

# Prototypical Cross-domain Self-supervised Learning for Few-shot Unsupervised Domain Adaptation

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## Prototypical Cross-domain Self-supervised Learning for Few-shot Unsupervised Domain Adaptation

### (1) In-domain Prototypical Contrastive Learning

$$\bar{\mathcal{D}}_s = \{(\mathbf{x}_i^s, y_i^s)\}_{i=1}^{N_s} \quad \mathcal{D}_{su} = \{(\mathbf{x}_i^{su})\}_{i=1}^{N_{su}} \quad \mathcal{D}_{tu} = \{(\mathbf{x}_i^{tu})\}_{i=1}^{N_{tu}}$$

Stored vectors,  $\mathbf{V}$

feature encoder  $F$ ,

feature vector  $\mathbf{f}_i^s = F(\mathbf{x}_i^s)$

$\mathbf{v}_i \leftarrow m\mathbf{v}_i + (1 - m)\mathbf{f}_i$

$\mathbf{v}_i$  is the stored feature vector of  $\mathbf{x}_i$

$\mathbf{V}^s = [\mathbf{v}_1^s, \dots, \mathbf{v}_{(N_s+N_{su})}^s]$ ,  $\mathbf{V}^t = [\mathbf{v}_1^t, \dots, \mathbf{v}_{N_{tu}}^t]$

Normalized prototypes

$$\mu_j^s = \frac{\mathbf{u}_j^s}{\|\mathbf{u}_j^s\|} \quad \mathbf{u}_j^s = \frac{1}{|C_j^{(s)}|} \sum_{\mathbf{v}_i^s \in C_j^{(s)}} \mathbf{v}_i^s$$

normalized source prototypes  $\{\mu_j^s\}_{j=1}^k$

target prototypes  $\{\mu_j^t\}_{j=1}^k$

Get cluster by k-means clustering

$$\mathbf{C}^s = \{C_1^{(s)}, C_2^{(s)}, \dots, C_k^{(s)}\}$$

$$P_i^s = [P_{i,1}^s, P_{i,2}^s, \dots, P_{i,k}^s]$$

$$P_{i,j}^s = \frac{\exp(\mu_j^s \cdot \mathbf{f}_i^s / \phi)}{\sum_{r=1}^k \exp(\mu_r^s \cdot \mathbf{f}_i^s / \phi)}$$

$$\mathcal{L}_{PC} = \sum_{i=1}^{N_s+N_{su}} \mathcal{L}_{CE}(P_i^s, c_s(i)) + \sum_{i=1}^{N_{tu}} \mathcal{L}_{CE}(P_i^t, c_t(i))$$

where  $c_s(\cdot)$  and  $c_t(\cdot)$  return the cluster index of the instance

Perform k-means on the samples  $M$  times with different number of cluster

$$\mathcal{L}_{InSelf} = \frac{1}{M} \sum_{m=1}^M \mathcal{L}_{PC}^{(m)} \quad (5)$$

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### (2) Cross-domain Instance-Prototype SSL

$$P_{i,j}^{s \rightarrow t} = \frac{\exp(\mu_j^t \cdot \mathbf{f}_i^s / \tau)}{\sum_{r=1}^k \exp(\mu_r^t \cdot \mathbf{f}_i^s / \tau)} \quad \mathcal{L}_{\text{CrossSelf}} = \sum_{i=1}^{N_s + N_{su}} H(P_i^{s \rightarrow t}) + \sum_{i=1}^{N_{tu}} H(P_i^{t \rightarrow s})$$

### (3) Adaptive Prototypical Classifier Learning

$$\mathcal{L}_{\text{cls}} = \mathbb{E}_{(\mathbf{x}, y) \in \mathcal{D}_s} \mathcal{L}_{CE}(\mathbf{p}(\mathbf{x}), y)$$

