {} (cost={}):".format(steps, current_cost))
print_board(current)

if current_cost == 0:
    print("Solution found in {} steps ✅".format(steps))
    return current

print("Local minimum reached (cost={}) ❌".format(current_cost))
return current

initial_state = [3, 1, 2, 0]

final = hill_climb(initial_state, max_sideways=10)

```

OUTPUT:

```
Initial State (cost=2):
```

```
. . . Q  
. Q . .  
. . Q .  
Q . . .
```

```
Step 1 (cost=2):
```

```
. . . Q  
Q Q . .  
. . Q .  
. . . .
```

```
Step 2 (cost=1):
```

```
. . . Q  
Q . . .  
. . Q .  
. Q . .
```

```
Step 3 (cost=1):
```

```
. . Q Q  
Q . . .  
. . . .  
. Q . .
```

```
Step 4 (cost=0):
```

```
. . Q .  
Q . . .  
. . . Q  
. Q . .
```

```
Solution found in 4 steps ✓
```

## Program 5

## Simulated Annealing to Solve 8-Queens problem

Algorithm:

② Simulated Annealing  
 $\Rightarrow$  finds a near-optimal solution by iteratively exploring the solution space.

Pseudocode:-

```

Function SimulatedAnnealing(initial_solution,
initial_temperature, cooling_rate, termination_criteria)
    current_solution = initial_solution
    current_energy = Energy(current_solution)
    best_solution = current_solution
    best_energy = current_energy
    temperature = initial_temperature

    while |TerminationCondition(temperature,
termination_criteria)|

        neighbor_solution = GenerateNeighbor(
            current_solution)

        neighbor_energy = Energy(neighbor_solution)
        // change in energy
        delta_energy = neighbor_energy - current_energy

        if delta_energy < 0 or random() < exp(-delta_energy / temperature)
            current_solution = neighbor_solution
    end
end

```

```
    Current-energy = neighbor-energy  
    if Current-energy < best-energy.  
        best-solution = current-solution  
        best-energy = current-energy  
    end if  
end if  
temperature = temperature * cooling_rate.  
end while.  
return bestSolution.  
End Function
```



Code:

```
from scipy.optimize import dual_annealing
import numpy as np

def queens_max(x):
    cols = np.round(x).astype(int)
    n = len(cols)

    if len(set(cols)) < n:
        return 1e6

    attacks = 0

    for i in range(n):
        for j in range(i + 1, n):
            if abs(i - j) == abs(cols[i] - cols[j]):
                attacks += 1

    return attacks

n = 8
bounds = [(0, n - 1)] * n
result = dual_annealing(queens_max, bounds)

best_cols = np.round(result.x).astype(int).tolist()
not_attacking = n

print(f"The best position found is: {best_cols}")
print(f"The number of queens that are not attacking each other is: {not_attacking}")
```

OUTPUT:

```
The best position found is: [7, 4, 6, 1, 3, 5, 0, 2]
The number of queens that are not attacking each other is: 8
```

## Program 6

Create a knowledge base using propositional logic and show that the given query entails the knowledge base or not.

Algorithm:

→  
16.10.25.

Consider a knowledge base  $KB$  that contains the following  $PL$  [x]

Q. Create a knowledge base using propositional logic and show that the given query entails the knowledge base or not.

⇒ Truth-table enumeration algorithm for deciding propositional entailment.

Pseudocode:

```
function TT-Entails?(KB, α) returns true or false
    inputs: KB, the knowledge base, a sentence in propositional logic
            α, the query, a sentence in propositional logic
    Symbols ← a list of the proposition symbols in KB
    and α.
    return TT-Check-All(KB, α, Symbols, {})

