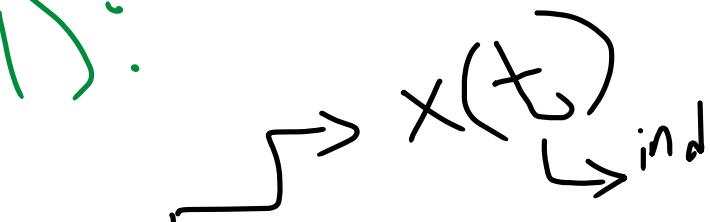


Review:

week (1): $\xrightarrow{\text{Intro}}$

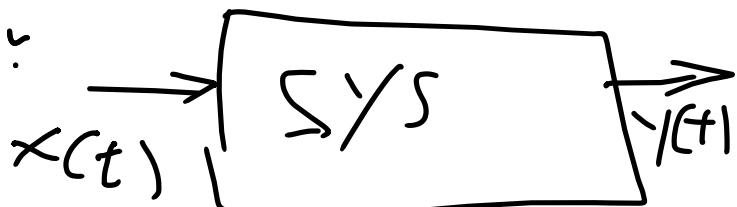


- Signal: Function,

carry info \xrightarrow{CTS}
 $\xrightarrow{DTS \sim \text{Digital Sig}}$

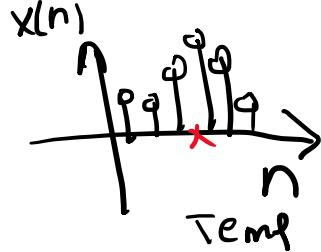
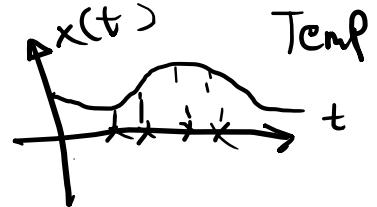
* DC $\xrightarrow{\text{Signal}}$

- System:



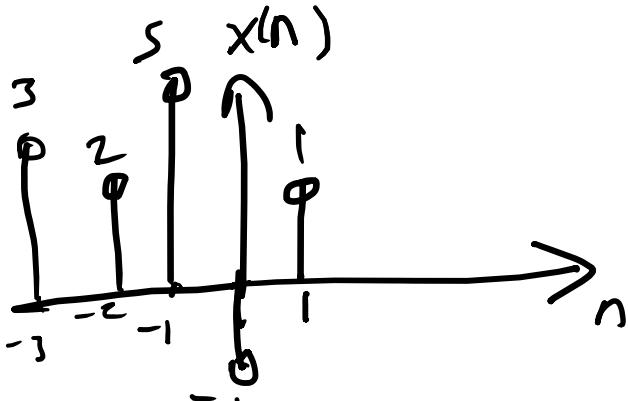
CTS: $x(t) \rightarrow \text{time}$

DTS: $x(n) \rightarrow \text{time}$



$$x(n) = \{3, 2, 5, -1, 1\} \rightarrow$$

-3 -2 -1 0 1



week (2)

always

Periodic & Non-Periodic Signal

$\downarrow (-\infty, \infty)$

$$x(t) = x(t + nT_0) \quad \begin{matrix} \text{Fundamental time} \\ \text{period} \end{matrix}$$

\boxed{n}

$\boxed{T_0}$

Integer

$$\sin(\theta) \Rightarrow T_0 = 2\pi \text{ sec} \quad , \quad f_0 = \frac{1}{T_0} \text{ Hz}$$

$$\omega_0 = 2\pi f_0 \text{ rad/sec}$$

$$\omega_0 = \frac{2\pi}{T_0} \quad , \quad T_0 = \frac{2\pi}{\omega_0}$$

CTS if one signal

$$y(t) = x_1(t) + x_2(t)$$

$\Rightarrow \omega_0, T_0$

$\frac{T_0}{T_0}$ Rational or not?

