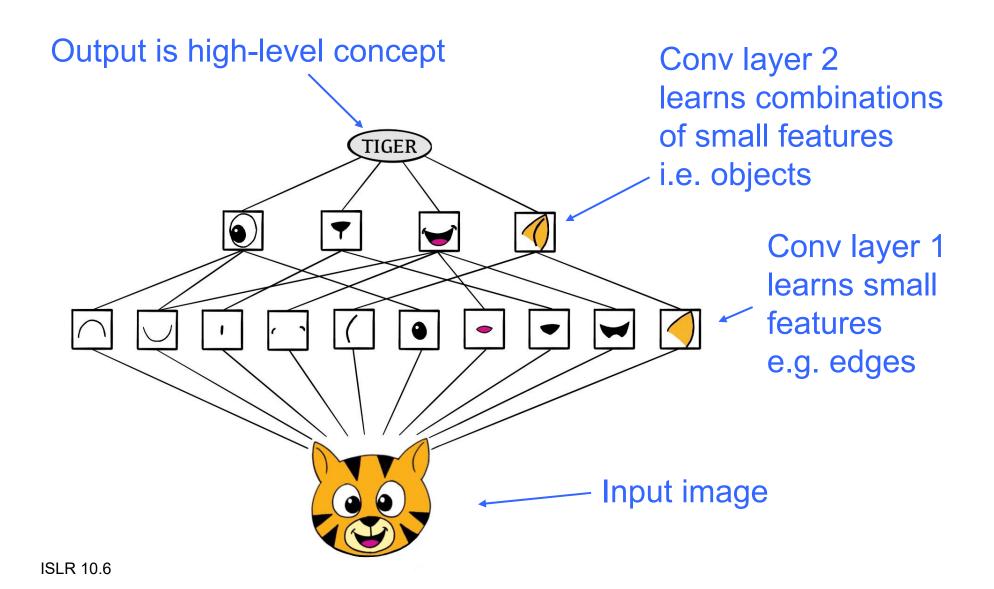
Today

- Neural networks and deep learning
 - Single layer neural networks
 - using keras package
 - architectures for different questions
 - regression, classification, multifunction
 - Multi-layer neural networks
 - Convolutional neural networks
 - U-net
 - Transformers

deep

Convolutional NNs



Convolutional NNs

- Example: CIFAR100
 - standard benchmark dataset: 100 categories
 - ecology subset: 61 categories
- 08 4 convolutional nnet.R

Input image matrix
$$\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \\ j & k & l \end{bmatrix}$$

$$\begin{bmatrix} lpha & eta \ \gamma & \delta \end{bmatrix}$$

Output matrix
$$\begin{bmatrix} a\alpha + b\beta + d\gamma + e\delta & b\alpha + c\beta + e\gamma + f\delta \\ d\alpha + e\beta + g\gamma + h\delta & e\alpha + f\beta + h\gamma + i\delta \\ g\alpha + h\beta + j\gamma + k\delta & h\alpha + i\beta + k\gamma + l\delta \end{bmatrix}$$

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$$b\alpha + c\beta + e\gamma +$$

$$e\alpha + f\beta + h\gamma + i\delta$$

$$h\alpha + i\beta + k\gamma + l\delta$$

Input image matrix
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Convolution filter

$$\begin{bmatrix} \alpha & \beta \\ \gamma & \delta \end{bmatrix}$$

convolve

$$\begin{bmatrix} a\alpha + b\beta + d\gamma + e\delta \\ d\alpha + e\beta + g\gamma + h\delta \\ g\alpha + h\beta + j\gamma + k\delta \end{bmatrix}$$

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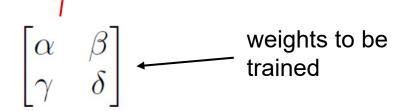
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Convolution filter



Dimension determined by rows & cols of the filter windows

Output matrix
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input image filter convolved image vertical features horizontal features

