

Exercises 3.15

Exercise 3.15.1

Let p , p_i , q , q_i be density functions on \mathbb{R} and $\alpha \in \mathbb{R}$. Show that the cross-entropy satisfies the following properties:

- a. $S(p_i + p_2, q) = S(p_1, q) + S(p_2, q)$;
- b. $S(\alpha p, q) = \alpha S(p, q) = S(p, q^\alpha)$;
- c. $S(p, q_1 q_2) = S(p, q_1) + S(p, q_2)$.

Exercise x.y.2

Describe the problem for Exercise x.y.2.

- a. Prove a statement.
- b. Derive a formula.

SOLUTIONS

x.y.1 (a)

At vero eos et accusamus et iusto odio dignissimos ducimus qui blanditiis praesentium voluptatum deleniti atque corrupti quos dolores et quas molestias excepturi sint occaecati cupiditate non provident, similique sunt in culpa qui officia deserunt mollitia animi, id est laborum et dolorum fuga.

Proof.

$$\begin{aligned}\sigma'''(x) &= \frac{d}{dx} \frac{e^x - e^{2x}}{(1 + e^x)^3} = \frac{(e^x - 2e^{2x})(1 + e^x)^3 - 3(1 + e^x)^2 e^x (e^x - e^{2x})}{(1 + e^x)^6} \\ &= \frac{e^x \{1 - 4e^x + e^{2x}\} (1 + e^x)^2}{(1 + e^x)^6} = \frac{e^x \{1 - 4e^x + e^{2x}\}}{(1 + e^x)^4}\end{aligned}$$

□

x.y.2 (a)

Et harum quidem rerum facilis est et expedita distinctio. Nam libero tempore, cum soluta nobis est eligendi optio cumque nihil impedit quo minus id quod maxime placeat facere possimus, omnis voluptas assumenda est, omnis dolor repellendus.

Proof. a = a

□