

Smart Control of 2-Degree of Freedom Helicopters

by

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Abstract

This project proposes a modular and cost-effective smart real-time motion control framework for a group of two degrees of freedom (2-DOF) helicopters. The helicopter are controlled by a mobile device which sends position signals over a wireless network to a microcontroller. The microcontroller uses control algorithms to determine the amount of voltage to apply to DC motors. This project tests and compares three control algorithms, LQR, LQG, and ADP as well as theorizes possible methods to improve the control in future projects.

Acknowledgements

Special Thanks to Andrew Fandel, Anthony Birge, and Dr. Suruz Miah for their work with Machine Learning on a 2-DOF Helicopter.

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Thank you to everyone else who helped make this project possible and sucessful.

Dedication

This is dedicated to the one I love.

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Abbreviations

2-DOF - 2 Degrees-Of-Freedom

ADP - Approximate Dynamic Programming

LQG - Linear Quadratic Gaussian

LQR - Linear Quadratic Regulator

RMSE - Root Mean Square Error

SPI - Serial Peripheral Interface

TCP - Transmission Control Protocol

UDP - User Datagram Protocol

USB - Universal Serial Bus

Mathematical Symbols

D_p - viscous damping of the pitch axis

D_y - viscous damping of the yaw axis

J_p - moment of inertia about pitch axis

J_y - moment of inertia about yaw axis

K_{sp} - stiffness of the axes

K_{pp} - pitch motor thrust constant

K_{py} - thrust constant acting on the pitch angle from the yaw motor

K_{yp} - thrust constant acting on yaw angle from pitch motor

K_{yy} - yaw motor thrust constant

Chapter 1

Introduction

1.1 Problem Statement

Helicopters are of a paramount importance as they are used in many civilian and military applications due to their ability for vertical take-off and landing. To enable their use in such applications, intensive research has been conducted to date since helicopters involve complex nonlinear dynamics. Most of the work on helicopter based research requires dedicated computers for controlling their motion to specific configurations and resistant to turbulent conditions. Such methods are expensive and time-consuming to develop. Implementation of motion control techniques using cost-effective hardware is still a challenge.

In this project, we are proposing an algorithm for smart control of a team of two degree-of freedom (two-DOF) helicopters using conventional motion control in cooperation with machine learning techniques where a user will be able to configure helicopters from any initial position. Even though conventional techniques have been tested with simple platforms in the literature, the current project employs conventional motion control strategies in cooperation with machine learning technique (reinforcement learning, for instance) for a team of helicopters as well as introducing user control via mobile devices. This project is expected to encourage research in this area as well as serve as an educational tool in teaching environments.

1.2 Literature Review

Our project requires a great deal of research as some of our tasks have not been attempted before. As a result, we have examined research papers, work complete by other projects at Bradley University, and documentation/teaching materials from Quanser Inc.

Among the major challenges in developing unmanned systems is to implement a modular, cost-effective, and robust teleoperation system, where the motion of a group of helicopters is controlled by mobile devices. In some cases, computer simulations are conducted

to reveal the performance control structures of a 2-DOF helicopter [7]. A large body of research has been conducted in the literature to focus on developing different control structures, such as linear-quadratic regulators (LQR)/Gaussian (LQG), sliding-mode controls (SMC), and advance nonlinear controls, that are specifically applied to 2-DOF helicopters. See [8, 1], for example, and some references therein. Furthermore, soft-computing tools, such as fuzzy-logic, neural networks, and a few combinations of them are employed for controlling the motion of a 2-DOF helicopter [2, 6, 4, 5].

The documentation of Quanser AERO¹ employs LQR and LQG motion control techniques for teaching purposes. This involves creating a linearized system model to calculate the LQR state-feedback gain. A model reference adaptive control (MARC) scheme using Lyapunov functions has been used by [8] for adaptive motion control of a 2-DOF helicopter. SMC is a nonlinear control technique to drive the system states onto a surface in the state space. This method has been used by [1]. Fuzzy-logic controllers use an inference engine to produce an output as used in [2, 6]. The ADP technique does not rely on knowledge of the system model. Instead, it uses data to reconstruct the states as preformed by [4]. Authors in [5] used high order neural networks (HONN) to approximate non-linearities in the system model.

As can be noticed, most of the motion control techniques are either tested using computer simulations or use dedicated computational platforms, that may not be modular and/or cost-effective, for developing motion control algorithms. This is due to the fact that the aforementioned techniques are mainly to propose novel motion control techniques and not focused on hardware implementation platforms. Therefore, the current work considers implementing a conventional motion control technique using modular and cost-effective hardware platforms in the context of a teleoperation system, where a human operator has the ability to control the motion of a team of helicopters using a smart mobile device.

1.3 Report Organization

This report is organised into 6 chapters. Chapter 1 discusses what this project hopes to accomplish and what similar projects have completed. Chapter 2 explains how to create a mathematical model for the system. Chapter 3 provides a brief explanation of the control algorithms and architectures used. Chapter 4 contains the results from our simulations. Chapter 5 discusses results from USB, Raspberry Pi, and Mobile Device implementation. Chapter 6 concludes the paper and provides insight into future directions.

¹See <https://www.quanser.com/> for details

Chapter 2

Modeling 2-DOF Helicopters

The 2-DOF helicopter, Quanser Aero [manufactured by Quanser Inc. (<https://www.quanser.com/>)], used in the current work can be configured as a dual-rotor helicopter that has a fixed base. The front rotor (horizontal to the ground) is configured to rotate about pitch axis and the

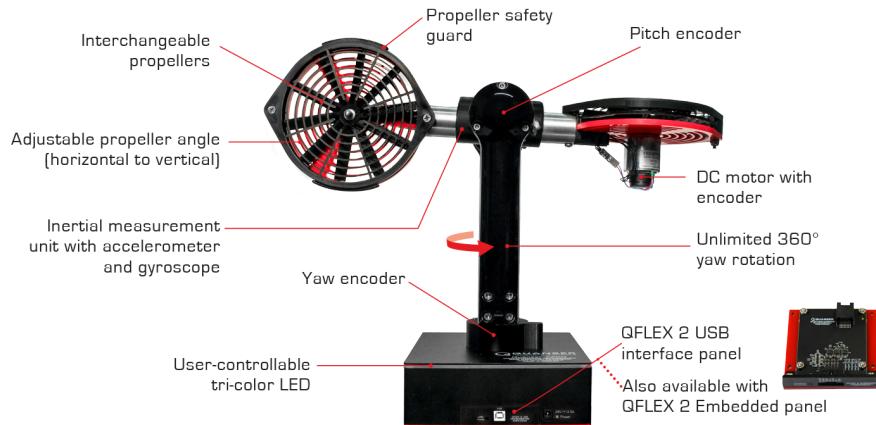


Figure 2.1: The Quanser Aero 2-DOF used for experiments in the project.

tail rotor (parallel to vertical plane) is mounted to rotate about yaw axis. To measure the pitch (θ) and yaw (ψ) angles, two position sensors (encoders) are mounted as shown in Fig. 2. For sake of simplicity in modeling 2-DOF helicopter, the dynamic coupling of the Quanser Aero is omitted due to high-efficiency rotors mounted on it¹. The main (tail) rotor is attached to the horizontal (vertical) propeller, which is rotated by applying input voltages to corresponding DC motors. Let $v_p(v_y)$ denote the input voltage to pitch (yaw) DC motor and the state of the 2-DOF helicopter at time $t \geq 0$ is denoted by $\mathbf{x}^T(t) \equiv [\theta(t), \psi(t), \dot{\theta}(t), \dot{\psi}(t)]$, where $\dot{\theta}(\dot{\psi})$ denote the rotational speed of the pitch (yaw). The free-body diagram of the 2-DOF helicopter is shown in Fig. 2.2,

where $F_p(F_y)$ is force from the pitch (yaw) motor. If $\mathbf{u}^T(t) \equiv [v_p(t), v_y(t)]$ denote the vector of the input voltages for DC motors at time $t \geq 0$, then the state-space model of

¹See Quanser Aero user manual for details.

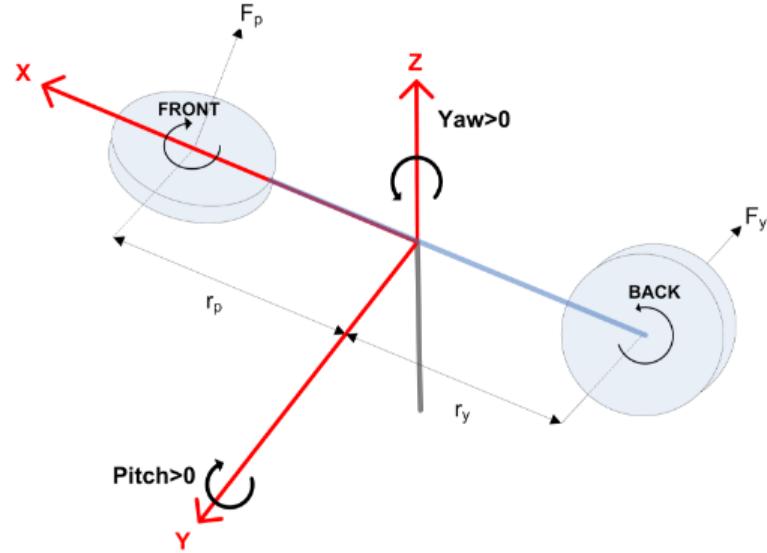


Figure 2.2: Freebody diagram of the forces exerted on a 2-DOF helicopter.

the 2-DOF helicopter (Quanser Aero) is described by [3]:

$$\dot{\mathbf{x}}(t) = \mathbf{Ax}(t) + \mathbf{Bu}(t), \text{ where} \quad (2.1)$$

$$\mathbf{A} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ -\frac{K_{sp}}{J_p} & 0 & -\frac{D_p}{J_p} & 0 \\ 0 & 0 & 0 & -\frac{D_y}{J_y} \end{bmatrix} \text{ and } \mathbf{B} = \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ \frac{K_{pp}}{J_p} & \frac{K_{py}}{J_p} \\ \frac{K_{yp}}{J_y} & \frac{K_{yy}}{J_y} \end{bmatrix},$$

with K_{sp} , K_{pp} , K_{py} , K_{yp} , K_{yy} , J_p , J_y , D_p , and D_y being the stiffness of the axes, pitch motor thrust constant, thrust constant acting on the pitch angle from the yaw motor, thrust constant acting on yaw angle from pitch motor, yaw motor thrust constant, moment of inertia about pitch axis, moment of inertia about yaw axis, viscous damping of the pitch axis, and viscous damping of the yaw axis, respectively.

In the context of a teleoperation system, a standard problem in controlling motion of states of a 2-DOF helicopter is to find optimal actuator commands $\mathbf{u}^*(t) \equiv [v_p^*(t), v_y^*(t)]^T$, such that it follows the command signal, which is the desired (reference) state $\mathbf{x}^d = [\theta^d, \psi^d, 0, 0]^T$, sent by the human operator through a mobile device.

Chapter 3

Control Algorithms

This chapter discusses the three control algorithms used in the experiment. These are linear quadric regulator (LQR)

3.1 LQR

After creating the system model

$$\dot{\mathbf{x}} = \mathbf{Ax} + \mathbf{Bu}$$

use the state feedback law

$$\mathbf{u} = -\mathbf{Kx}$$

to minimize the quadratic cost function:

$$J(\mathbf{u}) = \int_0^{\infty} (\mathbf{x}^T \mathbf{Q} \mathbf{x} + \mathbf{u}^T \mathbf{R} \mathbf{u} + 2\mathbf{x}^T \mathbf{N} \mathbf{u}) dt$$

Find the solution \mathbf{S} to the Riccati equation

$$\mathbf{A}^T \mathbf{S} + \mathbf{S} \mathbf{A} - (\mathbf{S} \mathbf{B} + \mathbf{N}) \mathbf{R}^{-1} (\mathbf{B}^T \mathbf{S} + \mathbf{N}^T) + \mathbf{Q} = 0$$

Calculate gain, \mathbf{K}

$$\mathbf{K} = \mathbf{R}^{-1} (\mathbf{B}^T \mathbf{S} + \mathbf{N}^T)$$

3.2 LQG

- Utilizes gain calculated in LQR
- Added Kalman filter to reduce external disturbances to the system

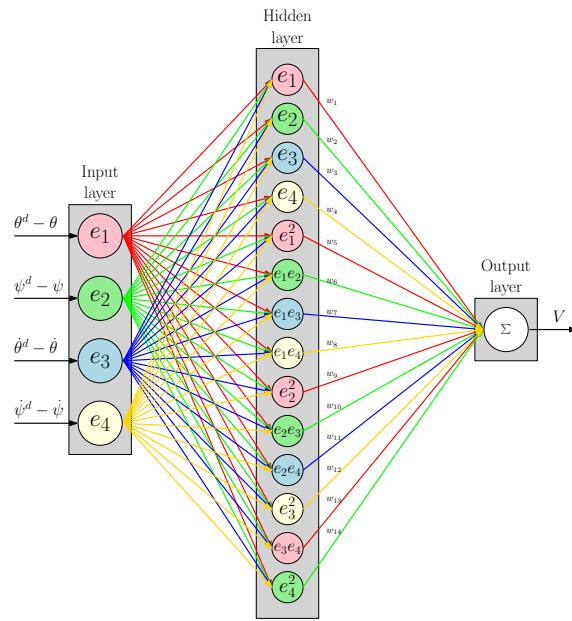


Figure 3.1: Input nodes are connected to the hidden layer and then to the output layer.

