

# Propositional Validity Checker

**Task.** Implement a validity checker of propositional formulas in form of  $\varphi \rightarrow \psi$ , where  $\varphi$  and  $\psi$  use  $\wedge$ ,  $\vee$ ,  $\neg$ , and propositional variables.

## Background.

- We can evaluate a formula over variables  $x_1, x_2, \dots, x_n$  given an assignment  $\{x_1 \mapsto v_1, x_2 \mapsto v_2, \dots\}$ .
- We say that formula is unsatisfiable if it evaluates to *false* under all possible assignments.
  - We may try all the assignments one by one to determine satisfiability.
- We say that formula is valid if its negation is unsatisfiable.
  - Therefore,  $\varphi \rightarrow \psi$  is valid when  $\varphi \wedge \neg\psi$  is unsatisfiable, otherwise it is invalid.
  - If the negation evaluates to *true*, the assignment is called a *counterexample* to the validity query.

## Input.

- The checker is given a filename as its only command-line parameter.

```
$ java ValidityChecker definition.txt
```

- The file contains one line. An example of the syntax of the input file `definition.txt`:

```
AND(X, OR(Y, Z)) => AND(X, Y)
```

## Output.

- **Valid.** or **Invalid.** (**Counterexample:** [  $X = \text{true}$ ,  $Y = \text{false}$ , ... ])