# Adaptive Aggregation of Recommender Systems

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# Terminology

term	description
и	a user
i	an item (article, website, movie, product)
r	the rating, relevance, utility (domain specific)
m	a method for predicting ratings.
p(m, u, i)	rating prediction from method $m$ for $(u, i)$

# 2006: The Netflix Challenge

- ▶ USD 1MM prize for a 10% accuracy improvement.
- ▶ Breakthrough: Combining methods from many teams.
- ► Team BellKor finally achieved a 10.06% improvement by combining **107** different recommender algorithms.

#### Today: Web Search

"Today we use more than 200 signals, including PageRank, to order websites, and we update these algorithms on a weekly basis."

— Google

(google.com/corporate/tech.html)

"We use over 1,000 different signals and features in our ranking algorithm."

- Microsoft Bing

 $\label{logsbound} \begin{tabular}{ll} (bing.\ com/\ community/site\_\ blogs/\ b/search/\ archive/\ 2011/\ 02/\ 01/\ thoughts-\ on-search-\ quality.\ aspx) \end{tabular}$ 

### Why multiple algorithms?

- ▶ The unreasonable effectiveness of data
- ► Capture more predictive aspects of existing data.
- Specialized predictors for subsets of data.

"Quite frequently we have found that the more accurate predictors are less useful within the full blend."

— Bell, R., Koren, Y., and Volinsky, C. (2007) (Netflix)



# The Problem: Latent Subjectivity

$$\hat{r}_{u,i} = \sum_{m \in M} w_m \times p_r(m, u, i)$$
 (1)

- Generalized optimal weights.
- Treats all users and items the same.
- Varying accuracy across users and items.
- Methods are chosen by the system, not the users or items.

The Problem: Latent Subjectivity

Systems that insist on being adaptive in a certain way are not really adaptive at all.

#### Adaptive Recommenders

Multiple rating algorithms weighed by contextual accuracy.

$$\hat{r}_{u,i} = \sum_{m \in M} p_w(m, u, i) \times p_r(m, u, i)$$
 (2)

- $\triangleright$   $p_r$ : predicted rating from method m for (u, i).
- $\triangleright$   $p_w$ : predicted optimal weight for method m for (u, i).
- ▶ We can use recommender systems for **both**  $p_r$  and  $p_w$ .

#### Adaptive Recommenders

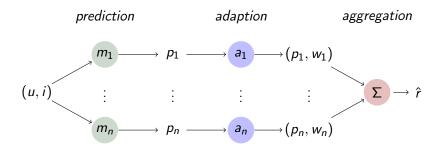


Figure: Layers of recommenders.

#### Training phase

- ▶ Split into two sets using bootstrap aggregation:  $(d_m, d_e)$ .
- Use  $d_m$  to train the basic recommenders.
- ▶ Create an error matrix using the basic recommenders and  $d_e$ .
- ▶ The error matrix values are predicted errors for (u, i, m).
- ► Train adaptive recommenders on the error matrix.

$$\forall (u, i, r) \in (d_e - d_m) : E(m)_{u,i} = |r - p(m, u, i)|$$
 (3)



# Training phase

$$R_{u,i} = \begin{pmatrix} r_{1,1} & r_{1,2} & \cdots & r_{1,i} \\ r_{2,1} & r_{2,2} & \cdots & r_{2,i} \\ \vdots & \vdots & \ddots & \vdots \\ r_{u,1} & r_{u,2} & \cdots & r_{u,i} \end{pmatrix}$$

$$E_{u,i} = \begin{pmatrix} e_{1,1} & e_{1,2} & \cdots & e_{1,i} \\ e_{2,1} & e_{2,2} & \cdots & e_{2,i} \\ \vdots & \vdots & \ddots & \vdots \\ e_{n,n} & e_{n,n} & e_{n,n} \end{pmatrix}$$

Train  $p_r$  with R and  $p_w$   $(p_e)$  with E.

#### Prediction phase

- ► Calculate each prediction  $\hat{r}_{(u,i,m)}$ .
- ► Calculate each predicted error  $\hat{e}_{(u,i,m)}$ .
- ▶ The adaptive weights are the inverses of the normalized error.
- ▶ Sum the weighted predictions to get the final  $\hat{r}$ .

# Prediction phase

$$\hat{r}_{u,i} = \sum_{(m_e, m_r) \in M} \left(1 - \frac{p(m_e, u, i)}{error(u, i)}\right) \times p(m_r, u, i) \tag{4}$$

$$error(u,i) = \sum_{m_e \in M} p(m_e, u, i)$$
 (5)

- Experiment: RMSE values for basic recommenders, simple aggregations and adaptive aggregation.
- Used the Movielens movie rating dataset.
- See paper for more details.

$$RMSE(\hat{R}, R) = \sqrt{\frac{\sum_{i=1}^{n} (\hat{R}_i - R_i)^2}{n}}$$
 (6)