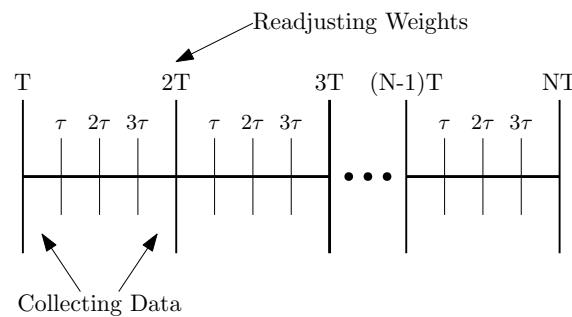


Figure 3.2: Data is collected for every τ seconds and then the weights are adjusted every T seconds.

3.3 ADP

3.4 Improvements

Most of these algorithms are typically implemented only using proportional gain which causes steady-state error to certain input signals in some systems. In our case, we experience steady-state error for a step input. To reduce this, the type of the controller needs to be increased by adding an integrator. We solve this problem by implementing a PI controller where LQR and ADP are used to find the optimal proportional and integral gain.

This is done by creating an augmented matrix with A and B with different dimensions

Chapter 4

Numerical Simulations

4.1 LQR (P controller)

Using MATLAB, we created a program, as seen in [B.1](#), that calculates LQR for our helicopter and then uses differential equations to simulate the trajectory. [4.1\(a\)](#) [4.1\(b\)](#) [4.1\(c\)](#)

4.2 LQR (PI controller)

Insert Block diagram for LQR PI simulation

4.3 LQG (PI Controller)

Insert Block diagram for LQG PI simulation

4.4 Conclusions

Note: constant used pitch XXXX degrees, yaw XXXX degrees

Note: square used pitch XXXX degrees with period of XXXX, yaw XXXX degrees with period of XXXX

Note: sine used pitch XXXX degrees with period of XXXX, yaw XXXX degrees with period of XXXX

Based on the results XXXX preformed better in the simulations.

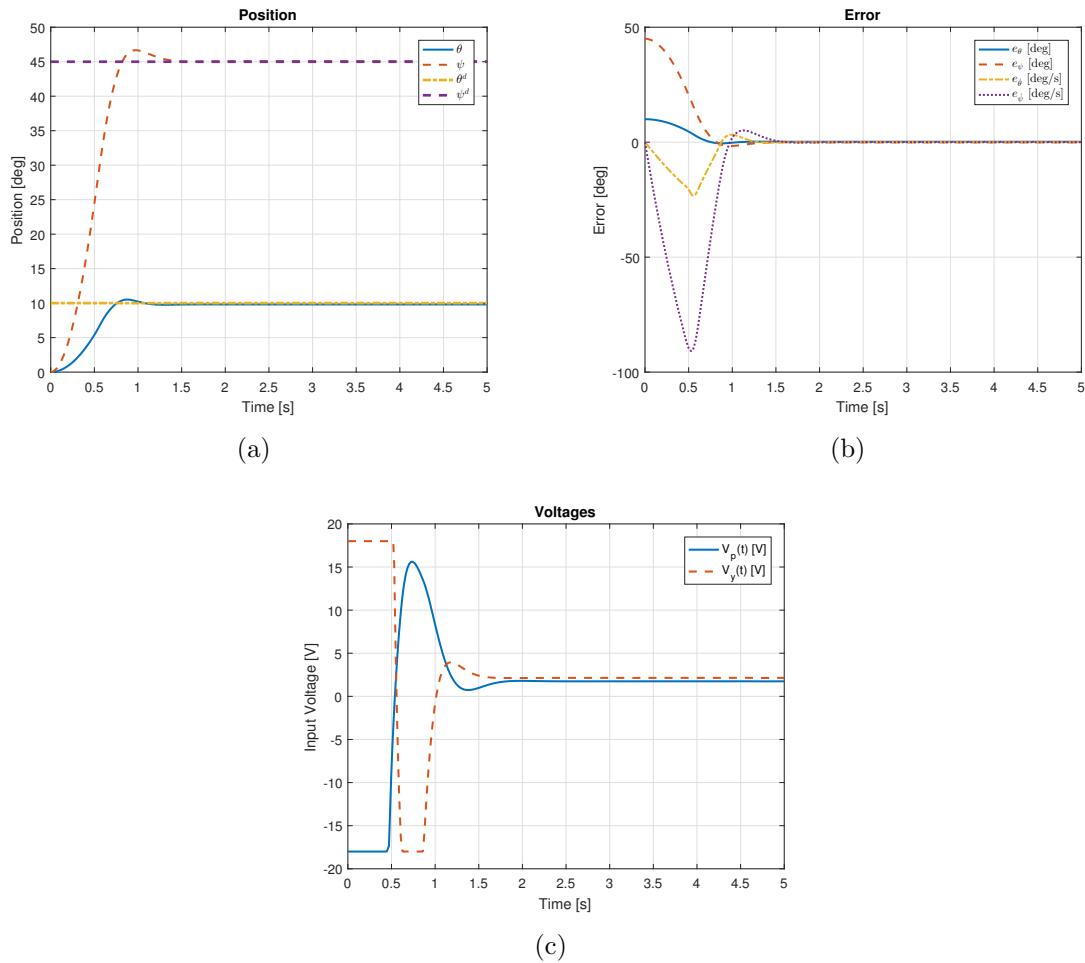


Figure 4.1: Simulations for proportional gain calculated by LQR.

	LQR(P)	LQR(PI)	LQG(PI)
RMSE Pitch Step	?	?	?
RMSE Yaw Step	?	?	?
RMSE Pitch Square	?	?	?
RMSE Yaw Square	?	?	?
RMSE Pitch Sine	?	?	?
RMSE Yaw Sine	?	?	?

Table 4.1: Error Comparison for Simulated Algorithms

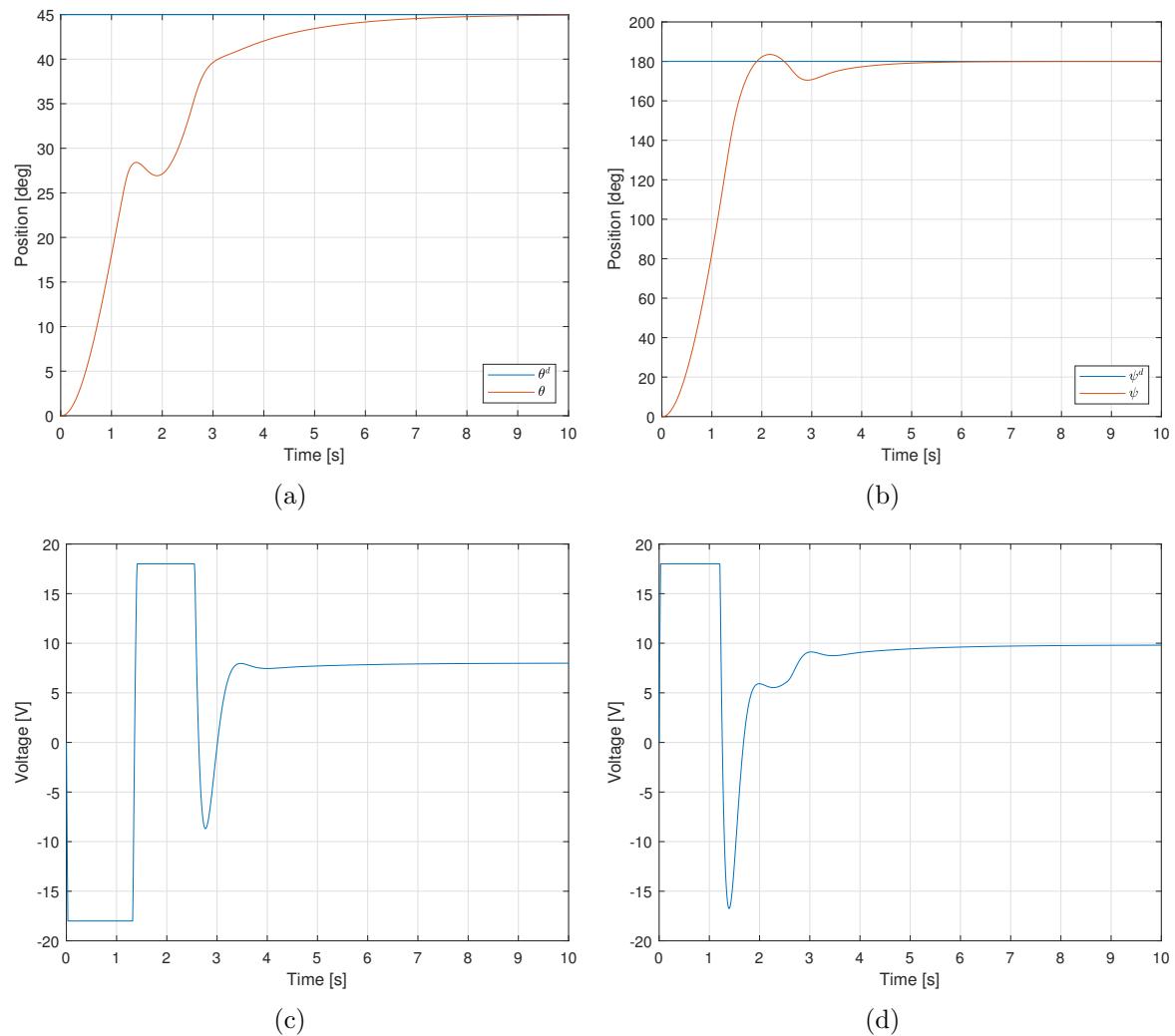


Figure 4.2: Simulations for proportional and integral gain calculated by LQR.

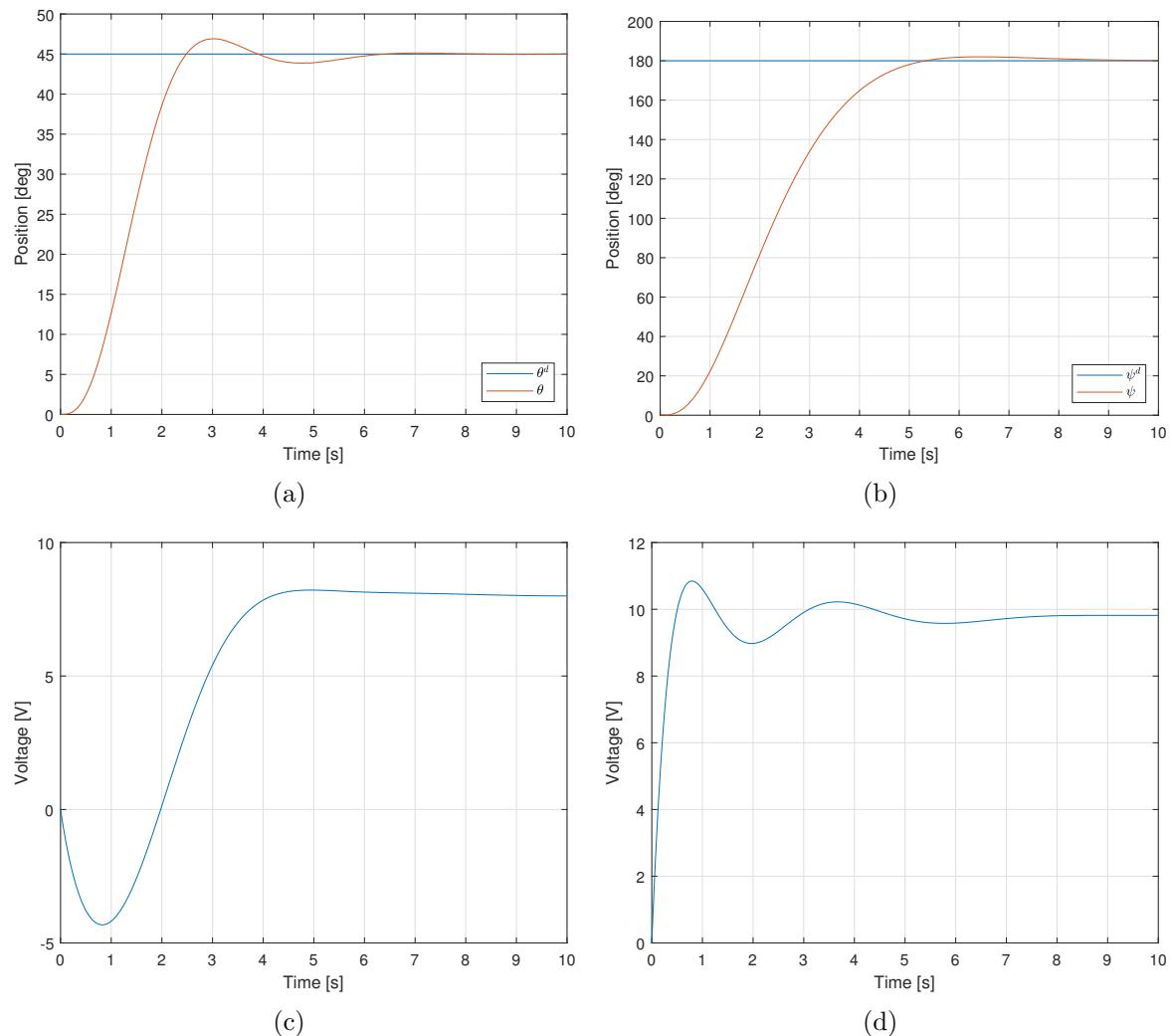


Figure 4.3: Simulations for proportional and integral gain calculated by LQG.

