Today

- **Ensemble methods**
  - Bagging
  - Random forest

Random forest

for many repetitions

      randomly select m predictor variables

      resample the data (rows) with replacement

      train the tree model

      record prediction

final prediction = mean of predictions

Random forest as R

```r
# Parameters
m <- 2 #Number of predictors to sample at each iteration
boot_reps <- 500

# Setup
n <- nrow(ants)
c <- ncol(ants)
nn <- nrow(grid_data)
boot_preds <- matrix(rep(NA, nn*boot_reps), nrow=nn, ncol=boot_reps)

# Main algorithm
for ( i in 1:boot_reps ) {
#    randomly select m predictor variables
    predictor_indices <- sample(2:c, m)
    boot_data <- ants[,c(1,predictor_indices)]
#    resample the data (rows) with replacement
    boot_indices <- sample(1:n, n, replace=TRUE)
    boot_data <- boot_data[boot_indices,]
#    train the tree model
    boot_fit <- tree(richness ~ ., data=boot_data)
#    record prediction
    boot_preds[,i] <- predict(boot_fit, newdata=grid_data)
}
rf_preds <- rowMeans(boot_preds)
```
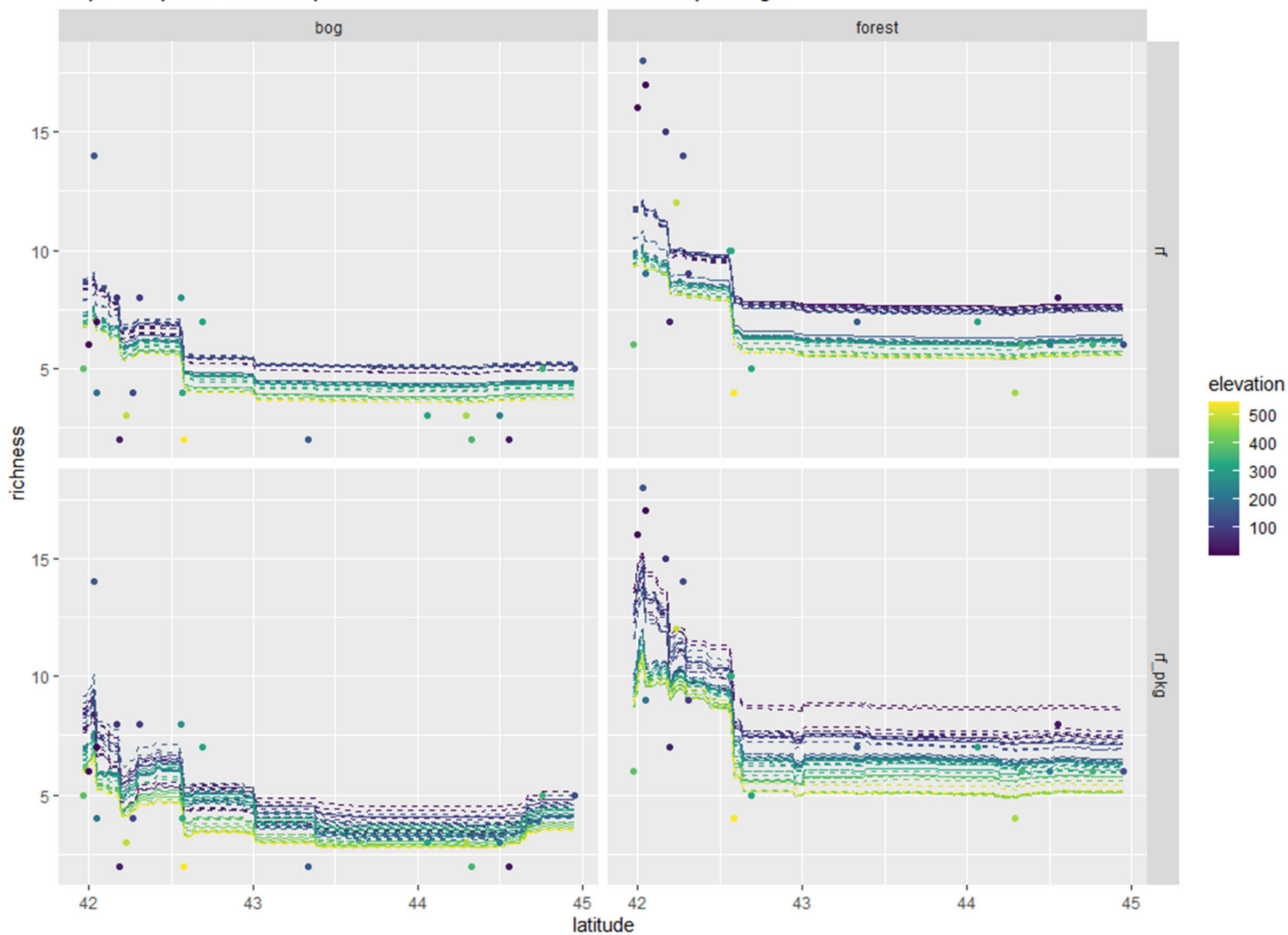
the new bit
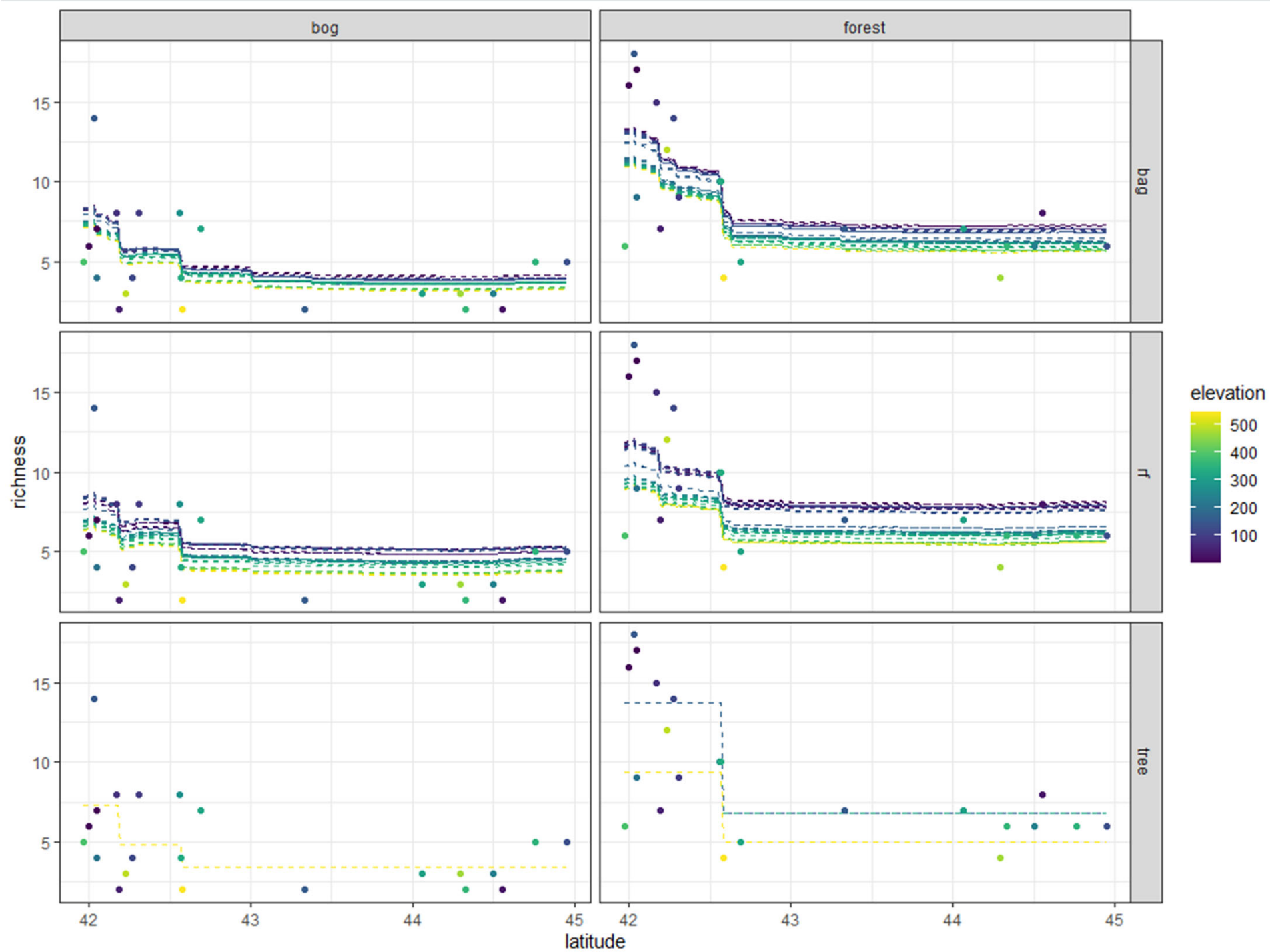
Full implementation

