TP 2 - Members in the US Electoral College

General information

Population data is from 2016. We chose to use the eligible population as it is more representative of the 2016 Elections.

Linear Programming problem

Results and optimization

With our problem as stated before, we have a rather disturbing problem as we can see that some states have fairly similar populations but sometimes have double the members in the electoral college. This is particularly obvious when we took at the lower end of the population spectrum where there isn't a lot of population but we might see for example (insert problem with close population but 1 vs 2 members). This is due to a matrix conditioning problem when working on the LP problem as the orders of magnitude vary greatly between 10^{-6} ($u,\ v$), 10^{0} (α_i) and 10^{6} (x_i).

Thus, our problem has been slightly modified to :

$$\begin{cases} min\ u - v & \\ v - \frac{\alpha_i}{x_i} \times 10^6 & \leq 0 \\ \frac{\alpha_i}{x_i} \times 10^6 - u & \leq 0 \\ \sum\limits_i \alpha_i & = N \end{cases} \tag{1}$$

By doing this, we will do some kind of preconditioning which will make our results better. With this change, the number of members per state is given by (using the state ANSI abreviations):

State	Voting Population	Members in Electoral C.	$\frac{\alpha_i \times 10^6}{x_i}$
Alabama	3 609 447	9	2.493
Alaska	522 679	1	1.913
Arizona	4 740 310	12	2.531
Arkansas	2 140 097	5	2.336
California	25 104 844	49	1.952
Colorado	3 974 405	10	2.516
Connecticut	2 582 761	6	2.323
Delaware	691 720	1	1.446
DC	515 248	1	1.941
Florida	14 601 066	37	2.534
Georgia	6 959 963	17	2.443
Hawaii	1 012 860	2	1.975
Idaho	1 166 706	2	1.714
Illinois	8 985 443	22	2.448
Indiana	4 849 937	12	2.474
Iowa	2 288 536	5	2.185
Kansas	2 054 025	5	2.434
Kentucky	3 282 420	8	2.437
Louisiana	3 384 435	8	2.364
Maine	1 058 372	2	1.890
Maryland	4 189 616	10	2.387
Massachusetts	4 948 028	12	2.425
Michigan	7 420 628	18	2.426
Minnesota	3 973 204	10	2.517
Mississippi	2 191 241	5	2.282
Missouri	4 517 925	11	2.435
Montana	804 250	2	2.487
Nebraska	1 343 821	3	2.232
Nevada	1 961 587	4	2.039
New Hampshire	1 042 795	2	1.918
New Jersey	6 013 656	15	2.494
New Mexico	1 464 515	3	2.048
New York	13 604 645	34	2.499
North Carolina	7 352 501	18	2.448
North Dakota	566 783	1	1.764
Ohio	8 736 808	22	2.518
Oklahoma	2 778 219	7	2.520
Oregon	3 024 174	7	2.315
Pennsylvania	9 691 160	24	2.476
Rhode Island	786 012	2	2.554
South Carolina	3 709 283	9	2.426
South Dakota	631 173	1	1.584
Tennessee	4 909 426	12	2.444
Texas	17 448 910	44	2.522
Utah	1 991 885	5	2.510
Vermont	494 871	1	2.021
Virginia	6 027 152	15	2.489
Washington	5 123 020	13	2.538
West Virginia	1 423 031	3	2.108
Wisconsin	4 285 071	10	2.334
Wyoming	429 682	1	2.327

US Maps

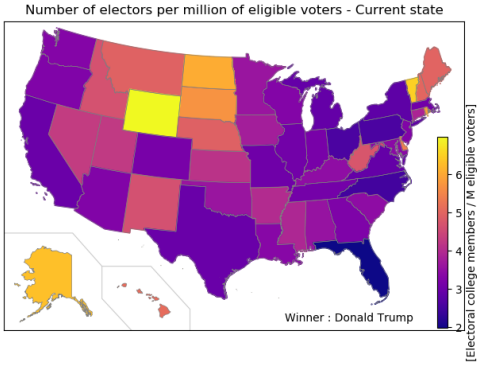

Figure 1: Current distribution : $\frac{\alpha_{real,eligible_i}}{x_i}$

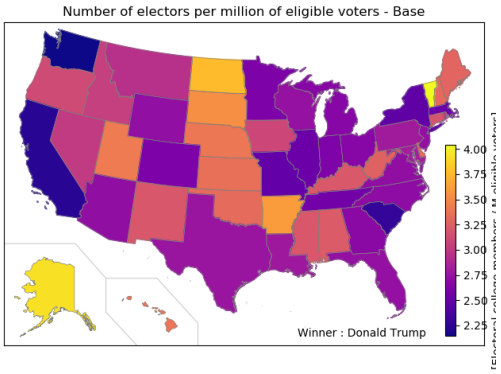

Figure 2: Distribution without conditioning - Eligible voters only

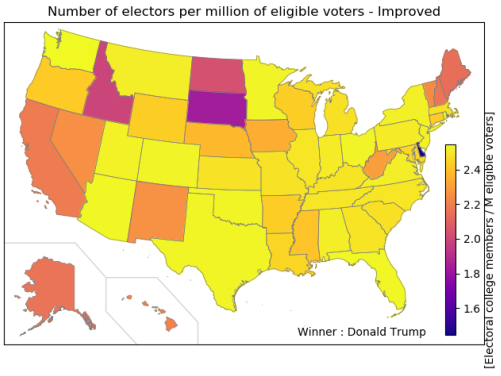

Figure 3: Distribution with conditioning - Eligible voters only

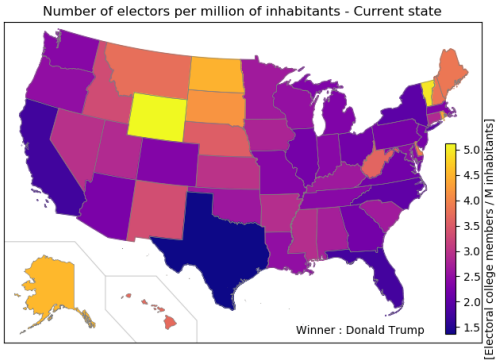

Figure 4: Current distribution : $\frac{\alpha_{real,total_i}}{x_i}$

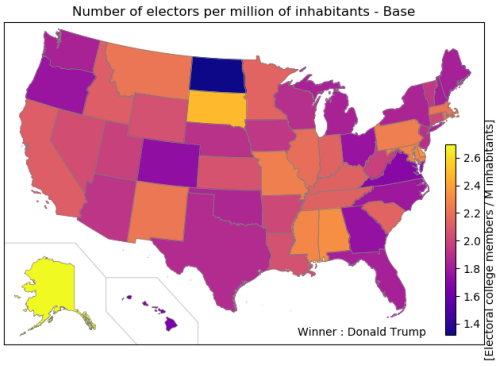

Figure 5: Distribution without conditioning - Whole population

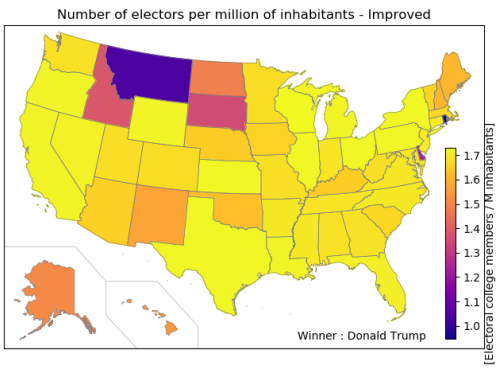

Figure 6: Distribution with conditioning - Whole population