

# Today

- Recap & questions from homework
- Functions
- Coding descent algorithm (training)
  - using `optim()`

# Git skills

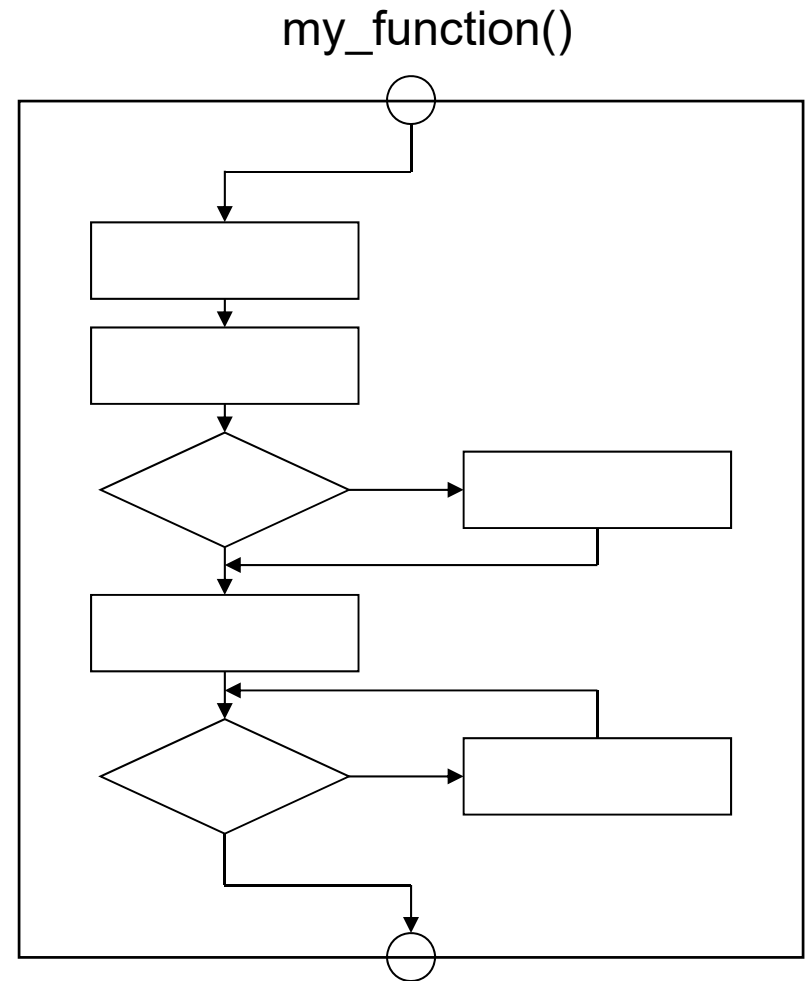
- `git amend`
- `.gitignore`
- `gitgui`
- `gitk`

# Fit ecological model

- Natural process culture of data science
- Paramecium logistic growth
- Parameters:  $r$ ,  $K$ ,  $N(0)$
- Grid search

# Programming: functions

- A function **encapsulates an algorithm**
- Functions break a program down into **modules**
- Modularized programs are easier to write, debug, maintain, and modify
- Functions make algorithms easier to **reuse**



# Making a function in R

- ?"function" – only the bare bones

```
function_name <- function(arguments) {  
  expression  
  return(object)  
}
```

Class style

← explicit return

← indent (4 spaces)

← closing brace aligns with first letter of function name

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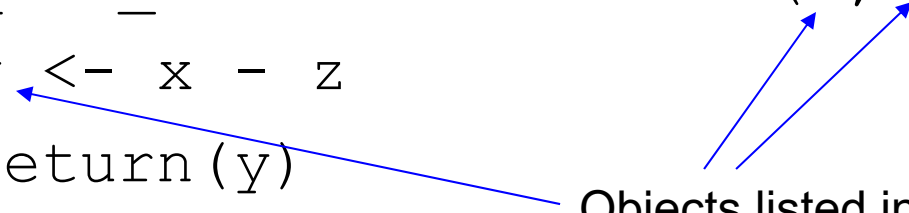
```
diff_two_nums <- function(x, z) {  
  y <- x - z  
  return(y)  
}
```

# Making a function in R

- ?"function" – only the bare bones

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```
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```



Objects listed in the arguments or defined in the function can only be seen inside the function. These are called **local variables**.  
Concept: **scope**.

