

ECCO Modeling Utilities (EMU)



Version 1.0

User Guide

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DRAFT April 5, 2024

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1. Introduction

This document describes the ECCO Modeling Utilities (EMU), a set of computational tools summarized in <u>Table 1</u> for analyzing the ECCO ocean state estimate (presently Version 4 release 4, V4r4, https://www.ecco-group.org/products-ECCO-V4r4.htm). EMU is geared toward analyzing the *model* underlying the ECCO estimate, as opposed to exploring its *discrete state output* in itself (Table 2), so as to study the physical relationships governing variables in space, time and type that are difficult to infer from the state alone (e.g., causation).

EMU is *menu-driven* with no modeling expertise required for its usage, aimed at separating the technical tasks of devising and implementing model computations (what EMU does) from the scientific application of these calculations (what EMU enables). The tools are based on those employed in *Fukumori et al.* [2021] where examples of their application can be found.

	Tool	Description		
1	Sampling	Evaluates time-series of <i>user-specified quantity</i> .		
2	Forward Gradient	Computes model's response to <u>user-specified change in</u> <u>forcing</u> (forward gradient).		
3	Adjoint	Computes sensitivity of <u>user-specified quantity</u> to different forcing (adjoint gradient).		
4	Convolution	Evaluates convolution of <u>user-specified adjoint</u> gradients and <u>forcing</u> (adjoint gradient decomposition).		
5	Tracer	Computes evolution of <u>user-defined passive tracer</u> and <u>its</u> <u>adjoint</u> .		
6	Budget	Evaluates variables and fluxes underlying the budget of user-specified quantity		
7	Modified Simulation	Conducts simulation with <u>user-defined changes</u> (e.g., forcing, diagnostic output)		
8	Attribution	Evaluates contributions to time-series of <u>user-specified</u> <u>quantity</u> from separate <u>types</u> of controls.		

Table 1: ECCO Modeling Utilities (EMUs)¹

EMU's model is a *flux-forced* version of ECCO's Version 4 release 4 (V4r4) ocean model (*Wang et al., 2021, 2022*). Whereas the V4r4 state estimate employs bulk formulae that diagnostically evaluate the interactions (forcing) among ocean, atmosphere, and sea ice, the *flux-forced* version employs fluxes associated with these interactions as pre-computed input saved from the V4r4 estimate. Results of the two models are virtually identical to each other. The *flux-forced* formulation provides a convenient means for evaluating the effects of separate processes (e.g., heat flux, freshwater flux) as opposed to those of individual atmospheric state (e.g., air temperature, humidity). This *flux-forced* version of ECCO's V4r4 ocean model will be referred to simply as the *model* in this guide. The pre-computed V4r4 equivalent output from this *model*,

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¹ Tools described as "evaluating" analyze *model* output provided with EMU and/or output from other Tools that run the *model* anew.

hereafter referred to as the *reference run* (emu_ref), is part of EMU and is downloadable along with the Tools (Section 4).

2. What the Individual Tools do

2.1. Sampling Tool

The Sampling Tool evaluates time-series of a user-defined variable from the *reference run* (emu_ref) and/or its variations (Section 2.7), hereafter the *Objective Function* (*J*, OBJF), also known as the *cost function* or *quantity of interest*. The Objective Function can simply be one of the *standard state variables* v (Table 2) at a particular model grid point or a user-defined linear function (combination, transformation) of these variables (e.g., spatial integral, steric sea level). In its general form, the Objective Function is written as,

$$J(t) = \sum_{i} \alpha_{i} \sum_{\mathbf{x}} \mathbf{T}_{i}(\mathbf{x}) v_{i}(\mathbf{x}, t)$$
 (1)

Here, t is time, α is a scalar multiplication factor (scaling), \mathbf{T} is a linear operator (weight, mask) in space (\mathbf{x}), and subscript i distinguishes different variables. (The Tool allows the Objective Function to be a combination of any number of variables.)

The Sampling Tool is useful for assessing the fidelity of V4r4 (e.g., comparison to observations) and, thereby, the suitability of the ECCO *model* and EMU's other tools for an application. Users are advised to look for resources elsewhere in case the ECCO estimate is found to be inconsistent with users' observations of interest.

Index	Variable	Unit	Description	temporal mean
1	ssh	m	dynamic sea level	daily & monthly
2	obp	m	ocean bottom pressure (unit in equivalent sea level)	daily & monthly
3	theta	°C	potential temperature	monthly
4	salt	PSU	salinity	monthly
5	uvel	m/s	i-direction velocity	monthly
6	vvel	m/s	j-direction velocity	monthly

Table 2: **Standard model state variables** (*v*) available as daily and/or monthly means.

2.2. Forward Gradient Tool

The Forward Gradient Tool computes the model's response to unit changes in forcing (aka control); i.e., forward gradient,

$$\frac{\partial v(\mathbf{x},t)}{\partial \phi(\mathbf{r},s)} \tag{2}$$

Here, the numerator $v(\mathbf{x},t)$ is a standard state variable (Table 2) at location \mathbf{x} and time t. $\phi(\mathbf{r},s)$ in the denominator, chosen by the user, is a particular forcing (Table 3) at a specific location \mathbf{r} and time s. The Forward Gradient Tool computes this gradient for all standard state variables v (Table 2) at different locations \mathbf{x} and time t of the model.

The gradients are useful for studying the *model's* response to change in forcing and for assessing the accuracy of the *model's* adjoint gradients (Adjoint Tool, Section 2.3).

Index	Variable Name	Unit	Description
1	empmr	kg/m ² /s	upward freshwater flux
2	pload	N/m ²	downward surface pressure load
3	qnet	W/m ²	net upward heat flux
4	qsw	W/m^2	net upward shortwave radiation
5	saltflux	$g/m^2/s$	net upward salt flux
6	spflx	$g/m^2/s$	net downward salt plume flux
7	tauu	N/m ²	westward wind stress
8	tauv	N/m ²	southward wind stress

Table 3: Model Forcing (ϕ) . Forcing perturbation is defined weekly. Salt flux (saltflux and spflx) is associated with the ocean's interaction with sea ice. All other fluxes combine ocean's interactions with both atmosphere and sea ice.

The Forward Gradient Tool computes the gradient (Eq 2) by finite difference, i.e., as the difference of the state (v) between a model integration with and without the forcing perturbation, divided (normalized) by the amplitude of that perturbation. Namely,

$$\frac{v(\mathbf{x},t;\phi') - v(\mathbf{x},t;\phi)}{\delta\phi} \approx \frac{\partial v(\mathbf{x},t)}{\partial \phi(\mathbf{r},s)}$$
(3)

Here on the left-hand-side, the model's forcing used in deriving the state is noted parametrically, i.e., $v(\mathbf{x},t;\phi)$ denotes model state v at location \mathbf{x} and time t using forcing ϕ . ϕ' is identical to ϕ except at location \mathbf{r} and time s where it has been perturbed by $\delta\phi$, viz.,

$$\phi'(\mathbf{r},s) = \phi(\mathbf{r},s) + \delta\phi \tag{4}$$

The user choses $\delta \phi$ among the different controls that are available (Table 3), its magnitude, spatial location (\mathbf{r}), and specific instant (s) defined at 7-day intervals, starting from 12Z January 01, 1992, which is the starting instant of ECCO V4r4. The model time-step is 1-hour and the forcing perturbation is interpolated linearly in time. The Tool integrates the model with the perturbation and evaluates the gradient (Eq 3) as daily and/or monthly means corresponding to the standard model state (Table 2). The second term in the numerator on the left-hand-side of Eq 3 is the un-perturbed model, viz., the reference run (emu_ref).

2.3. Adjoint Tool

The Adjoint Tool computes the model's sensitivity to different forcing, i.e., adjoint gradient,

$$\frac{\partial \overline{J}(t_g)}{\partial \phi(\mathbf{r},s)} \tag{5}$$

Here the numerator $\overline{J}(t_g)$ is a user-defined mean Objective Function (<u>Eq 1</u>) defined as,

$$\overline{J}(t_g) = \frac{1}{t_g - t_{start}} \int_{t_{start}}^{t_g} J(t) dt$$
 (6)

i.e., time-mean of J between some instances t_{start} and t_g . Time t_g is the nominal instant of $\overline{J}(t_g)$ and is, hereafter, called the *target instant*. The denominator $\phi(\mathbf{r}, s)$ is a forcing (<u>Table 3</u>) at location \mathbf{r} and time s. By definition, the gradient is zero for $s > t_g$ due to causality.

Adjoint gradients are useful for studying the sensitivity of the model to different forcing, including identification of forcing responsible for the model's variation (Convolution Tool, Section 2.4). (See also Fukumori, 2022.)

The Tool allows J to be chosen as a particular state variable at a specific location \mathbf{x} or, more generally, a user-defined linear function of the state such as a spatial integral as in the Sampling Tool (Eq 1). In time, J for this Tool is based on monthly means; for example, J could be an average of a particular month or an average over a longer period based on monthly means such as a particular year or over the entire period of V4r4. Using the adjoint of the model, the Adjoint Tool computes this gradient for different controls ϕ (Table 3) at different locations \mathbf{r} and time s. As in the Forward Gradient Tool (Section 2.2), controls (ϕ) are defined weekly, starting from 12Z January 01, 1992, that are interpolated linearly in time.

Adjoint gradients (Eq 5) are closely related to forward gradients (Eq 2). The two tools differ in whether it is the numerator or the denominator that is specified/fixed (the other one spans the entire model space of the corresponding variable). Whereas the Forward Gradient Tool computes the gradients for a particular denominator, the Adjoint Tool computes the gradients for a particular numerator. Otherwise, the two gradients are mathematically the same for corresponding numerators and denominators. (Numerical differences arise from approximations.)

2.4. Convolution Tool

The Convolution Tool computes the product of a particular set of adjoint gradients (Section 2.3) and the variations of corresponding controls $\delta \phi$. The product approximates changes in the gradients' Objective Function $\delta \overline{J}$; viz.,

$$\delta \overline{J}(t) \approx \sum_{i} \sum_{\mathbf{r}} \sum_{\Delta t=0}^{\Delta t_{\text{max}}} \frac{\partial \overline{J}(t_g)}{\partial \phi_i(\mathbf{r}, t_g - \Delta t)} \delta \phi_i(\mathbf{r}, t - \Delta t)$$
(7)

Here \overline{J} is defined by Eq.(6). The summation is conducted over subscript i that distinguishes different controls ϕ (Table 3), \mathbf{r} that denotes their spatial location (2-dimensional), and Δt their temporal lag from t_g . Variable t denotes an arbitrary instant. Δt_{max} defines the maximum lag used in the computation. The target instant t_g being parametrically defined, Equation (7) can be recognized as a convolution over temporal lag (Δt) between the gradients and the controls.

