

Homework 3

● Graded

Student

苏慧哲

Total Points

15 / 15 pts

Question 1

Sorting Pratice

4 / 4 pts

1.1 Q1

2 / 2 pts

✓ - 0 pts Correct

- 0.5 pts One error

- 1 pt Multiple errors

- 1.5 pts Partial Credit

- 2 pts Completely wrong or missing

- 0.5 pts Minor error (missing a number, underlining, etc)

1.2 Q2

2 / 2 pts

✓ - 0 pts Correct

- 0.5 pts One error

- 1 pt Two error

- 1.5 pts Three error

- 2 pts All wrong

Question 2

Identifying Sorts

4 / 4 pts

2.1 Q3

1 / 1 pt

✓ - 0 pts Correct

- 1 pt Wrong

- 1 pt Empty or NOT Matched

2.2 Q4

1 / 1 pt

✓ - 0 pts Correct

- 1 pt Wrong

- 1 pt Blank or NOT Matched

2.3 Q5

1 / 1 pt

✓ - 0 pts Correct

- 1 pt Wrong

2.4 Q6

1 / 1 pt

✓ - 0 pts Correct

- 1 pt Wrong

Question 3

Single Choice Q7-Q9

3 / 3 pts

✓ - 0 pts Correct

- 1 pt Q7 A || C

- 1 pt Q8 C

- 1 pt Q9 D

Question 4

Stable Sort Q10

4 / 4 pts

✓ - 0 pts Correct

- 1 pt Only mention 1 or 2 sort algorithms in the explanation.
- 2 pts Wrong for quicksort
- 0.5 pts The question says "a sort is stable if there is an implementation ..." Your implementation is reasonable, but there is some implementation to preserve the order.
- 1.3 pts Wrong for insertion sort.
- 1.3 pts Wrong for quicksort.
- 0.01 pts There is some implementation making it stable with additional space. But in the in-place implementation, quicksort is unstable. You still gain the point as the problem's ambiguity for "additional".
- 4 pts Wrong

No questions assigned to the following page.

CS101 Algorithms and Data Structures
Fall 2021
Homework 3

Due date: 23:59, October 17, 2021

1. Please write your solutions in English.
2. Submit your solutions to gradescope.com.
3. Set your FULL NAME to your Chinese name and your STUDENT ID correctly in Account Settings.
4. If you want to submit a handwritten version, scan it clearly. CamScanner is recommended.
5. When submitting, match your solutions to the according problem numbers correctly.
6. No late submission will be accepted.
7. Violations to any of the above may result in zero grade.

Questions assigned to the following page: [1.1](#) and [1.2](#)

1: (2'+2') Sorting Practice

Given array:

1, 5, 3, 8, 7, 2, 4, 6

we want to sort this array in ascending order in-place.

Please **show your steps** taken by each type of sorting method on this array:

Question 1. Quicksort. After each partition during the algorithm, write the ordering of the list, **circle** the pivot that was used for that partition, and **underline** the sub-array being partitioned. Assume that the pivot is always the first item in the sublist being sorted.

Example: 1 5 3 8 7 2 4 6

We use in-place quicksort, and red letter to represent the swapped elements.

1 5 3 8 7 2 4 6
 1 5 3 8 7 2 4 6
 1 5 3 4 7 2 8 6
 1 5 3 4 7 8 6
 1 2 3 4 5 7 8 6
 1 2 3 4 5 7 8 6
 1 2 3 4 5 7 8 6
 1 2 3 4 5 7 8 6
 1 2 3 4 5 7 6 8
 1 2 3 4 5 6 7 8
 1 2 3 4 5 6 7 8

Question 2. Merge sort. Show the intermediate merging steps. In each merging step, circle the subarray that is to be merged.

1 5 3 8 7 2 4 6
 1 5 3 8 7 2 4 6
 1 5 3 8 7 2 4 6
 1 5 3 8 7 2 4 6
 1 3 5 8 7 2 4 6
 1 3 5 8 7 2 4 6
 1 3 5 8 2 7 4 6
 1 3 5 8 2 7 4 6
 1 3 5 8 2 7 4 6
 1 3 5 8 2 7 4 6
 1 3 5 8 2 4 6 7
 1 3 5 8 2 4 6 7
 1 2 3 4 5 6 7 8
 1 2 3 4 5 6 7 8

Questions assigned to the following page: [2.2](#), [2.3](#), [2.4](#), and [2.1](#)

2: (4×1') Identifying Sorts

Below you will find intermediate steps in performing various sorting algorithms that sort the input in ascending order on the same input list. The steps **do not necessarily represent consecutive steps in the algorithm** (that is, many steps are missing), but they are in the correct order. For each of them, **select the correct algorithm from the following choices**: insertion sort, bubble sort, quicksort (first element of sequence as pivot), and mergesort.

