

Due: 11:59 pm on December 3, 2024

Problem 1

Part A

Light traveling downward is incident on a horizontal film of thickness d as shown below. The incident ray splits into two rays, A and B . Ray A reflects from the top of the film. Ray B reflects from the bottom of the film and then refracts back into the material that is above the film. If the film has parallel faces, show that rays A and B end up parallel to each other.

Part B

An inside corner of a cube is lined with mirrors to make a corner reflector. A ray of light is reflected successively from each of three mutually perpendicular mirrors. Show that its final direction is always exactly opposite to its initial direction.

Part C

Light is incident normally on the short face of a 30° - 60° - 90° prism (see the figure). A drop of liquid is placed on the hypotenuse of the prism. If the index of refraction of the prism is 1.62, find the maximum index that the liquid may have if the light is to be totally reflected.

Part D

A compact disk (CD) is read from the bottom by a semiconductor laser with wavelength 790 nm passing through a plastic substrate of refractive index 1.8. When the beam encounters a pit, part of the beam is reflected from the pit and part from the flat region between the pits (see the figure), so these two beams interfere with each other. What must the minimum pit depth be so that the part of the beam reflected from a pit cancels the part of the beam reflected from the flat region? (It is this cancellation that allows the player to recognize the beginning and the end of a pit.)

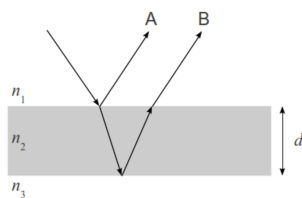


Figure 1: 1A

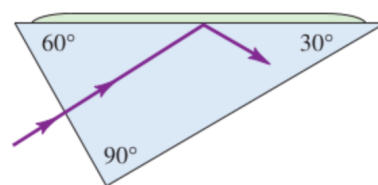


Figure 2: 1C

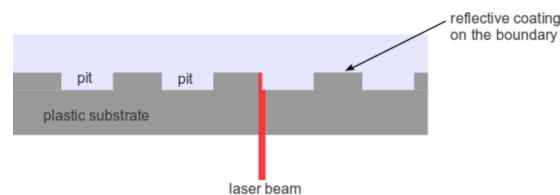


Figure 3: 1D

Problem 2

Part A

We want to rotate the direction of polarization of a beam of linearly polarized light by 90° using one or more polarizing sheets.

1. What is the minimum number of sheets required?
2. What is the minimum number of sheets required if the transmitted intensity is to be more than 60% of the original density?

Part B

For interference of waves from two coherent sources show that the nodal lines and the antinodal lines are families of hyperbolas.

Part C

Consider a two-slit interference experiment, with waves polarized linearly in the same direction, in which the two slits are of different widths. As measured on a distant screen, the amplitude of the wave from the first slit is E , while the amplitude of the wave from the second slit is $2E$.

1. Show that the intensity at any point in the interference pattern is

$$I = I_{\max} \left(\frac{5}{9} + \frac{4}{9} \cos \phi \right)$$

where ϕ is the phase difference between the two waves as measured at a particular point of the screen and I_{\max} is the maximum intensity in the pattern.

2. Graph I versus ϕ . What is the minimum value of intensity, and for which values of ϕ does it occur?

Part D

Consider a two-slit interference pattern, for which the intensity distribution is given by formula $I = I_{\max} \cos^2(\pi dy/\lambda l)$ (for the meaning of the symbols, see the lecture). Let θ_m be the angular position of the m -th bright fringe, where the intensity is I_{\max} . Assume that θ_m is small, so that $\sin \theta_m \approx \theta_m$. Let θ_m^+ and θ_m^- be the two angles on either side of θ_m for which $I = \frac{1}{2} I_{\max}$. The quantity $\Delta \theta_m = |\theta_m^+ - \theta_m^-|$ is the half-width of the m -th fringe. Calculate $\Delta \theta_m$. How does it depend on m ?

Part E

Find the radii of bright Newton's rings in the configuration discussed in the lecture, but this time assume that the lens is of a paraboloidal shape $z = (x^2 + y^2)/\alpha$, where α is a positive constant. $(0, 0, 0)$ is the point of contact of the lens with the surface that it rests on ($z = 0$).