The Tool is useful for studying causal relationships between an objection function and its controls, i.e., J and ϕ in Eq (7). Equation (7) is an approximation of a first-order Taylor Series expansion of variations in J at time t, $\delta J(t)$, using gradients at a particular target instant, t_g , rather than the actual instant of J, namely,

$$\frac{\partial \overline{J}(t)}{\partial \phi_i(\mathbf{r}, t - \Delta t)} \approx \frac{\partial \overline{J}(t_g)}{\partial \phi_i(\mathbf{r}, t_g - \Delta t)}$$
(8)

Termed adjoint gradient decomposition (*Fukumori et al., 2015*), Equation (7) provides an explicit causal relationship between forcing and quantity of interest, permitting identification of elements of the former (its type, location, and time) responsible for the latter.

By definition, the Tool treats the controls in the denominator of the gradeints and the forcing used in the convolution having the same temporal resolution. For consistency with the Adjoint Tool (Section 2.3), the Convolution Tool assumes that this temporal resolution is weekly. The Tool by default employs gradients computed by the Adjoint Tool and forcing used by the model (7-day averaged), but also allows Users to substitute them with alternate files (e.g., *Fukumori et al., 2021*).

2.5. Tracer Tool

The Tracer Tool computes the temporal evolution of a user-defined passive tracer and its adjoint.

The tool integrates the tracer evolution using the model's pre-computed circulation (weekly-mean advection and mixing). Users specify the initial tracer distribution (terminal distribution in case of adjoint) and the start (t_{start}) and end (t_{end}) dates of the integration. When $t_{end} < t_{start}$ the Tool computes the adjoint tracer evolution, otherwise the evolution of the forward tracer.

The initial tracer can be chosen interactively as either a unit tracer at a particular location or a general three-dimensional distribution specified in a user-provided file.

Passive tracers are useful for studying the origin and fate of water masses and pathways of ocean circulation. Whereas the evolution of a passive tracer describes where the tracer-tagged water

goes, the evolution of an adjoint passive tracer describes where the tracer-tagged water comes from (*Fukumori et al., 2004*). Unlike advected particles, tracer evolution accounts for effects of both advection and mixing, including convection.

2.6. Budget Tool

The Budget Tool evaluates time-series of variables and fluxes for analyzing property budgets of a user-defined domain of the *reference run* (emu_ref) and its variations (Section 2.7). The analyzed budget is of a scalar quantity integrated over the domain and can be either volume, heat, salt, or salinity, following the recipe outlined by *Piecuch* [2022].

The user-defined domain can be specified as either a single model grid point or a larger body. For the latter, the larger domain can be interactively specified by a range in latitude, longitude, and depth or specified in a file containing an array spanning the model's three-dimensional grid (a value of one indicating a grid point within the volume and zero otherwise).

Budgets are useful for assessing processes (e.g., advection vs external forcing) controlling the user-defined quantity of interest.

2.7. Modified Simulation Tool

The Modified Simulation Tool carries out a modified *reference run* by replacing the *model*'s default input files with those of the same name from a user specified directory. If there are no corresponding files in the user specified directory, the Tool will reproduce the *reference run* (Section 1). The replaced files could be, for example, the model's forcing, initial condition, or input files that control what is output. Model forcing files are summarized in Table 4.

Index	File Name Prefix	Unit	Description
1	oceFWflx	kg/m ² /s	upward freshwater flux
2	sIceLoadPatmPload_nopabar	N/m ²	downward surface pressure load
3	TFLUX	W/m^2	net upward heat flux
4	oceQsw	W/m^2	net upward shortwave radiation
5	oceSflux	$g/m^2/s$	net upward salt flux
6	oceSPflx	g/m ² /s	net downward salt plume flux
7	oceTAUX	N/m ²	westward wind stress
8	oceTAUY	N/m ²	southward wind stress

Table 4: Model forcing files. The *model*'s forcing files are named PREFIX_6hourlyavg_YEAR where PREFIX is one of the eight listed above and YEAR is year from 1992 to 2017. Files contain fluxes on the model grid at 6-hour intervals for each year. Variables in each file correspond to those in Table 3.

The Tool is useful for analyzing the model's response to changes made, such as its controls (forcing and initial condition), as well as to save variables not included in standard output (Table

2). The Modified Simulation Tool provides an interface to run the model with a more variety of changes than in the Forward Gradient Tool (Section 2.2).

EMU includes examples (shell scripts and programs) to create time-mean forcing files and time-mean state as initial condition. Results using the Modified Simulation Tool with these examples are part of EMU and are utilized in the Attribution Tool (Section 2.8).

2.8. Attribution Tool

The Attribution Tool evaluates contributions from separate types of controls to a user-defined quantity of the *reference run* (emu_ref). Contributions are evaluated for anomalies (relative to respective time-mean) in wind stress (both taux and tauy; cf Table 3), heat flux (qnet and qsw), freshwater flux (empmr), salt flux (saltflux and spflx), pressure load (pload), and the model's initial state. The user-defined quantity is specified interactively as in the Sampling Tool (Section 2.1).

The separate contributions are obtained by comparing the *reference run* (Section 1) with *model* simulations using modified input (Section 2.7). For instance, differences between the *reference run* and a model simulation replacing a particular control with its time-mean (e.g., wind) is regarded as contributions from that replaced control's temporal variation. The standard states (Table 2) from such modified simulations (emu_msim) are pre-computed and are available as part of EMU's installation (Section 4) as is the *reference run* (emu_ref).

The Tool is useful for identifying the type of controls (e.g., wind vs heat flux) responsible for a user-defined quantity. The Tool is also useful in assessing and correcting results of the Convolution Tool (Section 2.3). Results of the Attribution Tool are equivalent to comparing different terms that make up the first summation in Equation (7) of the Convolution Tool. The Attribution Tool entails fewer approximations than the Convolution Tool and is therefore more accurate. (The Attribution Tool only approximates the model linearly with respect to the controls.) The Attribution Tool, however, does not distinguish contributions as a function of the control's location or instance that the Convolution Tool does (the second and third sums in Equation 7).

3. How to use the Tools

EMU's Tools (Table 1) are run by following the prompt of command emu, e.g.,

pfe25>emu

Here, user input will be noted in RED, system prompts in CYAN; pfe25> denotes the Unix prompt on NAS Pleiades. Names of files (which command emu above is such) and directories are denoted in **bold** type. Brief descriptions of the prompts are given in **bold italic highlighted in vellow**.

EMU's Tools are accessed through files installed in a user access directory, hereafter denoted **FORUSERDIR** (what is specified in step 17 of "Section 4 Installing the Tools"). On Pleiades, **FORUSERDIR** for the present EMU Version 1 is /nobackup/ifukumor/emu_v1_access. If directory **FORUSERDIR** is not in the user's search path, enter the full pathname to **emu** above (e.g., /nobackup/ifukumor/emu_v1_access/emu).

The **emu** command will prompt the user to select a tool;

```
pfe25>emu
```

ECCO Modeling Utilities (EMU) ...
See /nobackup/ifukumor/emu v1 access/README

The README file provides a brief description of EMU

Choose among the following tools ...

- 1) Sampling (samp); Evaluates state time-series from model output.
- 2) Forward Gradient (fgrd); Computes model's forward gradient.
- 3) Adjoint (adj); Computes model's adjoint gradient.
- 4) Convolution (conv); Computes adjoint gradient decomposition.
- 5) Tracer (trc); Computes passive tracer evolution.
- 6) Budget (budg); Evaluates budget time-series from model output.
- 7) Modified Simulation (msim); Re-runs model with modified input.
- 8) Attribution (atrb); Evaluates state time-series by control type.

Enter choice ... (1-8)? **Prompt for Tool**

Enter a number from 1 to 8 corresponding to the Tool of interest. Examples of using the different tools are described below.

EMU's Tools will generate files under the directory from which the **emu** command is initiated. Unless noted otherwise, all files are binary files. Numbers in EMU's binary input and output files are 32-bit big endian for both float and integer.

3.1. Sampling Tool

a) Example running the Sampling Tool

To run the Sampling Tool, choose 1 in response to command **emu**'s prompt for choice of tool. The example below evaluates monthly-mean time-series of dynamic sea level relative to its global mean at a model grid point closest to 148°W 73.1°N, which is model grid point (85, 604).

```
See /nobackup/ifukumor/emu v1 access/README samp
                                                               File provides brief
                                                               description of
                                                               Sampling Tool
                                 "Native" indicates locally compiled version of the tool
  EMU Sampling Tool (native)
                                  being invoked, not a containerized version.
**** Step 1: Tool Setup
   Running setup samp.sh
**** Step 2: Specification
By default, tool will sample EMU reference run from state files in directory
/nobackupp17/ifukumor/emu_v1/MITgcm/ECCOV4/release4/flux-
forced/emu_ref/diags This is the directory where model's diagnostic output is.
Enter return or enter an alternate directory if sampling another run ...?
                Press Enter/Return to choose default option above.
 ... sampling default EMU reference run.
   Running samp.x
State will be read from:
/nobackupp17/ifukumor/emu v1/MITgcm/ECCOV4/release4/flux-
forced/emu ref/diags
Evaluating model time-series ...
Define objective function (OBJF) ...
Available VARIABLES are ... List of variables for Objective Function. cf Table 2
  1) SSH (m)
  2) OBP (equivalent sea level m)
  3) THETA (deg C)
  4) SALT (PSU)
  5) UV (m/s)
 Monthly or Daily mean ... (m/d)?
 (NOTE: daily mean available for SSH and OBP only.)
     This example chooses monthly mean variables for its Objective Function (Eq 1).
m
 fmd = m
 ==> Sampling MONTHLY means ...
 Choose OBFJ variable (v in Eq 1 of Guide) # 1 ... (1-5)? Variable i=1 in Eq (1)
 (Enter 0 to end variable selection)
                                                  Choose from 1 to 5 from list above.
1
```

```
OBJF variable 1 is SSH
  Choose either VARIABLE at a point (1) or VARIABLE weighted in space (2) ...
(1/2)?
1 Choosing 1 causes samp.x to form a sampling operator as weight T in Eq (1), i.e., T=1
   at the chosen point but zero otherwise. See Section 3.3 for an example choosing 2.
  ... OBJF will be a scaled VARIABLE at a point
  i.e., MULT * VARIABLE
Choose horizontal location ...
 Enter 1 to select native grid location (i,j),
   or 9 to select by longitude/latitude ... (1 or 9)?
9
 Enter location's lon/lat (x,y) ...
   longitude ... (E)?
-148
   latitude ... (N)?
73.1
..... Chosen point is (i,j) = 85 604
      C-grid is (long E, lat N) = -148.1 73.2
     Depth (m)= 3675.7
  Should value at point be relative to global mean ... (enter 1 for yes)?
   1 Choosing 1 modifies the weight T in Eq. (1) accordingly by subtracting the
      fractional area at each grid point (i.e., area of each grid point relative to area over
      the globe.)
  ... OBJF will be relative to global mean
 Enter scaling factor (alpha in Eq 1 of Guide)...?
1
 amult = 1.0000E+00
 Choose OBFJ variable (v in Eq 1 of Guide) # 2 ... (1-5)?
                                                                Variable i=2 in Eq (1).
 (Enter 0 to end variable selection)
                 Selecting 0 ends definition of Objective Function.
Sampling Tool output will be in: emu samp m 1 85 604 1
... Done samp setup of data.ecco. This is the end of the Tool's Specification (Step 2).
**** Step 3: Calculation
                               This step does the actual sampling.
```

```
Running do samp.x
inputdir read : /nobackupp17/ifukumor/emu v1/MITgcm/ECCOV4/release4/flux-
forced/emu ref/diags
                       Number of terms (i) chosen for Eq (1) in Step 2.
nobjf =
Sampling MONTHLY means ... Sampling chosen in Step 2.
 Mask file: objf_1_mask_C
                                    Filename for T in E_q(1) for i=1.
                             Values for T below are output for confirmation.
 Masks maximum absolute value = 9.9999E-01 Maximum value of T is not 1,
                because sampling in this example is at a point relative to global mean.
                                    Maximum element of T in Eq (1) for i=1.
     at (i,j) = 85 604
 Masks sum = -2.5539E-05 The sum of elements in T. This is virtually zero, because
                sampling in this example is at a point relative to global mean.
  Results are in emu_samp_m_1_85_604_1/output
                                                        Directory where output
                                                         can be found
```