Input list: 5, 6, 9, 4, 1, 2, 7, 10, 8, 0, 3

Question 3.

5, 6, 9, 1, 4, 2, 7, 10, 8, 0, 3

5, 6, 1, 4, 9, 2, 7, 10, 0, 3, 8

1, 4, 5, 6, 9, 0, 2, 3, 7, 8, 10

Merge Sort

Question 4.

4, 1, 2, 0, 3, 5, 6, 9, 7, 10, 8

1, 2, 0, 3, 4, 5, 6, 9, 7, 10, 8

0, 1, 2, 3, 4, 5, 6, 7, 10, 8, 9

Quick Sort

Question 5.

4, 5, 6, 9, 1, 2, 7, 10, 8, 0, 3

1, 4, 5, 6, 9, 2, 7, 10, 8, 0, 3

1, 2, 4, 5, 6, 9, 7, 10, 8, 0, 3

Insertion Sort

Question 6.

5, 6, 4, 9, 1, 2, 7, 10, 8, 0, 3

5, 6, 4, 1, 2, 7, 9, 8, 0, 3, 10

5, 4, 1, 2, 6, 7, 9, 8, 0, 3, 10

Bubble Sort

Question assigned to the following page: [3](#)

3: (3×1') Single Choice

The following questions are single choice questions, each question has **only one** correct answer. Select the correct answer.

Note: You should write those answers in the box below.

| | | |
|------------|------------|------------|
| Question 7 | Question 8 | Question 9 |
| A | C | D |

Question 7. Consider the quicksort algorithm which sorts elements in ascending order using the first element as pivot. Then which of the following input sequence will require a maximum number of comparisons when this algorithm is applied on it?

- (A) 22 25 56 67 89
- (B) 52 25 76 67 89
- (C) 22 52 67 25 76
- (D) 52 25 89 67 76

Question 8. Which of the following statements is **NOT** true?

- (A) The worst case time complexity of quicksort is $O(n^2)$.
- (B) Given 2 sorted lists of size m and n respectively, and we want to merge them to one sorted list by mergesort. Then in the worst case, we need $m + n - 1$ comparisons.
- (C) The time complexity of quicksort, compared with mergesort, is less affected by the initial order of the input array.
- (D) Comparing to quicksort, mergesort requires additional space complexity.

Question 9. Given extra information about the input array, we may design sorting algorithms that perform faster than $O(N \log N)$. Which of the following prior knowledge will lead to worst time complexity **slower** than $O(N)$?

- (A) Knowing the input array has no more than N inversions.
- (B) Knowing the input array has exactly $(N^2 - N)/2$ inversions.
- (C) Knowing the input array has less than N pairs of numbers that are not inversions.
- (D) None of the above.

Question assigned to the following page: [4](#)

Question 10. (4') Stable sort

We say a sort is “stable” if there is an implementation that it **always** preserves the original order of equal elements in an array without using additional space. For example, if we have an array: $4, 2, 3_a, 3_b, 1$, after sorting it has a chance to become $1, 2, 3_b, 3_a, 4$ (3_a and 3_b are equal when comparing), then this sorting algorithm is **NOT** stable.

Among insertion sort, quicksort and mergesort, which of them are stable? (1') Briefly explain your answer. (3')

Insertion sort and mergesort are stable, quicksort is not stable.

Insertion sort:

Insertion sort will not swap the two number when they are equal. During the insertion procedure, when two number of the same value meet, the procedure will stop immediately. The relative position of these two same number will never be changed. Therefore the insertion sort is stable.

Mergesort:

When merging two sorted arrays(left array and right array) into one bigger array, if there're two number of same value in both arrays, the number in the left array will always be put into the bigger array first. If the two number of the same value appeared in the same array, the former one will always be put into the bigger array first. The initial position of the numbers in the right array is always bigger then the numbers in the left array before merging. Therefore, the number with bigger initial position will always be put at right to the number with smaller initial position if they are of the same value. Therefore, the relative position of two same number will neber be changed.

Quicksort:

The swapping is done according to the pivot, so chances are that two number of the same value swap there posion.

For example. Give an array: $2\ 3_a\ 3_b\ 4\ 1$

We choose the first element as the pivot, and use the in-place quicksort method.

```

2 3a 3b 1 4
2 1 3b 3a 4
1 2 3b 3a 4
1 2 3b 3a 4
1 2 3b 3a 4
1 2 3b 3a 4

```

The in-place quicksort in not stable.

We choose the first element as the pivot, and use another array to help sorting.

```

2 3a 3b 1 4
1 2 4 3b 3a
1 2 4 3b 3a
1 2 3b 3a 4
1 2 3b 3a 4
1 2 3b 3a 4

```

The quicksort is not stable.