Chapter 5

Implementation

5.1 Experimental Setup

5.1.1 USB

5.1.2 Raspberry Pi

The communication protocol utilized by the Q-Flex2 embedded panel is SPI.

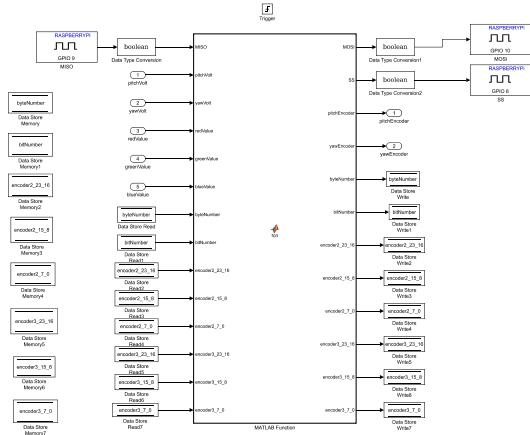


Figure 5.1: Block diagram of SPI communication protocol used for communication between the Raspberry Pi and Quanser Aero.

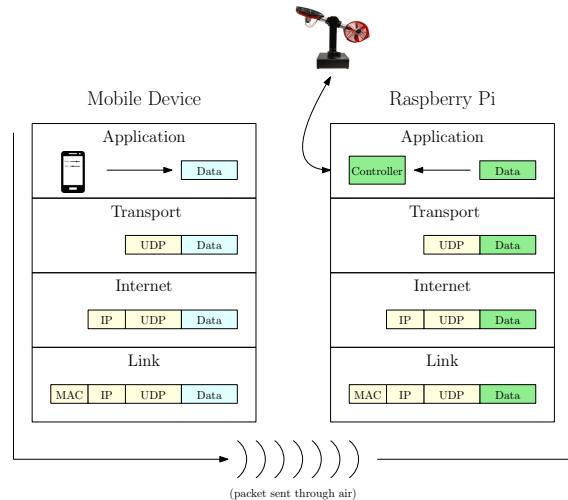


Figure 5.2: Illustration of the TCP model which describes how packets are sent and received from mobile devices to the Quanser Aero.

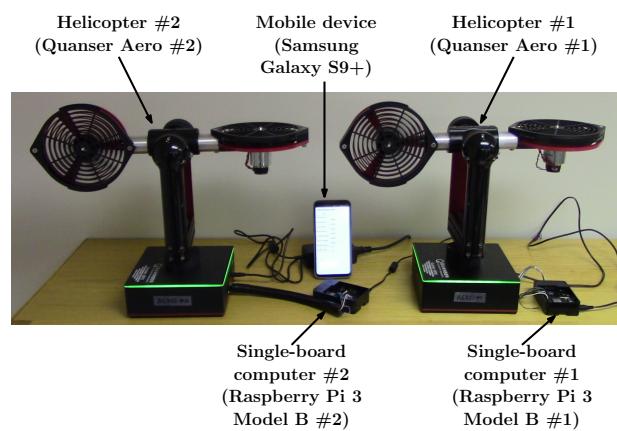


Figure 5.3: Experiment setup for controlling the Quanser Aerostats via a mobile device.

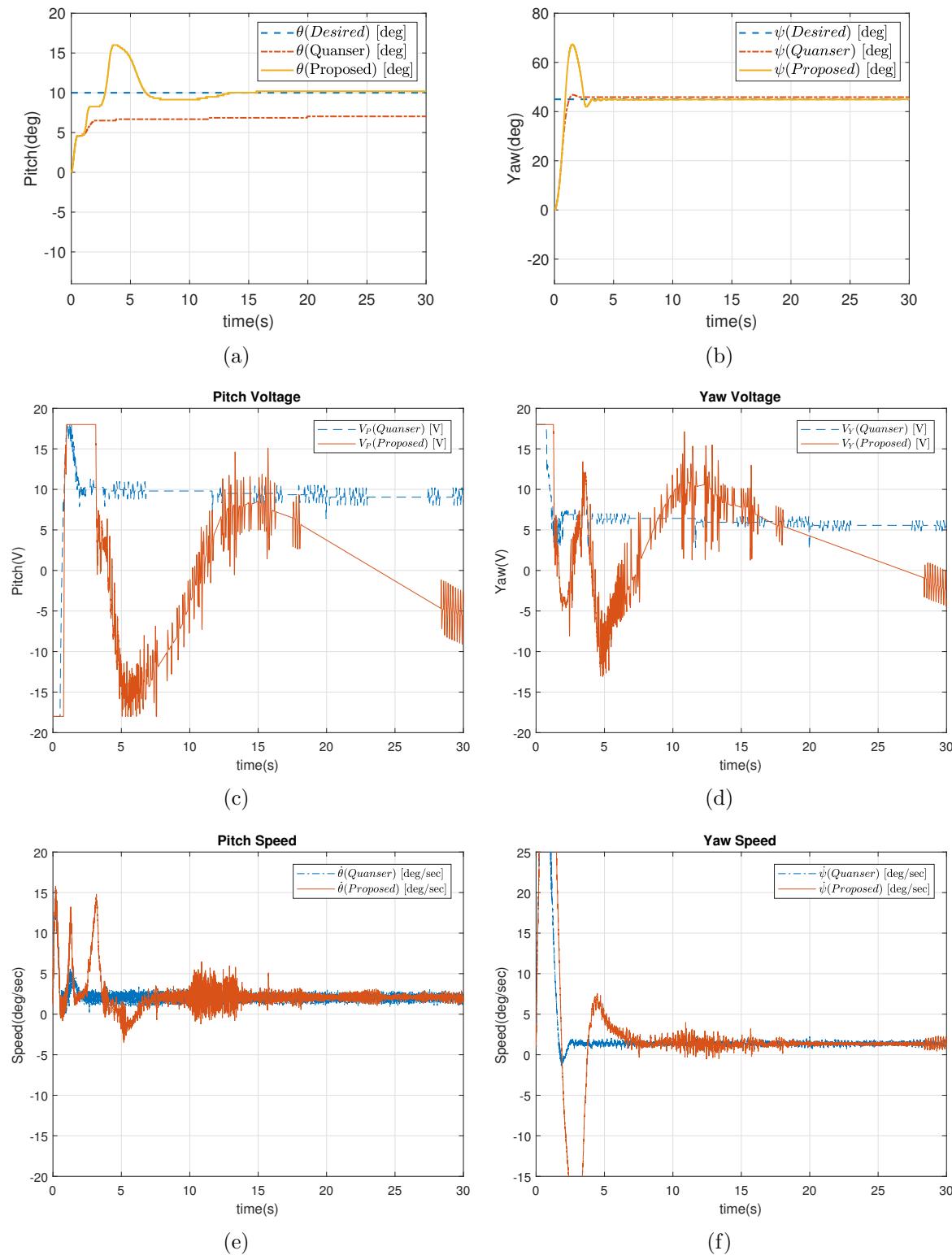


Figure 5.4: USB implementation for proportional controller and proportional-integral controller calculated by LQR with a step input.

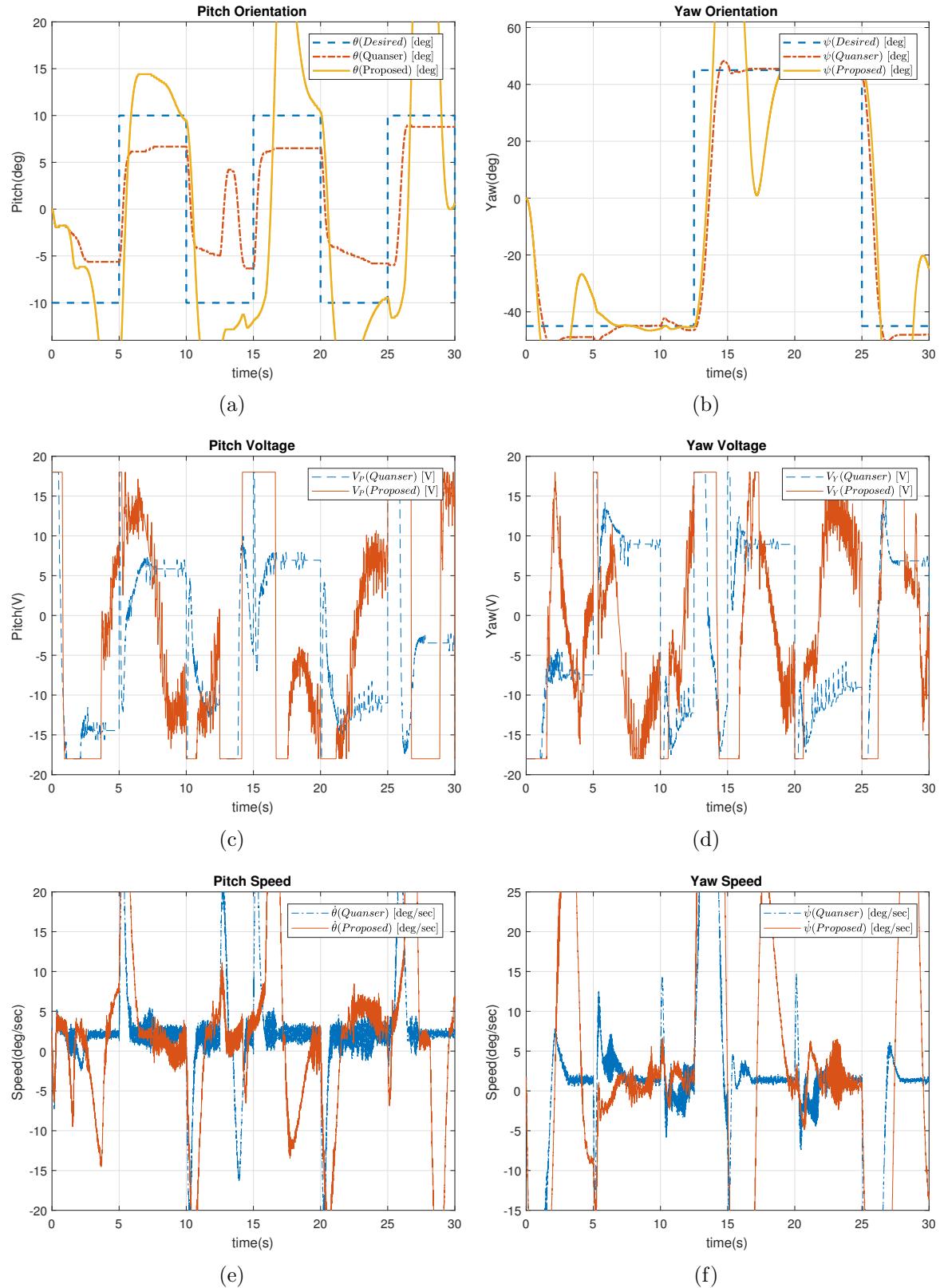


Figure 5.5: USB implementation for proportional controller and proportional-integral controller calculated by LQR with a square wave input.