b) Sampling Tool output.

The Sampling Tool creates files in a directory bearing specification of the evaluated variable (Objective Function) in its name, which is **emu_samp_m_1_85_604_1** for the case above. Here "**emu_samp**" indicates output from the Sampling Tool, "m" for monthly mean variable, "1" for SSH, "85_604" for location (i,j)=(85, 604), and the last "1" for number of variables defining the Objective Function (nobjf=1). User output is collected in a subdirectory named **output**.

The files in this **output** directory are described below for the example above.

File **samp.txt** is an ASCII text file with the time-series of the user specified variable, with time (1-hour time-step from 12Z January 1, 1992) and corresponding sampled quantity listed in a table format. The time here is the end instant of the averaging period of the sampled quantity (e.g., end of month).

Files **samp.out_312** and **samp.step_312** are equivalent to **samp.txt** but in binary format. File **samp.out_312** has *anomaly time-series of the sampled quantity from its time-mean* (float); The last number after "" in the file name indicates the number of

records in the anomaly time-series, which in this case is 312 monthly mean values from 1992 to 2017 of V4r4's analysis period. The time-mean reference value (float) is given as the last variable in the file (313th in the example above.) File **samp.step_312** has the time record of the time-series (integer). An example FORTRAN code to read these binary output files is given below.

File **samp.info** is a text file summarizing the user-defined Objective Function and file **data.ecco** is an ECCO MITgcm input file defining the objective function.

FORTRAN

```
integer nrec
parameter (nrec=312)
real*4 anom(nrec), ref
character*256 f in
integer istep(nrec)
f in = 'samp.out 312'
open(60, file=trim(f in), action='read', access='stream')
read(60) anom
                    Anomaly time-series of the Objective Function.
read(60) ref
                    Time-mean reference of the anomaly.
close(60)
f in = 'samp.step 312'
open(61, file=trim(f in), action='read', access='stream')
read(61) istep
                   Time of variable "anom" read above.
close(61)
```

3.2. Forward Gradient Tool

a) Example running the Forward Gradient Tool.

To run the Forward Gradient Tool, choose 2 in response to command **emu**'s prompt for choice of tool. The example below computes the model's gradient (Eqs $\underline{2} \& \underline{3}$) with respect to "tauu" (Table 3) at model grid (87,605) at week 518 using a perturbation magnitude of $0.1 \text{ (N/m}^2)$ (Eq.4). (This is similar to the perturbation used in Figure A3 of Fukumori et al., 2021.)

```
EMU Forward Gradient Tool
                                                           Lists the Tool's name
**** Step 1: Tool Setup
                                                   Setting up the Tool (Step 1)
   Running setup pert.csh
... Setting up ECCO V4r4 Perturbation Tool ...
  See FORUSERDIR/README pert
  Run pert.x to specify computation.
**** Step 2: Specification
                                            Specifying what to perturb (Step 2)
   Running pert.x
Perturbation Tool ...
Define control perturbation (denominator in Eq 2 of Guide) ...
Available control variables to perturb ... List of controls. cf Table 3
  1) empmr
  2) pload
  3) qnet
  4) qsw
  5) saltflux
  6) spflx
  7) tauu
  8) tauv
 Enter control (phi in Eq 2 of Guide) ... (1-8)? phi in in denominator Eq (2)
 .... perturbing tauu
Choose location for perturbation (r in Eq 2 of Guide) ... r in denominator of Eq (2)
  Enter 1 to choose native grid location (i,i).
      9 to select by longitude/latitude ... (1 or 9)?
1
  Enter native (i,j) grid to perturb ...
 i... (1-90)?
87
 j... (1-1170)?
605
 ..... perturbation at (i,j) = 87
                                         605
    C-grid is (long E, lat N) = -147.8 72.3
     Depth (m) = 3539.5
Enter week to perturb (s in Eq 2) ... (1-1358)?
                                                   s in denominator of Eq (2)
```

```
518
 ..... perturbing week =
                              518
Default perturbation (delta phi in Eq 4 of Guide):
                                                         delta phi in Eq (4)
     -0.1000E+00 in unit N/m2 (westward wind stress)
Enter 1 to keep, 9 to change ... ?
                                     option to choose magnitude of delta phi
Perturbation amplitude = -0.1000E+00
    in unit N/m2 (westward wind stress)
V4r4 integrates 312-months from 1/1/1992 12Z to 12/31/2017 12Z
which requires 10-hours wallclock time.
                                            Rough measure of required wallclock time.
Enter months to integrate (Max t in Eq 2)... (1-312)?
                                                            Max t in Ea (2).
                                            Tool always integrates from 1/1/1992.
                              Number of months to integrate starting from 1/1/1992.
312
Will integrate model over 312 months
 ... Program has set computation periods in files data and pbs pert.csh accordingly.
 ... Estimated wallclock hours is 12 Tool sets wallclock period of computation.
Wrote pert xx.nml
Wrote pert xx.str
Perturbation Tool output will be in: emu pert 7 87 605 518 -1.00E-01
  Run "do pert.csh" to compute model response.
**** Step 3: Calculation
                                     Conduct gradient computation (Step 3)
  Running do pert.csh
15264481.pbspl1.nas.nasa.gov
                                   A batch job has been submitted for the computation<sup>2</sup>
... Batch job pbs pert.csh has been submitted
  to compute the model's response to perturbation.
  Estimated wallclock time:
```

pfe27>ls emu_pert_7_87_605_518_-1.00E-01/temp/diags/*2d*day*data | wc -l

² Step 3 of the Forward Gradient Tool may require many hours to complete. Progress of this computation can be monitored by the number of intermediate daily-mean standard model state files (one file per day, 9497-days for V4r4's 26-year integration) of the perturbed run written in subdirectory **temp/diags**; e.g.,

Results will be in **emu_pert_7_87_605_518_-1.00E-01/output**. *Output directory*

b) Analyze the results.

The Forward Gradient Tool creates files in a directory bearing the perturbation's specification in its name, which is **emu_pert_7_87_605_518_-1.00E-01** for the case above. Here "**emu_fgrd**" indicates output from the Perturbation Tool, "7" for perturbing tauu, "**87_605**" for the perturbation's location (i,j)=(87, 605), "**518**" for perturbing week 518, and the last "-1.00E-01" for perturbation magnitude. User output is collected in a subdirectory named **output**.

The files in the Tool's **output** directory are described below for the example above.

fgrd xx.nml

Namelist file with specifics of the perturbation saved for reference.

fgrd_spec.info

A text file summarizing the user's response to the Tool's prompt describing its computation.

```
state_2d_set1_day.***TIMESTEP***.data state_2d_set1_day.***TIMESTEP***.meta state_2d_set1_mon.***TIMESTEP***.data state_2d_set1_mon.***TIMESTEP***.meta state_3d_set1_mon.***TIMESTEP***.data state_3d_set1_mon.***TIMESTEP***.data state_3d_set1_mon.***TIMESTEP***.meta
```

Forward gradient in MITgcm diagnostic output format; "data" are binary, "meta" are text files with "data" file information. The ***TIMESTEP*** in the filenames are model timesteps (center step of average); each file corresponds to a particular instant. The fields are on the model's native grid.

Files "state_2d_set1_day" have gradients of daily mean dynamic sea level (ssh) and ocean bottom pressure (obp) on the model's 2-dimensional horizontal grid. Files "state_2d_set1_mon" have monthly means of these same variables. Units are meters for both variables (equivalent sea level for obp) per unit perturbation of the chosen control.

Files "state_3d_set1_mon" have gradients of monthly mean temperature (theta; deg C), salinity (salt; PSU), i-direction velocity (uvel; m/s), and j-direction velocity (vvel; m/s) on the model's 3-dimensional grid per unit perturbation of the chosen control. (NOTE: Although controls tauu and tauv are westward and southward on the native grid, uvel and vvel are in the model's i- and j-directions.)

```
Units and direction of the different controls are (as noted by fgrd.x prompts), control (1) = 'empmr' 'kg/m2/s (upward freshwater flux)' control (2) = 'pload' 'N/m2 (downward surface pressure loading)' control (3) = 'qnet' 'W/m2 (net upward heat flux)' control (4) = 'qsw' 'W/m2 (net upward shortwave radiation)' control (5) = 'saltflux' 'g/m2/s (net upward salt flux)' control (6) = 'spflx' 'g/m2/s (net downward salt plume flux)' control (7) = 'tauu' 'N/m2 (westward wind stress)' control (8) = 'tauv' 'N/m2 (southward wind stress)'
```

Example code to read temperature, theta (the first record; irec), from file **state_3d_set1_mon.0000012396.data** as variable "fvar".