# Scope

- See examples in functions.R
- Good programming practice: **avoid global variables**
  - Define **local variables** by including in argument list or initializing within the function
  - Global variables make programs harder to maintain and debug



# Make a function

```
function_name <- (arguments) {  
  expression  
  return(object)  
}
```

Exercise:

Make a function to calculate the linear model given the model parameters and a vector of x data. In other words, turn the following into a function:

$$y \leftarrow b_0 + b_1 * x$$

# Make a function

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## Exercise:

Make a function to calculate the linear model given the model parameters and a vector of x data. In other words, turn the following into a function:

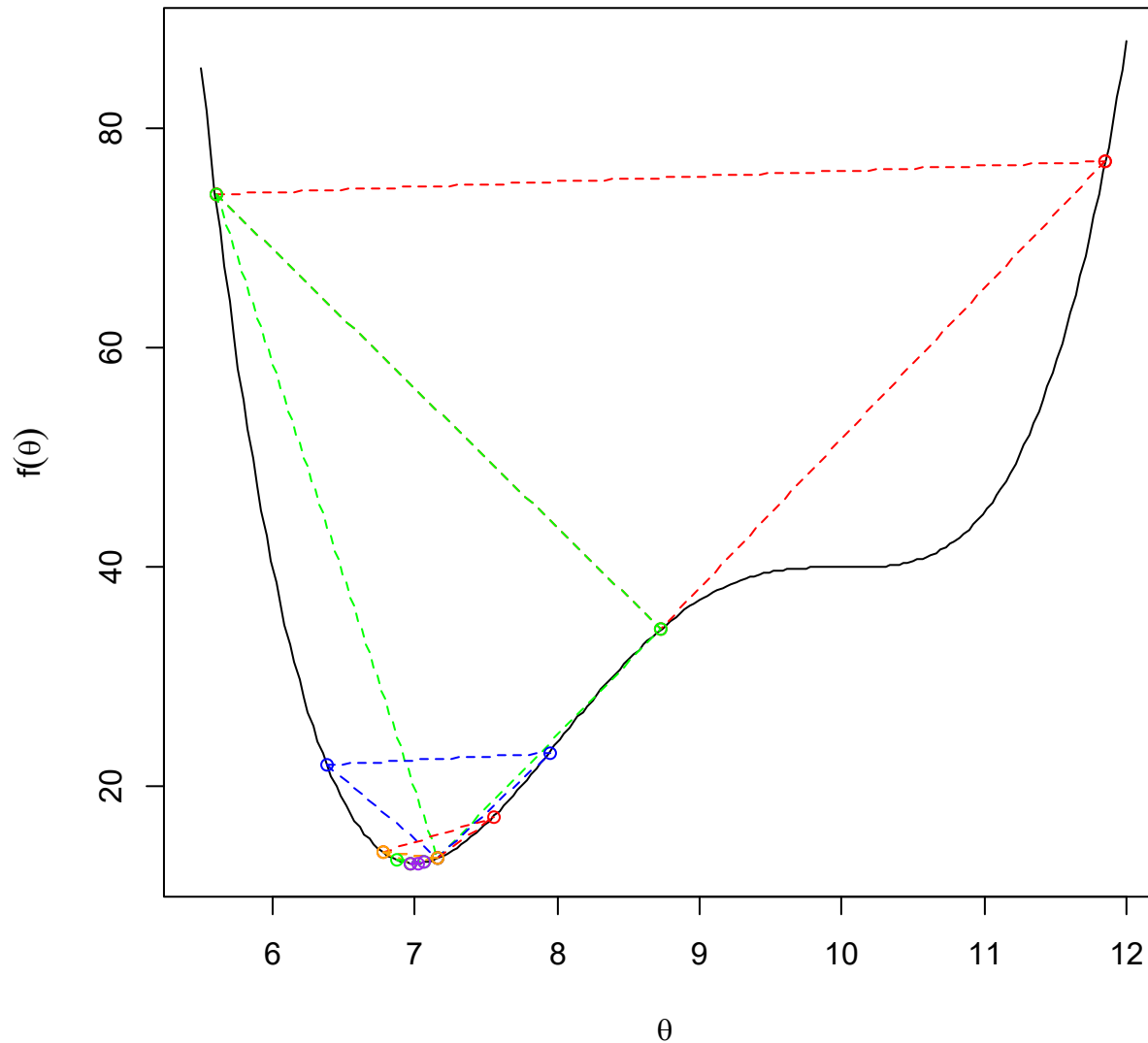
$$y <- b_0 + b_1 * x$$

## Solution:

```
linmod <- function(b_0, b_1, x) {  
  y <- b_0 + b_1 * x  
  return(y)  
}
```

# Descent algorithms

Optimize  $\theta$ : find  $\theta$  such that  $f(\theta)$  is minimum



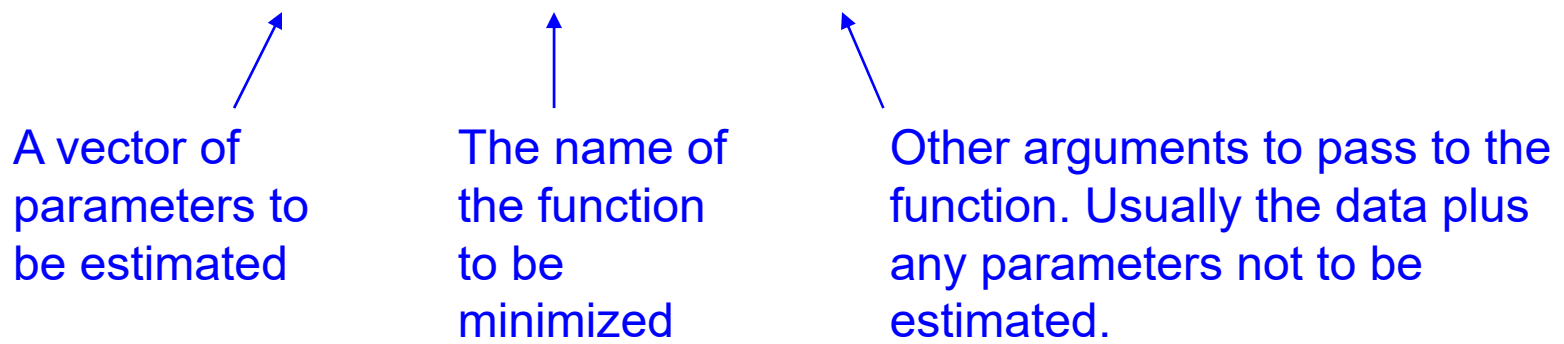
Narrowing in:

keep changing  
parameters in the  
direction that leads to  
lower SSQ

# optim()

- Has various descent and Monte Carlo methods
- **Nelder-Mead** algorithm is default  