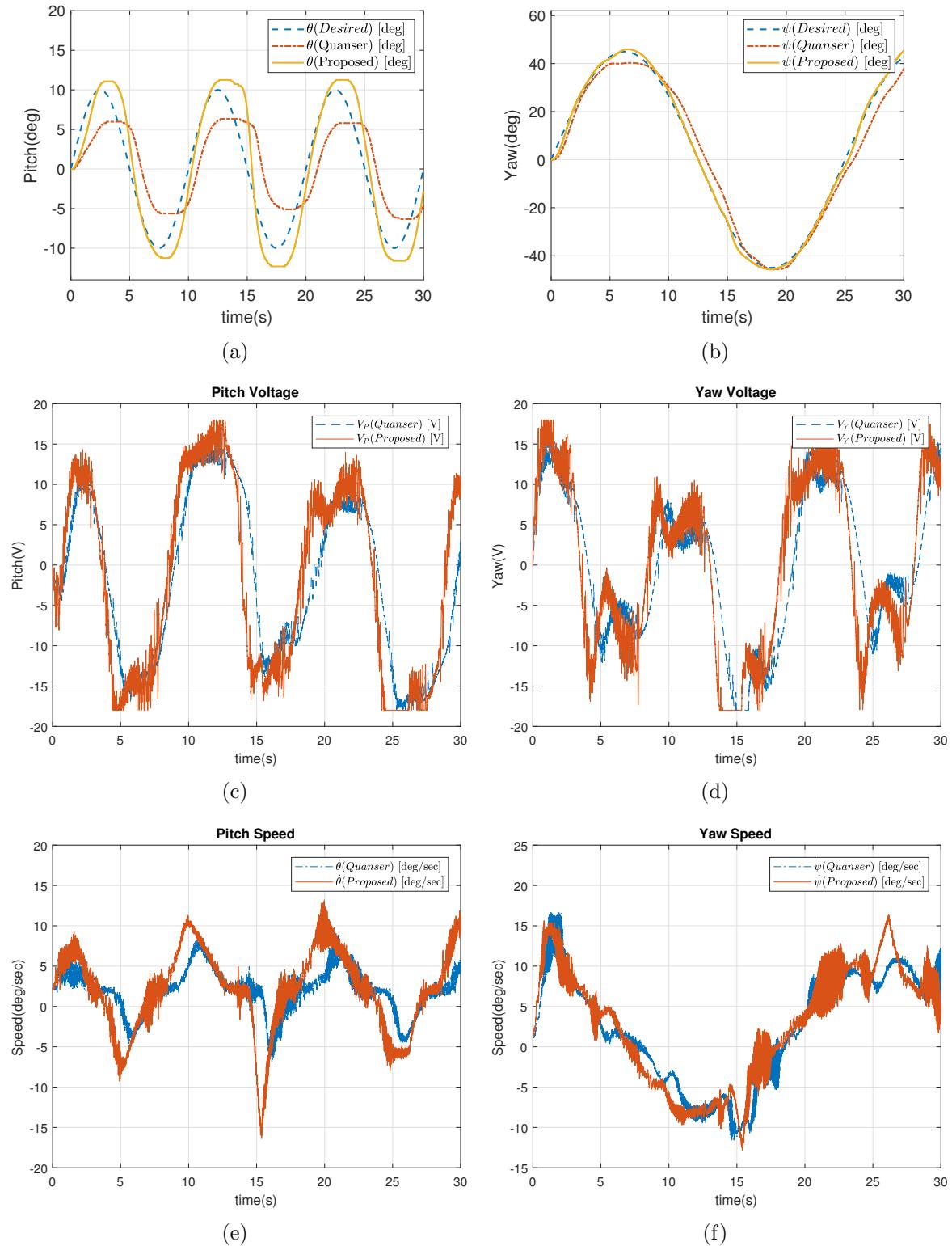


Figure 5.6: USB implementation for proportional controller and proportional-integral controller calculated by LQR with a sinusoidal input.

5.1.3 Android

5.2 USB

5.2.1 LQR

5.2.2 LQG (PI Controller)

5.2.3 ADP

5.2.4 Conclusions

Note: constant used pitch 10 degrees, yaw 45 degrees

Note: square used pitch XXXX degrees with period of XXXX, yaw XXXX degrees with period of XXXX

Note: sine used pitch XXXX degrees with period of XXXX, yaw XXXX degrees with period of XXXX

Based on the results XXXX preformed better for USB.

	LQR(P)	LQR(PI)	ADP(P)
RMSE Pitch Step	2.6454	?	1.3067
RMSE Yaw Step	5.7991	?	6.1991
RMSE Pitch Square	?	?	?
RMSE Yaw Square	?	?	?
RMSE Pitch Sine	?	?	?
RMSE Yaw Sine	?	?	?

Table 5.1: Error Comparison for USB Algorithms

5.3 Raspberry Pi

5.3.1 LQR (P Controller)

5.3.2 ADP

5.3.3 Conclusions

Note: constant used pitch XXXX degrees, yaw XXXX degrees

Note: square used pitch XXXX degrees with period of XXXX, yaw XXXX degrees with period of XXXX

Note: sine used pitch XXXX degrees with period of XXXX, yaw XXXX degrees with period of XXXX

Based on the results XXXX preformed better for Raspberry Pi.

	LQR(P)	ADP(P)
RMSE Pitch Step	?	?
RMSE Yaw Step	?	?
RMSE Pitch Square	?	?
RMSE Yaw Square	?	?
RMSE Pitch Sine	?	?
RMSE Yaw Sine	?	?

Table 5.2: Error Comparison for USB Algorithms

5.4 Mobile Device

5.4.1 LQR (P Controller)

5.4.2 ADP

5.4.3 Conclusions

Note: constant used pitch XXXX degrees, yaw XXXX degrees

Note: square used pitch XXXX degrees with period of XXXX, yaw XXXX degrees with period of XXXX

Note: sine used pitch XXXX degrees with period of XXXX, yaw XXXX degrees with period of XXXX

Based on the results XXXX preformed better for Android.

	LQR(P)	ADP(P)
RMSE Pitch Step	?	?
RMSE Yaw Step	?	?
RMSE Pitch Square	?	?
RMSE Yaw Square	?	?
RMSE Pitch Sine	?	?
RMSE Yaw Sine	?	?

Table 5.3: Error Comparison for USB Algorithms

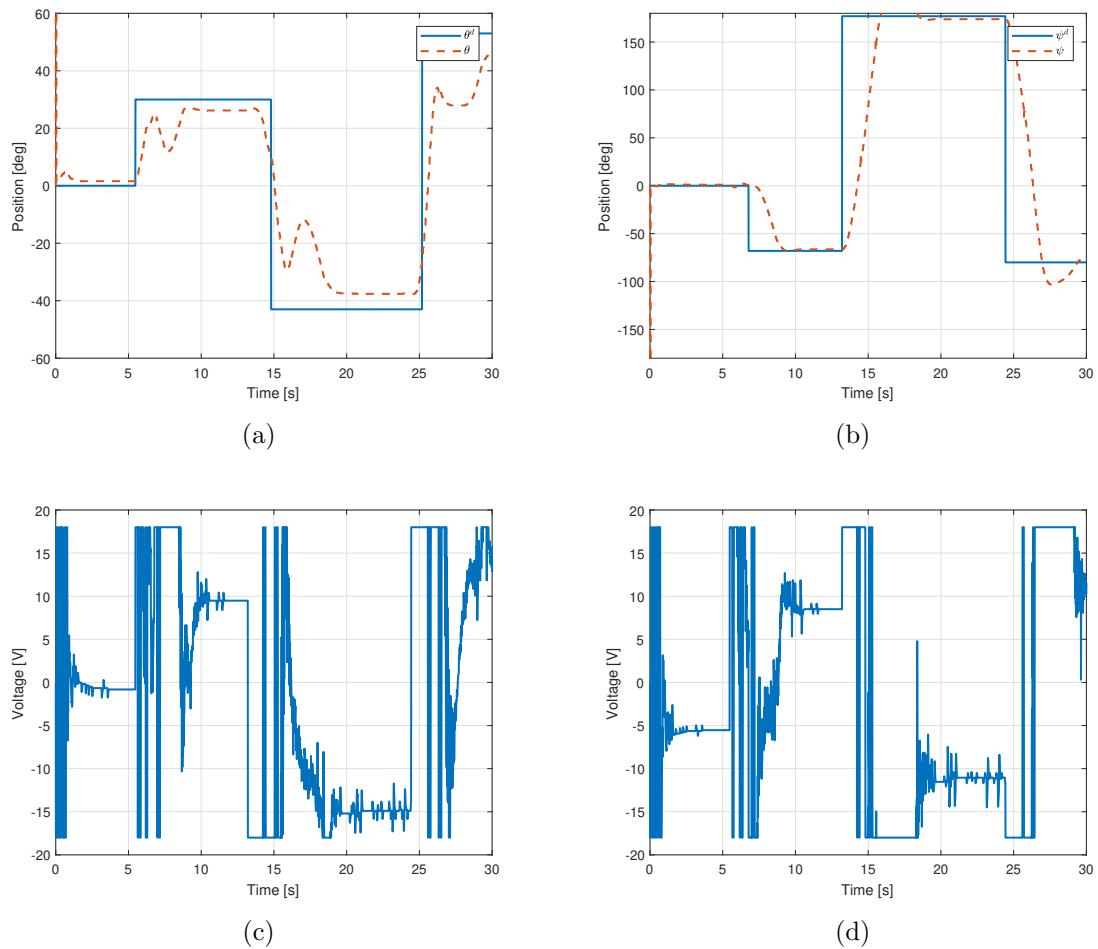


Figure 5.7: LQR Android Results

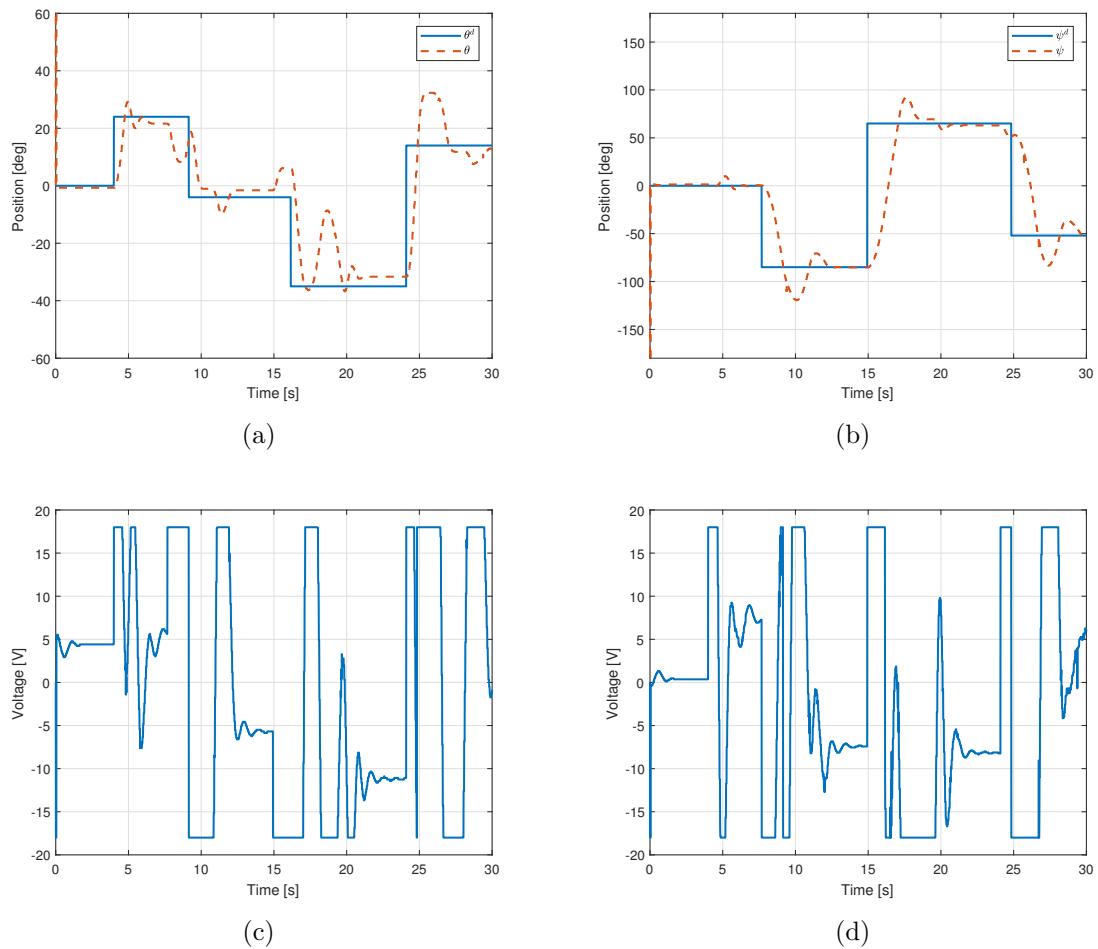


Figure 5.8: ADP Android Results

Chapter 6

Conclusion and Future Work

6.1 Algorithm Comparison

6.2 Conclusion

6.3 Future Work

6.3.1 Enhanced Smart Framework

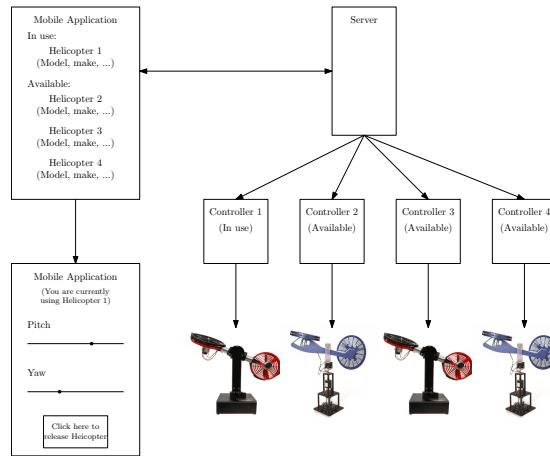


Figure 6.1: Smart Algorithm Server Connectivity

6.3.2 Digital Compass

6.3.3 Expanded PI Control

We had trouble implementing the PI control architecture as well as LQG on the Raspberry Pi. This may be because the integrator and the kalman filter require a fixed sampling time. Simulink has the option to use a variable sampling time when set to continuous time. Since the model is being loaded onto a embedded system which relies upon a fixed sampling time, this may be affected the values being outputted by these blocks.

To correct this issue, we recommend that future work done on this project convert the model to discrete time. Consider 6.1 and 6.2 to convert the continuous model in 2.1:

$$x(k+1) = \Phi x(k) + \Gamma u(k) \quad (6.1)$$

$$y(k) = Hx(k) + Ju(k) \quad (6.2)$$

where T is the sampling time, $\Phi = e^{AT}$, and $\Gamma = \int_0^T e^{A\eta} d\eta B$.

