

# Today

- Recap & questions from homework
- Pair programming

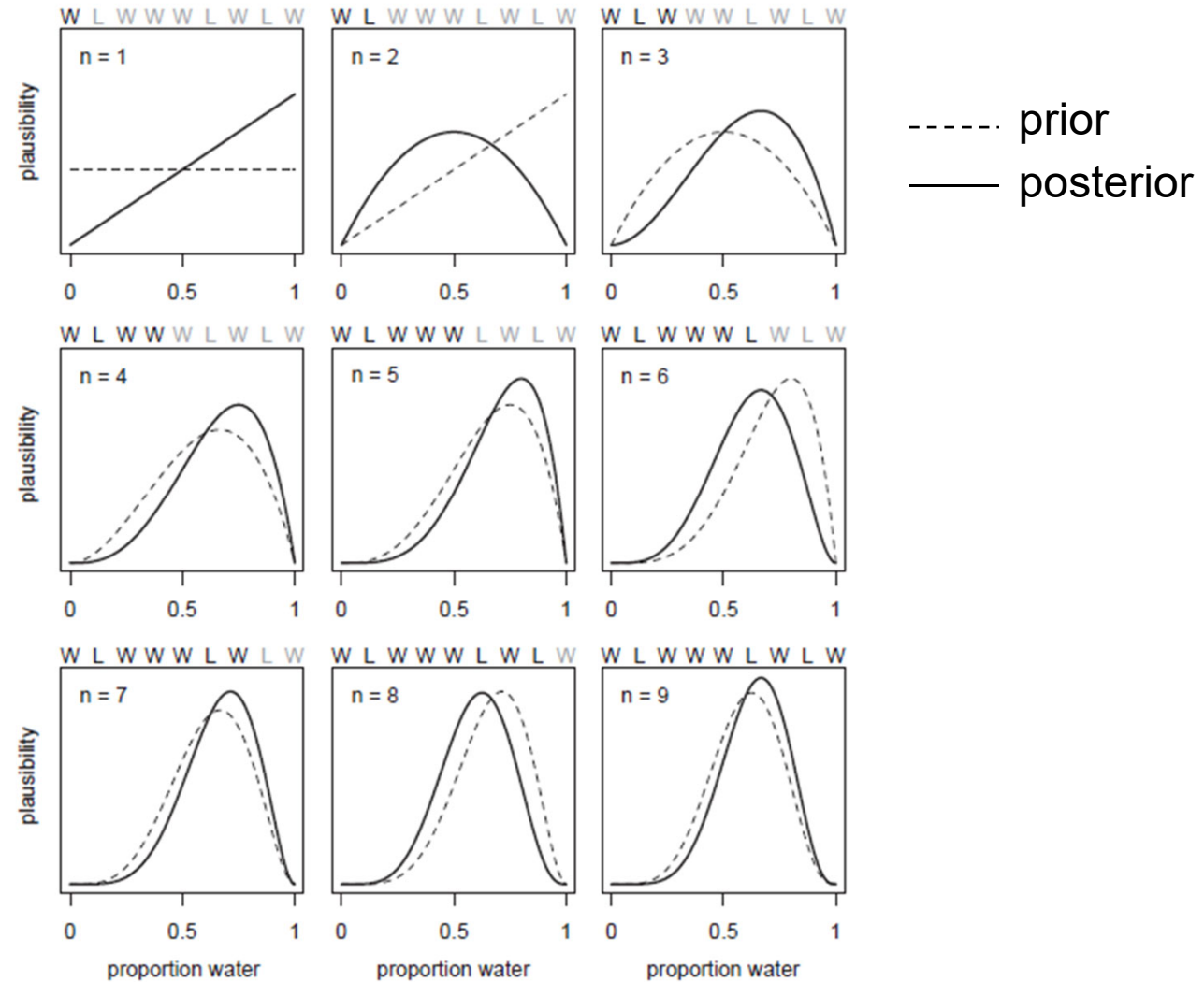
# GitGUI & Gitk

- MacOS
  - install via homebrew
  - <https://git-scm.com/downloads/mac>
  - `$ brew install git-gui`