- Randomly draws variables at every tree split

- Generates lots of variety among trees

R packages

- randomForest
  - original Breimen (2001) algorithm
  - Fortran

- ranger
  - fast implementation
  - C++

Top row: proof of concept code. Bottom row: randomForest package

```
randomForest(richness ~ ., data=ants, ntree=500, mtry=2)
```

Inference algorithm

- k-fold CV
  - most general strategy
  - expensive, as we've seen
  - use to compare with other models
- Out-of-bag estimate
  - specific to bagging and random forest
  - can use for tuning number of trees and number of models to try

"Out of bag" error estimate

- Out of bag samples
  - data not included in a bootstrap sample
  - on average ca 1/3 are out of bag
- Each bootstrap, use the out of bag samples to gauge prediction error
  - average error across trees within a forest
- Approx equal to LOOCV (n_trees = large)
- Computationally efficient
  - part of the bagging step

Tuning number of trees with OOB error: ants data
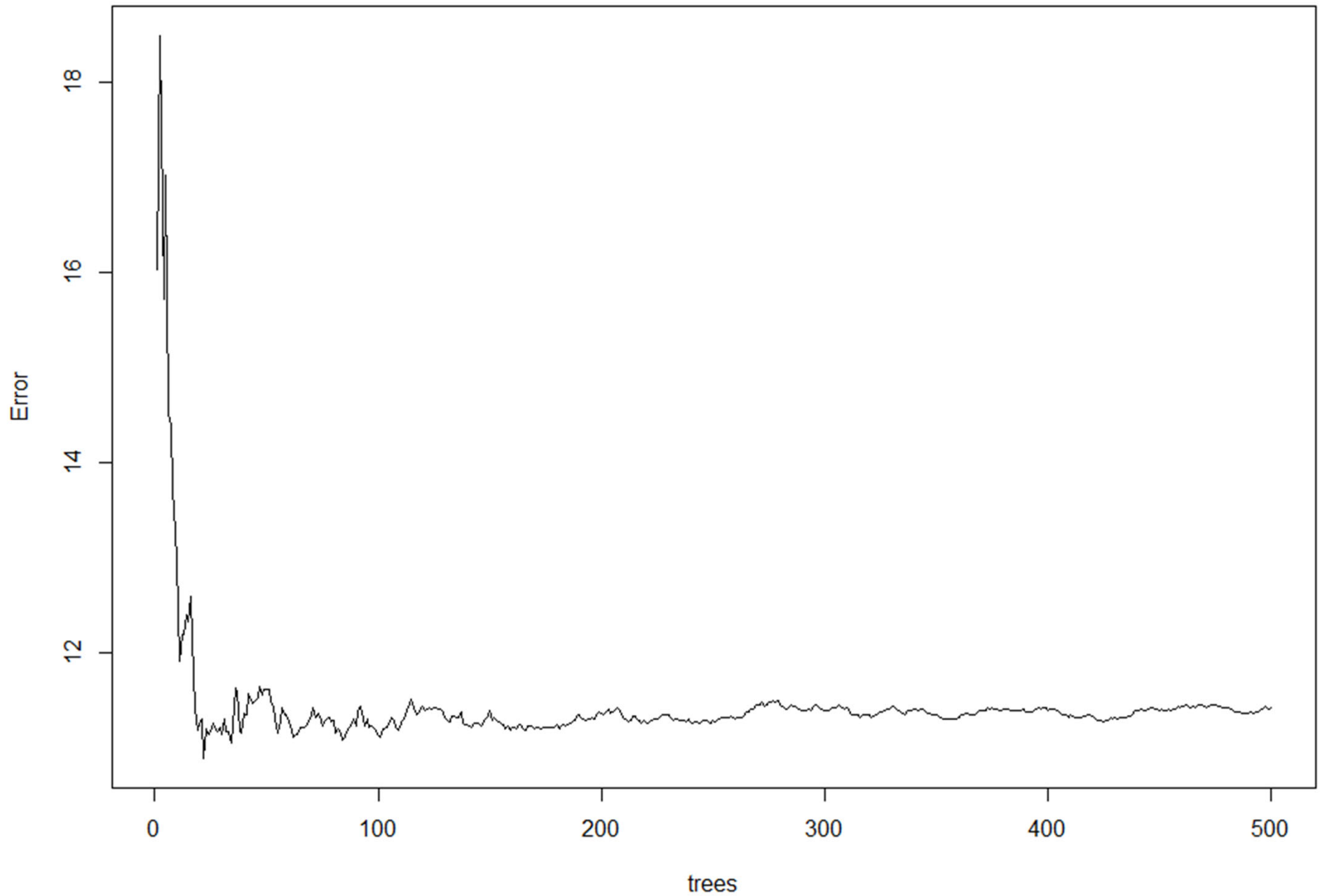
Variable importance