Appendix A

Parameters and State-Space

A.1 Parameters

Symbol	Description	Value
DC Motor		
V_{nom}	Nominal input voltage	18.0 V
τ_{nom}	Nominal torque	22.0 mN-m
ω_{nom}	Nominal speed	3050 RPM
I_{nom}	Nominal current	0.540 A
R_m	Terminal resistance	8.4 Ω
k_t	Torque constant	0.042 N-m/A
k_m	Motor back-emf constant	0.042 V/(rad/s)
J_m	Rotor inertia	4.0×10^{-6} kg-m ²
L_m	Rotor inductance	1.16 mH
Aero Body		
M_b	Mass of body	1.075 kg
D_m	Center of mass	-7.59 mm
J_p	Pitch inertia	2.15×10^{-2} kg-m ²
J_y	Yaw inertia	2.37×10^{-2} kg-m ²
D_t	Thrust displacement	15.8 cm
Motor and Pitch Encoders		
	Encoder line count	512 lines/rev
	Encoder line count in quadrature	2048 lines/rev
	Encoder resolution (in quadrature)	0.176 deg/count
Yaw Encoder		
	Encoder line count	1024 lines/rev
	Encoder line count in quadrature	4096 lines/rev
	Encoder resolution (in quadrature)	0.088 deg/count
Amplifier		
	Amplifier type	PWM
	Peak Current	2 A
	Continuous Current	0.5 A
	Output voltage range (recommended)	±18 V
	Output voltage range (maximum)	±24 V

Figure A.1: Quanser Aero System Parameters

```

1 %
2 %% Quanser Aero Parameters
3 % Moment of Inertia of helicopter body (kg-m^2)
4 L_body = 6.5*0.0254; % length of horizontal body (metal tube)
5 m_body = 0.094; % mass of horizontal body (metal tube)
6 J_body = m_body * L_body^2 / 12; % horizontal cylinder rotating about CM
7 %
8 % Moment of Inertia of yoke fork that rotates about yaw axis (kg-m^2)
9 m_yoke = 0.526; % mass of entire yoke assembly (kg)
10 % h_yoke = 9*0.0254; % height of yoke assembly (m)
11 r_fork = 0.04/2; % radius of each fork (approximated as cylinder)
12 J_yoke = 0.5*m_yoke*r_fork^2;
13 %
14 % Moment of Inertia from motor + guard assembly about pivot (kg-m^2)
15 m_prop = 0.43; % mass of dc motor + shield + propeller shield
16 % m_motor = 0.203; % mass of dc motor
17 r_prop = 6.25*0.0254; % distance from CM to center of pitch axis
18 J_prop = m_prop * r_prop^2; % using parallel axis theorem
19 %
20 % Equivalent Moment of Inertia about Pitch and Yaw Axis (kg-m^2)
21 Jp = J_body + 2*J_prop; % pitch: body and 2 props
22 Jy = J_body + 2*J_prop + J_yoke; % yaw: body, 2 props, and yoke
23 %
24 % Thrust-torque constant (N-m/V) [found experimentally]
25 Kpp = 0.0011; % (pre-production unit: 0.0015)
26 Kyy = 0.0022; % (pre-production unit: 0.0040)
27 Kpy = 0.0021; % thrust acting on pitch from yaw (pre-production unit: ...
    0.0020)
28 Kyp = -0.0027; % thrust acting on yaw from pitch (pre-production ...
    unit: -0.0017)
29 %
30 % Stiffness (N-m/rad) [found experimentally]
31 Ksp = 0.037463;
32 %
33 % Viscous damping (N-m-s/rad) [found experimentally]
34 Dp = 0.0071116; % pitch axis (pre-production unit: Dp = 0.0226)
35 Dy = 0.0220; % yaw axis (pre-production unit: Dy = 0.0211)
36 %

```

A.2 State-Space Model

```

1 %% State-Space Representation
2 A = [0 0 1 0;
3     0 0 0 1;
4     -Ksp/Jp 0 -Dp/Jp 0;
5     0 0 0 -Dy/Jy];
6
7 B = [0 0;
8     0 0;

```

```
9      Kpp/Jp  Kpy/Jp;  
10     Kyp/Jy  KyY/Jy];  
11  
12 C = eye(2,4);  
13 D = zeros(2,2);  
14 %
```

Appendix B

MATLAB Simulation Code

B.1 LQR (P controller)

```
1 function KV_LQRContinuousTime
2 %% Setup Differential Equation
3 close all
4 clear
5 clc
6
7 quanser_aero_parameters; % contains parameters Quanser Aero
8 quanser_aero_state_space; % puts parameters into state-space model
9
10 Q = diag([3500 500 0 0 ]); % Quadratic term
11 R = 0.005*eye(2,2); % Regulator term
12 K = lqr(A,B,Q,R);
13
14 xInit = zeros(1,4); % set the initial conditions to 0 degrees pitch
15 % and 0 degrees yaw
16 xD = [deg2rad(10) deg2rad(45) 0 0]'; % desidied position is 45 degrees
17 % pitch and 90 degrees yaw
18 eInit = xD'-xInit; % error matrix is desired transposed minus actual
19
20 maxInputVoltage = 18; % cannot exceed this output in [V]
21
22 options = odeset('RelTol', 1e-4, 'AbsTol', 1e-4*ones(1,4));
23
24 t_sim = 10; % [sec]
25 [Te,E] = ode45(@(t,e) stateEqn(t,e,A,B,K,xD,maxInputVoltage), [0 ...
26 t_sim/2], ...
27 eInit, options);
28 xD=-xD;
29 [Te,E] = ode45(@(t,e) stateEqn(t,e,A,B,K,xD,maxInputVoltage), [t_sim/2 ...
30 t_sim], ...
31 eInit, options);
32 %% Position Error Graph
33 figure;
```

```

32 e_1 = plot(Te, rad2deg(E(:,1)), '-','LineWidth', 1.5);
33 hold on
34 e_2 = plot(Te, rad2deg(E(:,2)), '--','LineWidth', 1.5);
35 hold on
36 e_3 = plot(Te, rad2deg(E(:,3)), '-. ','LineWidth', 1.5);
37 hold on
38 e_4 = plot(Te, rad2deg(E(:,4)), ':','LineWidth', 1.5);
39
40 xlabel('Time [s]');
41 ylabel('Error [deg]');
42 title('Error');
43 legend([e_1 e_2 e_3 e_4],{'$e_{\theta}^{\sim}[deg]$', '$e_{\psi}^{\sim}[deg]$', ...
44     '$e_{\dot{\theta}}^{\sim}[deg/s]$', '$e_{\dot{\psi}}^{\sim}[deg/s]$'}, ...
45     'Interpreter', 'latex');
46
47 grid on
48
49 %% Position Graph
50 for i=1:size(E,1)
51     u(i,:) = (K*(E(i,:)))';
52     uLimit(i,:) = sign(u(i,:)).*min(abs(u(i,:)),[maxInputVoltage, ...
53         maxInputVoltage]);
54 end
55
56 xDt = repmat(xD',size(E,1),1); % repeat xDt for all time instants
57 QuanserAeroStates = xDt - E;
58
59 figure;
60 theta = plot(Te, rad2deg(QuanserAeroStates(:,1)), '-','LineWidth', 1.5);
61 hold on
62 psi = plot(Te, rad2deg(QuanserAeroStates(:,2)), '--','LineWidth', 1.5);
63 hold on
64 thetaD = plot(Te, rad2deg(xDt(:,1)), '-. ','LineWidth', 2);
65 hold on
66 psiD = plot(Te, rad2deg(xDt(:,2)), '--','LineWidth', 2);
67
68 xlabel('Time [s]');
69 ylabel('Position [deg]');
70 title('Position');
71 legend([theta psi thetaD psiD],{'$\theta$', '$\psi$', '$\theta^d$', ...
72     '$\psi^d$'}, 'Interpreter', 'latex');
73 grid on
74
75 %% Voltage Graph
76 figure;
77 vP = plot(Te,uLimit(:,1), '-','LineWidth', 1.5);
78 hold on
79 vY = plot(Te,uLimit(:,2), '--','LineWidth', 1.5);
80
81 xlabel('Time [s]');
82 ylabel('Input Voltage [V]');
83 title('Voltages');
84 legend([vP vY], 'V_p(t) [V]', 'V_y(t) [V]');
85 grid on

```

```
86
87 function eDot = stateEqn(t,e,A,B,K,xD,uMax)
88     u = K*e;
89     uLimit = sign(u).*min(abs(u),[uMax;uMax]);
90     eDot = A*e-B*uLimit - A*xD;
```

Appendix C

USB MATLAB Code

Appendix D

Raspberry Pi MATLAB Code

D.1 Initialization Code

```
1 %rpi = raspi('192.168.1.79','pi','raspberry'); %Raspberry Pi 1
2 rpi = raspi('192.168.1.20','pi','raspberry'); %Raspberry Pi 2
3
4
5 enableSPI(rpi);
6 disableSPI(rpi);
7
8 % Configure pins on Raspberry Pi for the SPI communication
9 % MOSI Output
10 configurePin(rpi, 10,'DigitalOutput');
11 % SPI Clock Output
12 configurePin(rpi, 11,'DigitalOutput');
13 % SS Output
14 configurePin(rpi, 8,'DigitalOutput');
15 % MISO Input
16 configurePin(rpi, 9,'DigitalInput');
17
18 % SPI output clock period 2us (500kHz)
19 spiPeriod = 0.0001;
20
21 enableSPI(rpi);
22
23 clearvars -except rpi spiPeriod K
```

D.2 SPI Protocol

```
1 % THIS FUNCTION CONTROLS THE SPI INTERFACING
2 % THIS FUNCTION DETERMINES WHAT DATA IS SENT TO THE QUANSER AERO AND WHAT
```

```

3 % DATA IS RETRIEVED FROM THE QUANSER AERO
4 function ...
    [MOSI,SS,pitchEncoder,yawEncoder,byteNumber,bitNumber,encoder2_23_16,encoder2_15_8,
     = fcn(MISO, ...
            pitchVolt,yawVolt,redValue,greenValue,blueValue,byteNumber,bitNumber,encoder2_23_16
5 % Variables used in the function
6 complement = '0000000000000000';
7 pitchEncoderBin = '00000000000000000000000000000000';
8 yawEncoderBin = '00000000000000000000000000000000';
9 tempBin = '00000000000000000000000000000000';
10 tempVoltBin = '00000000';
11
12 % Output the value of the pitch encoder using the latest byte values
13 % Combine all of the encoder bytes
14 pitchEncoderIn = [encoder2_23_16 encoder2_15_8 encoder2_7_0];
15 % Convert the encoder binary vector into a character array
16 for i = 1:24
17     if (pitchEncoderIn(i) == 1)
18         pitchEncoderBin(i) = '1';
19     else
20         pitchEncoderBin(i) = '0';
21     end
22 end
23 % Calculate the 2's complement value of the encoder
24 if(pitchEncoderBin(1) == '1')
25     for i = 1:32
26         if (i < 9)
27             tempBin(i) = '1';
28         else
29             tempBin(i) = pitchEncoderBin(i - 8);
30         end
31     end
32 else
33     for i = 1:32
34         if (i < 9)
35             tempBin(i) = '0';
36         else
37             tempBin(i) = pitchEncoderBin(i - 8);
38         end
39     end
40 end
41 pitchEncoderTemp = typecast(uint32(bin2dec(tempBin)), 'int32');
42 pitchEncoderOut = cast(pitchEncoderTemp, 'double');
43 pitchEncoder = pitchEncoderOut(1);
44
45 % Output the value of the yaw encoder using the latest byte values
46 % Combine all of the encoder bytes
47 yawEncoderIn = [encoder3_23_16 encoder3_15_8 encoder3_7_0];
48 % Convert the encoder binary vector into a character array
49 for i = 1:24
50     if (yawEncoderIn(i) == 1)
51         yawEncoderBin(i) = '1';
52     else
53         yawEncoderBin(i) = '0';

```

```

54     end
55 end
56 % Calculate the 2's complement value of the encoder
57 if(yawEncoderBin(1) == '1')
58     for i = 1:32
59         if (i < 9)
60             tempBin(i) = '1';
61         else
62             tempBin(i) = yawEncoderBin(i - 8);
63         end
64     end
65 else
66     for i = 1:32
67         if (i < 9)
68             tempBin(i) = '0';
69         else
70             tempBin(i) = yawEncoderBin(i - 8);
71         end
72     end
73 end
74 yawEncoderTemp = typecast(uint32(bin2dec(tempBin)), 'int32');
75 yawEncoderOut = cast(yawEncoderTemp, 'double');
76 yawEncoder = yawEncoderOut(1);
77
78 % Determine which byte we are currently sending
79 % Specify the slave select value
80 % - 0 to activate the SPI on the Quanser AERO
81 % - 1 to de-activate the SPI on the Quanser AERO
82 % Determine the what the byte to be transmitted should be
83 switch byteNumber
84     case 0
85         % ** START OF BASE PACKET ***
86         % BYTE 0
87         % MOSI DATA - BASE MODE (0X01)
88         % MISO DATA - BASE ID MSB
89         % Beginning of the transmission, so SS goes low
90         SS = 0;
91         readyMOSI = dec2bin(1,8);
92
93     case 1
94         % BYTE 1
95         % MOSI DATA - PADDING BYTE (0X00)
96         % MISO DATA - BASE ID LSB
97         SS = 0;
98         readyMOSI = dec2bin(0,8);
99
100    case 2
101        % BYTE 2
102        % MOSI DATA - BASE WRITE MASK
103        % MISO DATA - ENCODER 2 (23-16)
104        SS = 0;
105        % Enable the overwriting of encoders 2 and 3 and the LED colors
106        % Bit 4 - Set encoder 3 enable
107        % Bit 3 - Set encoder 2 enable