# Main concepts McElreath 2

- Golem = algorithm
- Small world (model) vs large world (reality)
- Likelihood: counting all the ways data could have happened
- Bayesian updating: prior x likelihood
  - using counts (marbles)
  - using probabilities (marbles; divide by sum of numerator)
  - using distributions (p\_water via Earth toss)

# Bayesian updating



# Pair programming

- Chapter 2
  - Coding Bayesian updating
  - Questions: 2M1, 2M2

# Components of model

## 1) Likelihood

- "data story" = data generating process
- from first principles, or “off the shelf”

## 2) Parameters

- quantities that don't change
- to be estimated

## 3) Prior distribution

## 4) Posterior distribution (inference)

- histogram is the posterior

# Bayesian inference

$$P(B|A) = \frac{P(B)P(A|B)}{P(A)}$$

Bayes' rule for two events A, B

“Posterior”

$$P(\theta|y) = \frac{P(\theta)P(y|\theta)}{P(y)}$$

Model

Data

“Prior”

Likelihood

Total probability of the data

Apply Bayes' rule to convert the likelihood into what we really want to know: the probability of the model given the data

$P(y)$ : probability added up or integrated over all of the models

$$P(y) = \sum_{\theta} P(\theta)P(y|\theta)$$

Discrete parameter

$$P(y) = \int P(\theta)P(y|\theta) d\theta$$

Continuous parameter

# Bayesian inference

$$P(\theta|y) = \frac{P(\theta)P(y|\theta)}{P(y)}$$

Unstandardized posterior

Total probability standardizes the posterior to a probability (discrete parameter) or probability density (continuous parameter)

$$P(y) = \sum_{\theta} P(\theta)P(y|\theta)$$

Discrete parameter

$$P(y) = \int P(\theta)P(y|\theta) d\theta$$

Continuous parameter



# Posterior distribution algorithm

## Algorithm

load data

for each parameter value

    unstandardized posterior = prior \* likelihood

calculate the total probability

for each parameter value

    posterior probability =

        unstandardized posterior / total probability

plot posterior probability vs parameter values

posterior  
distribution

$$P(\theta|y) = \frac{P(\theta)P(y|\theta)}{P(y)}$$

# Discrete parameter

## Algorithm

load data

for each parameter value

unstandardized posterior = prior \* likelihood

total probability = sum(unstandardized posteriors)

for each parameter value

posterior probability =

unstandardized posterior / total probability

plot posterior probability vs parameter values

posterior  
distribution

$$P(y) = \sum_{\theta} P(\theta)P(y|\theta)$$

probability mass function (pmf)

$$P(\theta|y) = \frac{P(\theta)P(y|\theta)}{P(y)}$$

# Discrete parameter

- Uncommon
- Usually a latent (hidden) state
- Examples
  - male/female in population model
  - occupied/unoccupied in species occupancy model

# Continuous parameter

## Exact algorithm

load data

define grid of parameter values

for each parameter value

unstandardized posterior = prior \* likelihood

total probability = integral(unstandardized posterior function)

for each parameter value

posterior Pr density =

unstandardized posterior / total probability

plot posterior Pr density vs parameter values

posterior  
distribution

area under curve

$$P(y) = \int P(\theta)P(y|\theta) d\theta$$

probability density function (pdf)