$T_0 = \text{LCM}(T_{01}, T_{02})$

DTS:

 $y(t) = \text{one sig}$
 ω_0, T_0, f_0
 $N = \frac{K}{T_0} \rightarrow \text{Fund time period}$

CTS

- Find ω_0 (coefficient of t)
- Find $f_0, \omega_0 = 2\pi f_0$
- Find $T_0, T_0 = \frac{1}{f_0}, T_0 = \frac{2\pi}{\omega_0}$
- $x(t+T_0) = x(t) \Rightarrow \text{CTS is Periodic}$ N: The period constant
 $\frac{T_0}{T_2}$ (See if its rational or not, when we have 2 signals)
 $\text{rational ratio} \Rightarrow \text{Periodic}, \text{irrational} \Rightarrow \text{non Periodic}$

DTS

- Find ω_0 (coefficient of t)
- Find $f_0, \omega_0 = 2\pi f_0$
- Find $N, f = \frac{K}{N}$

Review about Rational & Irrational numbers

1) Rational: Every number that can be represented by a "ratio" $\frac{\text{of two integers}}$ is a rational number

e.g.: $1 = \frac{1}{1} = \frac{-3}{-3} = \frac{10^6}{10^6}$

$-6 = \frac{-6}{1} = \frac{6}{-3} = \frac{-12}{6}$

$4.75 = \frac{475}{100} = \frac{-1}{200} = \frac{38}{8} = \frac{-78}{-16}$

$0.3333 = 0.\overline{3} = \frac{1}{3}$, $0.6 = \frac{2}{3}$ (the bar means repeating decimal)

4) If $\frac{K}{N}$ is Rational \Rightarrow Signal is Periodic

If $\frac{K}{N}$ is Irrational, \Rightarrow Signal is Not Periodic

$\frac{K}{N}$ must be integer

No 1 Rational
No 2 Irrational
 $N = \text{LCM}(N_{01}, N_{02})$

CTS (2) case

Example: $x(t) = \sin 6\pi t + \cos 5\pi t$

DTS (1) case

Example: Find out if $x[n] = \sin(\frac{\pi}{4}n)$ is periodic, if yes find N

DTS (2) case

Example: $x[n] = \sin \frac{2\pi}{3} n + \cos \frac{\pi}{2} n$

*LCM for fraction $(\frac{A}{B})$

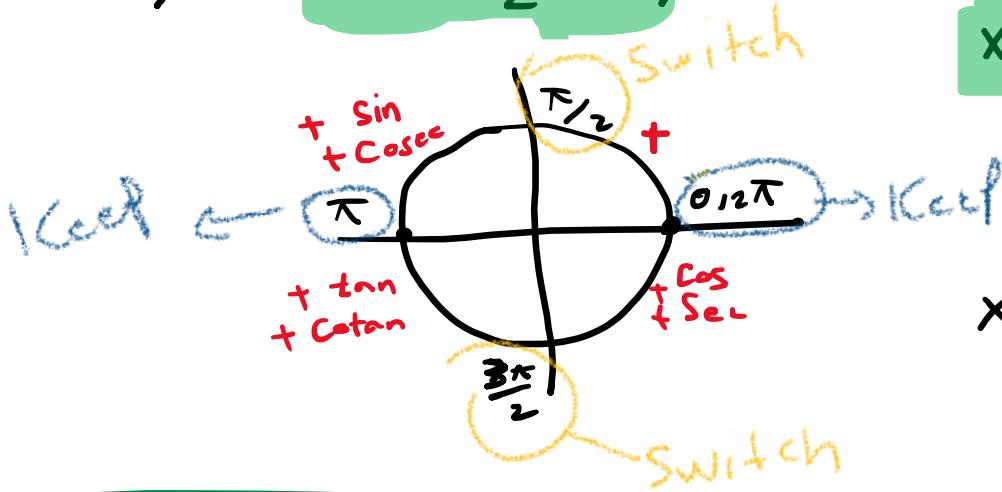
$$\text{LCM}\left(\frac{A_1}{B_1}, \frac{A_2}{B_2}\right) = \frac{\text{LCM}(A_1, A_2)}{\text{HCF}(B_1, B_2)}$$

Be careful!