Prototype Classifier Update

cosine classifier  $C$  consists of weight vectors  $\mathbf{W} = [\mathbf{w}_1, \mathbf{w}_2, \dots, \mathbf{w}_{n_c}]$

$$\mathbf{p}(\mathbf{x}) = \sigma(\frac{1}{T} \mathbf{W}^T \mathbf{f}) \quad \mathbf{p}(\mathbf{x}) = [\mathbf{p}(\mathbf{x})_1, \dots, \mathbf{p}(\mathbf{x})_{n_c}]$$

$$\mathcal{D}_s^{(i)} = \{\mathbf{x} | (\mathbf{x}, y) \in \mathcal{D}_s, y = i\} \quad \mathcal{D}_{su}^{(i)} = \{\mathbf{x} | \mathbf{x} \in \mathcal{D}_{su}, \mathbf{p}(\mathbf{x})_i > t\}$$

$$\hat{\mathbf{w}}_i^s = \frac{1}{|\mathcal{D}_{s+}^{(i)}|} \sum_{\mathbf{x} \in \mathcal{D}_{s+}^{(i)}} \mathbf{V}^s(\mathbf{x}) \quad \hat{\mathbf{w}}_i^t = \frac{1}{|\mathcal{D}_{tu}^{(i)}|} \sum_{\mathbf{x} \in \mathcal{D}_{tu}^{(i)}} \mathbf{V}^t(\mathbf{x})$$

$$\mathcal{D}_{s+}^{(i)} = \mathcal{D}_s^{(i)} \cup \mathcal{D}_{su}^{(i)} \quad \mathbf{w}_i = \begin{cases} \text{unit}(\hat{\mathbf{w}}_i^s) & \text{if } |\mathcal{D}_{tu}^{(i)}| < t_w \\ \text{unit}(\hat{\mathbf{w}}_i^t) & \text{otherwise} \end{cases}$$

Mutual Information Maximization

- (1) To promote the network to have diversified outputs over the dataset  
→ Maximize the entropy of expected network prediction
- (2) To get high confident prediction for each sample  
→ entropy minimization on the network output

$$\mathcal{I}(y; \mathbf{x}) = \mathcal{H}(\mathbf{p}_0) - \mathbb{E}_{\mathbf{x}}[\mathcal{H}(p(y|\mathbf{x}; \theta))]$$