$$P(\theta|y) = \frac{P(\theta)P(y|\theta)}{P(y)}$$

# Continuous parameter

## Grid approximation algorithm

load data

define grid of parameter values with resolution  $r$

for each parameter value

unstandardized posterior = prior \* likelihood

total probability =  $\text{sum}(\text{unstandardized posteriors}) * r$

for each parameter value

posterior Pr density =

unstandardized posterior / total probability

plot posterior Pr density vs parameter values

posterior  
distribution

numerical integration

$$P(y) = \int P(\theta)P(y|\theta) d\theta$$

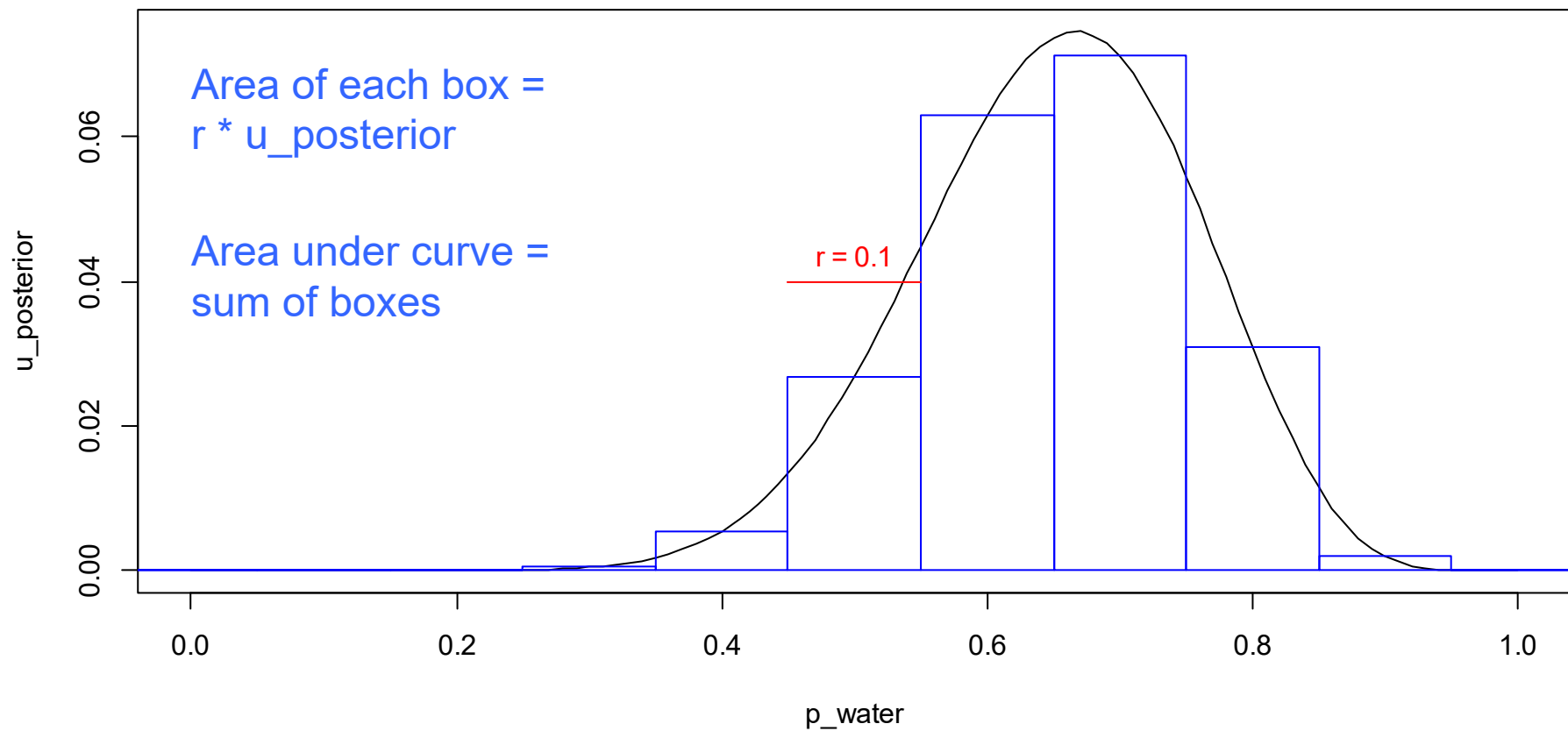
probability density function (pdf)