function TT-Check-All(KB, α, Symbols, model) returns
    true or false
    if Empty?(Symbols) then
        if PL-True?(KB, model) then return PL-True?
            (α, model).
        else return true // when KB is false, always
            return true.
    else do
        p ← first(Symbols)
        Rest ← Rest(Symbols)
        return TT-Check-All(KB, α, rest, model ∪ {p =
            true?})
        and.
        TT-Check-All(KB, α, rest, model ∪
            {p = false?}).
```

Q2. Consider a knowledge base KB that contains the following propositional logic sentences:

$$\left. \begin{array}{l} Q \rightarrow P \\ P \rightarrow \neg Q \\ Q \vee R \end{array} \right\}$$

i) Construct a truth table that shows the truth value of each sentence in KB and indicate the models in which the KB is true.

$$KB = (Q \rightarrow P, P \rightarrow \neg Q, Q \vee R)$$

P	Q	R	$Q \rightarrow P$	$P \rightarrow \neg Q$	$Q \vee R$	KB
false	false	false	true	false	false	
false	false	true	true	false	true	
false	true	false	false	true	true	
false	true	true	false	false	true	
true	false	false	false	false	true	
true	false	true	false	false	true	
true	true	false	true	true	true	
true	true	true	true	true	true	

Annotations below the table:

- $T \wedge F = F$
- $T \vee F = T$
- $T \wedge T = T$
- $T \vee T = T$
- $F \wedge F = F$
- $F \vee F = F$
- $F \wedge T = F$
- $F \vee T = T$

P	Q	R	$Q \rightarrow P$	$P \rightarrow \neg Q$	$Q \vee R$	KB
F	F	T	T	F	F	✓
F	F	T	T	T	T	
F	T	F	F	T	T	
F	T	T	F	F	T	
T	F	E	F	T	F	✓
T	F	T	F	T	T	
T	E	F	F	F	T	
T	E	T	F	T	T	
(T, F)	F	T	T	F	T	
(T, F)	T	T	F	T	T	

$\Rightarrow$  KB is true when the conditions are

$$\begin{array}{lll} P = \text{false} & Q = \text{false} & R = \text{true} \\ P = \text{true} & Q = \text{false} & R = \text{true} \end{array}$$

(ii) Does KB entail R?

$$KB = \{Q \rightarrow P, P \rightarrow \neg Q, Q \vee R\}.$$

$$\alpha = R.$$

KB is true when.  $P=F, Q=F, R=T$ .

and  $P=T, Q=F, R=T$ .

in both case  $R=True$ .

$\therefore KB$  entails R

(iii) Does KB entail  $R \rightarrow P$ ?

$$KB = \{Q \rightarrow P, P \rightarrow \neg Q, Q \vee R\}.$$

$$\alpha = R \rightarrow P ?$$

KB is true when

$$P=T, Q=F, R=T.$$

$$P=F, Q=F, R=T.$$

$$R \rightarrow P$$

$$KB$$

$$T$$

$$\checkmark$$

$$F$$

$\therefore KB$  does not entail  $R \rightarrow P$ .

(iv) Does KB entail  $Q \rightarrow R$ ?

$$KB = \{Q \rightarrow P, P \rightarrow \neg Q, Q \vee R\}.$$

$$\alpha = Q \rightarrow R.$$

KB is true when

$$P=T, Q=F, R=T.$$

$$P=F, Q=P, R=T.$$

$$Q \rightarrow R.$$

$$T$$

$$\cancel{T}$$

In both condition  $Q \rightarrow R$  is T.

$\therefore KB$  entails  $Q \rightarrow R$ .

P	Q	R	KB	$KB \Rightarrow R$	$KB \Rightarrow R \rightarrow P$	$KB \Rightarrow Q \rightarrow R$
F	F	P	F			
F	F	T	T	True	False	True
F	T	F	F			
F	T	T	F	True	True	True
T	F	F	T			
T	F	T	F			
T	T	F	P			
T	T	T	P			

Q1

$$KB = (A \vee C) \wedge (B \vee \neg C)$$

$$\alpha = A \vee B.$$

A	B	C	$A \vee C$	$B \vee \neg C$	$KB$	$\alpha$
F	F	F	F	T	F	F
F	T	F	F	T	F	F
T	T	T	T	T	T	T
T	F	E	T	T	T	T
T	E	T	T	F	F	F
T	T	F	T	T	T	T
T	T	T	F	T	T	T

✓  
V1 v2 ✓  
Qer

Code:

```
import itertools
```

```
from sympy import symbols, sympify
```

```
A, B, C = symbols('A B C')
```

```
alpha_input = input("Enter alpha (example: A | B): ")
```

```
kb_input = input("Enter KB (example: (A | C) & (B | ~C)): ")
```

```
alpha = sympify(alpha_input, evaluate=False)
```

```
kb = sympify(kb_input, evaluate=False)
```

```
GREEN = "\033[92m"
```

```
RESET = "\033[0m"
```

```
print(f"\nTruth Table for  $\alpha = \{alpha\_input\}$ , KB = \{kb\_input\}\n")
```

