

- Norm:

Typically, we use norm for vectors: $\|e\|_p = \sqrt[p]{\sum |e_i|^p}$

So, we have:

$$\text{if } p=1, \quad \|e\|_1 = \sum |e_i|$$

$$\text{if } p=2, \quad \|e\|_2 = \sqrt{\sum e_i^2} = e^T e$$

$$\text{if } p=\infty, \quad \|e\|_\infty = \max_i |e_i|$$

Application:

When considering optimization with norm, we always consider 2-th norm,

Because if e_i is smooth, then 2-th norm is always smooth