```

```

108     % Bit 2 - Write blue LED
109     % Bit 1 - Write green LED
110     % Bit 0 - Write red LED
111     % Don't want to overwrite the encoder values
112     readyMOSI = dec2bin(7,8);
113     % Receive the MISO byte bit by bit and update the vector holding the
114     % byte
115     switch bitNumber
116         case 1
117             if (MISO == true)
118                 encoder2_23_16(1) = 1;
119             else
120                 encoder2_23_16(1) = 0;
121             end
122         case 2
123             if (MISO == true)
124                 encoder2_23_16(2) = 1;
125             else
126                 encoder2_23_16(2) = 0;
127             end
128         case 3
129             if (MISO == true)
130                 encoder2_23_16(3) = 1;
131             else
132                 encoder2_23_16(3) = 0;
133             end
134         case 4
135             if (MISO == true)
136                 encoder2_23_16(4) = 1;
137             else
138                 encoder2_23_16(4) = 0;
139             end
140         case 5
141             if (MISO == true)
142                 encoder2_23_16(5) = 1;
143             else
144                 encoder2_23_16(5) = 0;
145             end
146         case 6
147             if (MISO == true)
148                 encoder2_23_16(6) = 1;
149             else
150                 encoder2_23_16(6) = 0;
151             end
152         case 7
153             if (MISO == true)
154                 encoder2_23_16(7) = 1;
155             else
156                 encoder2_23_16(7) = 0;
157             end
158         case 8
159             if (MISO == true)
160                 encoder2_23_16(8) = 1;
161             else

```

```
162         encoder2_23_16(8) = 0;
163     end
164 end
165
166 case 3
167 % BYTE 3
168 % MOSI DATA - RED LED MSB
169 % MISO DATA - ENCODER 2 (15-8)
170 SS = 0;
171 readyMOSI = dec2bin(redValue(1),8);
172 % Receive the MISO byte bit by bit and update the vector holding the
173 % byte
174 switch bitNumber
175     case 1
176         if (MISO == true)
177             encoder2_15_8(1) = 1;
178         else
179             encoder2_15_8(1) = 0;
180         end
181     case 2
182         if (MISO == true)
183             encoder2_15_8(2) = 1;
184         else
185             encoder2_15_8(2) = 0;
186         end
187     case 3
188         if (MISO == true)
189             encoder2_15_8(3) = 1;
190         else
191             encoder2_15_8(3) = 0;
192         end
193     case 4
194         if (MISO == true)
195             encoder2_15_8(4) = 1;
196         else
197             encoder2_15_8(4) = 0;
198         end
199     case 5
200         if (MISO == true)
201             encoder2_15_8(5) = 1;
202         else
203             encoder2_15_8(5) = 0;
204         end
205     case 6
206         if (MISO == true)
207             encoder2_15_8(6) = 1;
208         else
209             encoder2_15_8(6) = 0;
210         end
211     case 7
212         if (MISO == true)
213             encoder2_15_8(7) = 1;
214         else
215             encoder2_15_8(7) = 0;
```

```

216         end
217     case 8
218         if (MISO == true)
219             encoder2_15_8(8) = 1;
220         else
221             encoder2_15_8(8) = 0;
222         end
223     end
224
225 case 4
226 % BYTE 4
227 % MOSI DATA - RED LED LSB
228 % MISO DATA - ENCODER 2 (7-0)
229 SS = 0;
230 readyMOSI = dec2bin(redValue(2),8);
231 % Receive the MISO byte bit by bit and update the vector holding the
232 % byte
233 switch bitNumber
234     case 1
235         if (MISO == true)
236             encoder2_7_0(1) = 1;
237         else
238             encoder2_7_0(1) = 0;
239         end
240     case 2
241         if (MISO == true)
242             encoder2_7_0(2) = 1;
243         else
244             encoder2_7_0(2) = 0;
245         end
246     case 3
247         if (MISO == true)
248             encoder2_7_0(3) = 1;
249         else
250             encoder2_7_0(3) = 0;
251         end
252     case 4
253         if (MISO == true)
254             encoder2_7_0(4) = 1;
255         else
256             encoder2_7_0(4) = 0;
257         end
258     case 5
259         if (MISO == true)
260             encoder2_7_0(5) = 1;
261         else
262             encoder2_7_0(5) = 0;
263         end
264     case 6
265         if (MISO == true)
266             encoder2_7_0(6) = 1;
267         else
268             encoder2_7_0(6) = 0;
269         end

```

```

270      case 7
271          if (MISO == true)
272              encoder2_7_0(7) = 1;
273          else
274              encoder2_7_0(7) = 0;
275          end
276      case 8
277          if (MISO == true)
278              encoder2_7_0(8) = 1;
279          else
280              encoder2_7_0(8) = 0;
281          end
282      end
283
284      case 5
285      % BYTE 5
286      % MOSI DATA — GREEN LED MSB
287      % MISO DATA — ENCODER 3 (23–16)
288      SS = 0;
289      readyMOSI = dec2bin(greenValue(1),8);
290      % Receive the MISO byte bit by bit and update the vector holding the
291      % byte
292      switch bitNumber
293          case 1
294              if (MISO == true)
295                  encoder3_23_16(1) = 1;
296              else
297                  encoder3_23_16(1) = 0;
298              end
299          case 2
300              if (MISO == true)
301                  encoder3_23_16(2) = 1;
302              else
303                  encoder3_23_16(2) = 0;
304              end
305          case 3
306              if (MISO == true)
307                  encoder3_23_16(3) = 1;
308              else
309                  encoder3_23_16(3) = 0;
310              end
311          case 4
312              if (MISO == true)
313                  encoder3_23_16(4) = 1;
314              else
315                  encoder3_23_16(4) = 0;
316              end
317          case 5
318              if (MISO == true)
319                  encoder3_23_16(5) = 1;
320              else
321                  encoder3_23_16(5) = 0;
322              end
323          case 6

```

```

324         if (MISO == true)
325             encoder3_23_16(6) = 1;
326         else
327             encoder3_23_16(6) = 0;
328         end
329     case 7
330         if (MISO == true)
331             encoder3_23_16(7) = 1;
332         else
333             encoder3_23_16(7) = 0;
334         end
335     case 8
336         if (MISO == true)
337             encoder3_23_16(8) = 1;
338         else
339             encoder3_23_16(8) = 0;
340         end
341     end
342
343 case 6
344 % BYTE 6
345 % MOSI DATA — GREEN LED LSB
346 % MISO DATA — ENCODER 3 (15–8)
347 SS = 0;
348 readyMOSI = dec2bin(greenValue(2),8);
349 % Receive the MISO byte bit by bit and update the vector holding the
350 % byte
351 switch bitNumber
352     case 1
353         if (MISO == true)
354             encoder3_15_8(1) = 1;
355         else
356             encoder3_15_8(1) = 0;
357         end
358     case 2
359         if (MISO == true)
360             encoder3_15_8(2) = 1;
361         else
362             encoder3_15_8(2) = 0;
363         end
364     case 3
365         if (MISO == true)
366             encoder3_15_8(3) = 1;
367         else
368             encoder3_15_8(3) = 0;
369         end
370     case 4
371         if (MISO == true)
372             encoder3_15_8(4) = 1;
373         else
374             encoder3_15_8(4) = 0;
375         end
376     case 5
377         if (MISO == true)

```

```

378         encoder3_15_8(5) = 1;
379     else
380         encoder3_15_8(5) = 0;
381     end
382     case 6
383         if (MISO == true)
384             encoder3_15_8(6) = 1;
385         else
386             encoder3_15_8(6) = 0;
387         end
388     case 7
389         if (MISO == true)
390             encoder3_15_8(7) = 1;
391         else
392             encoder3_15_8(7) = 0;
393         end
394     case 8
395         if (MISO == true)
396             encoder3_15_8(8) = 1;
397         else
398             encoder3_15_8(8) = 0;
399         end
400     end
401
402     case 7
403     % BYTE 7
404     % MOSI DATA - BLUE LED MSB
405     % MISO DATA - ENCODER 3 (7-0)
406     SS = 0;
407     readyMOSI = dec2bin(blueValue(1),8);
408     % Receive the MISO byte bit by bit and update the vector holding the
409     % byte
410     switch bitNumber
411         case 1
412             if (MISO == true)
413                 encoder3_7_0(1) = 1;
414             else
415                 encoder3_7_0(1) = 0;
416             end
417         case 2
418             if (MISO == true)
419                 encoder3_7_0(2) = 1;
420             else
421                 encoder3_7_0(2) = 0;
422             end
423         case 3
424             if (MISO == true)
425                 encoder3_7_0(3) = 1;
426             else
427                 encoder3_7_0(3) = 0;
428             end
429         case 4
430             if (MISO == true)
431                 encoder3_7_0(4) = 1;

```

```

432         else
433             encoder3_7_0(4) = 0;
434         end
435     case 5
436         if (MISO == true)
437             encoder3_7_0(5) = 1;
438         else
439             encoder3_7_0(5) = 0;
440         end
441     case 6
442         if (MISO == true)
443             encoder3_7_0(6) = 1;
444         else
445             encoder3_7_0(6) = 0;
446         end
447     case 7
448         if (MISO == true)
449             encoder3_7_0(7) = 1;
450         else
451             encoder3_7_0(7) = 0;
452         end
453     case 8
454         if (MISO == true)
455             encoder3_7_0(8) = 1;
456         else
457             encoder3_7_0(8) = 0;
458         end
459     end
460
461     case 8
462     % BYTE 8
463     % MOSI DATA — BLUE LED LSB
464     % MISO DATA — TACHOMETER 2 (23–16)
465     SS = 0;
466     readyMOSI = dec2bin(blueValue(2),8);
467
468     case 9
469     % BYTE 9
470     % MOSI DATA — SET ENCODER 2 (23–16)
471     % MISO DATA — TACHOMETER 2 (15–8)
472     SS = 0;
473     readyMOSI = dec2bin(0,8);
474
475     case 10
476     % BYTE 10
477     % MOSI DATA — SET ENCODER 2 (15–8)
478     % MISO DATA — TACHOMETER 2 (7–0)
479     SS = 0;
480     readyMOSI = dec2bin(0,8);
481
482     case 11
483     % BYTE 11
484     % MOSI DATA — SET ENCODER 2 (7–0)
485     % MISO DATA — TACHOMETER 3 (23–16)

```

```

486     SS = 0;
487     readyMOSI = dec2bin(0,8);
488
489     case 12
490     % BYTE 12
491     % MOSI DATA — SET ENCODER 3 (23–16)
492     % MISO DATA — TACHOMETER 3 (15–8)
493     SS = 0;
494     readyMOSI = dec2bin(0,8);
495
496     case 13
497     % BYTE 13
498     % MOSI DATA — SET ENCODER 3 (15–8)
499     % MISO DATA — TACHOMETER 3 (7–0)
500     SS = 0;
501     readyMOSI = dec2bin(0,8);
502
503     case 14
504     % BYTE 14
505     % MOSI DATA — SET ENCODER 3 (7–0)
506     % MISO DATA — RESERVED (0X00)
507     SS = 0;
508     readyMOSI = dec2bin(0,8);
509
510     case 15
511     % ** START OF CORE PACKET **
512     % BYTE 15
513     % MOSI DATA — CORE MODE (0X01)
514     % MISO DATA — CORE ID MSB
515     SS = 0;
516     readyMOSI = dec2bin(1,8);
517
518     case 16
519     % BYTE 16
520     % MOSI DATA — PADDING BYTE (0X00)
521     % MISO DATA — CORE ID LSB
522     SS = 0;
523     readyMOSI = dec2bin(0,8);
524
525     case 17
526     % BYTE 17
527     % MOSI DATA — CORE WRITE MASK
528     % MISO DATA — CURRENT SENSE 0 (15–8)
529     SS = 0;
530     % Do not enable the overwriting of encoders 0 and 1, but do ...
      enable the
      % overwriting of the motor voltages
531     % Bit 5 — Set encoder 1 enable
532     % Bit 4 — Set encoder 0 enable
533     % Bit 3 — Write motor 1 voltage
534     % Bit 2 — Write motor 1 enable
535     % Bit 1 — Write motor 0 voltage
536     % Bit 0 — Write motor 0 enable
537
538     readyMOSI = dec2bin(15,8);

