

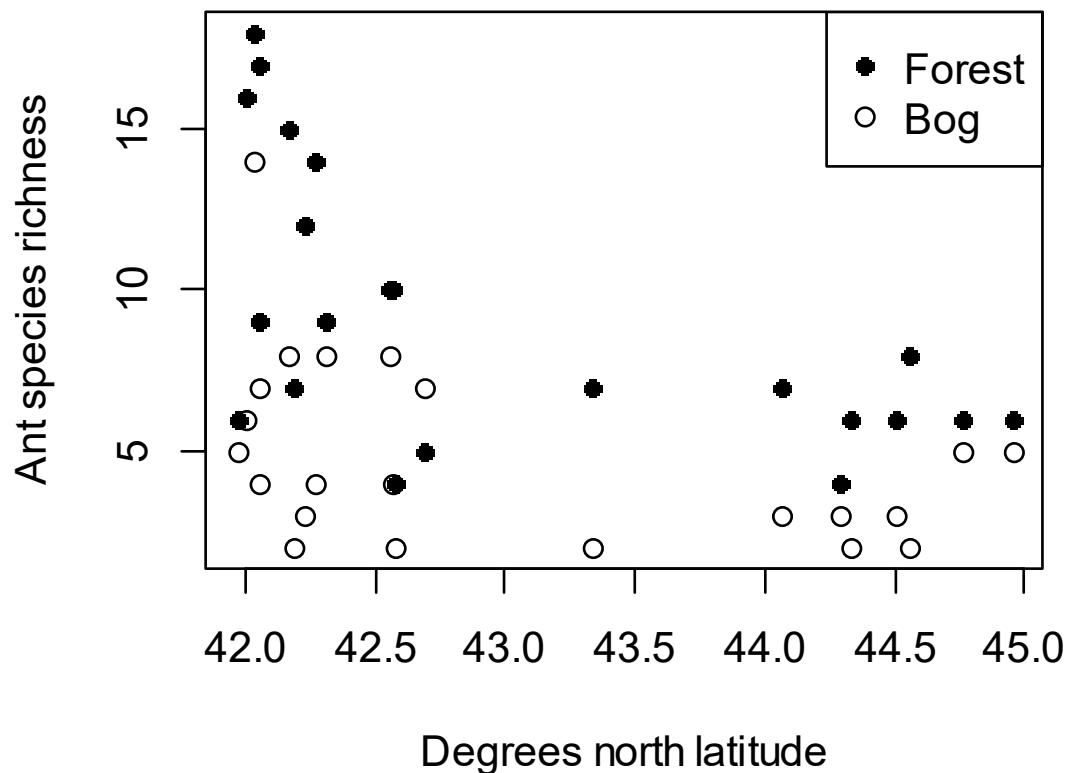
Dataset to analyze

Scientific questions:

How different is species richness between habitats?

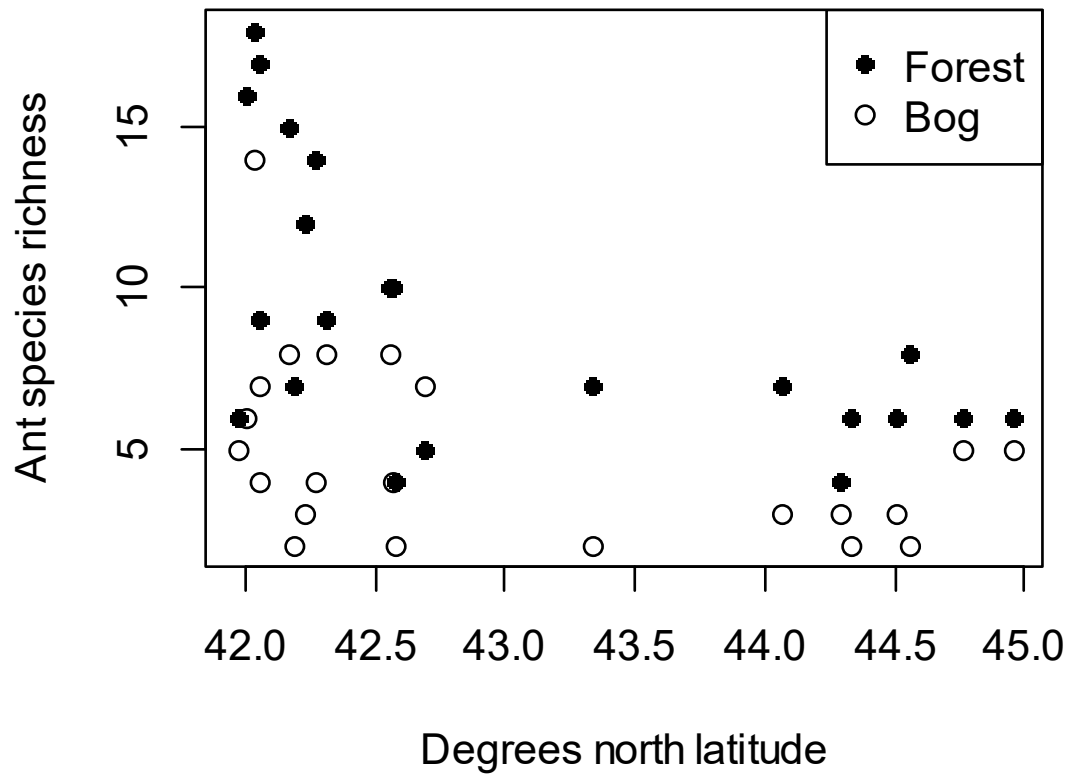
How does species richness vary with latitude?

