Problem 1)

1. Task: Write a function to return the intervals of a one iteration golden section search.

**function** **[**lowerX**,**upperX**]** **=** GetGoldenRulePoints**(**lowerBound**,**upperBound**)**

%

% [lowerX, upperX] = GetGoldenRulePoints(lowerBound, upperBound)

%

% This is a function used to get the starting x values for the golden rule

% search. It will return these two x values.

% Input:

% lowerBound: This is the lower bracket of our search

% upperBound: This is the upper bracket of our search

% Outuput:

% lowerX: This is the lower x value for the start of our search

% upperX: This is the upper x value for the search.

lowerX **=** upperBound **-** **((**1.618 **-** 1**)** **\*** **(**upperBound **-** lowerBound**));** % Calculates our lower x value

upperX **=** lowerBound **+** **((**1.618 **-** 1**)** **\*** **(**upperBound **-** lowerBound**));** % Calculates our upper x value

**end** % end function

1. Task: Use the function from 1A, and calculate x1, and x2, given the interval [5, 7]. Then, throw out the left most area and repeat. Next, do the same for the right most, and finally throw out the last left most area.

Below is the code for this, as well as a graph showing the X values after each run of this function.

% Problem 1

% base function call with bounds of 5 and 7

**[**lowerX0**,** upperX0**]** **=** GetGoldenRulePoints**(**5**,** 7**);**

% second function call, throwing out the left region

**[**lowerX1**,** upperX1**]** **=** GetGoldenRulePoints**(**lowerX0**,** 7**);**

% third function call, throwing out right region

**[**lowerX2**,** upperX2**]** **=** GetGoldenRulePoints**(**lowerX0**,** upperX1**);**

% the final bounds after throwing out the final left region are lowerX2, and upperX1

|  |  |  |  |
| --- | --- | --- | --- |
| x | First Function Call | Second Function Call | Third Function Call |
| x2 (lower x) | 5.7640 | 6.2362 | 6.0558 |
| x1 (upper x) | 6.2360 | 6.5278 | 6.2361 |

This is the table for the x values after each function call

The final bounds after throwing out the last left region are lower x: 6.0558, upper x:6.5278

Problem 2)

1. Task: Find the derivative of the function:
2. Task: Write a Newton Raphson root solver function.

**function** **[**rootLocation**,**numIterations**]** **=** NewtonRaphson**(**initialGuess**,**func**,** ...

funcDerivative**,** error**,** maxIterations**)**

%

% function [rootLoc,numIterations] = NewtonRaphson(initialGuess,func, ...

% funcDerivative, aoe, maxIterations)

%

% This is a function using the newton raphson method to calculate a root

% This calculation is done based on the func, and funcDerivative

% Inputs:

% initalGuess: This is our initial guess for the root of the function

% func: This is the function we are evaluating at

% funcDerivative: This is the derivative of the function used

% error: This is our desired margin of error. Once we reach this we are done

% maxIterations: This is the maximum number of times we want to loop

% through this function, searching for a root

% Outputs:

% rootLocation: This is our location of the root of the func

% numIterations: This is the number of iterations taken to find root

% If the user doesnt inclue 5 items in constructor

% or if our max iterations is empty

% then set max iterations to 100

**if** **(**nargin **<** 5 **||** isempty**(**maxIterations**))**

maxIterations **=** 100**;**

**end** % end if

% If the user doesnt include 4 items in constructor

% or if the error is empty, then set our error

**if** **(**nargin **<** 4 **||** isempty**(**error**))**

error **=** 1e-6**;**

**end** % end if

numIterations **=** 0**;** % sets our initial iterations

y0 **=** func**(**initialGuess**);** % gets our y naught

y0Prime **=** funcDerivative**(**initialGuess**);** % gets y prime naught

relativeChange **=** abs**(**error**)** **\*** 100**;** % Forces the function to run once

% This is a while loop for finding our intercept

% while our relative change is greater than our error,

% and while the iterations is less than our max

% we continue calculations for finding the intercept

**while** **((**relativeChange **>** error**)** **&&** **(**numIterations **<** maxIterations**))**

numIterations **=** numIterations **+** 1**;** % increment iterations

newPointX **=** initialGuess **-** **(**y0 **/** y0Prime**);** % find our new x value

% this calcualtes our new relative change

relativeChange **=** abs**((**newPointX **-** initialGuess**)** **/** newPointX**);**

initialGuess **=** newPointX**;** % assign our 'guess' to our new point

y0 **=** func**(**initialGuess**);** % calculate y naught

y0Prime **=** funcDerivative**(**initialGuess**);** % calculate y naught prime

**end** % end while

% once we are done looping, we assign

%the root location to our initial guess

rootLocation **=** initialGuess**;**

1. Task: Create a vector with several hundred points ranging from -3 to 3, then use these points as our guesses and call the Newton Raphson method. Then, store the result of the function call in a vector of same size as the guesses.

% Problem 2

% func is the function used in 2a

func **=** **@(**x**)** x**^**10 **-** **(**10 **\*** **(**x**^**5**))** **+** **(**0.5 **\*** exp**(**x**))** **-** 0.45**;**

% derivativeFunc is the derivative of func

derivativeFunc **=** **@(**x**)** **(**10 **\*** x**^**9**)** **-** **(**50 **\*** **(**x**^**4**))** **+** **(**0.5 **\*** exp**(**x**));**

guessValue **=** linspace**(-**3**,** 3**,** 400**);** % 400 guesses from -3 to 3

root **=** linspace**(**1**,** 400**,** 1**);** % 400 space vector filled with guesses

% i is a value used for indexing root

% fill each spot of root with the root guess

% from the function call to newton raphson

**for** i **=** 1**:**400

root**(**i**)** **=** NewtonRaphson**(**guessValue**(**i**),** func**,** derivativeFunc**);**

**end** % end for

The four values that show up in the root vector are: -0.4120, -0.1057, 0.5243, and 1.5785.

1. Task: Does N-R always find the closest root? Find at least one spot where it doesn’t, and explain what happens in words.

No, Newton Raphson does not always find the closest root. In my vector of 400 guesses evenly spaced from -3 to 3, at a guess value of 0.02932, it tells me the root is -0.4120. This happens when we are near a maximum or minimum value of the function. In the case above, it skips to the -0.4120 value because it is a point near a maximum, so the slope is not very steep. So, when it does the necessary calculations to find the next X value, because y’ is closer to 1, it goes back farther and it skips over the closest root it had previously been attaching to.