

# Today

- Poisson data generating processes
- Study design: part of the DGP
- Scope of inference

# Common DGP models

Normal

Lognormal:  $\ln(y)$

Poisson

Binomial

Bernoulli:  $n=1$

$$y_i \sim \text{Normal}(\mu_i, \sigma)$$

$$y_i \sim \text{Poisson}(\mu_i)$$

$$y_i \sim \text{Binomial}(\mu_i, n)$$

alternative  $\mu : \lambda$

alternative  $\mu : p$

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## Key properties:

$y$ :  $-\infty$  to  $\infty$ , continuous  
 $\mu$ :  $-\infty$  to  $\infty$ , continuous

$y$ : 0 to  $\infty$ , discrete, integer  
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 $\mu$ : 0 to 1, probability

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# Poisson

- Code the DGP
- Simulation to show  $\text{variance} = \text{mean}$

# Poisson GLM

Poisson

+

Log link

$$y_i \sim \text{Poisson}(\mu_i)$$

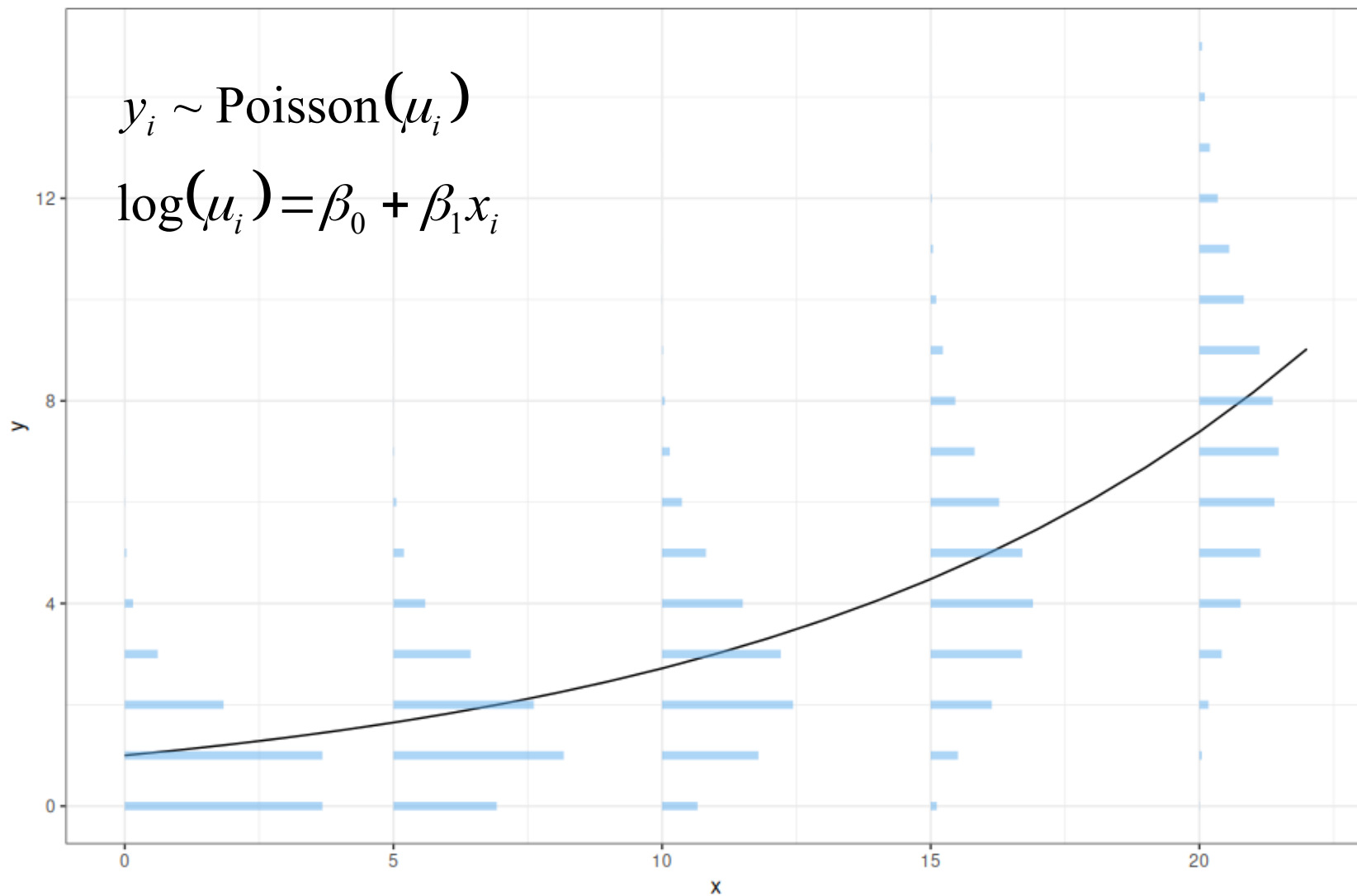
$$\log(\mu_i) = \beta_0 + \beta_1 x_i$$

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# Poisson GLM



# Poisson scenario

- Ant species richness
- Declines with latitude
- Possible DGPs?
- Possible study designs?

# Scope of inference

- What statistical **population** do you want the study to **generalize** to?
- Generalization is determined by **study design** and assumptions we're willing to accept (wrt data  $\rightarrow$  population)
- Causal or descriptive?
- Randomization, replication, control
- Structure in space and time