HW 11

Given the equation $y'' = -(x+1)y' + 2y + (1-x^2)e^{-x}$, $0 \le x \le 1$, y(0) = 1, y(1) = 2

Questions:

use h = 0.1

- a. Use the shooting method to approximate the solution of the problem
- b. Use the finite-difference method to approximate the solution
- c. Use the variation approach to approximate the solution.

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-------- RESTART: D:/大學/大三下/數值方法/hw11/q.py =-----
--- HW11: Boundary-value problem for 0.D.E. --- Given equation: y'' = -(x+1)y' + 2y + (1-x^2)e^{h}(-x), 0 \le x \le 1, y(0) = 1, y(1) = 2, h = 0.1
  --- a. Shooting Method ---
C = 0.024157618028824695
y values: [1, 1.01664898 1.05929008 1.12447309 1.20911769 1.31052469
1.42637382 1.55470926 1.69391549 1.8426876 2, ]
 --- b. Finite-Difference Method ---
y values: [1, 1.01653219 1.05910229 1.12425112 1.2088902 1.31031341 1.42619408 1.55457046 1.69382243 1.84264199 2. ]
  --- c. Variation Approach (Galerkin Method) ---
Coefficients c: [-0.19690203 -0.01747145 -0.00884708 -0.00223296 -0.00196785]
y values: [1. 1.0176355 1.05792097 1.12463303 1.20978944 1.30997721
1.42608101 1.5552407 1.69377865 1.84242177 2. ]
 --- Summary Table ---
x Shooting
0.0 1.000000
  0.0
0.1
0.2
0.3
0.4
0.5
0.6
0.7
0.8
0.9
                                              1.000000
1.016532
1.059102
1.124251
                                                                         1.000000
1.017635
1.057921
1.124633
                                              1.208890
1.310313
                                              1.426194
1.554570
1.693822
1.842642
2.000000
                                                                         1.693779
1.842422
```

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