$$P(\theta|y) = \frac{P(\theta)P(y|\theta)}{P(y)}$$

approximate  
area under curve

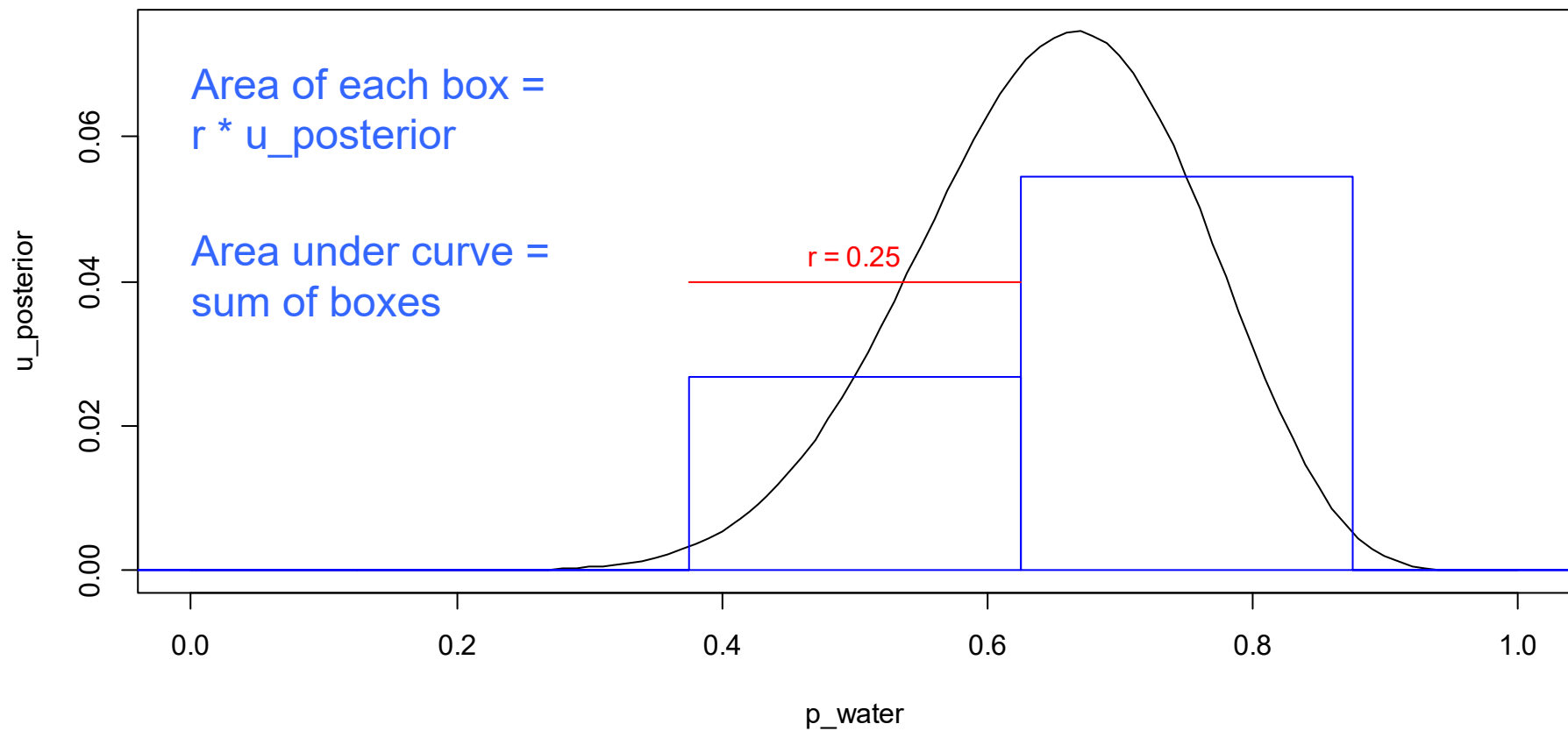
# Numerical integration

Approximating area under the curve