```
print(f"{'A':<6} {'B':<6} {'C':<6} {' $\alpha$ ':<10} {'KB':<10}")
```

```
entailed = True
```

```
for values in itertools.product([False, True], repeat=3):
```

```
    subs = {A: values[0], B: values[1], C: values[2]}
```

```
    alpha_val = alpha.subs(subs)
```

```
    kb_val = kb.subs(subs)
```

```
    alpha_str = f"\033[92m{alpha_val}\033[0m" if kb_val else str(alpha_val)
```

```
    kb_str = f"\033[92m{kb_val}\033[0m" if kb_val else str(kb_val)
```

```
    print(f"\n{str(values[0]):<6} {str(values[1]):<6} {str(values[2]):<6}"
```

```
        f" {alpha_str:<10} {kb_str:<10}")
```

```

if kb_val and not alpha_val:
    entailed = False

if entailed:
    print(f"\n KB |= α holds (KB entails α)\n")
else:
    print(f"\n KB does NOT entail α\n")

```

OUTPUT:

```

Enter alpha (example: A | B): A|B
Enter KB (example: (A | C) & (B | ~C)): (A | C) & (B | ~C)

Truth Table for α = A|B, KB = (A | C) & (B | ~C)

A      B      C      α      KB
False  False  False  False  False
False  False  True   False  False
False  True   False  True   False
False  True   True   True   TrueTrue
True   False  False  True   TrueTrue
True   False  True   True   False
True   True   False  True   TrueTrue
True   True   True   True   TrueTrue

KB |= α holds (KB entails α)

```

## Program 7

Implement unification in first order logic

Algorithm:

50.10.25.

$\Rightarrow$  Unification.

$\Rightarrow$  is the process of making two logical expressions identical by finding suitable values for their variables.

Three conditions in Unification.

Condition 1:

If both conditions are constants:

If they are identical;  
unification succeeds.

If they are different:  
unification fails.

Condition 2:

If expression is a variable and the other is any term: If variable does not occur inside the term.  
Replace the variable with that term  
(Substitution).

Condition 3:

If both expressions are compound term:

The function name must be identical.

The number of arguments must be same.

Then, unify their corresponding arguments  
one by one.

$$① p(f(x), q(y), y)$$

$$p(f(g(z)), q(f(a)), f(a)).$$

$$\Rightarrow f(x) \rightarrow f(g(z)) \rightarrow x = g(z) : \{x/g(z)\}.$$

$$q(y) \rightarrow q(f(a)) \rightarrow y = f(a) : \{y/f(a)\}.$$

$$y \rightarrow f(a). \rightarrow y = f(a) : \{y/f(a)\}$$

2.  $Q(x, f(x))$

$Q(f(y), y)$

$\Rightarrow x \rightarrow f(y) \rightarrow x = f(y) : \{x/f(y)\} \text{ --- } ①$

$f(x) \rightarrow y \rightarrow f(x) = \text{replacing } x \text{ from the } ①$

$\Rightarrow f(f(y)) = y$

= These two expressions cannot be unified.

$\because$  it causes an infinite recursion.

3.  $P(x, g(x))$

$P(g(y)), g(g(z)))$

$\Rightarrow x \rightarrow g(y) \rightarrow x = g(y) : \{x/g(y)\} \text{ --- } ①$

$g(x) \rightarrow g(g(z))$

$\hookrightarrow x = g(z) \text{ --- } ②$

From 1 and 2:

$x = g(y) = g(z) ; y = z$

Substitute  $y = z$  into  $x = g(y)$  to get  $x = g(z)^*$

MGU  
 $\Rightarrow \{x \rightarrow g(z) , y \mapsto z\}$

~~30/11/25~~

Code:

```

def occurs_check(var, expr):
    if var == expr:
        return True
    if isinstance(expr, tuple):
        return any(occurs_check(var, sub) for sub in expr[1:]) # Skip function symbol
    return False

def substitute(expr, subst):
    if isinstance(expr, str):
        # Follow substitution chain until fully resolved
        while expr in subst:
            expr = subst[expr]
        return expr
    # If it's a function term: (f, arg1, arg2, ...)
    return (expr[0],) + tuple(substitute(sub, subst) for sub in expr[1:])

def unify(Y1, Y2, subst=None):
    if subst is None:
        subst = {}
    Y1 = substitute(Y1, subst)
    Y2 = substitute(Y2, subst)

    # Case 1: identical
    if Y1 == Y2:
        return subst

    # Case 2: Y1 is variable
    if isinstance(Y1, str):
        if occurs_check(Y1, Y2):
            return "FAILURE"
        subst[Y1] = Y2
    return subst

```

```

# Case 3: Y2 is variable

if isinstance(Y2, str):
    if occurs_check(Y2, Y1):
        return "FAILURE"
    subst[Y2] = Y1
return subst

# Case 4: function mismatch

if Y1[0] != Y2[0] or len(Y1) != len(Y2):
    return "FAILURE"

# Case 5: unify arguments

for a, b in zip(Y1[1:], Y2[1:]):
    subst = unify(a, b, subst)
    if subst == "FAILURE":
        return "FAILURE"

return subst

expr1 = ("p", "X", ("f", "Y"))
expr2 = ("p", "a", ("f", "b"))

output = unify(expr1, expr2)
print(output)

```

OUTPUT:

```
{'X': 'a', 'Y': 'b'}
```

## Program 8

Create a knowledge base consisting of first order logic statements and prove the given query using forward reasoning.

Algorithm:

6.11'25.

1. Create a know  
Convert a given first order logic statement into Conjunctive Normal Form (CNF)

$\Rightarrow \forall x [\exists y (\neg \text{Animal}(y) \vee \text{Loves}(x, y)) \vee [\exists y \text{Loves}(y, x)]]$

$\Rightarrow$  English meaning. Animal.  
Everyone either loves (someone or something)  
or is loved by someone.

① Simplifying inner negations.

$\neg(\neg \text{Animal}(y) \vee \text{Loves}(x, y)) \equiv$   
 $\neg \neg \text{Animal}(y) \wedge \neg \text{Loves}(x, y)$

So:

$\forall y \neg(\neg \text{Animal}(y) \vee \text{Loves}(x, y)) \equiv$   
 $\forall y (\neg \text{Animal}(y) \wedge \neg \text{Loves}(x, y))$

Then that whole " $\neg \forall y$ " becomes:

$\neg \forall y (\neg \text{Animal}(y) \wedge \neg \text{Loves}(x, y)) \equiv$   
 $\exists y \neg(\neg \text{Animal}(y) \wedge \neg \text{Loves}(x, y))$

Apply De Morgan's law again:

$\neg(\neg \text{Animal}(y) \wedge \neg \text{Loves}(x, y)) \equiv$   
 $\text{Animal}(y) \vee \text{Loves}(x, y)$

So the left part of that formula simplified to:  
 $\exists y (\text{Animal}(y) \vee \text{Loves}(x, y))$ .

② Substitute back into the full formula.

$$\forall x [\exists y (\text{Animal}(y) \vee \text{Loves}(x, y))] \vee [\exists y \text{ Loves}(y, x)]$$

③ Simplify Structure

For every  $x$ : either there exists some  $y$  such that  $y$  is an animal or  $x$  loves  $y$ , or there exists some  $y$  who loves  $x$ .

$$\forall x (\exists y (\text{Animal}(y) \vee \text{Loves}(x, y)) \vee$$

$$\exists y \text{ Loves}(y, x))$$

or equivalently (plurals form):

$$\forall x \exists y \exists z [\text{Animal}(y) \vee \text{Loves}(x, y) \vee$$

$$\vee \text{Loves}(z, x)].$$

1. Bring to plural form.

$$\forall x \exists y \exists z (\text{Animal}(y) \vee \text{Loves}(x, y) \vee \text{Loves}(z, x))$$

2. Skolemize (remove existential quantifiers)

$$\begin{array}{l} y \mapsto f(x) \\ z \mapsto g(x) \end{array}$$

$$\forall x (\text{Animal}(f(x)) \vee \text{Loves}(x, f(x)) \vee$$

$$\text{Loves}(g(x), x))$$

3. Drop universal quantifiers.

$$\text{Animal}(f(x)) \vee \text{Loves}(x, f(x)) \vee$$

$$\text{Loves}(g(x), x).$$

4. Convert to CNF (clauses).

$$\{\text{Animal}(f(x)) \vee \text{Loves}(x, f(x)) \vee$$

$$\text{Loves}(g(x), x).$$

$$(\text{Animal}(f(x)) \vee \text{Loves}(x, f(x)) \vee \text{Loves}(g(x), x))$$

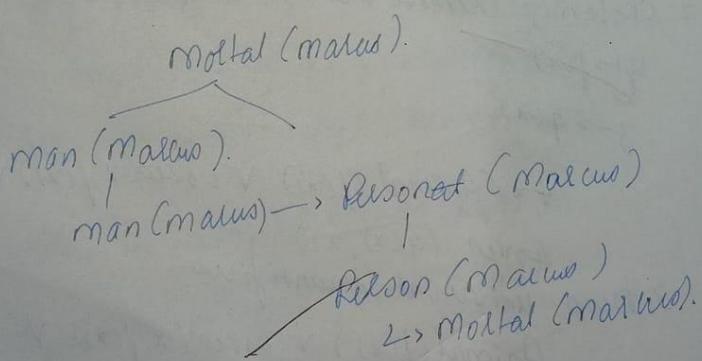
1. Create a knowledge base consisting of first order logic statements and proves the given query using forward reasoning.

Knowledge Base (First-Order Logic statements):

- \*  $\text{Man}(\text{Marcus})$ : Marcus is a man.
- \*  $\text{Pompeian}(\text{Marcus})$ : Marcus is a pompeian.
- \*  $\forall(x) (\text{Pompeian}(x) \rightarrow \text{Roman}(x))$ :  
All Pompeians are Romans.
- \*  $\forall(x) (\text{Roman}(x) \rightarrow \text{Loyal}(x))$ : All Romans are loyal.
- \*  $\forall(x) (\text{Man}(x) \rightarrow \text{Person}(x))$ : All men are persons.
- \*  $\forall(x) (\text{Person}(x) \rightarrow \text{Mortal}(x))$ : All persons are mortal.

Query:

$\text{Mortal}(\text{Marcus})$ : Is Marcus mortal?



$\Rightarrow$  Unification implementation using First Order logic

- Expression 1: ('Loved'; 'x', 'John')

Expression 2: ('Loved', 'Mary', 'y')

Unification Result:

Unified: { 'x': 'Mary', 'y': 'John' }

~~A~~  
False

Code:

```
from collections import deque

class KnowledgeBase:

    def __init__(self):
        self.facts = set()
        self.rules = []
        self.inferred = set()

    def add_fact(self, fact):
        if fact not in self.facts:
            print(f"Adding fact: {fact}")
            self.facts.add(fact)
            return True
        return False

    def add_rule(self, premises, conclusion):
        self.rules.append((premises, conclusion))

    def forward_chain(self):
        agenda = deque(self.facts)

        while agenda:
            fact = agenda.popleft()
            if fact in self.inferred:
                continue
            self.inferred.add(fact)

            for (premises, conclusion) in self.rules:
                if all(p in self.inferred for p in premises):
                    if conclusion not in self.facts:
```

```

print(f"Inferred new fact: {conclusion} from {premises} => {conclusion}")

self.facts.add(conclusion)

agenda.append(conclusion)

```

```

if conclusion == 'Criminal(West)':
    print("\n Goal Reached: West is Criminal")
    return True

```

```
return False
```

```
kb = KnowledgeBase()
```

```

kb.add_fact('American(West)')
kb.add_fact('Enemy(Nono, America)')
kb.add_fact('Missile(M1)')
kb.add_fact('Owns(Nono, M1)')

```

```
kb.add_rule(premises=['Missile(M1)'], conclusion='Weapon(M1)')
```

```
kb.add_rule(premises=['Missile(M1)', 'Owns(Nono, M1)'], conclusion='Sells(West, M1, Nono)')
```

```

kb.add_rule(premises=['Enemy(Nono, America)'], conclusion='Hostile(Nono)')
kb.add_rule(premises=['American(West)', 'Weapon(M1)', 'Sells(West, M1, Nono)', 'Hostile(Nono)'],
            conclusion='Criminal(West)')

```