Is this relationship different between habitats?



What will the data-generating model be?
Ignore pairs for now

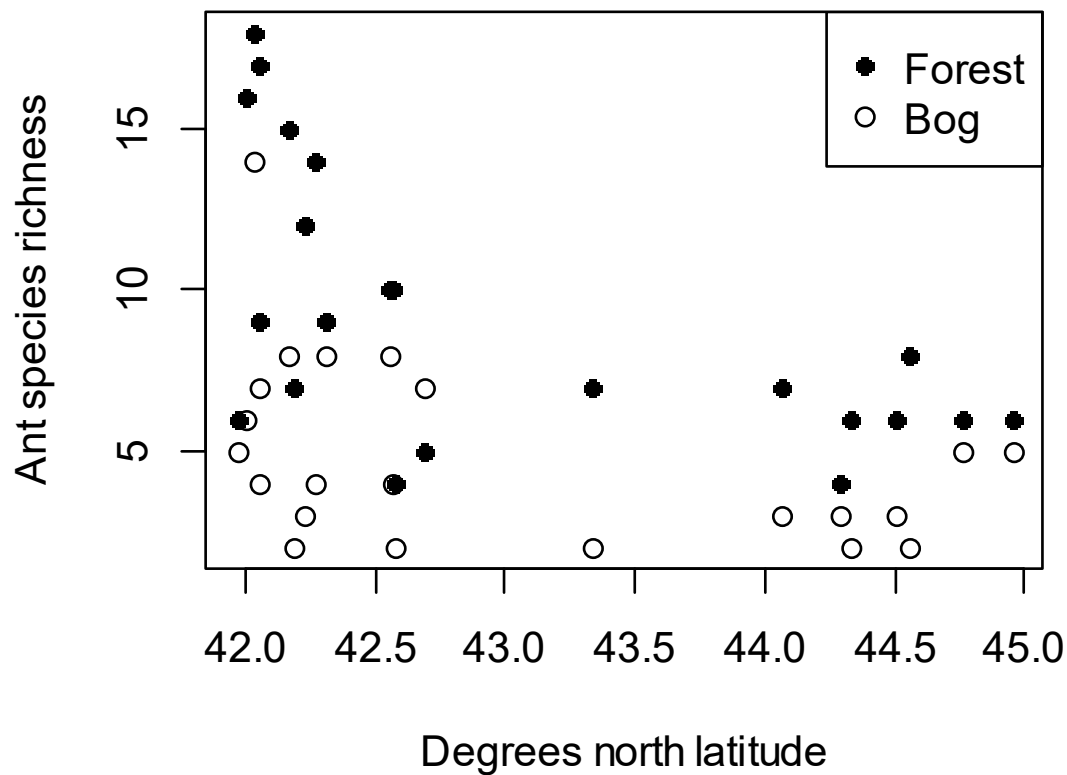
Dataset to analyze



Model:

GLM
Poisson
Log link

Dataset to analyze



Model:

Distribution

$$y_i \sim \text{Poisson}(\mu_i)$$

Link function

$$\begin{aligned} \log(\mu_i) = & \beta_0 + \beta_1 \text{forest}_i \\ & + \beta_2 \text{latitude}_i \\ & + \beta_3 \text{forest}_i \times \text{latitude}_i \end{aligned}$$

Inverse link function

$$\mu_i = e^{\eta_i}$$

Model matrix

$$\eta_i = \beta_0 + \beta_1 \text{forest}_i + \beta_2 \text{latitude}_i + \beta_3 \text{forest}_i \times \text{latitude}_i$$

```
fit <- glm(richness ~ habitat + latitude + habitat:latitude,
           family=poisson(link="log"), data=ant)
```

Data

habitat	latitude	richness
forest	42	16
forest	42.56	10
forest	43.33	7
forest	44.76	6
bog	42.17	8
bog	42.57	4
bog	44.06	3
bog	44.95	5

Design matrix

intercept	forest
1	1
1	1
1	1
1	1
1	0
1	0
1	0
1	0

model.matrix(fit)

latitude	forest:latitude
42	42
42.56	42.56
43.33	43.33
44.76	44.76
42.17	0
42.57	0
44.06	0
44.95	0

$$\eta_i = \beta_0 \text{intercept}_i + \beta_1 \text{forest}_i + \beta_2 \text{latitude}_i + \beta_3 \text{forest}_i \times \text{latitude}_i$$