FORTRAN

integer nx, ny, nr

```
parameter (nx=90, ny=1170, nr=50)
   integer irec
   real*4 fvar(nx,ny,nr)
   character*256 f in
   f in = 'state 3d set1 mon.0000012396.data'
   open(60, file=f in, access='direct',
       recl=nx*ny*nr*4, form='unformatted')
   irec = 1
   read(60,rec=irec) fvar
IDL
  nx = 90
  ny = 1170
  nr = 50
  f in = 'state 3d set1 mon.0000012396.data'
  close,1 & openr,1,f in,/swap if little endian
  d file = assoc(1,fltarr(nx,ny,nr))
  irec = 0
  fvar = d file(irec)
```

```
MATLAB
```

```
nx = 90;
ny = 1170;
nr = 50;
f_in = 'state_3d_set1_mon.0000012396.data';
fid=fopen(f_in,'r','ieee-be');
irec = 1;
status=fseek(fid,(irec-1)*(nx*ny*nr*4),'bof');
fvar=fread(fid, [nx*ny*nr], 'single');
fvar=reshape(fvar, [nx,ny,nr]);
fclose(fid);
```

PYTHON

```
import numpy as np

nx = 90

ny = 1170

nr = 50

f_in = 'state_3d_set1_mon.0000012396.data'

dt = np.dtype([ ('fld', '>f4', (nr,ny,nx))])

d_file = np.fromfile(f_in,dtype=dt)

irec = 0

fvar = d_file['fld'][irec]
```

3.3. Adjoint Tool

a) Example running the Adjoint Tool

To run the Adjoint Tool, choose 3 in response to command **emu**'s prompt for choice of tool. The example below computes the model's adjoint gradient (Eq 5) of mean dynamic sea-level averaged over the Beaufort Sea for December 1993. (The gradients are similar to those used in Fukumori et al., 2021.)

EMU Adjoint Tool Lists the Tool's name **** Step 1: Tool Setup Setting up the Tool (Step 1) Running setup adj.csh ... Setting up ECCO V4r4 Adjoint Tool ... See FORUSERDIR/README adj Run adj.x to specify computation. **** Step 2: Specification Specifying what to perturb (Step 2) Running adj.x J in Eq. (5) Define objective function (OBJF; J^bar in Eq 5 of Guide) ... First define OBJF time-period (t start and t g in Eq 6 of Guide) ... t_{start} and t_g in Eq (6) V4r4 can integrate from 1/1/1992 12Z to 12/31/2017 12Z which is 26-years (312-months). Select FIRST and LAST month of OBJF averaging period. Enter FIRST month of OBJF period (t start in Eq 6 of Guide) ... (1-312)? t_{start} in Eq (6) 24 Enter LAST month of OBJF period (t g in Eq 6 of Guide) ... (1-312)? t_e in Eq (6) 24 PERIOD start & end months = 24 24 ... Program has set computation periods in files data and pbs adj.csh accordingly. ... Estimated wallclock hours is 9 The Tool dynamically sets the period of integration from 01 January 1992 to the end of OBJF and adjusts the wallclock resource request accordingly. Gradients are computed for controls during this period. Next define OBJF variable(s) (v in Eq 1 of Guide) ... Variable v in Eq (1) Available VARIABLES are ... 1) SSH (m) 2) OBP (equivalent sea level m) 3) THETA (deg C) 4) SALT (PSU) 5) UV (m/s)

```
Choose OBFJ variable (v in Eq 1 of Guide) # 1 ... (1-5)? Variable i=1 in Eq (1)
  (Enter 0 to end variable selection)
  OBJF variable 1 is SSH
  Choose either VARIABLE at a point (1) or VARIABLE weighted in space (2) ...
(1/2)?
          Choosing 2 causes T in Eq (1) to be read from a user-specified file.
  ... OBJF will be a linear function of selected variable
  i.e., MULT * SUM( MASK * VARIABLE )
  !!!!! MASK must be uploaded (binary native format) before proceeding ...
  Enter MASK filename (T in Eq 1 of Guide) ... ?
../mask.beaufort
                              Example name of a mask file (T n Eq 1)
 fmask = ../mask.beaufort
 Mask file: ../mask.beaufort
 Masks maximum absolute value = 2.2296E-03
     at (i,j) = 86 597 Lists maximum value of mask and its location for reference.
  Masks sum = -1.0863E-06. Sum of mask's elements computed for reference.
                   Here the mask's sum value is virtually nil (much smaller than the
                   maximum) as the mask corresponds to mean sea-level of the Beaufort
                   Sea relative to global mean sea-level.
 Enter scaling factor (alpha in Eq 1 of Guide)...?
                                                     This is alpha in Eq (1).
1
  amult = 1.0000E+00
  Choose OBFJ variable (v in Eq 1 of Guide) # 2 ... (1-5)?
                                            Choosing variable for i=2 in Eq (1)
 (Enter 0 to end variable selection)
                 Selecting 0 ends definition of Objective Function.
Adjoint Tool output will be in: emu adj 24 24 1 mask.beaufort 1
                                                   Output directory.
Wrote adj.dir out
  Run "do adj.csh" to compute adjoint gradients.
**** Step 3: Calculation
                                     Calculating the adjoint gradient (Step 3)
```

Running do adj.csh

15266902.pbspl1.nas.nasa.gov. A batch job has been submitted for the computation³

... Batch job pbs_adj.csh has been submitted to compute the adjoint gradients.

```
Estimated wallclock time: #PBS -I walltime=9:00:00
```

Wallclock time of batch job.

Results will be in emu_adj_24_24_1_mask.beaufort_1/output. *Output directory*

b) Analyze the results.

The Adjoint Tool creates files in a directory bearing its objective function's specification in its name, which is **emu_adj_24_24_1_mask.beaufort_1** for the case above. Here **"emu_adj"** indicates output from the Adjoint Tool, **"24_24"** for the first and last months of the Objective Function's averaging period, **"mask.beaufort"** for the file name of the spatial mask used, and **"1"** for the number of variables defining the Objective Function (nobjf=1). User output is collected in a subdirectory named **output**.

The files in the Tool's **output** directory are described below for the example above.

adj.info:

A text file summarizing the objective function created by **adj.x**.

```
adxx_***CTRL***_0000000129.data
adxx_***CTRL***_0000000129.meta
```

Adjoint gradient in MITgcm output format; "data" files are binary, "meta" files are text files with "data" file information. ***CTRL*** is the name of the model's different forcing (Table 3). (0000000129 is the "iteration" number of the particular ECCO estimate.)

```
pfe27>cd emu_adj_24_24_1_mask.beaufort_1
pfe27>grep ad_time_tsnumber temp/STDOUT.0000 | tail -n 3

(PID.TID 0000.0001) %MON ad_time_tsnumber = 720

(PID.TID 0000.0001) %MON ad_time_tsnumber = 480

(PID.TID 0000.0001) %MON ad_time_tsnumber = 240
```

³ Progress of this computation can be monitored by variable "ad_time_tsnumber" printed in PBS job output file **STDOUT.0000** output in subdirectory temp. This variable is the time-step counter of the model. The time-step size is 1-hour and *counts* down backward from the ending of OBJF's definition to zero at the beginning of 01 January 1992, V4r4's initial condition. The variable is printed out every 10-days; e.g.,

Example code to read the adjoint gradient with respect to tauu at 10-weeks lag from the end of OBJF averaging period.

FORTRAN

```
integer nx, ny
parameter (nx=90, ny=1170)
integer irec, f_size, nrec, nlag
real*4 fvar(nx,ny)
character*256 f_in

f_in = 'adxx_tauu.0000000129.data'
inquire(file=f_in, size=f_size)
nrec = f_size / (nx*ny*4)

Number of records in file.

open(60, file=f_in, access='direct',
$ recl=nx*ny*4, form='unformatted')

nlag = 10
irec = nrec - nlag

Record number for 10 week lag.

read(60,rec=irec) fvar
```

3.4. Convolution Tool

a) Example running the Convolution Tool

To run the Convolution Tool, choose 4 in response to command **emu**'s prompt for choice of tool. The example below computes the convolution between the adjoint gradients derived in the example in Section 3.3 and the model's forcing. (This is similar to the convolution conducted in Fukumori et al., 2021.)

```
... Setting up ECCO V4r4 Convolution Tool ...
  See FORUSERDIR/README conv
************
  Run conv.x to specify convolution.
**** Step 2: Specification
                                   Specifying what to convolve (Step 2)
   Running conv.x
Convolution Tool ...
Specify forcing, adjoint gradient, and maximum lag below ... Defining RHS of Eq. (7)
V4r4 weekly forcing is in directory
   /nobackupp17/ifukumor/emu/MITgcm/ECCOV4/release4/flux-
forced/forcing/other/flux-forced/forcing weekly
Use V4r4's weekly forcing for convolution (phi in Eq 7 of Guide) ... (Y/N)?
                                                                    phi in Eq(7)
y
Reading forcing from directory
   /nobackupp17/ifukumor/emu/MITqcm/ECCOV4/release4/flux-
forced/forcing/other/flux-forced/forcing weekly
Specify adjoint gradients ...
 Gradients must have equivalent file and directory names as Adjoint Tool output.
 Gradient files must be named adxx ***CTRL***..0000000129.data etc
 and be present in a directory named 'output'
 under a parent directory prefixed 'emu adj'
Enter directory name of Adjoint Tool output or its equivalent ... ? Gradients in Eq (7)
emu adj 24 24 1 mask.beaufort 1/output
   Reading adxx from
   emu adj 24 24 1 mask.beaufort 1/output
   number of adxx records = 107
   Zero lag at (weeks) = 106
Enter maximum lag (weeks) to use in convolution (delta t max in Eq 7 of Guide) ...
(0-105)?
            \Delta t_{max} in Eq (7)
105
   nlag = 105
```

Convolution Tool output will be in: emu conv 24 24 1 mask.beaufort 1 105

... Done conv setup (conv.out)

Run "do_conv.csh" to conduct convolution.

**** Step 3: Calculation Running do conv.csh

Conduct convolution (Step 3)

15267426.pbspl1.nas.nasa.gov. A batch job has been submitted for the computation

... Batch job pbs_conv.csh has been submitted to compute adjoint gradient convolution with control.

Estimated wallclock time:

#PBS -I walltime=02:00:00

Results will be in emu_conv_24_24_1_mask.beaufort_1_105/output

Output directory

b) Analyze the results.

