

Today

- Poisson data generating processes
- Study design: part of the DGP
- Scope of inference

Common DGP models

Normal

Lognormal: $\ln(y)$

$$y_i \sim \text{Normal}(\mu_i, \sigma)$$

Poisson

$$y_i \sim \text{Poisson}(\mu_i)$$

alternative $\mu: \lambda$

Binomial

Bernoulli: $n=1$

$$y_i \sim \text{Binomial}(\mu_i, n)$$

alternative $\mu: p$

Key properties:

y : $-\infty$ to ∞ , continuous
 μ : $-\infty$ to ∞ , continuous

y : 0 to ∞ , discrete, integer
 μ : 0 to ∞ , continuous

y : 0 to n , discrete, integer
 μ : 0 to 1, probability

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Poisson

- Code the DGP
- Simulation to show variance = mean

Poisson GLM

Poisson

+

Log link

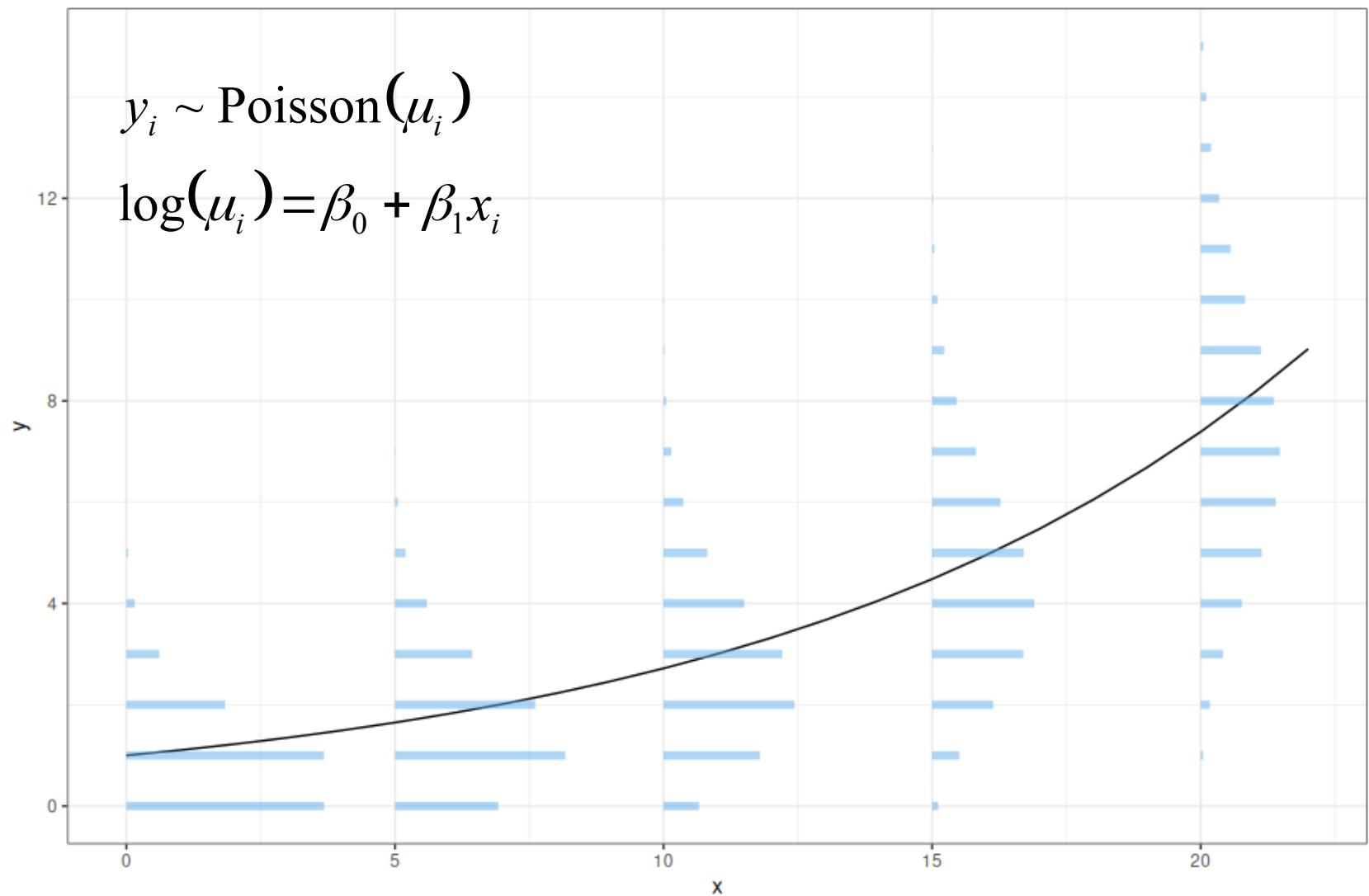
$$y_i \sim \text{Poisson}(\mu_i)$$

$$\log(\mu_i) = \beta_0 + \beta_1 x_i$$

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Poisson GLM



Poisson scenario

- Ant species richness
- Declines with latitude
- Possible DGPs?
- Possible study designs?

Scope of inference

- What statistical population do you want the study to generalize to?
- Generalization is determined by study design and assumptions we're willing to accept (wrt data → population)
- Causal or descriptive?
- Randomization, replication, control
- Structure in space and time