```
kb.forward_chain()
```

OUTPUT:

```

Adding fact: American(West)
Adding fact: Enemy(Nono, America)
Adding fact: Missile(M1)
Adding fact: Owns(Nono, M1)
Inferred new fact: Weapon(M1) from ['Missile(M1)'] => Weapon(M1)
Inferred new fact: Hostile(Nono) from ['Enemy(Nono, America)'] => Hostile(Nono)
Inferred new fact: Sells(West, M1, Nono) from ['Missile(M1)', 'Owns(Nono, M1)'] => Sells(West, M1, Nono)
Inferred new fact: Criminal(West) from ['American(West)', 'Weapon(M1)', 'Sells(West, M1, Nono)', 'Hostile(Nono)'] => Criminal(West)

 Goal Reached: West is Criminal
True

```

## Program 9

Create a knowledge base consisting of first order logic statements and prove the given query using Resolution

Algorithm:

13.11'25

A Resolution Algorithm.

**Input:** Knowledge base ( $KB$ )  
; Goal ( $G$ )

**Output:** TRUE if  $KB \vdash G$  (proved), otherwise FALSE.

**Steps:**

1. Convert to CNF:
  - Write all statements in predicate logic
  - \* Eliminate  $\rightarrow, \leftrightarrow$ , move  $\neg$  inward;
  - Standardize variables and convert to conjunctive normal form (CNF)
2. Negate the goal
  - \* Add  $\neg G$  to the  $KB$ .

B. Initialize:  
let clauses =  $KB \cup \{\neg G\}$

4. Resolution loop:  
Repeat until contradiction found or no new clauses:
  1. Select two clauses containing completely literals.
  2. Unify variables (find substitution  $O_i$ )  
needed)
  3. Resolve them to form a new clause
  4. If the new clause is empty ( $\perp$ ) →  
Goal is proved.
  5. Add the new clause to the set if it's new.
5. Termination:
  - \* If 1 deleted → success.  $\text{BUT}$
  - ← If no new clauses → failure. See

Code:

```
from itertools import combinations
```

```
def get_clauses():

    n = int(input("Enter number of clauses in Knowledge Base: "))

    clauses = []

    for i in range(n):

        clause = input(f'Enter clause {i+1}: ')

        clause_set = set(clause.replace(" ", "").split("v"))

        clauses.append(clause_set)

    return clauses
```

```
def resolve(ci, cj):

    resolvents = []

    for di in ci:

        for dj in cj:

            if di == ('~' + dj) or dj == ('~' + di):

                new_clause = (ci - {di}) | (cj - {dj})

                resolvents.append(new_clause)

    return resolvents
```

```
def resolution_algorithm(kb, query):

    kb.append(set(['~' + query]))

    derived = []

    clause_id = {frozenset(c): f'C{i+1}' for i, c in enumerate(kb)}
```

```
step = 1

while True:

    new = []

    for (ci, cj) in combinations(kb, 2):
```

```

resolvents = resolve(ci, cj)

for res in resolvents:

    if res not in kb and res not in new:

        cid_i, cid_j = clause_id[frozenset(ci)], clause_id[frozenset(cj)]
        clause_name = f'R{step}'

        derived.append((clause_name, res, cid_i, cid_j))
        clause_id[frozenset(res)] = clause_name
        new.append(res)

        print(f'[Step {step}] {clause_name} = Resolve({cid_i}, {cid_j}) → {res or "{}"}')

        step += 1

# If empty clause found → proof complete

if res == set():

    print("\n✓ Query is proved by resolution (empty clause found).")

    print("\n--- Proof Tree ---")
    print_tree(derived, clause_name)

    return True

if not new:

    print("\n✗ Query cannot be proved by resolution.")

    return False

kb.extend(new)

def print_tree(derived, goal):

    tree = {name: (parents, clause) for name, clause, *parents in [(r[0], r[1], r[2:][0], r[2:][1]) for r in derived]}

def show(node, indent=0):

    if node not in tree:

        print(" " * indent + node)

    return

```

```

parents, clause = tree[node]
print(" " * indent + f'{node}: {set(clause) or "{}"}')
for p in parents:
    show(p, indent + 4)

show(goal)

```

OUPUT:

```

==== FOL Resolution Demo with Proof Tree ====
Enter number of clauses in Knowledge Base: 3
Enter clause 1: P
Enter clause 2: ~P v Q
Enter clause 3: ~Q
Enter query to prove: Q
[Step 1] R1 = Resolve(C1, C2) → {'Q'}
[Step 2] R2 = Resolve(C2, C4) → {'~P'}
[Step 3] R3 = Resolve(C1, R2) → {}

✓ Query is proved by resolution (empty clause found).