```

```

539
540     case 18
541         % BYTE 18
542         % MOSI DATA - MOTOR 0 COMMAND (15-8)
543         % MISO DATA - CURRENT SENSE 0 (7-0)
544         SS = 0;
545         % Convert the desired voltage to a value between -999 and 999
546         % 24 is the saturation level in the model
547         pitchVoltTemp = ceil((999*pitchVolt)/24);
548         % If the desired voltage is positive, concatenate a '1' to the ...
549             front of
550             % the voltage value
551             % Pass the MSB of the new value
552             if (sign(pitchVoltTemp) == 1)
553                 temp = dec2bin(pitchVoltTemp,15);
554                 for i = 1:8
555                     if (i == 1)
556                         tempVoltBin(i) = '1';
557                     else
558                         tempVoltBin(i) = temp(i - 1);
559                     end
560                 end
561                 readyMOSI = tempVoltBin;
562                 % If the desired voltage is negative, find the 2's complement ...
563                 % value of
564                 % the voltage
565                 elseif (sign(pitchVoltTemp) == -1)
566                     temp = dec2bin(-1*pitchVoltTemp,15);
567                     % Find the complement
568                     for i = 1:15
569                         if (temp(i) == '1')
570                             complement(i) = '0';
571                         else
572                             complement(i) = '1';
573                         end
574                     end
575                     temp1 = bin2dec(complement) + 1;
576                     temp2 = dec2bin(temp1,15);
577                     for i = 1:8
578                         if (i == 1)
579                             tempVoltBin(i) = '1';
580                         else
581                             tempVoltBin(i) = temp2(i - 1);
582                         end
583                     end
584                     readyMOSI = tempVoltBin;
585                     % If the desired voltage is zero, don't activate the motor
586                     else
587                         readyMOSI = dec2bin(0,8);
588                     end
589
590     case 19
591         % BYTE 19
592         % MOSI DATA - MOTOR 0 COMMAND (7-0)

```

```

591 % MISO DATA - CURRENT SENSE 1 (15-8)
592 SS = 0;
593 % Convert the desired voltage to a value between -999 and 999
594 % 24 is the saturation level in the model
595 pitchVoltTemp = ceil((999*pitchVolt)/24);
596 % If the voltage is positive, pass the LSB
597 if (sign(pitchVoltTemp) == 1)
598     temp = dec2bin(pitchVoltTemp,15);
599     readyMOSI = temp(8:15);
600 % If the voltage is negative, find the 2's complement value and then
601 % pass the LSB
602 elseif (sign(pitchVoltTemp) == -1)
603     temp = dec2bin(-1*pitchVoltTemp,15);
604     % Find the complement
605     for i = 1:15
606         if (temp(i) == '1')
607             complement(i) = '0';
608         else
609             complement(i) = '1';
610         end
611     end
612     temp1 = bin2dec(complement) + 1;
613     temp2 = dec2bin(temp1,15);
614     readyMOSI = temp2(8:15);
615 % If the desired voltage is zero, do not activate the motor
616 else
617     readyMOSI = dec2bin(0,8);
618 end
619
620 case 20
621 % BYTE 20
622 % MOSI DATA - MOTOR 1 COMMAND (15-8)
623 % MISO DATA - CURRENT SENSE 1 (7-0)
624 SS = 0;
625 % Convert the desired voltage to a value between -999 and 999
626 % 24 is the saturation level in the model
627 yawVoltTemp = ceil((999*yawVolt)/24);
628 % If the desired voltage is positive, concatenate a '1' to the ...
629 % front of
630 % the voltage value
631 % Pass the MSB of the new value
632 if (sign(yawVoltTemp) == 1)
633     temp = dec2bin(yawVoltTemp,15);
634     for i = 1:8
635         if (i == 1)
636             tempVoltBin(i) = '1';
637         else
638             tempVoltBin(i) = temp(i - 1);
639         end
640     end
641     readyMOSI = tempVoltBin;
642 % If the desired voltage is negative, find the 2's complement ...
643 % value of
644 % the voltage

```

```

643     elseif (sign(yawVoltTemp) == -1)
644         temp = dec2bin(-1*yawVoltTemp,15);
645         % Find the complement
646         for i = 1:15
647             if (temp(i) == '1')
648                 complement(i) = '0';
649             else
650                 complement(i) = '1';
651             end
652         end
653         temp1 = bin2dec(complement) + 1;
654         temp2 = dec2bin(temp1,15);
655         for i = 1:8
656             if (i == 1)
657                 tempVoltBin(i) = '1';
658             else
659                 tempVoltBin(i) = temp2(i - 1);
660             end
661         end
662         readyMOSI = tempVoltBin;
663         % If the desired voltage is zero, don't activate the motor
664     else
665         readyMOSI = dec2bin(0,8);
666     end
667
668 case 21
669 % BYTE 21
670 % MOSI DATA — MOTOR 1 COMMAND (7–0)
671 % MISO DATA — TACHOMETER 0 (23–16)
672 SS = 0;
673 % Convert the desired voltage to a value between -999 and 999
674 % 24 is the saturation level in the model
675 yawVoltTemp = ceil((999*yawVolt)/24);
676 % If the voltage is positive, pass the LSB
677 if (sign(yawVoltTemp) == 1)
678     temp = dec2bin(yawVoltTemp,15);
679     readyMOSI = temp(8:15);
680 % If the voltage is negative, find the 2's complement value and then
681 % pass the LSB
682 elseif (sign(yawVoltTemp) == -1)
683     temp = dec2bin(-1*yawVoltTemp,15);
684     for i = 1:15
685         if (temp(i) == '1')
686             complement(i) = '0';
687         else
688             complement(i) = '1';
689         end
690     end
691     temp1 = bin2dec(complement) + 1;
692     temp2 = dec2bin(temp1,15);
693     readyMOSI = temp2(8:15);
694 % If the desired voltage is zero, do not activate the motor
695 else
696     readyMOSI = dec2bin(0,8);

```

```
697     end
698
699 case 22
700 % BYTE 22
701 % MOSI DATA — SET ENCODER 0 (23–16)
702 % MISO DATA — TACHOMETER 0 (15–8)
703 SS = 0;
704 readyMOSI = dec2bin(0,8);
705
706 case 23
707 % BYTE 23
708 % MOSI DATA — SET ENCODER (7–0)
709 % MISO DATA — TACHOMETER 0 (7–0)
710 SS = 0;
711 readyMOSI = dec2bin(0,8);
712
713 case 24
714 % BYTE 24
715 % MOSI DATA — SET ENCODER 0 (7–0)
716 % MISO DATA — TACHOMETER 1 (23–16)
717 SS = 0;
718 readyMOSI = dec2bin(0,8);
719
720 case 25
721 % BYTE 25
722 % MOSI DATA — SET ENCODER 1 (23–16)
723 % MISO DATA — TACHOMETER 1 (15–8)
724 SS = 0;
725 readyMOSI = dec2bin(0,8);
726
727 case 26
728 % BYTE 26
729 % MOSI DATA — SET ENCODER 1 (15–8)
730 % MISO DATA — TACHOMETER 1 (7–0)
731 SS = 0;
732 readyMOSI = dec2bin(0,8);
733
734 case 27
735 % BYTE 27
736 % MOSI DATA — SET ENCODER 1 (7–0)
737 % MISO DATA — STATUS
738 SS = 0;
739 readyMOSI = dec2bin(0,8);
740
741 case 28
742 % BYTE 28
743 % MOSI DATA — PADDING BYTE (0X00)
744 % MISO DATA — ENCODER 0 (23–16)
745 SS = 0;
746 readyMOSI = dec2bin(0,8);
747
748 case 29
749 % BYTE 29
750 % MOSI DATA — PADDING BYTE (0X00)
```

```

751 % MISO DATA - ENCODER 0 (15-8)
752 SS = 0;
753 readyMOSI = dec2bin(0,8);
754
755 case 30
756 % BYTE 30
757 % MOSI DATA - PADDING BYTE (0X00)
758 % MISO DATA - ENCODER 0 (7-0)
759 SS = 0;
760 readyMOSI = dec2bin(0,8);
761
762 case 31
763 % BYTE 31
764 % MOSI DATA - PADDING BYTE (0X00)
765 % MISO DATA - ENCODER 1 (23-16)
766 SS = 0;
767 readyMOSI = dec2bin(0,8);
768
769 case 32
770 % BYTE 32
771 % MOSI DATA - PADDING BYTE (0X00)
772 % MISO DATA - ENCODER 1 (15-8)
773 SS = 0;
774 readyMOSI = dec2bin(0,8);
775
776 case 33
777 % BYTE 33
778 % MOSI DATA - PADDING BYTE (0X00)
779 % MISO DATA - ENCODER 1 (7-0)
780 SS = 0;
781 readyMOSI = dec2bin(0,8);
782
783 case 34
784 % BYTE 34
785 % MOSI DATA - PADDING BYTE (0X00)
786 % MISO DATA - ACCELEROMETER X (15-8)
787 SS = 0;
788 readyMOSI = dec2bin(0,8);
789
790 case 35
791 % BYTE 35
792 % MOSI DATA - PADDING BYTE (0X00)
793 % MISO DATA - ACCELEROMETER X (7-0)
794 SS = 0;
795 readyMOSI = dec2bin(0,8);
796
797 case 36
798 % BYTE 36
799 % MOSI DATA - PADDING BYTE (0X00)
800 % MISO DATA - ACCELEROMETER Y (15-8)
801 SS = 0;
802 readyMOSI = dec2bin(0,8);
803
804 case 37

```

```

805    % BYTE 37
806    % MOSI DATA — PADDING BYTE (0X00)
807    % MISO DATA — ACCELEROMETER Y (7–0)
808    SS = 0;
809    readyMOSI = dec2bin(0,8);

810
811    case 38
812    % BYTE 38
813    % MOSI DATA — PADDING BYTE (0X00)
814    % MISO DATA — ACCELEROMETER Z (15–8)
815    SS = 0;
816    readyMOSI = dec2bin(0,8);

817
818    case 39
819    % BYTE 39
820    % MOSI DATA — PADDING BYTE (0X00)
821    % MISO DATA — ACCELEROMETER Z (7–0)
822    SS = 0;
823    readyMOSI = dec2bin(0,8);

824
825    case 40
826    % BYTE 40
827    % MOSI DATA — PADDING BYTE (0X00)
828    % MISO DATA — GYROSCOPE X (15–8)
829    SS = 0;
830    readyMOSI = dec2bin(0,8);

831
832    case 41
833    % BYTE 41
834    % MOSI DATA — PADDING BYTE (0X00)
835    % MISO DATA — GYROSCOPE X (7–0)
836    SS = 0;
837    readyMOSI = dec2bin(0,8);

838
839    case 42
840    % BYTE 42
841    % MOSI DATA — PADDING BYTE (0X00)
842    % MISO DATA — GYROSCOPE Y (15–8)
843    SS = 0;
844    readyMOSI = dec2bin(0,8);

845
846    case 43
847    % BYTE 43
848    % MOSI DATA — PADDING BYTE (0X00)
849    % MISO DATA — GYROSCOPE Y (7–0)
850    SS = 0;
851    readyMOSI = dec2bin(0,8);

852
853    case 44
854    % BYTE 44
855    % MOSI DATA — PADDING BYTE (0X00)
856    % MISO DATA — GYROSCOPE Z (15–8)
857    SS = 0;
858    readyMOSI = dec2bin(0,8);

```

```

859
860     case 45
861         % BYTE 45
862         % MOSI DATA — PADDING BYTE (0X00)
863         % MISO DATA — GYROSCOPE Z (7–0)
864         SS = 0;
865         readyMOSI = dec2bin(0,8);
866
867     case 46
868         % BYTE 46
869         % MOSI DATA — PADDING BYTE (0X00)
870         % MISO DATA — RESERVED (0X00)
871         SS = 0;
872         readyMOSI = dec2bin(0,8);
873
874     case 47
875         % BYTE 47
876         % MOSI DATA — PADDING BYTE (0X00)
877         % MISO DATA — RESERVED (0X00)
878         SS = 0;
879         readyMOSI = dec2bin(0,8);
880
881     case 48
882         % BYTE 48
883         % MOSI DATA — PADDING BYTE (0X00)
884         % MISO DATA — RESERVED (0X00)
885         SS = 0;
886         readyMOSI = dec2bin(0,8);
887
888     case 49
889         % BYTE 49
890         % MOSI DATA — PADDING BYTE (0X00)
891         % MISO DATA — RESERVED (0X00)
892         SS = 0;
893         readyMOSI = dec2bin(0,8);
894
895     case 50
896         % BYTE 50
897         % MOSI DATA — PADDING BYTE (0X00)
898         % MISO DATA — RESERVED (0X00)
899         readyMOSI = dec2bin(0,8);
900         % Reset the slave select to begin the process again
901         % Maybe not needed
902         SS = 1;
903
904     otherwise
905         % Just in case
906         readyMOSI = dec2bin(0,8);
907         SS = 0;
908 end
909 % Pass the byte we have derived bit by bit
910 % Use the character array to determine the bit value
911 switch bitNumber
912     case 1