The Convolution Tool creates files in a directory bearing the convolution's specification in its name, which is **emu_conv_24_24_1_mask.beaufort_1_105** for the case above. Here "**emu_conv**" indicates output from the Convolution Tool and "**24_24_1_mask.beaufort_1**" corresponds to the adjoint gradient used, and the last "**105**" is the maximum lag used. User output is collected in a subdirectory named **output**.

The files in the Tool's **output** directory are as follows.

recon2d_***CTRL***.data

Two-dimensional time-series of the convolution for individual controls, ***CTRL*** (<u>Table 3</u>),

$$\sum_{\Delta t=0}^{\Delta t_{\text{max}}} \frac{\partial \overline{J}(t_g)}{\partial \phi_i(\mathbf{r}, t_g - \Delta t)} \delta \phi_i(\mathbf{r}, t - \Delta t)$$
(9)

This sum is a function of space (\mathbf{r}) and time (t) for a particular control (i). The quantity represents a partial sum of the terms on the RHS of Eq.(7), and is useful in analyzing contributions to $\delta \overline{J}(t)$ from different locations of each separate control (e.g., Figure 9 of Fukumori et al., 2021).

recon1d_***CTRL***.data

Time-series of global sum of the convolution at different maximum lags (k) for individual controls, ***CTRL*** (Table 3),

$$\sum_{\mathbf{r}} \sum_{\Delta t=0}^{k} \frac{\partial J(t_g)}{\partial \phi_i(\mathbf{r}, t_g - \Delta t)} \delta \phi_i(\mathbf{r}, t - \Delta t)$$
(10)

This sum is a function time (t) and maximum $\log(k)$ for a particular control (i). The quantity represents a partial sum of the terms on the RHS of Eq.(7), and is useful in analyzing contributions to $\delta \overline{J}(t)$ up to different lags of each separate control (e.g., Figure 10 of Fukumori et al., 2021).

istep ***CTRL***.data

Time (t) of the convolution time-series for individual controls, ***CTRL*** (Table 3), defined as the end instant of each period (e.g., end of the 7-day mean), in terms of the model's time-step (1-hour time-step from 12Z January 1, 1992.) (Different forcing files can span different periods.)

conv.info

Specification of convolution set by **conv.x**, identifying forcing, adjoint gradients, maximum lag used, and name of output directory.

conv.out

Same as **conv.info** but without the comments (read by **do conv.x.**)

Example code to read the Convolution Tool's time-series output.

FORTRAN

```
integer nx, ny, nwks, nlag
parameter (nx=90, ny=1170, nwks=1357, nlag=105)
real*4 fvar2d(nx,ny,nwks), fvar1d(nwks,nlag+1)
integer istep(nwks)
character*256 f in
f in = 'recon2d tauu.data'
open(60, file=f in, access='direct',
$ recl=nx*ny*4, form='unformatted')
do i=1,nwks
  read(60,rec=i) fvar2d(:,:,i)
enddo
f in = 'recon1d tauu.data'
open(60, file=f in, access='direct',
$ recl=nwks*4, form='unformatted')
do i=1.nlag+1
                         Records correspond to maximum lag of 0 to nlag.
```

```
read(60,rec=i) fvar1d(:,i)
enddo

f_in = 'istep_tauu.data'
open(60, file=f_in, access='stream')
read(60) istep
enddo
```

3.5. Tracer Tool

a) Example running the Forward Gradient Tool.

To run the Tracer Tool, choose 5 in response to command **emu**'s prompt for choice of tool. The example below computes the forward tracer evolution from 30 January 1992 to 30 March 1992, initialized to a unit value for the model grid point closest to 0m depth at 160°W 0°N.

```
Enter choice ... (1-8)?
         Entering 5 to select EMU's Tracer Tool
choice is 5) Tracer Tool (trc)
See /nobackup/ifukumor/emu v1 access/README trc
                                                           File provides a brief
                                                    description of the Tracer Tool
*********
  EMU Tracer Tool
                                        Lists the Tool's name
**** Step 1: Tool Setup
                                        Setting up the Tool (Step 1)
  Running setup trc.csh
... Setting up ECCO V4r4 Passive Tracer Tool ...
  See FORUSERDIR/README trc
*************
  Run trc.x to specify computation.
**** Step 2: Specification
                                  Specifying what to compute (Step 2)
  Running trc.x
Passive Tracer Tool ...
Define passive tracer distribution ...
```

```
Enter START and END days of integration ...
(days since 01 January 1992, between 1 and 9495)
 Tool computes forward tracer when START It END and
 adjoint tracer when START gt END.
Enter start day ... (1-9495)?
                                Defining initial day of the computation.
Enter end day ... (1-9495)?
90
                                Defining end day of the computation.
Start and End days = 30 90. Computation will be adjoint if Start > End.
 Forward tracer computation
Enter tracer at start time ...
                                Specification of initial tracer distribution.
Choose either unit tracer at a point (1) or
user-provided distribution in a file (2) ... (1/2)?
1 Choosing 1 causes trc.x to create an initial tracer distribution file that is zero
   everywhere except a single point to be defined below. Choosing 2 will cause trc.x to ask
   for a user-provided file equivalent to what the tool creates here.
  ... starting TRC is unit value at a point.
Choose horizontal location ...
 Enter 1 to select native grid location (i,j),
    or 9 to select by longitude/latitude ... (1 or 9)?
9
 Enter location's lon/lat (x,y) ...
    longitude ... (E)?
-160
   latitude ... (N)?
0
..... Chosen point is (i,j) = 15 803 Information of chosen model grid point.
      C-grid is (long E, lat N) = -160.5 	 0.2
      Depth (m)= 5053.9
Choose depth ...
 Enter 1 to select native vertical level (k),
    or 9 to select by meters ... (1 or 9)?
9
```

```
Enter location's distance from surface ... (m)?
0
..... closest wet level is (k) = 1
                                   Information of chosen model grid point.
      at depth (m) =
                       5.0
Tracer Tool output will be in: emu trc 30 90 15 803 1
... Done trc setup
*********
  Run "do trc.csh" to compute tracer evolution.
**** Step 3: Calculation
                            Computing tracer evolution (Step 3)
  Running do trc.csh
                                A batch job has been submitted for the computation
15267761.pbspl1.nas.nasa.gov.
... Batch job pbs trc.csh has been submitted
  to compute the tracer evolution.
  Estimated wallclock time:
#PBS -I walltime=1:00:00
***********
  Results will be in emu_trc_30_90_15_803_1/output
                                                         Output directory
```

b) Analyze the results.

The Tracer Tool creates files in a directory bearing the tracer specification in its name, which is **emu_trc_30_90_15_803_1** for the case above. Here "**emu_trc**" indicates output from the Tracer Tool, "**30_90**" for the start and ending dates (1992-day) of the integration, "**15_803_1**" describing the initial perturbation perturbation which is grid (i,j,k)=(15, 803,1) in the example. User output is collected in a subdirectory named **output**.

The files in the Tool's **output** directory are described below for the example above.

trc.info

A text file summarizing the tracer computation specified by **trc.x**.

```
ptracer_mon_mean.***TIMESTEP***.data
ptracer mon_mean.***TIMESTEP***.meta
```

"Monthly" average tracer distribution in MITgcm diagnostic output format; "data" are binary files and "meta" are text files with "data" file information. The ***TIMESTEP*** in the filenames are model time-steps (1-hour time-steps) of each average from V4r4's initial instant (12Z 01 January 1992). These time-steps correspond to the end of each succeeding averaging period, which is nominally 30.5-days.

```
ptracer_mon_snap.***TIMESTEP***.data
ptracer_mon_snap.***TIMESTEP***.meta
```

Tracer distribution at particular instances ("snapshots") in MITgcm diagnostic output format; "data" are binary files and "meta" are text files with "data" file information. The ***TIMESTEP*** in the filenames are model time-steps (1-hour time-steps) of each instant from V4r4's initial instant (12Z 01 January 1992). These files are the same as corresponding ptracer_mon_mean files but the output here is instantaneous values instead of time-mean in the latter (30.5-day average).

3.6. Budget Tool

a) Example running the Budget Tool

To run the Budget Tool, choose 6 in response to command **emu**'s prompt for choice of tool. The example below evaluates variables and fluxes for the heat budget of the top 50m of the Nino 3.4 area (5N-5S, 170W-120W).

By default, tool will sample EMU reference run from state files in directory

```
forced/emu ref/diags
                               Reference run is installed as part of
                               EMU implementation (cf Section 4).
Enter return or enter an alternate directory if sampling another run ...?
                 Hit Enter or Return key to choose default option above.
<return>
... sampling default EMU reference run.
   Running budg.x
inputdir read : /nobackupp17/ifukumor/emu v1/MITgcm/ECCOV4/release4/flux-
          Directory where EMU is installed (cf Section 4).
srcdir read : /nobackupp17/ifukumor/emu v1/MITgcm/ECCOV4/release4/flux-
forced/emu_ref/diags_Directory_where budget files will be read from (chosen above).
tool files read : /nobackupp17/ifukumor/emu v1/MITgcm/ECCOV4/release4/flux-
forced
Evaluating budget time-series ...
Define budget variable ...
Available VARIABLES are ...
                                  Choice of budget variable.
  1) Volume (m<sup>3</sup>)
  2) Heat (theta) (degC)
  3) Salt (PSU)
  4) Salinity (PSU)
  ==> Budget is MONTHLY ...
                                   Budgets are evaluated monthly.
 Choose budget variable (v in Eq 1 of Guide) ... (1-5)? Choose 1-5 from list above.
2
          Here, we are entering 2 to conduct heat budget.
  Budget variable is Heat (theta)
Choose budget for a single model grid point (1) or
      over a larger volume (2) ... (1/2)?
2
          Here, we are entering 2 to analyze the budget over a volume.
... Budget will be over a volume
Choose either a lat/lon/depth volume (1) or
  a volume specified in a user-provided file (2) ... (1/2)?
(user file must be in model's native binary format)
1
          Here, we are entering 1 to specify the volume interactively
          by selecting a range for latitude, longitude and depth.
... Budget will be over a lat/lon/depth volume
Enter west most longitude (-180E to 180E)... x1?
          Numbers entered below correspond to the example volume.
-170
Enter east most longitude (-180E to 180E)... x2?
  (choose x2=x1 for zonally global volume)
```

/nobackupp17/ifukumor/emu v1/MITgcm/ECCOV4/release4/flux-

```
-120
Enter south most latitude (-90N to 90N)... y1?
Enter north most latitude (-90N to 90N)... y2?
Enter deepest depth (0-6000m) ... z1?
Enter shallowest depth (0-6000m)... z2?
 min/max longitude -170.0 -120.0
                                            All model grid points within this range
                                            defines the volume over which the budget
 min/max latitude
                     -5.0
                            5.0
 min/max depth
                   50.0
                           0.0
                                            will be evaluated.
Budget Tool output will be in : emu budg m 2 -170.0 -120.0 -5.0 5.0 50.0 0.0
... Done budg setup of data.ecco
                                     This is the end of the Tool's Specification (Step 2).
**** Step 3: Calculation
                               This step does the actual evaluation of variables.
   Running do budg.x
18675644.pbspl1.nas.nasa.gov
... Batch job pbs budg.sh has been submitted
                                                  Computation is performed in batch.
  to compute the budget.
  Estimated wallclock time:
#PBS -I walltime=02:00:00
  Results will be in emu budg m 2 -170.0 -120.0 -5.0 5.0 50.0 0.0/output
                                            Output will be placed in this directory upon
                                            completion of the batch job.
```

b) Budget Tool output.

