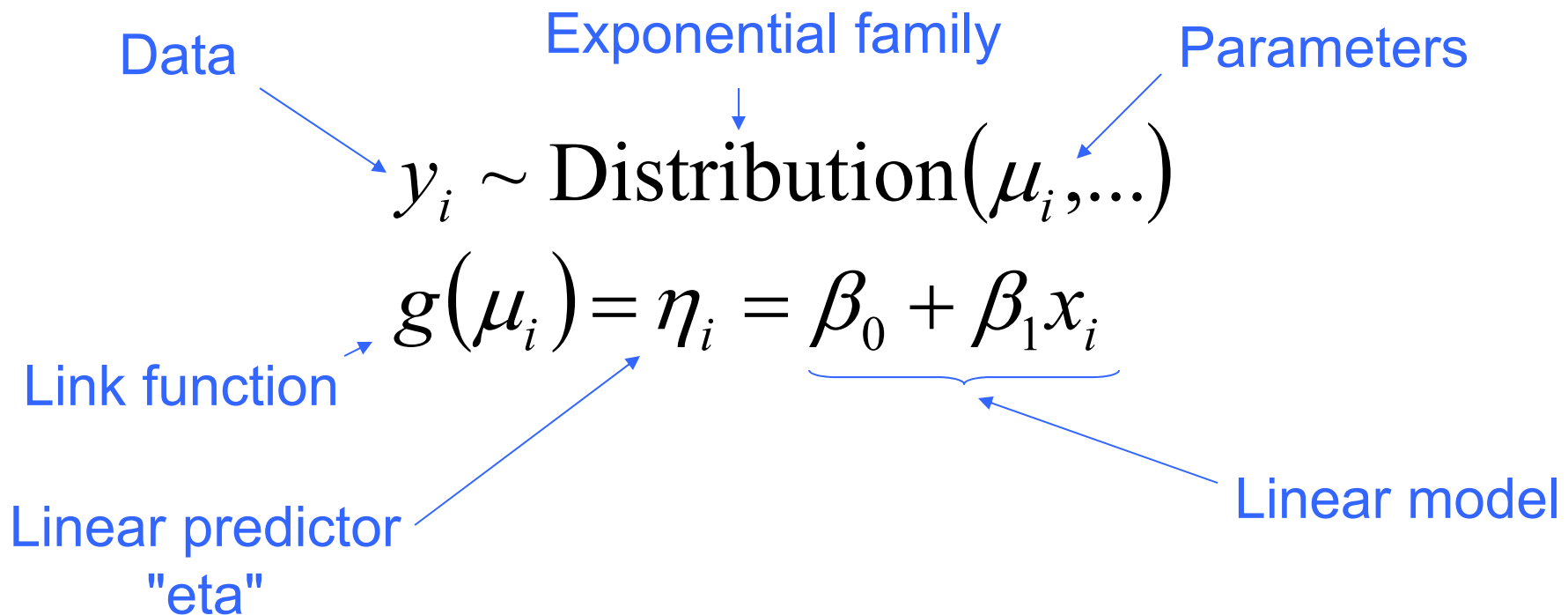


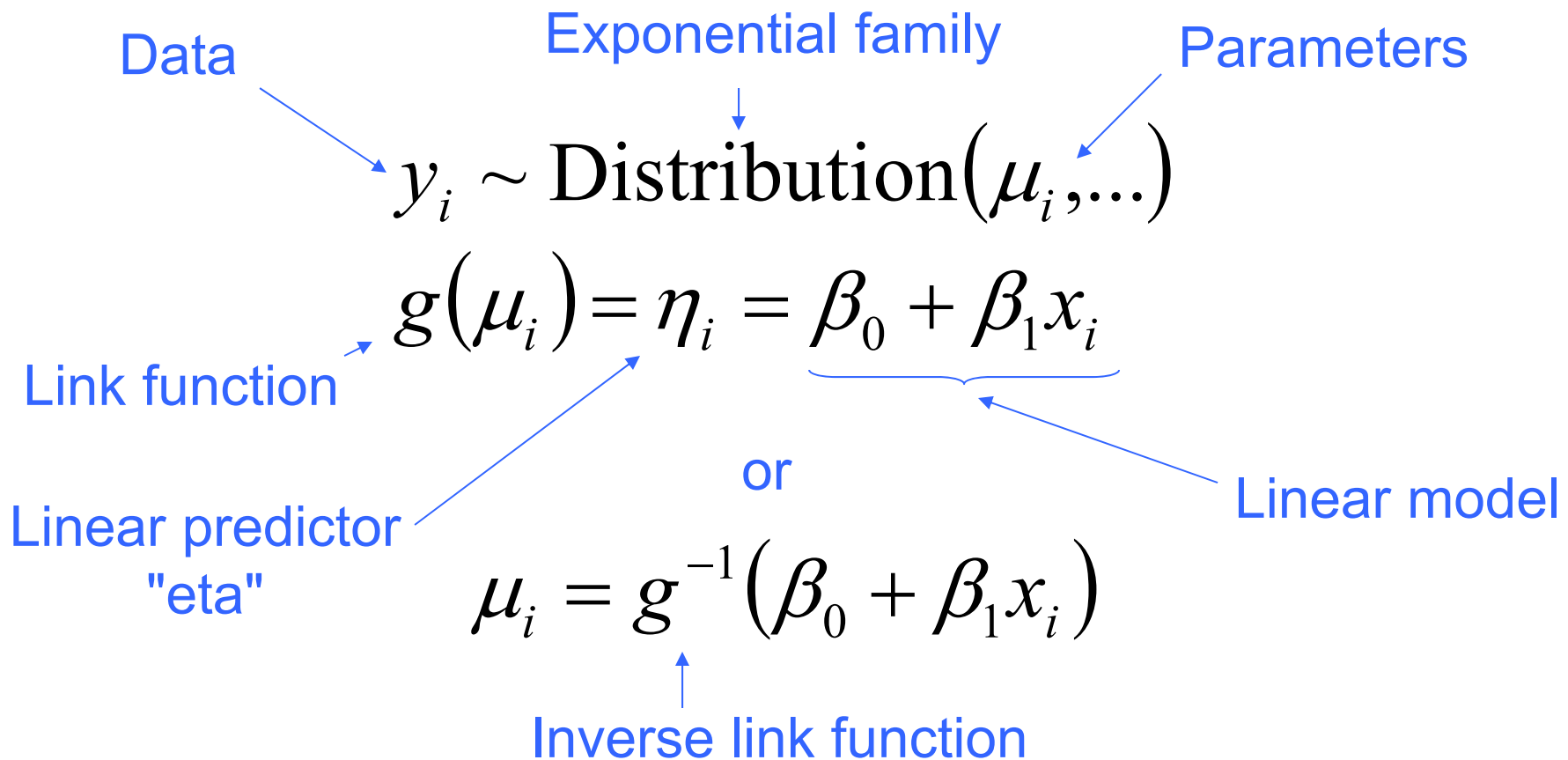
# Main points McElreath Ch 9

- Generalized linear models



# Main points McElreath Ch 9

- Generalized linear models



# Main points McElreath Ch 9

- Exponential family (some)
  - Exponential, Gamma, Normal, Poisson, Binomial
- Link functions (some)
  - identity, log, logit

# Most common models

Normal  
+  
Identity link

$$y_i \sim \text{Normal}(\mu_i, \sigma)$$

$$\mu_i = \beta_0 + \beta_1 x_i$$

Poisson  
+  
Log link

$$y_i \sim \text{Poisson}(\mu_i)$$

$$\log(\mu_i) = \beta_0 + \beta_1 x_i$$

Binomial  
+  
Logit link

$$y_i \sim \text{Binomial}(\mu_i, n)$$

$$\log\left(\frac{\mu_i}{1 - \mu_i}\right) = \beta_0 + \beta_1 x_i$$

Inverse link functions:

$$\mu_i = \eta_i$$

$$\mu_i = e^{\eta_i}$$

$$\mu_i = \frac{e^{\eta_i}}{1 + e^{\eta_i}}$$

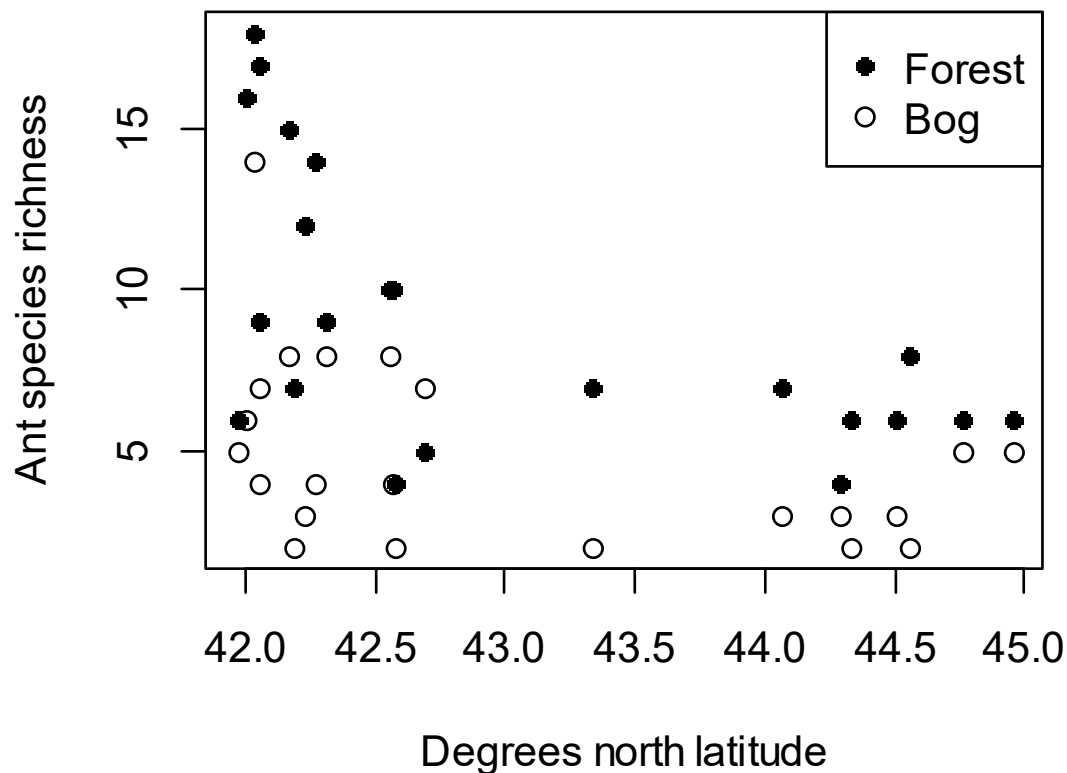
# Dataset to analyze

## Scientific questions:

How different is species richness between habitats?

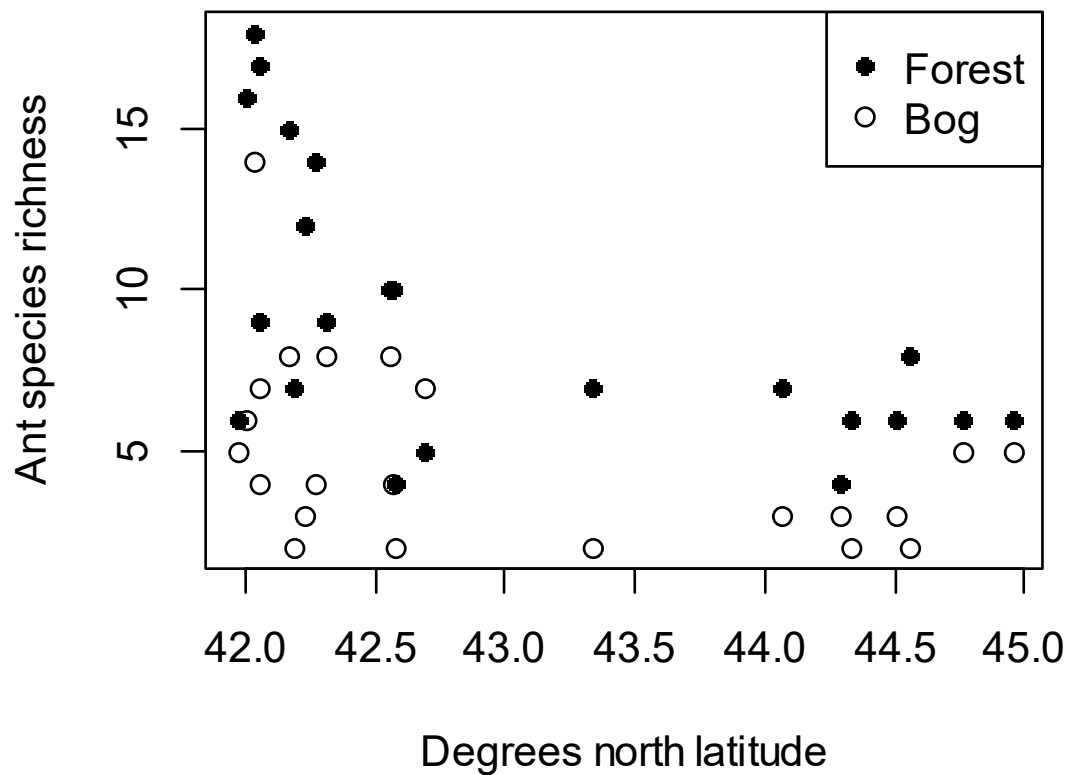
How does species richness vary with latitude?

Is this relationship different between habitats?



What will the data-generating model be?  
Ignore pairs for now

# Dataset to analyze



Model:

Distribution

Link function

Inverse link function

# Model matrix

$$\eta_i = \beta_0 + \beta_1 \text{forest}_i + \beta_2 \text{latitude}_i + \beta_3 \text{forest}_i \times \text{latitude}_i$$

## Data

habitat	latitude	richness
forest	42	16
forest	42.56	10
forest	43.33	7
forest	44.76	6
bog	42.17	8
bog	42.57	4
bog	44.06	3
bog	44.95	5

## Design matrix

intercept	forest
1	1
1	1
1	1
1	1
1	0
1	0
1	0
1	0

## model.matrix(fit)

latitude	forest:latitude
42	42
42.56	42.56
43.33	43.33
44.76	44.76
42.17	0
42.57	0
44.06	0
44.95	0

$$\eta_i = \beta_0 \text{intercept}_i + \beta_1 \text{forest}_i + \beta_2 \text{latitude}_i + \beta_3 \text{forest}_i \times \text{latitude}_i$$