--- Proof Tree ---
R3: {}
  C1
    R2: {'~P'}
      C2
        C4
      True

```

## Program 10

Implement Alpha-Beta Pruning.

Algorithm:

Alpha Beta Pruning  
Used in minimax algorithm to reduce no. of nodes evaluated in game trees.

```
function alphabeta (node, depth, α, β, maximizingPlayer);
    if depth == 0 or node is terminal:
        return heuristic(node)
    if maximizingPlayer:
        value = -∞
        for each child of node:
            value = max (value, alphabeta (child,
                depth-1, α, β, false))
            α = max (α, value)
            if α >= β:
                break
        return value
    else:
        value = +∞
        for each child of node:
            value = min (value, alphabeta (child,
                depth-1, α, β, true))
            β = min (β, value)
            if α >= β:
                break
        return value.
```

Output & leaf node values separated by spaces.  
3 5 6 9 1 2 0 7.

Game tree

$$R = 5$$

$$R0 = 5$$

$$R00 = 5$$

$$R000 = 3$$

$$R001 = 5$$

$$R01 = 6 \text{ [PRUNED]}$$

$$R1 = 2 \text{ [PRUNED]}$$

$$R10 = 9$$

$$R100 = 9$$

$$R101 = 1$$

$$R11 = 2$$

$$R110 = 2$$

$$R111 = 0$$

Optimal value at Root: 5.

Code:

class Node:

```
def __init__(self, name):
    self.name = name
    self.children = []
    self.value = None
    self.pruned = False
```

def alpha\_beta(node, depth, maximizing, values, alpha, beta, index):

# Terminal node

if depth == 3:

```
    node.value = values[index[0]]
    index[0] += 1
    return node.value
```

if maximizing:

best = float('-inf')

for i in range(2): # 2 children

```
        child = Node(f'{node.name} {i}')
        node.children.append(child)
```

```
        val = alpha_beta(child, depth + 1, False, values, alpha, beta, index)
```

```
        best = max(best, val)
```

```
        alpha = max(alpha, best)
```

if beta <= alpha:

```
            node.pruned = True
```

```
            break
```

```
    node.value = best
```

```
    return best
```

else:

```
    best = float('inf')
```

```

for i in range(2):
    child = Node(f"{{node.name}} {i}")
    node.children.append(child)
    val = alpha_beta(child, depth + 1, True, values, alpha, beta, index)
    best = min(best, val)
    beta = min(beta, best)
    if beta <= alpha:
        node.pruned = True
        break
    node.value = best
    return best

def print_tree(node, indent=0):
    prune_mark = "[PRUNED]" if node.pruned else ""
    val = f" = {node.value}" if node.value is not None else ""
    print(" " * indent + f"{{node.name}} {val} {prune_mark}")
    for child in node.children:
        print_tree(child, indent + 4)

# --- main ---
print("== Alpha-Beta Pruning with Tree ==")
values = list(map(int, input("Enter 8 leaf node values separated by spaces: ").split()))

root = Node("R")
alpha_beta(root, 0, True, values, float('-inf'), float('inf'), [0])

print("\n--- Game Tree ---")
print_tree(root)

print("\nOptimal Value at Root:", root.value)

```

OUTPUT:

```
--- Alpha-Beta Pruning with Tree ---
Enter 8 leaf node values separated by spaces: 3 5 6 9 1 2 0 7

--- Game Tree ---
R = 5
R0 = 5
R00 = 5
    R000 = 3
    R001 = 5
    R01 = 6 [PRUNED]
        R010 = 6
    R1 = 2 [PRUNED]
        R10 = 9
            R100 = 9
            R101 = 1
        R11 = 2
            R110 = 2
            R111 = 0

Optimal Value at Root: 5
```