The Budget Tool creates files in a directory bearing specification of the budget in its name, which is **emu_budg_m_2_-170.0_-120.0_-5.0_5.0_50.0_0.0** for the case above. Here "**emu_budg**" indicates output from the Budget Tool, "**m**" for monthly mean variable, "**2**" for Heat Budget, "-**170.0_-120.0_-5.0_50.0_0.0**" for the interactively chosen range of longitude, latitude, and depth of the volume. User output is collected in a subdirectory named **output**.

The files in this **output** directory are described below for the example above. (Here, command **lss** is a shorthand alias of **ls -log --time-style=+""**.)

```
pfe20>lss emu_budg_m_2_-170.0_-120.0_-5.0_5.0_50.0_0.0/output total 15364
```

```
554
                      budg.info
-rw-r--r--1
                       data.ecco
-rw-r--r-- 1
                 307
                       emu budg.mkup adv x
-rw-r--r-- 1
              624005
                       emu budg.mkup adv y
-rw-r--r-- 1
              249605
-rw-r--r-- 1 2496005
                       emu budg.mkup adv z
-rw-r--r-- 1 6240005
                       emu budg.mkup atm
-rw-r--r-- 1
              624005
                       emu budg.mkup mix x
              249605
                       emu budg.mkup mix y
-rw-r--r-- 1
                       emu budg.mkup mix z e
-rw-r--r-- 1 2496005
-rw-r--r-- 1 2496005
                       emu budg.mkup mix z i
-rw-r--r-- 1
               80004
                       emu budq.msk3d a
               80004
                       emu budg.msk3d v
-rw-r--r-- 1
                8004
                       emu budg.msk3d x
-rw-r--r-- 1
-rw-r--r-- 1
                3204
                       emu budg.msk3d y
-rw-r--r-- 1
                       emu budg.msk3d z
               32004
                8828
                       emu budg.sum tend
-rw-r--r--1
-rw-r--r-- 1
                8828
                       emu budg.sum tint
```

budg.info

A text file, created by **budg.x**, summarizing the user-specified budget computation.

data.ecco

An ECCO MITgcm namelist file (text file) defining the objective function, modified by **budg.x**, and used by **do budg.x** to conduct the budget computation.

emu_budg.mkup_****

Time-series of spatially varying converging fluxes making up individual terms of the budget. These files are useful for analyzing the spatial location of the fluxes contributing to the budgeted quantity. Time-series of the spatial sum of these files are summarized in **emu_budg.sum_tend**. The string **** indicates particular terms in the budget summarized below for heat budget. See *Piecuch (2022)* for description of the terms. (Some of these files will be absent if the budget has no corresponding elements, as in geothermal flux in the example above.) Per divergence theorem, the fluxes are those along the bounding surface of the budget's domain (2d surface in 3d space), except for short-wave radiation that penetrates the volume (included in **emu_budg.mkup_atm** for this heat budget example.) (Sea ice's salt-plume flux, a component for salt and salinity budgets, is also a penetrative flux deposited inside a budget's volume.)

```
adv_x: Advection in the horizontal i-direction.
adv_y: Advection in the horizontal j-direction.
adv_z: Advection in the vertical r-direction.
atm: Fluxes from atmosphere & sea ice.
geo: Geothermal heating.
mix_x: Mixing in the horizontal i-direction.
mix_y: Mixing in the horizontal j-direction.
mix_z_e: Explicit mixing in the vertical r-direction.
mix_z i: Implicit mixing (convection) in the vertical r-direction.
```

For volume budget, possible terms are

```
adv_x: Advection in the horizontal i-direction.
adv_y: Advection in the horizontal j-direction.
adv_z: Advection in the vertical r-direction.
srf: Surface fluxes.
```

For salt budget, possible terms are

```
adv_x: Advection in the horizontal i-direction.
adv_y: Advection in the horizontal j-direction.
adv_z: Advection in the vertical r-direction.
frc_sflux: Surface salt flux from sea ice.
frc_oceSP: Penetrative salt flux from sea ice.
mix_x: Mixing in the horizontal i-direction.
mix_y: Mixing in the horizontal j-direction.
mix_z e: Explicit mixing in the vertical r-direction.
mix_z i: Implicit mixing (convection) in the vertical r-direction.
```

The salinity budget does not take a divergence form and does not have directional information. For brevity, the spatial distribution of the fluxes that make up the budget are not individually output by the Tool. (Each term is 3-dimensional spanning the domain of interest making the file sizes much larger, if saved, than those for fluxes on the domain's boundary.) Spatially integrated summary of the salinity budget is, as are other budgets, given in files **emu_budg.sum_tend** and **emu_budg.sum_tint** described below.

The files contain the following items in this order;

```
msk: A single character identifying the spatial location of the fluxes (character). The character corresponds to string? in file emu_budg.msk3d_? below that defines this location.
```

i31: The term number in file **emu_budg.sum_tend** that fluxes in this file are aggregated in (integer)

b3d: An array of n3d elements with the fluxes where n3d is given in file emu_budg.msk3d_? (float)

Array **b3d** is repeated for each month that is available (which totals **nmonths** in file **emu_budg.sum_tend**).

emu budg.msk3d ?

Spatial location of the convergence in files **emu_budg.mkup_******. The string **?** is a letter denoting the type of location described below. The location string (**?**) is also the first record of each convergence file (**emu_budg.mkup_******) indicating the corresponding location for the converging fluxes in that file.

- **a**: Location of fluxes at the ocean surface including shortwave radiation.
- v: Location spanning the entire volume of the domain.
- **x**: Location of fluxes in the horizontal i-direction.
- **y**: Location of fluxes in the horizontal j-direction.
- **z**: Location of fluxes in the vertical r-direction.

```
s: Location of fluxes at the ocean surface.
```

g: Location of geothermal fluxes (ocean bottom).

The files contain the following items in this order;

```
n3d: number of locations in file (integer)
```

f3d: array with n3d elements used as weights in evaluating fluxes (float)

i3d: array with n3d elements indicating i-index of the flux (integer)

j3d: array with n3d elements indicating j-index of the flux (integer)

k3d: array with n3d elements indicating k-index of the flux (integer)

emu_budg.sum_tend

Spatially integrated summary scalar time-series of each term in the budget (tendency budget). (File is created as unit 31 in **do_budg.f**) The file contains the following items in this order;

```
ibud: type of budget (integer, 2 for heat budget)
```

nmonths: number of months (integer)

tname: name of variable (fixed-length string with 12 characters)

tvar: variable (float array with nmonths elements)

The pair of records **tname** and **tvar** are repeated for all items that make up the budget, which differ with budget type and budget domain. The first pair is always the length of time (hours) for each month (**tname**=dt) and the second pair is always the left-hand-side of the budget (**tname**=lhs). The left-hand-side is given here for reference purpose only in checking consistency with terms on the right-hand-side of the budget in this file. The left-hand-side in this file is based on instantaneous states at the end of the month, except for the first and last months whose tendency is artificially set to zero due to missing output.

For heat budget, there are an additional six possible pairs for **tname** and **tvar** depending on domain. The variable name **tname** for these six are:

```
advh: horizontal advection (sum of emu_budg.mkup_adv_x and emu_budg.mkup_adv_y)

mixh: horizontal mixing (sum of emu_budg.mkup_mix_x and emu_budg.mkup_mix_y.)

advv: vertical advection

mixv: vertical mixing (sum of emu_budg.mkup_mix_z_e and emu_budg.mkup_mix_z_i.)

tfrc: surface forcing (atmosphere & sea ice)

geo: geothermal forcing
```

For volume budget, there are an additional three possible pairs for **tname** and **tvar** depending on domain. The variable name **tname** for these three are;

```
advh: horizontal advection (sum of emu_budg.mkup_adv_x and emu_budg.mkup_adv_y)
```

advv: vertical advection vfrc: surface forcing

For salt budget, there are an additional five possible pairs for **tname** and **tvar** depending on domain. The variable name **tname** for these five are;

```
advh: horizontal advection (sum of emu_budg.mkup_adv_x and emu_budg.mkup_adv_y)
mixh: horizontal mixing (sum of emu_budg.mkup_mix_x and emu_budg.mkup_mix_y.)
advv: vertical advection
mixv: vertical mixing (sum of emu_budg.mkup_mix_z_e and emu_budg.mkup_mix_z_i.)
sfrc: surface forcing (sea ice)
```

For salinity budget, there are an additional five possible pairs for **tname** and **tvar** depending on domain. The variable name **tname** for these five are;

```
advh_slt: horizontal advection of salt
advh_vol: horizontal advection of volume
mixh: horizontal mixing
advv_slt: vertical advection of salt
advv_vol: vertical advection of volume
mixv: vertical mixing
sfrc_slt: surface forcing of salt (sea ice)
sfrc_vol: surface forcing of volume
```

emu_budg.sum_tint

Time-integral of the tendency budget (**emu_budg.sum_tend**). This file is useful for assessing processes controlling the quantity of interest itself (volume, heat, salt, salinity) instead of its tendency. The file content is the same as **emu_budg.sum_tend** but with all variables (except **tname**=dt) time-integrated relative to the second month.