Example: $x[n] = \sin\left(\frac{\pi}{4}n\right)$, Find N if this signal is periodic

$$x(t) = \sin\left(\frac{\pi}{2} - t\right) = \cos(t)$$

$$\begin{aligned}x(t) &= \cos\left(\frac{\pi}{2} + t\right) \\&= -\sin(t)\end{aligned}$$



$$\begin{aligned}x(t) &= \tan(\pi + t) \\&= +\tan(t)\end{aligned}$$

week(3) & (4) : Operations over signals

Time scaling $\rightarrow x(2t)$

$x(\sqrt{t})$

$x(0.5t)$

→ expanded

Time Shifting $\rightarrow x(t+4)$

Time Reversal $\rightarrow x(-2t)$

→ Reversed
Shrunked

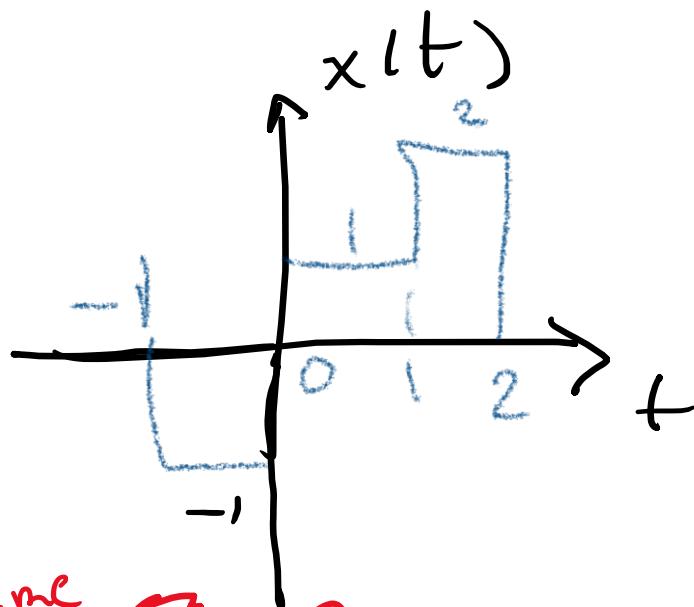
Amp Scaling $\rightarrow \pm 3x(t)$

' Shifting $\rightarrow x(t)+2$

$$y(t) = x\left(-\frac{1}{2}t - 4\right)$$

Plot $y(t) = ?$

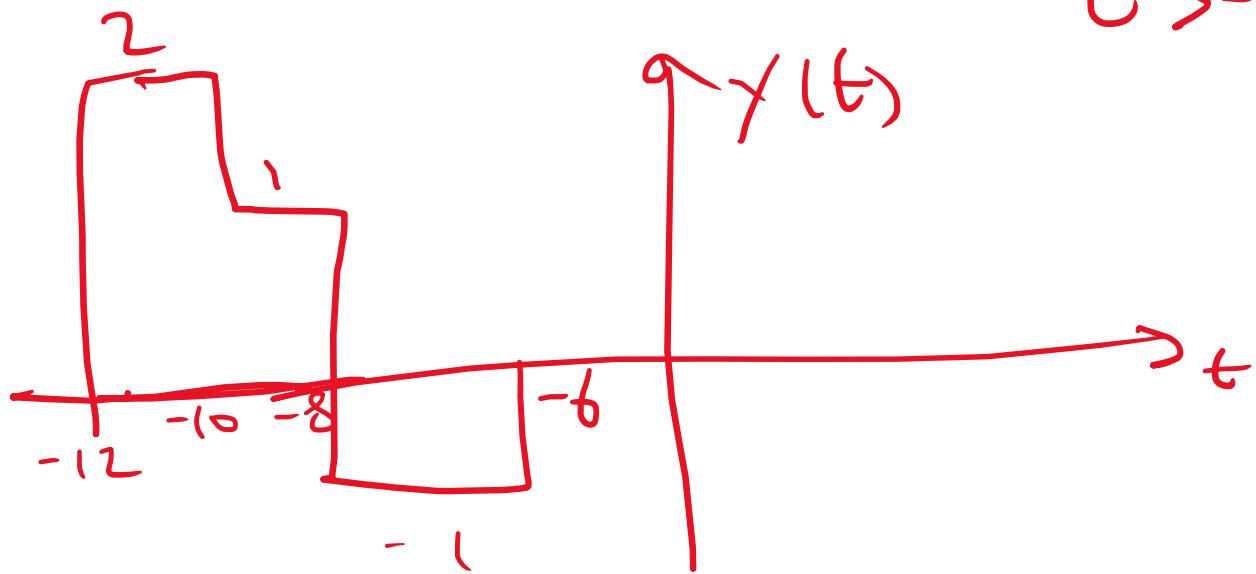
$$x(t) = \begin{cases} 0, & t < -1 \\ -1, & -1 \leq t \leq 0 \\ 1, & 0 < t \leq 1 \\ 2, & 1 < t \leq 2 \\ 0, & t > 2 \end{cases}$$



$x\left(-\frac{1}{2}t - 4\right) : 0, -\frac{1}{2}t - 4 < -1$

Time Reversal

$t > -6$



week(4) & (5)

Even & Odd

$$x(t) = x(-t) \rightarrow \text{Even}$$

Cosine Function

$$\begin{aligned} x(t) &= -x(-t) \\ -x(t) &= x(-t) \end{aligned} \quad \left. \begin{array}{l} \rightarrow \text{odd} \\ \end{array} \right.$$