$$\mathcal{L}_{\text{MIM}} = -\mathcal{I}(y; \mathbf{x})$$

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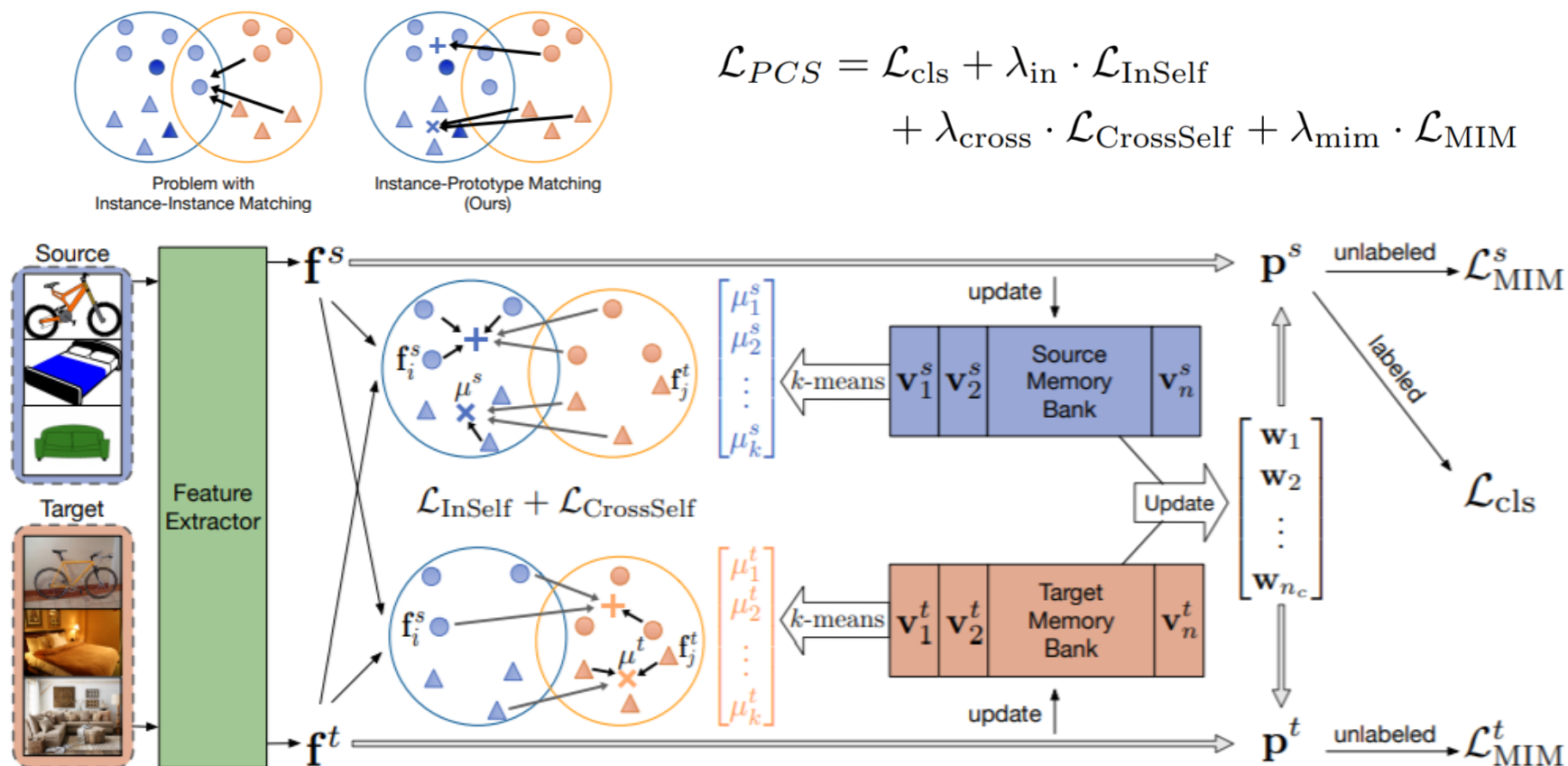


Figure 2: An overview of the PCS framework. In-domain and cross-domain self-supervision are performed between normalized feature vectors  $\mathbf{f}$  and prototypes  $\mu$  computed by clustering vectors  $\mathbf{v}$  in memory banks. Features with confident predictions ( $\mathbf{p}$ ) are used to adaptively update classifier vectors  $\mathbf{w}$ . MI maximization and classification loss are further used to extract discriminative features.

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Table 1: Adaptation accuracy (%) comparison on 1-shot and 3-shots per class on the Office dataset.

