Today

- Inference algorithms
- Recap & questions from homework
- Results for bootstrapped confidence intervals
 - sharing, questions
- Designing and coding a bootstrapped pvalue algorithm

Homework check in

- Quantity
 - 30% too much
 - 70% just right
- Difficulty
 - 40% too hard
 - 60% just right
- Completion
 - 60% have completed >75%
- Bottleneck: learning to program

Miscellaneous

- Big ideas in data science
- Coding style
 - Working together
 - Agreeing on a style

Git skills

Branching & merging

Sampling distribution algorithm

```
repeat very many times
sample data from the population
fit the model
estimate the parameters
plot sampling distribution (histogram) of the parameter estimates
```

Bootstrap algorithm

```
repeat very many times

generate data based on the sample 
fit the model
estimate the parameters
plot sampling distribution (histogram) of the parameter estimates
```

Bootstrap algorithms

- Non-parametric bootstrap
 - resample the data
- Empirical bootstrap
 - resample the residuals
- Parametric bootstrap
 - generate data from a distribution
 - use estimated parameters of the distribution

Code (e.g. empirical bootstrap)

```
for ( i in 1:10000 ) {
      e boot <- sample(e fit, replace=TRUE)</pre>
      df booty \leftarrow coef(fit)[1] + coef(fit)[2]*df boot<math>x + e boot
      fit boot <-lm(y \sim x, data=df boot)
      boot beta0[i] <- coef(fit boot)[1]</pre>
      boot beta1[i] <- coef(fit boot)[2]</pre>
                 Bootstrap distribution beta_0
                                           Bootstrap distribution beta_1
                                          80
                0.04
 plug in
                0.03
                                                                  Pseudocode
             Density
                                       Density
                                                                  For many times
                0.02
                                                                    Resample errors from model fit (with
                                                                  replacement)
                0.0
                                                                    Create new y-values at original x values
                                                                    Fit the model
                                                                    Keep parameter estimates
                       20
                          30
                             40
                                            8.0
                                                  9.0
                                                      10.0
                                                           11.0
                        boot beta0
                                                  boot beta1
```

Bootstrapped CI

- For β_0 , β_1
- For y|x
- Sharing and questions

Bootstrapped p-value

- Parametric bootstrap for H_0 : $\beta_1 = 0$
 - what is the definition of p-value?
 - what is the algorithm for parametric bootstrap?
 - combine these concepts
- Pseudocode first!
- R code from pseudocode