Sine Function

But Not all Functions

are even or odd

$$x_e(t) = \frac{x(t) + x(-t)}{2}$$

useful
for
plotting
even

$$x_o(t) = \frac{x(t) - x(-t)}{2}$$

odd
components

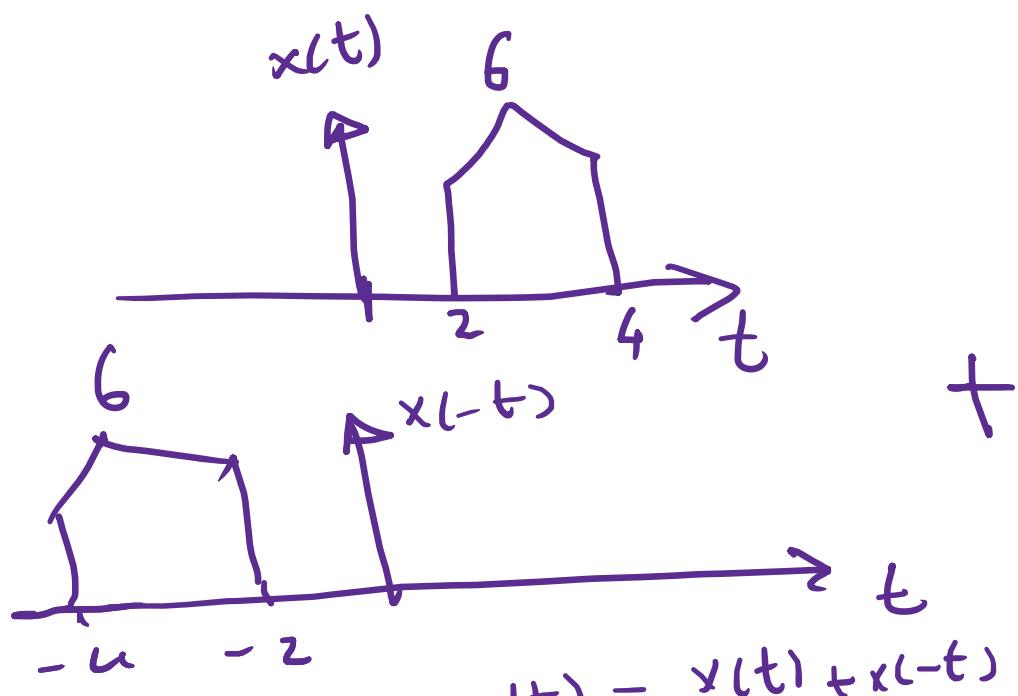
* Finding Even & Odd

components \rightarrow use Even & Odd Properties (14 Pro)