Condenses information

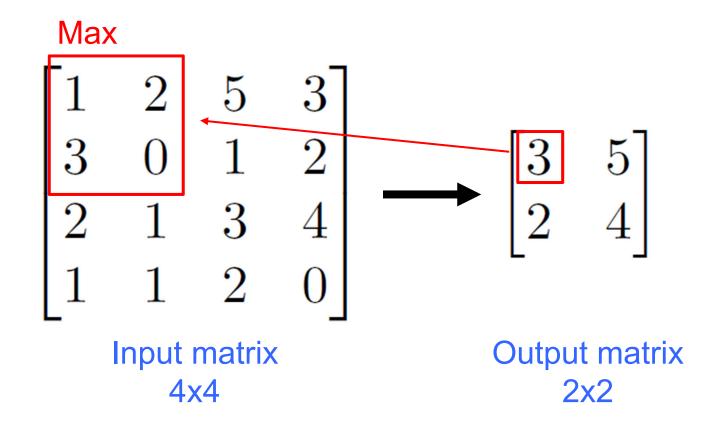
e.g. "Max pooling"

$$\begin{bmatrix} 1 & 2 & 5 & 3 \\ 3 & 0 & 1 & 2 \\ 2 & 1 & 3 & 4 \\ 1 & 1 & 2 & 0 \end{bmatrix} \longrightarrow \begin{bmatrix} 3 & 5 \\ 2 & 4 \end{bmatrix}$$

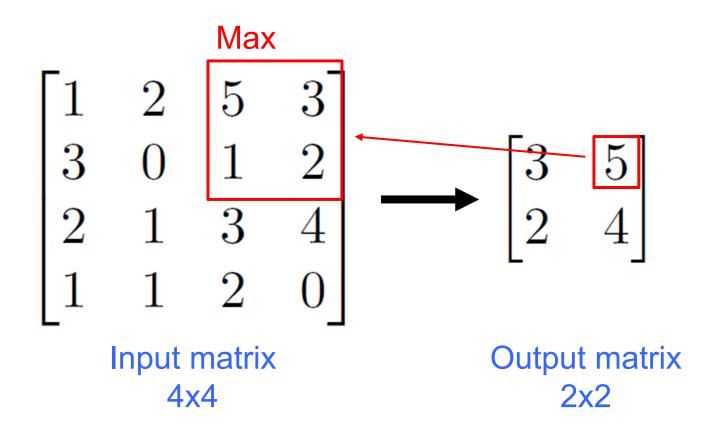
Input matrix 4x4

Output matrix 2x2

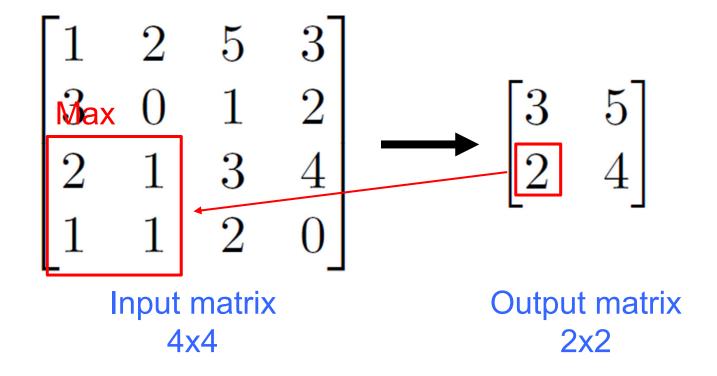
Condenses information



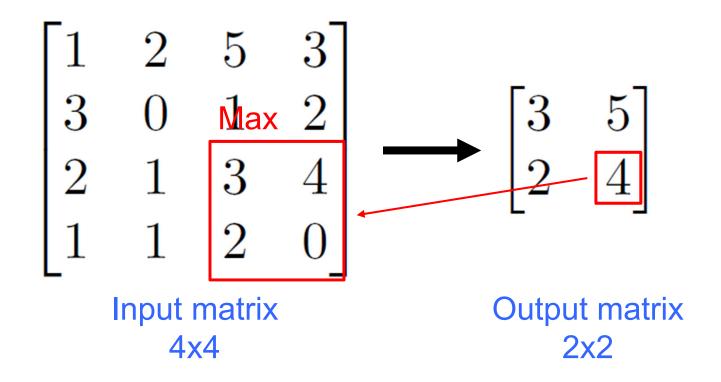
Condenses information



Condenses information



Condenses information



Architecture