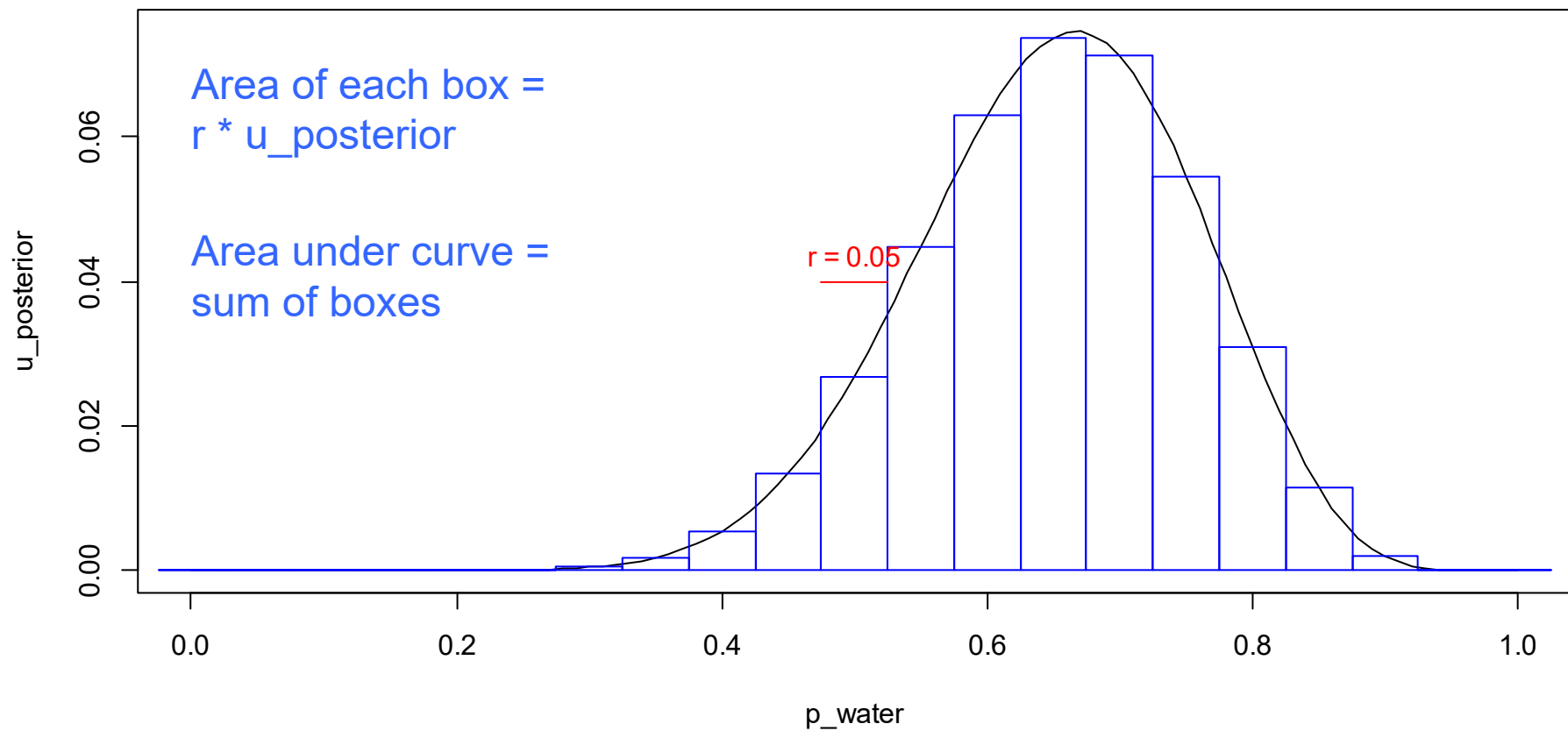
# Numerical integration

Approximating area under the curve



# Numerical integration

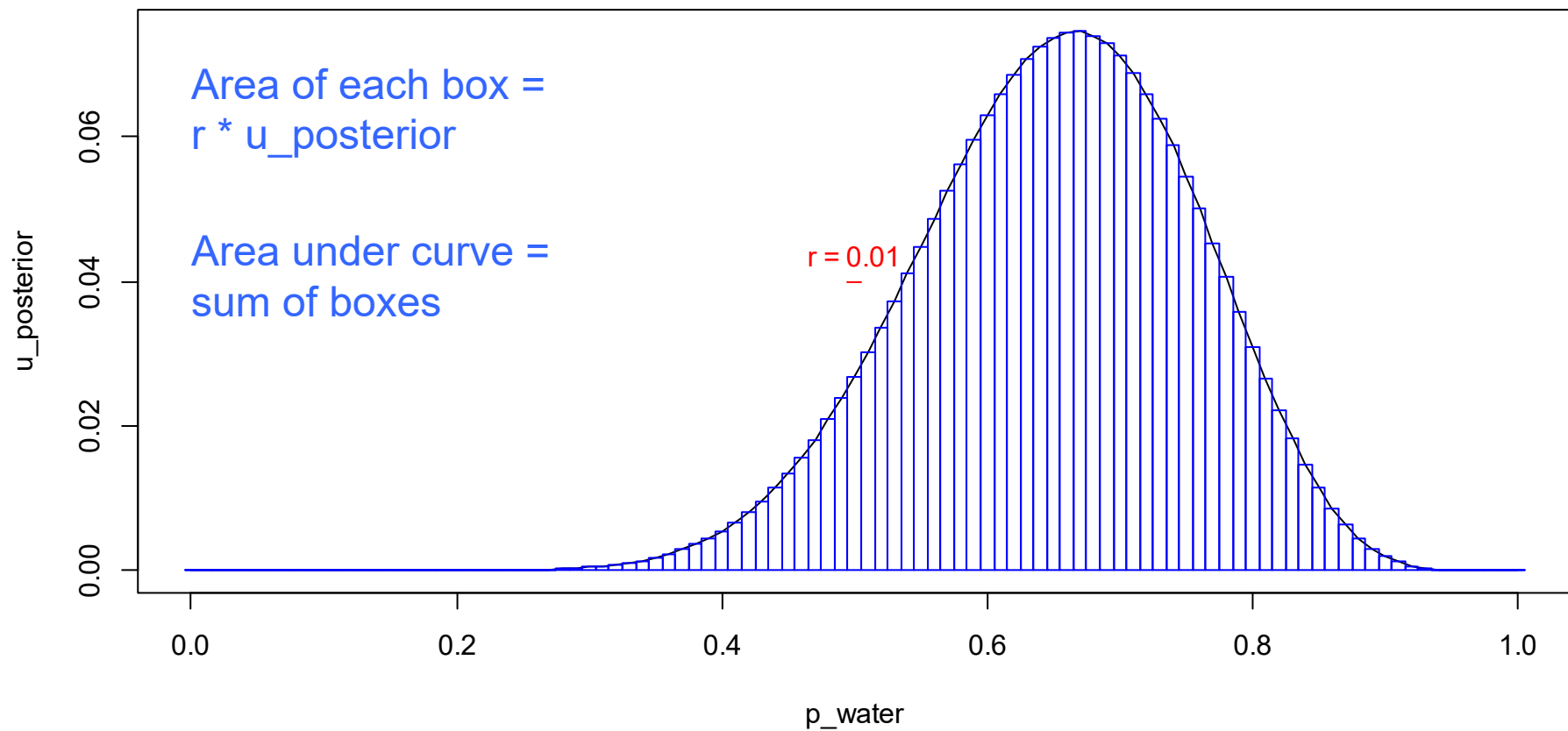
Approximating area under the curve





# Numerical integration

Approximating area under the curve



# Numerical integration

Approximating area under the curve