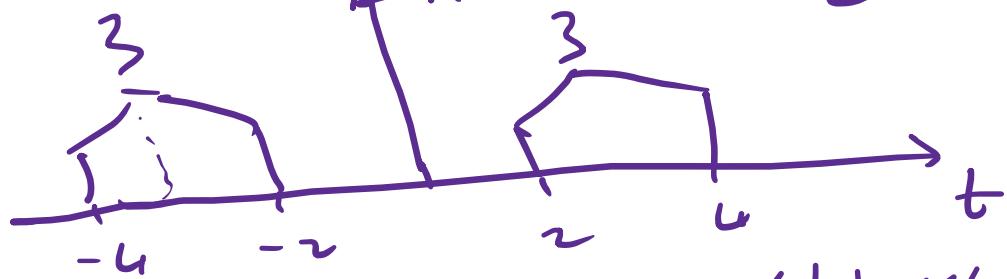
* Plotting Even & Odd \rightarrow

$$x_e(t) = \frac{x(t) + x(-t)}{2}$$

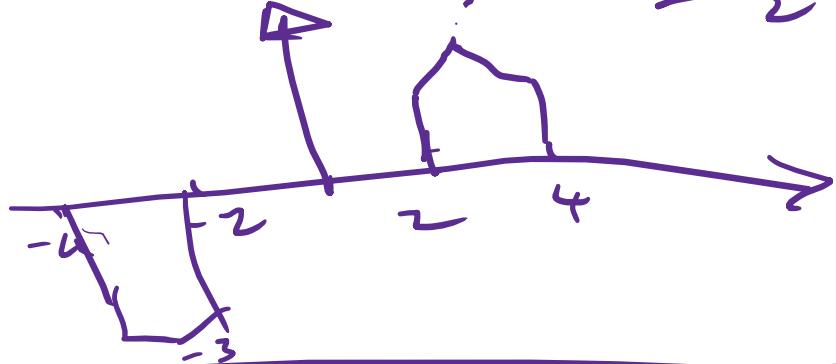
$$x_o(t) = \frac{x(t) - x(-t)}{2}$$



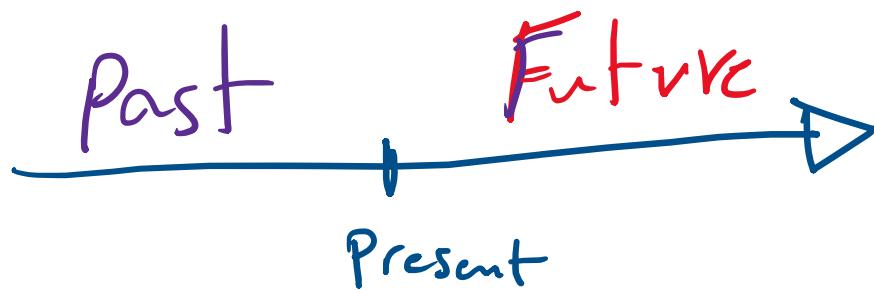