3.7. Modified Simulation Tool

a) Example running the Modified Simulation Tool

To run the Modified Simulation Tool, choose 7 in response to command **emu**'s prompt for choice of tool. The example below replaces wind forcing with its time-mean.

```
**** Steps 1 & 2: Setup & Specification
NB: V4r4's forcing is in
/nobackupp17/ifukumor/emu v1/MITgcm/ECCOV4/release4/flux-
forced/forcing/other/flux-forced/forcing Model forcing file installed with EMU
                                            listed for reference.
Enter directory name with user replacement files ...?
tau
          Directory where user-created replacement files are located.
Replacement files will be read from
/nobackupp17/ifukumor/temp53/tau Full pathname of user-directory above, where
Output directory will be /nobackup/ifukumor/temp53/emu msim tau
                              Tool creates directory where computation will take place.
 1) Set up files for MITgcm
Output budget (fluxes) ... (YES/NO)?

∨ Option to output fluxes for budget analysis.

... outputting budget
Replacement file ... oceTAUX 6hourlyavg 1992 List of replacement files identified
Replacement file ... oceTAUX_6hourlyavg_1993 in the user-created replacement
                                                  file directory. For brevity, only a
Replacement file ... oceTAUY_6hourlyavg_2016 few are shown here.
Replacement file ... oceTAUY 6hourlyavg 2017
Total # of files to be replaced ... 52 Number of files to be replaced. The example is
         from replacing all wind stress files (26 yearly files for each component of wind).
Proceed to replace and run the model ... (Y/N)?
Option to abort the Tool. Users could abort here to examine files in the Tool-created
  directory above to examine pre-replacement files.
Optionally, enter short description about the replacement files ...?
 (Will be copied in output file msim.info for reference.)
 (Skip if not needed.)
Using 1992-2017 time-mean wind. Short description of the simulation to be conducted.
Replacing ... oceTAUX_6hourlyavg_1992 Confirming files replaced. For brevity,
Replacing ... oceTAUX 6hourlyavg 1993 only a few are shown here.
Replacing ... oceTAUY 6hourlyavg 2016
Replacing ... oceTAUY_6hourlyavg_2017
Total # of files replaced ... 52
 3) Run MITgcm
                       Tool submits a batch job to conduct the modified simulation.
```

b) Modified Simulation Tool output.

The Modified Simulation Tool creates files in a directory, **emu_msim_tau** for the case above, which bears the name of the user specified directory with the replacement files. Here "**emu_msim**" indicates output from the Modified Simulation Tool and "**tau**" for the name of the user specified directory.

msim.info

A text file listing replacement *model* input files.

The Tool creates standard state output (Table 2) and budget output under subdirectory **diags** under the Tool's main output directory (**emu_msim_tau** for the case above). This output is controlled by the namelist file **data.diagnostics**, which can itself be modified (cf https://mitgcm.readthedocs.io/en/latest/).

```
state_2d_set1_day.***TIMESTEP***.data
state_2d_set1_day.***TIMESTEP***.meta
state_2d_set1_mon.***TIMESTEP***.data
state_2d_set1_mon.***TIMESTEP***.meta
state_3d_set1_mon.***TIMESTEP***.data
state_3d_set1_mon.***TIMESTEP***.meta
```

With the default **data.diagnostics** file, these files contain the standard state (Table 2) in MITgcm diagnostic output format; "data" are binary, "meta" are text files with "data" file information. The ***TIMESTEP*** in the filenames are model time-steps (center step of average); each file corresponds to a particular instant (for time-mean variables, the instant is the end time-step of the averaging period). The fields are on the model's native grid.

Files "state_2d_set1_day" have daily mean dynamic sea level (ssh) and ocean bottom pressure (obp) on the model's 2-dimensional horizontal grid. Files

"state_2d_set1_mon" have monthly means of these same variables. Units are meters for both variables (equivalent sea level for obp).

Files "state_3d_set1_mon" have monthly mean temperature (theta; deg C), salinity (salt; PSU), i-direction velocity (uvel; m/s), and j-direction velocity (vvel; m/s) on the model's 3-dimensional grid. (NOTE: Although controls tauu and tauv are westward and southward on the native grid, uvel and vvel are in the model's i- and j-directions.)

These model states can be sampled with the Sampling Tool by specifying the **diags** directory in response to the Sampling Tool's prompt.

ADVr SLT mon mean ADVr TH mon mean ADVx SLT mon mean ADVx TH mon mean ADVy SLT mon mean ADVy_TH_mon_mean DFrE_SLT_mon mean **DFrE TH mon mean** DFrI SLT mon mean DFrI TH mon mean DFxE_SLT_mon_mean DFxE_TH_mon_mean DFyE SLT mon mean DFyE TH mon mean **ETAN** mon inst **ETAN** mon mean oceFWflx mon mean oceQsw mon mean oceSPtnd mon mean **SALT** mon inst SFLUX mon mean TFLUX mon mean **THETA** mon inst UVELMASS_mon_mean **VVELMASS** mon mean WVELMASS_mon_mean

These subdirectories under **diags** contain variables (fluxes and instantaneous state) for the modified simulation's budget analysis. Budgets can be analyzed with EMU's Budget Tool by specifying the **diags** directory in response to the Budget Tool's prompt.

3.8. Attribution Tool

c) Example running the Attribution Tool

To run the Attribution Tool, choose 8 in response to command **emu**'s prompt for choice of tool. Prompts of the Attribution Tool are nearly the same as the Sampling Tool. The example below evaluates steric sea level (equal to difference between dynamic sea level and ocean bottom pressure) averaged over the Beaufort Sea relative to its global mean.

```
Enter choice ... (1-8)?
         Entering 1 to select EMU's Attribution Tool
8
choice is 8) Attribution Tool (atrb)
See /nobackup/ifukumor/emu v1 access/README atrb
                                                              File provides a brief
                                                 description of the Attribution Tool
*********
  EMU Attribution Tool (native)
**** Steps 1 & 2: Setup & Specification
Extracting model time-series ...
Define objective function (OBJF) ...
Available VARIABLES are ... List of variables for Objective Function. cf Table 2
  1) SSH (m)
  2) OBP (equivalent sea level m)
  3) THETA (deg C)
  4) SALT (PSU)
  5) UV (m/s)
 Monthly or Daily mean ... (m/d)?
 (NOTE: daily mean available for SSH and OBP only.)
m This example chooses monthly mean variables for its Objective Function (Eq 1).
 fmd = m
 ==> Sampling MONTHLY means ...
 Choose OBFJ variable (v in Eq 1 of Guide) # 1 ... (1-5)? Variable i=1 in Eq (1)
 (Enter 0 to end variable selection)
                                                 Choose from 1 to 5 from list above.
1 Dynamic sea level chosen as first variable of OBJF.
 OBJF variable 1 is SSH
 Choose either VARIABLE at a point (1) or VARIABLE weighted in space (2) ...
2. A spatial weight allows computation of Beaufort Sea mean relative to global mean.
 ... OBJF will be a linear function of selected variable
  i.e., MULT * SUM( MASK * VARIABLE )
```

!!!!! MASK must be uploaded (binary native format) before proceeding ...

Enter MASK filename (T in Eq 1 of Guide) ... ?

/nobackup/ifukumor/emu_v1/MITgcm/ECCOV4/release4/flux-forced/
emu/emu_input/beafortsea.msk The weight in this file consists of the difference
between two weights, i.e., the weight for computing the Beaufort Sea mean minus that for
computing the global mean. This particular file is included in EMU for reference in
subdirectory emu_input.

Mask file: /nobackup/ifukumor/emu_v1/MITgcm/ECCOV4/release4/flux-forced/emu/emu_input/beafortsea.msk

Masks maximum absolute value = 2.2279E-03 The maximum value of the weight, at (i,j) = 85 595 its location, and its global sum are printed for reference.

Masks sum = -7.2392E-07 The global sum in this instance is essentially zero as the weight is the difference between two area means.

Enter scaling factor (alpha in Eq 1 of Guide)...?

1. A unit scaling factor is chosen for dynamic sea level, as steric sea level is dynamic sea level minus ocean bottom pressure.

amult = 1.0000E+00

Choose OBFJ variable (v in Eq 1 of Guide) # 2 ... (1-5)? *Variable i=2 in Eq (1)*. (Enter 0 to end variable selection)

2 Ocean bottom pressure chosen as second variable of OBJF.

OBJF variable 2 is OBP

Choose either VARIABLE at a point (1) or VARIABLE weighted in space (2) ... (1/2)?

2 A spatial weight allows computation of Beaufort Sea mean relative to global mean.
... OBJF will be a linear function of selected variable
i.e., MULT * SUM(MASK * VARIABLE)

!!!!! MASK must be uploaded (binary native format) before proceeding ...

Enter MASK filename (T in Eq 1 of Guide) ... ?

/nobackup/ifukumor/emu_v1/MITgcm/ECCOV4/release4/flux-forced/ emu/emu_input/beafortsea.msk *The same weight as dynamic sea level is chosen*.

Mask file: /nobackup/ifukumor/emu_v1/MITgcm/ECCOV4/release4/flux-forced/emu/emu_input/beafortsea.msk

Masks maximum absolute value = 2.2279E-03 at (i,j) = 85 595 Masks sum = -7.2392E-07

Enter scaling factor (alpha in Eq 1 of Guide)...?

-1. A scaling factor of -1 is chosen for ocean bottom pressure, as steric sea level is dynamic sea level minus ocean bottom pressure.

amult = -1.0000E+00

Choose OBFJ variable (v in Eq 1 of Guide) # 3 ... (1-5)? *Variable i=3 in Eq (1)*. (Enter 0 to end variable selection)

O Selecting 0 ends definition of Objective Function.

Done interactive specification. Begin extracting time-series ...

Tool output will be in: **emu_atrb_m_1_beafortsea.msk_2.** *Tool creates directory where computation will be conducted.*

In following, the Tool samples OBJF from model results provided with EMU. These model results are the reference run and results from the Modified Simulation Tool with individual controls replaced by their corresponding time-mean.

Sampling reference run ...

from: /nobackupp17/ifukumor/emu_v1/MITgcm/ECCOV4/release4/flux-forced/emu_ref/diags

Sampling time-mean wind run ...

from: /nobackupp17/ifukumor/emu_v1/MITgcm/ECCOV4/release4/flux-forced/emu_msim/mean_oceTAUX_oceTAUY/diags

Sampling time-mean heat flux run ...

from: /nobackupp17/ifukumor/emu_v1/MITgcm/ECCOV4/release4/flux-forced/emu_msim/mean_TFLUX_oceQsw/diags

Sampling time-mean freshwater flux run ...

from: /nobackupp17/ifukumor/emu_v1/MITgcm/ECCOV4/release4/flux-forced/emu_msim/mean_oceFWflx/diags

Sampling time-mean salt flux run ...

from: /nobackupp17/ifukumor/emu_v1/MITgcm/ECCOV4/release4/flux-forced/emu_msim/mean_oceSflux_oceSPflx/diags

Sampling time-mean pressure load run ...

from: /nobackupp17/ifukumor/emu_v1/MITgcm/ECCOV4/release4/flux-forced/emu_msim/mean_slceLoadPatmPload_nopabar/diags

Sampling time-mean initial condition run ...

from: /nobackupp17/ifukumor/emu_v1/MITgcm/ECCOV4/release4/flux-forced/emu_msim/mean_IC/diags

Computing individual control contribution ...