- Average RSS decrease over branch splits for each variable

- Interpretation:

  – more reduction in RSS = more "important"

- Similar to regression concept of "explaining more variation"

- Advantage: explainable machine learning

Variable importance: ants data

latitude

elevation

habitat

IncNodePurity
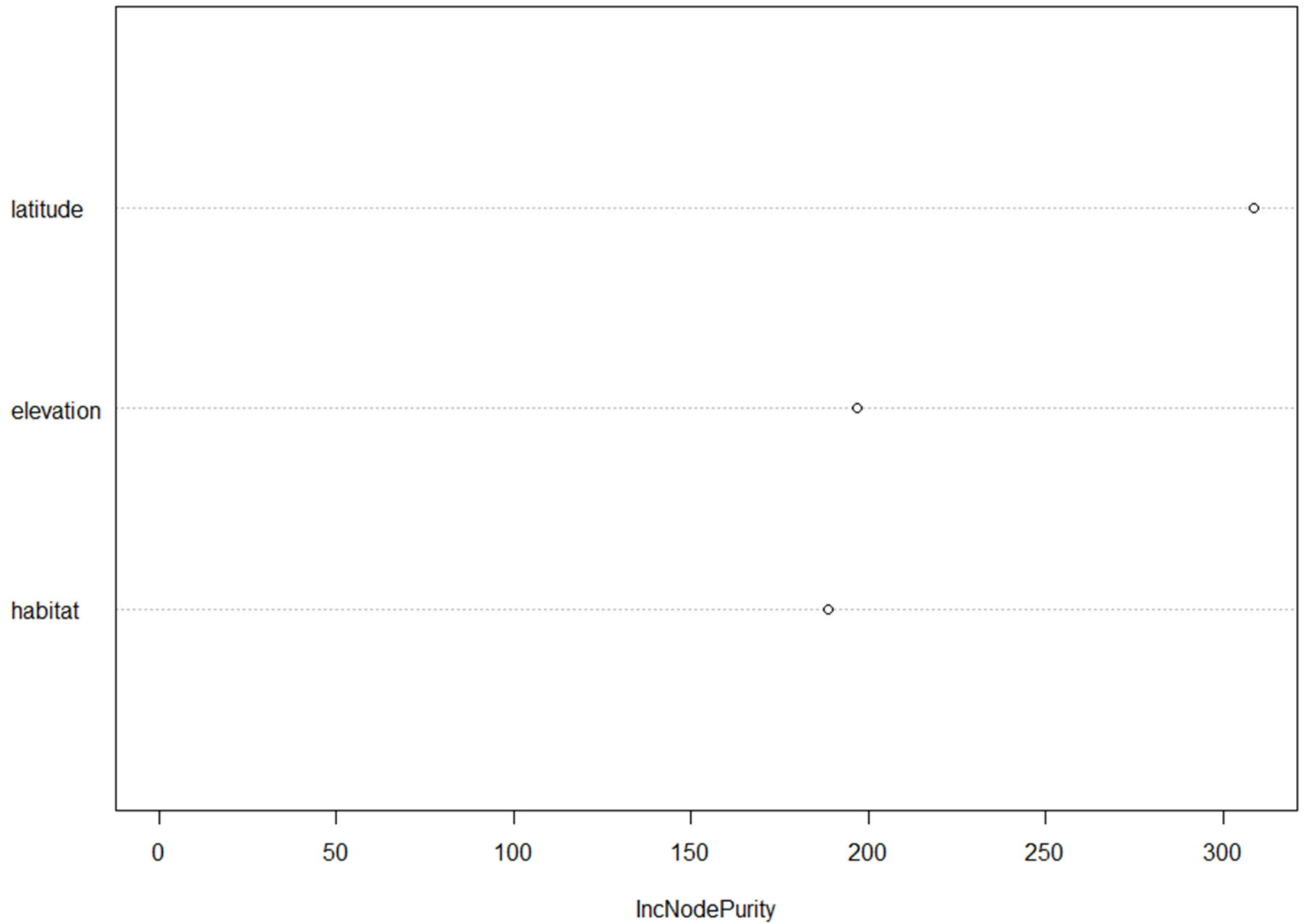
Bagging is a special case

bagging: mtry = number of variables

Random forest compared to bagged regression tree