$$x_e(t) = \frac{x(t) + x(-t)}{2}$$

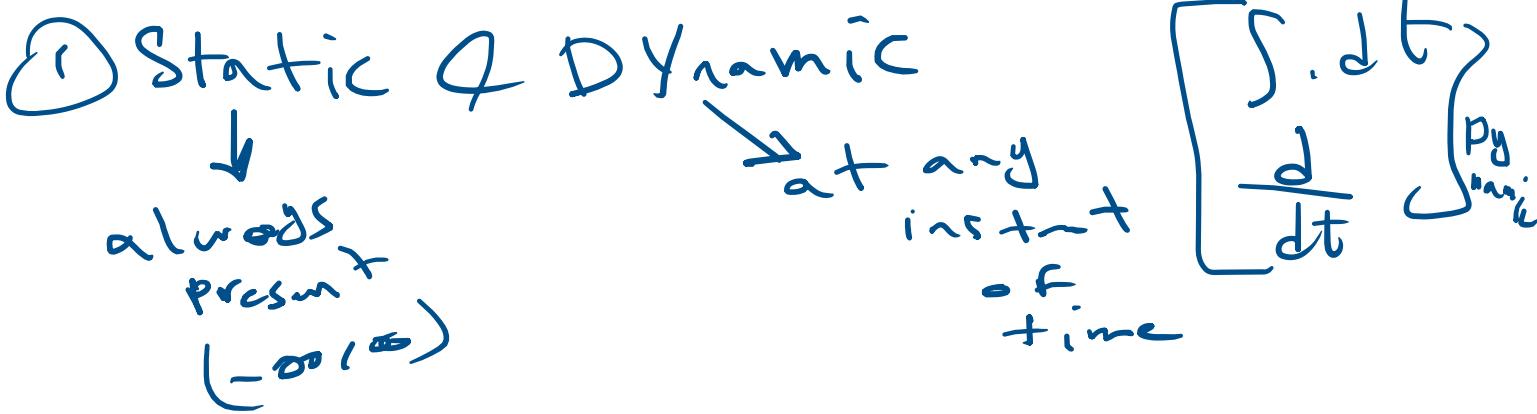


$$x_o(t) = \frac{x(t) - x(-t)}{2}$$



Systems (week 5 & 6)





$$y(t+10) = x(t+7) \quad S$$

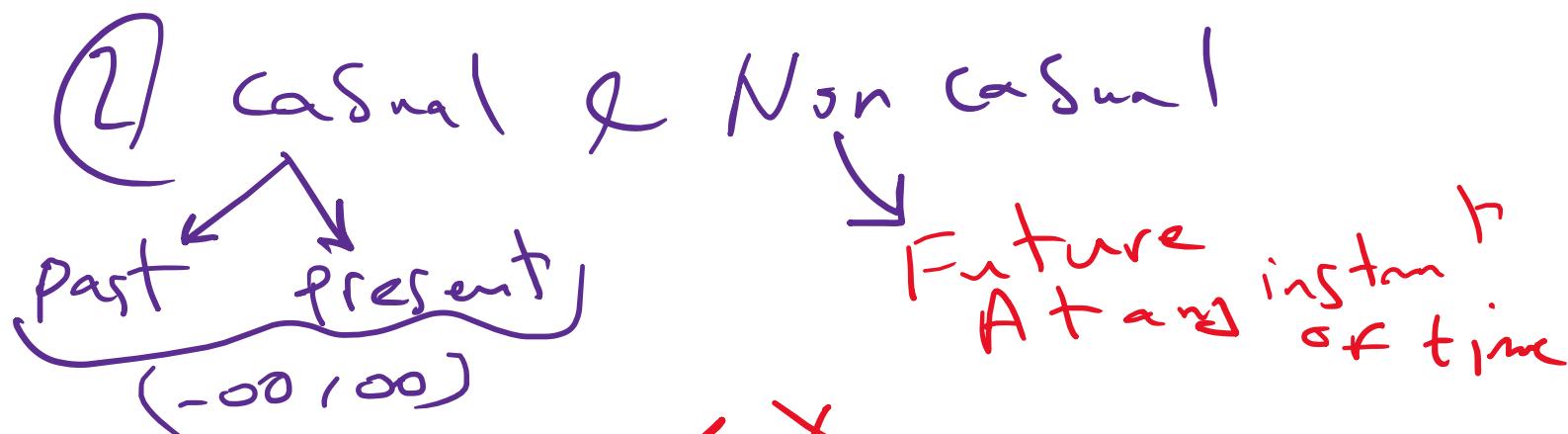
$$y(t+11) = \cancel{\frac{1}{2}} x(t+11) \quad S$$

