- 1. Determine the values  $\int_{1}^{2} e^{x} \sin(4x) dx$  with h = 0.1 by
- a. Use the composite trapezoidal rule
- b. Use the composite Simpsons' method
- c. Use the composite midpoint rule

2. Approximate  $\int_{1}^{1.5} x^2 \ln x dx$  using Gaussian Quadrature with n=3 and n=4. Then compare the result to the exact value of the integral.

```
2. Gaussian n=3 : 0.19225938
2. Gaussian n=4 : 0.19225936
2. Exact Value : 0.19225936
2. Error n=3 : 1.95e-08
2. Error n=4 : 7.21e-11
```

- 3. Approximate  $\int_0^{\pi/4} \int_{\sin x}^{\cos x} (2y \sin x + \cos^2 x) dy dx$  using
  - a. Simpson's rule for n = 4 and m = 4
  - b. Gaussian Quadrature, n=3 and m=3
  - c. Compare these results with the exact value.

```
3.a Simpson 2D (n=4, m=4): 0.51198754
3.b Gaussian 2D (n=3, m=3): 0.51186554
3.c Exact Value : 0.51184464
3.c Simpson Error : 1.43e-04
3.c Gauss Error : 2.09e-05
```

4. Use the composite Simpson's rule and n=4 to approximate the improper integral a)  $\int_0^1 x^{-1/4} \sin x dx$ , b)  $\int_1^\infty x^{-4} \sin x dx$  by use the transform