Method	Office: Target Acc. on 1-shot / 3-shots						
	A→D	A→W	D→A	D→W	W→A	W→D	Avg
SO	27.5 / 49.2	28.7 / 46.3	40.9 / 55.3	65.2 / 85.5	41.1 / 53.8	62.0 / 86.1	44.2 / 62.7
MME [59]	21.5 / 51.0	12.2 / 54.6	23.1 / 60.2	60.9 / 89.7	14.0 / 52.3	62.4 / 91.4	32.3 / 66.5
CDAN [45]	11.2 / 43.7	6.2 / 50.1	9.1 / 65.1	54.8 / 91.6	10.4 / 57.0	41.6 / 89.8	22.2 / 66.2
SPL [71]	12.0 / 77.1	7.7 / 80.3	7.3 / 74.2	7.2 / 93.5	7.2 / 64.4	10.2 / 91.6	8.6 / 80.1
CAN [38]	25.3 / 48.6	26.4 / 45.3	23.9 / 41.2	69.4 / 78.2	21.2 / 39.3	67.3 / 82.3	38.9 / 55.8
MDDIA [35]	45.0 / 62.9	54.5 / 65.4	55.6 / 67.9	84.4 / 93.3	53.4 / 70.3	79.5 / 93.2	62.1 / 75.5
CDS [39]	33.3 / 57.0	35.2 / 58.6	52.0 / 67.6	59.0 / 86.0	46.5 / 65.7	57.4 / 81.3	47.2 / 69.3
DANN + ENT [18]	32.5 / 57.6	37.2 / 54.1	36.9 / 54.1	70.1 / 87.4	43.0 / 51.4	58.8 / 89.4	46.4 / 65.7
MME + ENT	37.6 / 69.5	42.5 / 68.3	48.6 / 66.7	73.5 / 89.8	47.2 / 63.2	62.4 / 95.4	52.0 / 74.1
CDAN + ENT	31.5 / 68.3	26.4 / 71.8	39.1 / 57.3	70.4 / 88.2	37.5 / 61.5	61.9 / 93.8	44.5 / 73.5
CDS + ENT	40.4 / 61.2	44.7 / 66.7	<u>66.4</u> / 73.1	71.6 / 90.6	58.6 / 71.8	69.3 / 86.1	58.5 / 74.9
CDS + MME + ENT	39.4 / 61.6	43.6 / 66.3	<u>66.0</u> / <u>74.5</u>	75.7 / 92.1	53.1 / <u>73.0</u>	70.9 / 90.6	58.5 / 76.3
CDS + CDAN + ENT	52.6 / 65.1	55.2 / 68.8	65.7 / 71.2	76.6 / 88.1	59.7 / 71.0	73.3 / 87.3	63.9 / 75.3
CDS / MME + ENT <sup>†</sup>	<u>55.4</u> / 75.7	57.2 / 77.2	62.8 / 69.7	<u>84.9</u> / 92.1	<u>62.6</u> / 69.9	<u>77.7</u> / 95.4	65.3 / 80.0
CDS / CDAN + ENT <sup>†</sup>	<u>53.8</u> / <u>78.1</u>	<u>65.6</u> / <u>79.8</u>	59.5 / 70.7	83.0 / <u>93.2</u>	57.4 / 64.5	<u>77.1</u> / <u>97.4</u>	<u>66.1</u> / <u>80.6</u>
PCS (Ours)	<b>60.2 / 78.2</b>	<b>69.8 / 82.9</b>	<b>76.1 / 76.4</b>	<b>90.6 / 94.1</b>	<b>71.2 / 76.3</b>	<b>91.8 / 96.0</b>	<b>76.6 / 84.0</b>
Improvement	<b>+4.8 / +0.1</b>	<b>+4.2 / +3.1</b>	<b>+9.7 / +1.9</b>	<b>+5.7 / +0.9</b>	<b>+8.6 / +3.3</b>	<b>+14.1 / -1.4</b>	<b>+10.5 / +3.4</b>

<sup>†</sup> Two-stage training results reported in [39].



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Table 2: Performance contribution of each part in PCS framework on Office.

Method	Office: Target Acc. on 1-shot / 3-shots						
	A→D	A→W	D→A	D→W	W→A	W→D	Avg
$\mathcal{L}_{cls}$	27.5 / 49.2	28.7 / 46.3	40.9 / 55.3	65.2 / 85.5	41.1 / 53.8	62.0 / 86.1	44.2 / 62.7
+ $\mathcal{L}_{InSelf}$	39.0 / 55.6	38.6 / 55.1	47.2 / 68.5	71.7 / 89.4	50.9 / 68.4	65.1 / 90.6	52.1 / 71.3
+ $\mathcal{L}_{CrossSelf}$	47.2 / 71.1	52.7 / 70.6	59.0 / 75.5	76.4 / 90.3	58.5 / 74.1	66.9 / 91.8	60.1 / 78.9
+ $\mathcal{L}_{MIM}$	52.8 / 73.5	57.5 / 71.2	67.2 / 76.3	78.9 / 91.4	64.2 / 74.3	68.7 / 92.2	64.9 / 79.8
<b>+APCU (PCS)</b>	<b>60.2 / 78.2</b>	<b>69.8 / 82.9</b>	<b>76.1 / 76.4</b>	<b>90.6 / 94.1</b>	<b>71.2 / 76.3</b>	<b>91.8 / 96.0</b>	<b>76.6 / 84.0</b>
PCS w/o MIM	59.0 / 75.9	58.6 / 76.5	76.2 / 76.4	87.8 / 93.2	68.7 / 74.7	89.8 / 95.0	73.5 / 82.0