$$y(t^2) = x(t^2) \quad S$$

$$y(t) = x(t + \cancel{e^{\pi t}}) \quad S$$

$\xrightarrow{-1}$

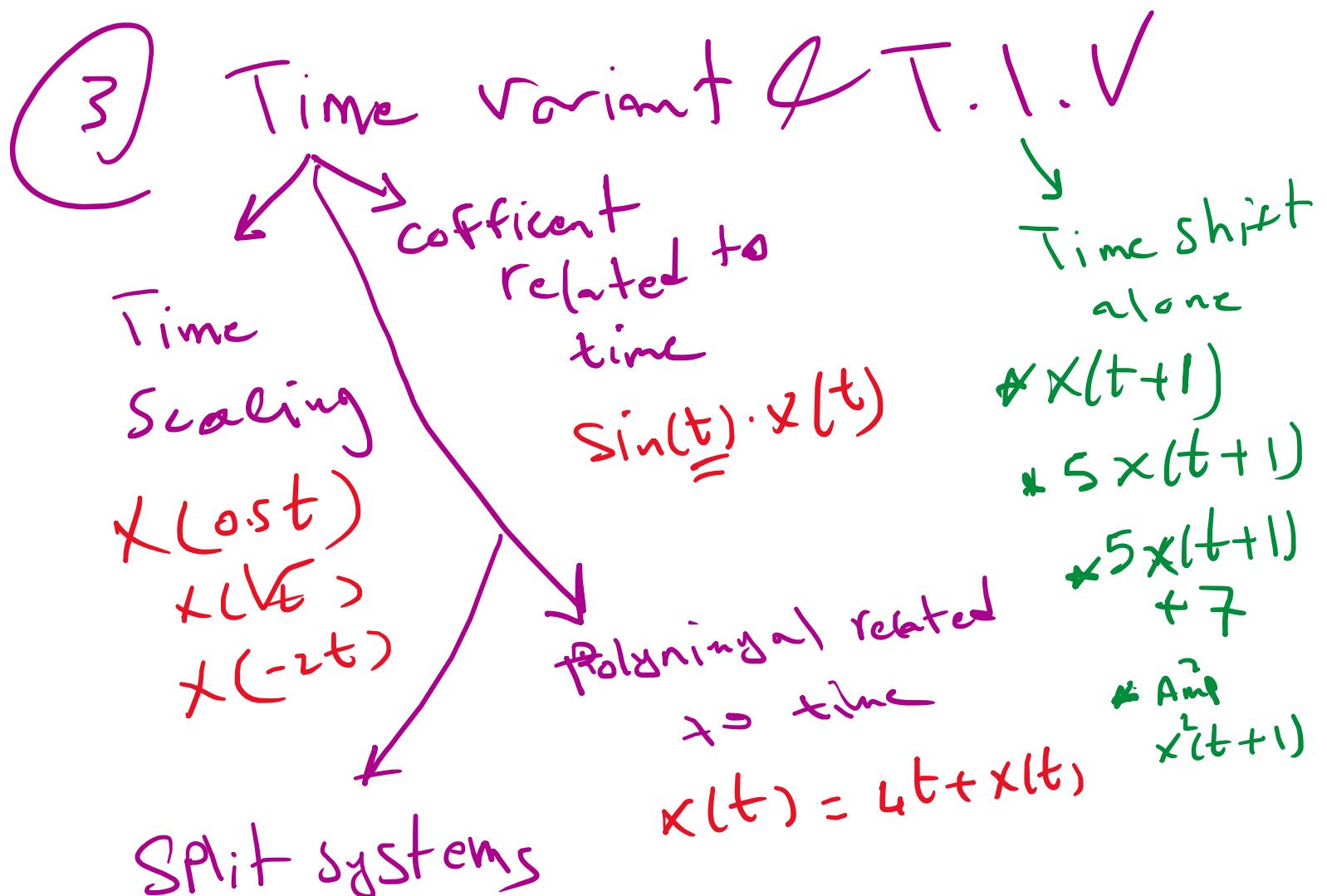
$$y(t) = x(\sqrt{t} - \sqrt{t}) \quad S$$