Done. Results are in

/nobackupp17/ifukumor/temp53/emu_atrb_m_1_beafortsea.msk_2/output

d) Attribution Tool output.

The Attribution Tool creates files in a directory bearing specification of the analysis in its name, which is **emu_atrb_m_1_beaufortsea.msk_2** for the case above. Here "**emu_atrb**" indicates output from the Attribution Tool, "**m**" for monthly mean variable, "1" for the first variable defining the objective function (1 is sea level), "**beaufortsea.msk**" for the file name defining the mask used for this first variable, and "2" for the total number of variables defining the objective function. User output is collected in a subdirectory named **output**.

The files in this **output** directory are described below for the example above. (Files are similar to those of the Sampling Tool, except there are more entries corresponding to different controls for the Attribution Tool.)

pfe20>lss emu_atrb_m_1_beaufortsea.msk_2/output

```
total 72
-rw-r--r-- 1 8764 atrb.out_312
-rw-r--r-- 1 1248 atrb.step_312
-rw-r--r-- 1 48202 atrb.txt
-rw-r--r-- 1 544 data.ecco
-rw-r--r-- 1 847 set samp.info
```

atrb.out 312

Monthly anomaly time-series of the objective function for the *Reference Run* (ref) and contributions to it from anomalies in different controls; i.e., surface forcing that consists of wind (tau), heat flux (htflx), freshwater flux (fwflx), salt flux (sflux) and pressure load (pload), and the initial state of the ocean (ic). The last number after "_" in the file name indicates the number of records in the anomaly time-series. The value 312 is the number of monthly mean values available from 1992 to 2017 for V4r4. The time-mean reference for the anomaly is given as the last set of variables in the file (mean).

The file contains the following variables in the order given. All variables are 312-element arrays except the last one (**mean**) which is a 7-element array with the time-mean references for the seven anomaly variables *ref*, *tau*, *htflx*, *fwflx*, *sflux*, *pload* and *ic*.

ref: Array of anomaly OBJF time-series of the *Reference Run* (float) tau: Array of anomaly OBJF time-series due to wind anomaly (float) htflx: Array of anomaly OBJF time-series due to heat flux anomaly (float) fwflx: Array of anomaly OBJF time-series due to freshwater flux anomaly (float) sflux: Array of anomaly OBJF time-series due to salt flux anomaly (float)

pload: Array of anomaly OBJF time-series due to pressure load anomaly (float) ic: Array of anomaly OBJF time-series due to initial state anomaly (float) mean: Array with time-mean OBJF reference for the variables above (float)

atrb.step 312

Time (hour from 12Z January 1, 1992) of the monthly mean values in **atrb.out_312**. Time here is the end instant of the averaging period of the sampled quantity (e.g., end of month). The file contains a single array (float) of 312-elements.

atrb.txt

A text file equivalent of binary files atrb.step_312 and atrb.out_312. The file has time-series of the user specified objective function (not its anomaly) listed in table format (see first line of file); time (hour from 12Z January 1, 1992), Reference Run (ref) and contributions to it from anomalies in different controls; i.e., surface forcing that consists of wind (tau), heat flux (htflx), freshwater flux (fwflx), salt flux (sflux) and pressure load (pload), and the initial state of the ocean (ic). The time here is the end instant of the averaging period of the sampled quantity (e.g., end of month).

data.ecco

An ECCO MITgcm namelist file (text file) defining the objective function, modified by **set_samp.x**, and used by **do_samp.x** to evaluate objective function from different runs.

set samp.info

A text file, created by **set_samp.x**, summarizing the user-specified objective function.

4. Installing the Tools

FOLLOWING IS OBSOLETE AND NEEDS UPDATING

This section describes steps to install the tool on NAS Pleiades, which should be similar for other computing systems.

User commands/input are given in RED. (Steps 1-4 in italic are the same as those for setting up the bulk-formula version of the model described in Wang et al. [2020].) System prompts, file names, and variables are in CYAN. (File names and directories are in **bold**.) pfe25> denotes Unix prompt.

Commands are summarized in file **install_cheatsheet.txt** for reference. Groups of commands are also available in shell script files **install_***.csh** where ******* refers to steps below.

1) Create and cd to a work directory

pfe25>mkdir WORKDIR

```
pfe25>cd WORKDIR
```

2) Download MITgcm "checkpoint 66g"

pfe25>git clone https://github.com/MITgcm/MITgcm.git -b checkpoint66g

3) Create and cd to subdirectory

```
pfe25>cd MITgcm

pfe25>mkdir -p ECCOV4/release4

pfe25>cd ECCOV4/release4
```

4) Download V4 configurations

pfe25>git clone https://github.com/ECCO-GROUP/ECCO-v4-Configurations

5) Extract flux-forced configuration of the model

```
pfe25>mv ECCO-v4-Configurations/ECCOv4\ Release\ 4/flux-forced .

pfe25>rm -rf ECCO-v4-Configurations

pfe25>cd flux-forced

pfe25>set basedir=`pwd`

pfe25>mkdir forcing
```

6) Download forcing from ECCO Drive. (Substitute username "fukumori" below with your own username and use your WebDAV password, <u>NOT</u> your Earthdata account password.) The second wget will take a while to complete.

```
pfe25>wget -P forcing -r --no-parent --user fukumori --ask-password -nH --cut-dirs=4 https://ecco.jpl.nasa.gov/drive/files/Version4/Release4/input_init
```

pfe25>wget -P forcing -r --no-parent --user *fukumori* --ask-password -nH --cut-dirs=4 https://ecco.jpl.nasa.gov/drive/files/Version4/Release4/other/flux-forced

7) Load module for compilation.

```
pfe25>module purge
pfe25>module load comp-intel/2020.4.304
```

```
pfe25>module load mpi-hpe/mpt
   pfe25>module load hdf4/4.2.12
   pfe25>module load hdf5/1.8.18 mpt
   pfe25>module load netcdf/4.4.1.1_mpt
   pfe25>module load python3/3.9.12
   pfe25>module list
8) Compile MITgcm program (generates executable "mitgcmuv")
   pfe25>mkdir build
   pfe25>cd build
   pfe25>../../../tools/genmake2 -mods=../code
   -optfile=../../../tools/build options/linux amd64 ifort+mpi ice nas -mpi
   pfe25>make depend
   pfe25>make all
   pfe25>cd ...
9) Derive adjoint of MITgcm by TAF and compile (generates executable "mitgcmuv_ad").
   This step requires a license for TAF. Skip if Adjoint Tool will not be used.
   pfe25>mkdir build ad
   pfe25>cd build_ad
   pfe25> ../../../tools/genmake2 -mods=../code -
   optfile=../code/linux amd64 ifort+mpi ice nas -mpi
   pfe25>make depend
   pfe25>make adtaf
   pfe25>make adall
```

```
pfe25>cd ...
10) Compile off-line passive tracer version of MITgcm (generates executable "mitgcmuv" in
   directory build_trc)
   pfe25>mkdir build trc
   pfe25>cd build trc
   pfe25>/bin/cp -f ../code offline ptracer/OFFLINE OPTIONS.h.fwd
   ../code offline ptracer/OFFLINE OPTIONS.h
   pfe25>../../../tools/genmake2 -mods=../code offline ptracer
   -optfile=../../../tools/build options/linux amd64 ifort+mpi ice nas -mpi
   pfe25>make depend
   pfe25>make all
   pfe25>cd ...
11) Compile off-line adjoint passive tracer version of MITgcm (generates executable
   "mitgcmuv" in directory build_trc_adj)
   pfe25>mkdir build_trc_adj
   pfe25>cd build trc adj
   pfe25>/bin/cp -f ../code offline ptracer/OFFLINE_OPTIONS.h.adj
   ../code offline ptracer/OFFLINE OPTIONS.h
   pfe25>../../../tools/genmake2 -mods=../code offline ptracer
   -optfile=../../../tools/build options/linux amd64 ifort+mpi ice nas -mpi
   pfe25>make depend
   pfe25>make all
   pfe25>cd ..
12) Prepare circulation fields for off-line adjoint passive tracer version of MITgcm
   pfe25>cd forcing/other/flux-forced
```

```
pfe25>cp -p ../../scripts/* .
   pfe25>sh -xv reverseintime all.sh
   pfe25>cd ../../..
13) Download scripts and programs for the Tools and compile.
   pfe25>git clone https://github.com/ECCO-GROUP/ECCO-EIS.git
   pfe25>mv ECCO-EIS/emu.
   pfe25>rm -rf ECCO-EIS
   pfe25>cd emu
   pfe25>make all
14) Download data files needed by the Tool (pert xx.scale). Substitute username "fukumori"
   below with your own username and use your WebDAV password, NOT your Earthdata
   account password.
   pfe25>wget -r --no-parent --user fukumori --ask-password -nH --cut-dirs=7
   https://ecco.jpl.nasa.gov/drive/files/Version4/Release4/other/flux-
   forced/tool_pert_data
15) Modify scripts. (Specify directory where the tool files are set up. cf step 5)
   pfe25>sed -i -e "s|SETUPDIR|${basedir}|g" *.csh
16) Run Perturbation Tool without perturbation to obtain reference results.
   This job will produce results under a new directory named emu pert ref in basedir (step
   5).
   pfe25>qsub pbs pert ref.csh
17) Copy tools (setup_*.csh, README_* and this Guide) for user access. Replace
   FORUSERDIR below to a full directory path name where you want to install (copy) the
   tools at.
   pfe25>set useraccessdir=FORUSERDIR
   pfe25>if (! -d ${useraccessdir}) mkdir ${useraccessdir}
```

```
pfe25>sed -i -e "s|PUBLICDIR|${useraccessdir}|g" setup_*.csh
pfe25>sed -i -e "s|PUBLICDIR|${useraccessdir}|g" README*

pfe25>cp -p emu_*.csh ${useraccessdir}}

pfe25>cp -p README_* ${useraccessdir}

pfe25>cp -p Guide*.pdf ${useraccessdir}
```

5. References

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- Wang, O., I. Fukumori, and I. Fenty, 2022: Offline passive tracer, https://github.com/ECCO-GROUP/ECCO-v4-Configurations/blob/master/ECCOv4%20Release%204/flux-forced/doc/README offline ptracer.md