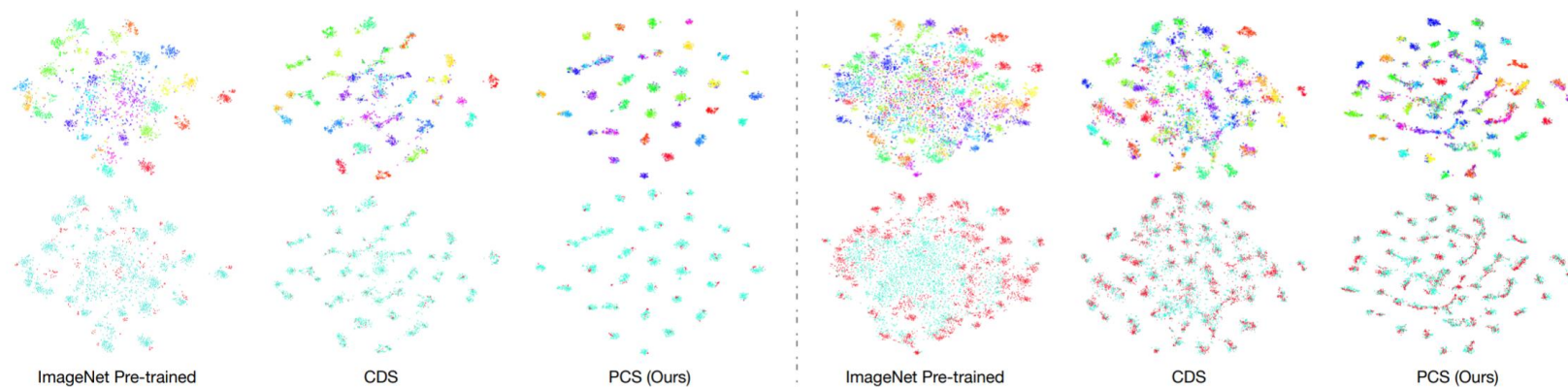


Figure 4: t-SNE visualization of ours and baselines on Office (left) and Office-Home (right). Top row: Coloring represents the class of each sample. Features with PCS are more discriminative than the ones with other methods. Bottom row: Cyan represents source features and Red represents target features. Feature from PCS are better-aligned between domains compared to other methods.

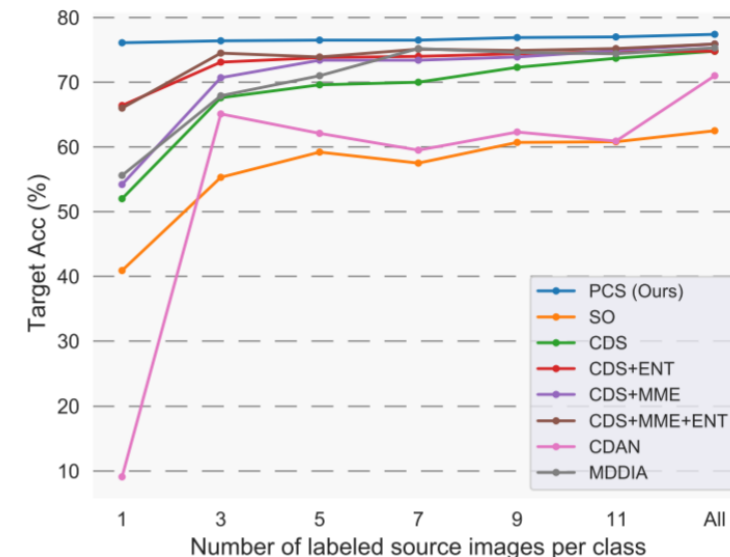


Figure 5: Sample efficiency comparison from DSLR to Amazon in Office dataset.

Top  
Color : class of each sample

bottom  
Cyan : source samples  
Red : target samples