#### (a) RMSE values for the five disjoint subsets:

S         svd1         1.2389         1.1260         1.1327         1.1045         1.1184           S         svd2         1.2630         1.1416         1.1260         1.1458         1.1260           S         svd3         1.0061         0.9825         0.9830         0.9815         0.9797           S         svd4         1.0040         0.9830         0.9849         0.9850         0.9798           S         slope_one         1.1919         1.0540         1.0476         1.0454         1.0393           S         item_avg         1.0713         0.9692         0.9683         0.9725           S         baseline         1.0698         0.9557         0.9527         0.9415         0.9492           S         cosine         1.1101         0.9463         0.9412         0.9413         0.9382           S         knn         1.4850         1.1435         1.1872         1.2156         1.2022           A         median         0.9869         0.8886         0.8857         0.8857         0.8855           A         adaptive         0.9324         0.8015         0.7993         0.8238         0.8192		method	d <sub>1</sub>	d <sub>2</sub>	d <sub>3</sub>	d <sub>4</sub>	d <sub>5</sub>	
S         svd3         1.0061         0.9825         0.9830         0.9815         0.9797           S         svd4         1.0040         0.9830         0.9849         0.9850         0.9798           S         slope_one         1.1919         1.0540         1.0476         1.0454         1.0393           S         item_avg         1.0713         0.9692         0.9662         0.9683         0.9725           S         baseline         1.0698         0.9557         0.9527         0.9415         0.9492           S         cosine         1.1101         0.9463         0.9412         0.9413         0.9382           S         knn         1.4850         1.1435         1.1872         1.2156         1.2022           A         median         0.9869         0.8856         0.8857         0.8555         0.8555           A         average         0.9900         0.8536         0.8525         0.8525         0.8519	S	svd1	1.2389	1.1260	1.1327	1.1045	1.1184	
S         svd4         1.0040         0.9830         0.9849         0.9850         0.9798           S         slope_one         1.1919         1.0540         1.0476         1.0454         1.0393           S         item_avg         1.0713         0.9692         0.9662         0.9683         0.9725           S         baseline         1.0698         0.9557         0.9527         0.9415         0.9492           S         cosine         1.1101         0.9463         0.9412         0.9413         0.9382           S         knn         1.4850         1.1435         1.1872         1.2156         1.2022           A         median         0.9869         0.8856         0.8857         0.8557         0.8555           A         average         0.9900         0.8536         0.8525         0.8525         0.8519	S	svd2	1.2630	1.1416	1.1260	1.1458	1.1260	
S         slope one item avg         1.1919         1.0540         1.0476         1.0454         1.0393           S         item avg         1.0713         0.9692         0.9662         0.9683         0.9725           S         baseline         1.0698         0.9557         0.9527         0.9415         0.9492           S         cosine         1.1101         0.9463         0.9412         0.9413         0.9382           S         knn         1.4850         1.1435         1.1872         1.2156         1.2022           A         median         0.9869         0.8886         0.8857         0.8857         0.8855           A         average         0.9900         0.8836         0.8525         0.8525         0.8519	S	svd3	1.0061	0.9825	0.9830	0.9815	0.9797	
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	Α	median	0.9869	0.8886	0.8857	0.8857	0.8855	
A adaptive 0.9324 0.8015 0.7993 0.8238 0.8192	Α	average	0.9900	0.8536	0.8525	0.8525	0.8519	
	Α	adaptive	0.9324	0.8015	0.7993	0.8238	0.8192	

#### (b) Statistics for the methods:

	method	min	max	mean	$\sigma$	Δ
S	knn	1.1435	1.4850	1.2467	0.3487	-
S	svd2	1.1260	1.2630	1.1605	0.2277	6.9%
S	svd1	1.1045	1.2389	1.1441	0.2197	1.4%
S	slope one	1.0393	1.1919	1.0756	0.2415	5.9%
S	item avg	0.9662	1.0713	0.9895	0.2023	8.0%
S	svd4	0.9798	1.0040	0.9873	0.0924	2.2%
S	svd3	0.9797	1.0061	0.9865	0.0991	0.1%
S	cosine	0.9382	1.1101	0.9754	0.2595	1.1%
S	baseline	0.9415	1.0698	0.9738	0.2196	1.6%
Α	median	0.8855	0.9865	0.9065	0.2005	6.9%
Α	average	0.8519	0.9900	0.8801	0.2344	2.9%
Α	adaptive	0.7993	0.9324	0.8352	0.2225	5.1%

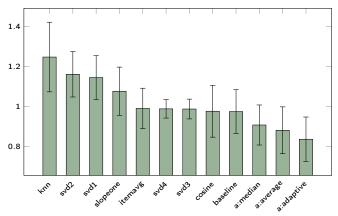


Figure: Average RMSE plot.

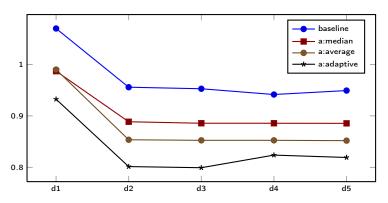


Figure: RMSE Standard deviation caused by dataset  $d_1$ .

#### Limitations

- ▶ Lots of added complexity for fairly unknown improvement.
- ▶ Only tested on a few datasets, no real world situations.
- Only compared to simple aggregation methods.
- Neither the aggregators nor the basic recommenders were heavily optimized to the domain of the dataset.

#### Adaptive Recommenders

- ► Combine disjoint algorithms
- Weigh recommenders by predicted accuracy.
- ▶ Accuracy predictions are contextually dependent on (u, i, m).
- Any applicable recommender becomes a worthy addition.

See paper for more references and results.