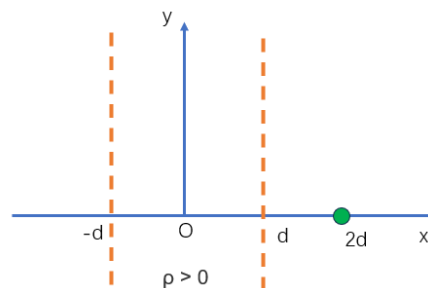


**Problem 1 [?? points]:** As shown in the figure, volumetric charge density,  $\rho > 0$ , is constant in the region  $-d \leq x \leq d$ . And it is vacuum everywhere else (i.e.  $\rho = 0$ ). Now, a point charge  $q$  ( $q < 0$ ), with mass  $m$  is set free from  $x = 2d$ . The initial velocity of the point charge is 0. How long does the charge take to move to  $x = 0$ , considering electric force only?



**Problem 2 [?? points]:** A uniformly charged spherical shell (radius  $R$ ) is located in vacuum and is rotating along one of its symmetric axis (any axis passing through the center of the sphere) at a constant angular velocity  $\omega$ . The shell is uniformly charged with a surface charge density  $\sigma$ .

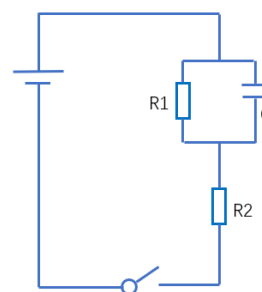
Q1: Find the electric potential energy in space;

Q2: Find the magnetic field  $\mathbf{B}$  along the axis of rotation.

**Problem 3 [?? points]:** As shown in the figure, a circuit is consisted of two resistors  $R_1$  and  $R_2$ , a capacitor and an EMF ( $V_0$ ). The capacitor is made of two circular disks (radius  $b$ ) which are parallelly separated by a distance  $d$ . Initially ( $t = 0$ ), the circuit is closed (switch is on, capacitor is charged), then we switch off the circuit (circuit is open).

Q1: Solve for the current in the circuit as a function of time.

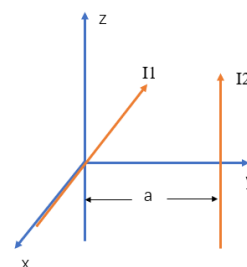
Q2: Find the magnetic field  $\mathbf{B}$  between the plates of the capacitor, as a function of time.



**Problem 4 [?? points]:** Two infinitely long wires are separated with a distance  $a$  in vacuum as shown in the figure. One (with  $I_1$ ) is located along the  $x$  axis, the other one (with  $I_2$ ) is located parallelly to  $z$  axis (in  $yOz$  plane). There exists constant current in each one of them  $I_1$  and  $I_2$ . Now, considering a segment on  $I_2$  from  $z = -l/2$  to  $l/2$  where  $l \ll a$ .

Q1: What is the net force acted by  $I_1$  on this segment of  $I_2$ ;

Q2: What is the net torque acted by  $I_1$  on this segment of  $I_2$ .



**Problem 5 [?? points]:** Calculate the magnetic field at the center of a uniformly charged spherical shell, of radius  $R$  and total charge  $Q$ , spinning at constant angular velocity  $\omega$ .

**Problem 6 [?? points]:** An infinite wire carrying a constant current  $I$  in the  $z$  direction is moving in the  $y$  direction at a constant speed  $v$ . Find the electric field, in the quasistatic approximation, at the instant the wire coincides with the  $z$  axis.

**Problem 7 [?? points]:** Show that the magnetic field is constant ( $\partial \mathbf{B} / \partial t = \mathbf{0}$ ), inside a perfect conductor. (b) Show that the magnetic flux through a perfectly conducting loop is constant. A **superconductor** is a perfect conductor with the additional property that the (constant)  $\mathbf{B}$  inside is in fact *zero*.