Static sys → Causal
not present

check the limits
 * Substitute the upper limit & down limit by (t) in the function

5.16
 check the limits



$$x(t) = \begin{cases} x(t-1), & t \leq 0 \\ x(t+1), & t > 0 \end{cases}$$

Linear & Non Linear

LoA LoH

Inst. char.

Shift +
 $y(t) = x(t) + \boxed{C}$

Amp scaling
 $y(t) = kx(t)$

give $i/p : o$

$\rightarrow o/p : o$

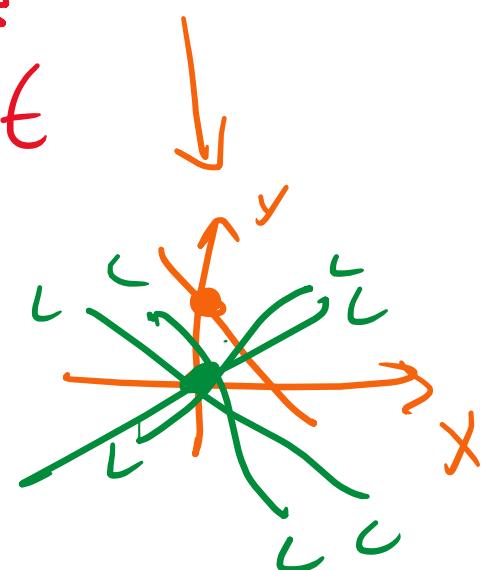
$$y(t) = 2x(t)$$

$$y(t) = 2x(t) + \boxed{2}$$

Nonlinear

$$y(t) = x(t+2) + C$$

NL ↳ time shift t



$$x_{\text{el}}(t) = \frac{x(t) + x(-t)}{2}$$

$$= \underbrace{\frac{1}{2}x(t)}_{\text{P.N.C}} + \underbrace{\frac{1}{2}\dot{x}(-t)}_{\text{I.U}}$$

$$x_0(t) = \frac{1}{2}x(t) - \underbrace{\frac{1}{2}x(-t)}_{\text{E}}$$

Non-Linear:

$$y(t) = \cos[x(t)]$$

$$y(t) = \cos^{-1}[x(t)]$$

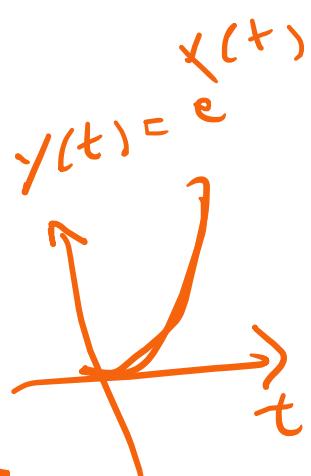
$$\log y(t) = x(t)$$

$$y(t) = \log[x(t)]$$

$$y(t) = e^{x(t)}$$

$$x(t) = \sqrt[3]{x(t)}$$

$$[y(t)]^3 = x(t)$$



SPLIT systems:

$$y(t) = \begin{cases} \cancel{NL}^{\cancel{x(t-1)}}^{+1}, & t < 0 \\ \cancel{NL}^{\cancel{x(t+1)}}, & t \geq 0 \end{cases}$$