(method="Nelder-Mead")

```
optim(par, fn, ...)
```



A vector of  
parameters to  
be estimated

The name of  
the function  
to be  
minimized

Other arguments to pass to the  
function. Usually the data plus  
any parameters not to be  
estimated.

# Training models: general recipe

- 1) biology function
  - complex mechanistic to abstract pattern
- 2) error function
  - e.g. SSQ: distance of the model from the data
$$\text{sum}((\text{observed} - \text{predicted})^2)$$
- 3) optimize
  - find biology parameters that minimize the error
- This recipe is the same no matter how complicated the process model or error function

# Code (train\_ssqr\_optim.R)

## Biology function (linear)

```
linmod <- function(b_0, b_1, x) {  
  y <- b_0 + b_1 * x  
  return(y)  
}
```

Parameters are first argument

Response data

## Error function (SSQ)

```
ssq_linmod <- function(p, y, x) {  
  y_pred <- linmod(b_0=p[1], b_1=p[2], x)  
  e <- y - y_pred  
  ssq <- sum(e^2)  
  return(ssq)  
}
```

Auxiliary data

Call the biology function to get predicted values

Compare predicted to the data

"Unpack" the parameters (self documenting)

## Call to optim

```
par <- c(b_0_start, b_1_start) Starting values for parameters  
fit <- optim(par, ssq_linmod, y=data$y, x=data$x)
```

Need = sign