```

```

913         if (readyMOSI(1) == '1')
914             MOSI = 1;
915         else
916             MOSI = 0;
917         end
918     case 2
919         if (readyMOSI(2) == '1')
920             MOSI = 1;
921         else
922             MOSI = 0;
923         end
924     case 3
925         if (readyMOSI(3) == '1')
926             MOSI = 1;
927         else
928             MOSI = 0;
929         end
930     case 4
931         if (readyMOSI(4) == '1')
932             MOSI = 1;
933         else
934             MOSI = 0;
935         end
936     case 5
937         if (readyMOSI(5) == '1')
938             MOSI = 1;
939         else
940             MOSI = 0;
941         end
942     case 6
943         if (readyMOSI(6) == '1')
944             MOSI = 1;
945         else
946             MOSI = 0;
947         end
948     case 7
949         if (readyMOSI(7) == '1')
950             MOSI = 1;
951         else
952             MOSI = 0;
953         end
954     case 8
955         if (readyMOSI(8) == '1')
956             MOSI = 1;
957         else
958             MOSI = 0;
959         end
960         % If we have just sent the last bit, update the byte number
961         byteNumber = byteNumber + 1;
962         % Reset back to zero if we have finished one transfer
963         if (byteNumber == 51)
964             byteNumber = 0;
965         end
966     otherwise

```

```
967         MOSI = 0;  
968     end  
969 % Update the bit number that we are sending  
970 bitNumber = bitNumber + 1;  
971 % Reset back to 1 if we have finished one byte  
972 if (bitNumber == 9)  
    bitNumber = 1;  
973 end  
974 end  
975 end
```

Appendix E

ADP MATLAB Code

E.1 Initialization Code

```
1 %Glenn Janiak & Ken Vonckx
2 close all;
3 clear;
4 clc;
5
6 quanser_aero_parameters;
7 quanser_aero_state_space;
8
9 % Sampling time [s]
10 tau = 0.01;
11 % Update time [s]
12 T = 1;
13
14 % COST FUNCTION
15 % Q and R matrices used in the cost function
16 Q_Mat_ADP = diag([270 100 1 1]);
17 R_Mat_ADP = 0.005*diag([1 1]);
18
19 [n,~] = size(B);
20
21 nbar = T/tau;      % T/tau = 20
22
23 e_vec = (2*(pi)).*rand(n,nbar) - (pi);
24
25 fbar = @(e) A*e;
26 gbar = -B;
27
28 f = @(e) fbar(e)*tau + e;
29 g = gbar*tau;
30
31 Qbar = @(e) e'*Q_Mat_ADP*e;
32 Rbar = R_Mat_ADP;
33
```

```

34 Q = @(e) Qbar(e)*tau;
35 R = Rbar*tau;
36
37
38 rho = @(e) [e(1); e(2); e(3); e(4); ...
39             e(1)^2; e(1)*e(2); e(1)*e(3); e(1)*e(4); ...
40             e(2)^2; e(2)*e(3); e(2)*e(4); e(3)^2; e(3)*e(4); e(4)^2];
41
42 drhode =@(e) [1, 0, 0, 0;
43                 0, 1, 0, 0;
44                 0, 0, 1, 0;
45                 0, 0, 0, 1;
46                 2*e(1), 0, 0, 0;
47                 e(2), e(1), 0, 0;
48                 e(3), 0, e(1), 0;
49                 e(4), 0, 0, e(1);
50                 0, 2*e(2), 0, 0;
51                 0, e(3), e(2), 0;
52                 0, e(4), 0, e(2);
53                 0, 0, 2*e(3), 0;
54                 0, 0, e(4), e(3);
55                 0, 0, 0, 2*e(4)];
56
57 % Learning Rate
58 EpsilonPolicy = 0.1;
59 EpsilonWcritic = 0.1;
60
61 % Number of outer loop iterations
62 outerLoopMax = 700;
63 % Number of inner loop iterations
64 innerLoopMax = 100;
65
66 % Number of training samples
67 [~,nbar] = size(e_vec);
68
69 % WEIGHT INITIALIZATION
70 % Initialize the weights of the critic neural network to zero
71 WcLast = zeros(length(rho(e_vec(:,1))),1);
72
73 % LEAST-SQUARES COMPUTATION INITIALIZATION
74 % Matrices required for computing least squares weights of the critic
75 % neural networks -- EQ 20
76 V = zeros(nbar,1);
77 Lambda = zeros(nbar,length(rho(e_vec(:,1)))); 
78
79 % Matrix to hold the derivative of the error model during policy
80 % updating
81 e_k_plus_1 = zeros(n,nbar);
82
83 % Product of the least squares matrices must be invertible
84 % Logic flag indicating if the critic weights are unsolvable
85 % The weights are unsolvable because the least squares matrices have no
86 % solution -- not invertible
87 diverged = 0;

```

```

88
89 % OUTER LOOP
90 for i = 1:(outerLoopMax-1)
91 % Determine if the least squares matrices are invertible
92 if diverged == 0
93     % For each of the data collection (discrete time index)
94     for k = 1:nbar
95         % Initialize the optimal inputs to zero
96         uNew = [0; 0];
97         % INNER LOOP
98         for j = 1:(innerLoopMax-1)
99             % Get the updated input value
100            uLast = uNew;
101            % Update the error model
102            e_k_plus_1(:,k) = f(e_vec(:,k)) + g*uLast;
103            % Compute the new optimal inputs
104            uNew = -0.5*(R^(-1))*g'*drhode(e_k_plus_1(:,k))'*WcLast;
105
106            % Check convergence of the optimal inputs
107            if norm(uNew - uLast) < EpsilonPolicy
108                break;
109            end
110        end
111
112        % Update the values for the least-squares computation
113        V(k,:) = Q(e_vec(:,k)) + uNew'*R*uNew + ...
114            WcLast'*rho(e_k_plus_1(:,k));
115        Lambda(k,:) = rho(e_vec(:,k))';
116    end
117
118    % Verify the least square solution exists for the critic's weights
119    % If the error data is consistent or there is no error, this will not
120    % hold, so set the weights to zero
121    if det(Lambda'*Lambda) == 0
122        weights = zeros(length(rho(e_vec(:,1))),1);
123        break;
124    end;
125
126    % Calculate least squares solution of critic's weights -- EQ 20
127    WcNew = (Lambda'*Lambda)^(-1)*Lambda'*V;
128    % Make sure the weights did not diverge
129    % If the weights are diverging, just set them to a large number
130    if isnan(WcNew)
131        weights = 1000*ones(length(rho(e_vec(:,1))),1);
132        break;
133    end;
134
135    % Check for convergence of the critic weights
136    if norm(WcNew - WcLast) < EpsilonWcritic
137        weights = WcNew;
138        break;
139    end
140    % If the weights did not converge, repeat the loop

```

```

141 WcLast = WcNew;
142
143 % If we reached the last iteration of the loop, just use the last
144 % weights found
145 if (i == (outerLoopMax-1))
146     weights = WcNew;
147 end
148 end
149
150 % Use the weights to determine the P matrix
151 P_Mat = [weights(5) weights(6) weights(7) weights(8);
152           weights(6) weights(9) weights(10) weights(11);
153           weights(7) weights(10) weights(12) weights(13);
154           weights(8) weights(11) weights(13) weights(14)];
155
156 % Find the state-feedback gain EQ
157 K = 0.5*(R_Mat_ADP^-1)*B'*P_Mat;
158
159 % Save the initial weights
160 wcInit = weights;
161
162 % Keep only the ADP gain
163 clearvars -except K tau T wcInit;

```

E.2 Update Weights

```

1 % CRITIC WEIGHT TUNING NEURAL NETWORK
2 % This function is specific to the helicopter because of the number of
3 % weights and error model
4 % THIS FUNCTION CANNOT HAVE ANY ANONYMOUS FUNCTIONS DUE TO THE C CODE
5 % GENERATION UNSUPPORTING IT
6 function K = ...
    quanserAEROCriticTuning(xd,pitchData,yawData,pitchDotData,yawDotData,wcInit)
7     % CREATE THE ERROR VECTOR MATRIX
8     % Use the data from the tapped delay blocks to create the error state
9     % vector matrix
10    e_vec = [pitchData'; yawData'; pitchDotData'; yawDotData'];
11
12    % REFERENCE DR. MIAH'S PAPER FOR EQUATION NUMBERS
13    % Sampling time [s]
14    tau = 0.05;
15
16    % COST FUNCTION
17    % Q and R matrices used in the cost function
18    Q_Mat = diag([270 100 1 1]);
19    R_Mat = 0.005*diag([1 1]);
20
21    % SYSTEM PARAMETERS SPECIFIC TO THE 2-DOF QUANSER AERO
22    A = [0 0 1 0; 0 0 0 1; -1.7442 0 -0.3307 0; 0 0 0 -0.9283];
23    B = [0 0; 0 0; -0.0149 0.0414; -0.0751 -0.1295];

```

```

24 % UNCOMMENT TO USE A STATE-SPACE MODEL THAT IS NOT THE CORRECT ...
25 % ONE DERIVED
26 % A = [1 1 1 1; 1 1 1 1; 1 1 1 1; 1 1 1 1];
27 % B = [0 0; 0 0; 0.1 0.1; -0.3 -0.3];
28 % System dimensions specific for our model
29 [n,~] = size(B);
30
31 % ERROR MODEL OF THE HELICOPTER
32 % gbar and hbar — EQ 8
33 % An anonymous function cannot be used for fbar
34 gbar = -B;
35 hbar = -A*xd;
36
37 % DISCRETE-TIME ERROR MODEL FOR TIME TAU
38 % g and h — EQ 10
39 % An anonymous function cannot be used for f
40 g = gbar*tau;
41 h = hbar*tau;
42
43 % COST FUNCTION PARAMETERS
44 % The Q matrix cannot be treated as an anonymous function as in the
45 % MATLAB simulations
46 % Control penalizing matrix in the continuous cost function
47 Rbar = R_Mat;
48 % The discrete-time cost function will have terms:
49 % Right after EQ 11 in paper
50 % Control penalizing matrix in the discretized cost function
51 R = Rbar*tau;
52
53 % NEURAL NETWORK FUNCTIONS
54 % These functions cannot be written as anonymous functions as in the
55 % MATLAB simulations
56
57 % TOLERANCES
58 % Convergence tolerance for control policy
59 EpsilonPolicy = 0.1;
60 % Convergence tolerance for critic neural network
61 EpsilonWcritic = 0.1;
62
63 % TRAINING PARAMETERS
64 % Number of outer loop iterations
65 outerLoopMax = 700;
66 % Number of inner loop iterations
67 innerLoopMax = 100;
68 % Number of equations needed for training, number of sub-intervals
69 % Number of training samples
70 [~,nbar] = size(e_vec);
71
72 % WEIGHT INITIALIZATION
73 % Initialize the weights of the critic neural network to zero
74 % Number of rows hard-coded for the helicopter
75 WcLast = zeros(14,1);
76
77 % LEAST-SQUARES COMPUTATION INITIALIZATION

```

```

77 % Matrices required for computing least squares weights of the critic
78 % neural networks -- EQ 20
79 V = zeros(nbar,1);
80 Lambda = zeros(nbar,14);
81
82 % Matrix to hold the derivative of the error model during policy
83 % updating
84 e_k_plus_1 = zeros(n,nbar);
85
86 % Product of the least squares matrices must be invertible
87 % Logic flag indicating if the critic weights are unsolvable
88 % The weights are unsolvable because the least squares matrices ...
89 % have no
90 % solution -- not invertible
91 diverged = 0;
92
93 % OUTER LOOP
94 for i = 1:(outerLoopMax-1)
95 % Determine if the least squares matrices are invertible
96 if diverged == 0
97     % For each of the data collection (discrete time index)
98     for k = 1:nbar
99         % Initialize the optimal inputs to zero
100        uNew = [0; 0];
101        % INNER LOOP
102        for j = 1:(innerLoopMax-1)
103            % Get the updated input value
104            uLast = uNew;
105            % Update the error model
106            % Because of no anonymous functions we have modified f
107            % fbar = @(e) A*e;
108            % f = @(e) fbar(e)*tau + e;
109            e_k_plus_1(:,k) = (A*e_vec(:,k)*tau) + e_vec(:,k) + ...
110                g*uLast + h;
111            % Compute the new optimal inputs
112            % Partial derivative of rho with respect to e
113            drhode = [1, 0, 0, 0;
114                      0, 1, 0, 0;
115                      0, 0, 1, 0;
116                      0, 0, 0, 1;
117                      2*e_vec(1,k), 0, 0, 0;
118                      e_vec(2,k), e_vec(1,k), 0, 0;
119                      e_vec(3,k), 0, e_vec(1,k), 0;
120                      e_vec(4,k), 0, 0, e_vec(1,k);
121                      0, 2*e_vec(2,k), 0, 0;
122                      0, e_vec(3,k), e_vec(2,k), 0;
123                      0, e_vec(4,k), 0, e_vec(2,k);
124                      0, 0, 2*e_vec(3,k), 0;
125                      0, 0, e_vec(4,k), e_vec(3,k);
126                      0, 0, 0, 2*e_vec(4,k)];
127            uNew = -0.5*(R^(-1))*g'*drhode'*WcLast;
128
129            % Check convergence of the optimal inputs
130            if norm(uNew - uLast) < EpsilonPolicy

```

```

129             break;
130         end
131     end
132
133     % Update the values for the least-squares computation
134     % Critic neural network activation functions
135     rhoE = [e_vec(1,k); e_vec(2,k); e_vec(3,k); e_vec(4,k); ...
136             e_vec(1,k)^2; e_vec(1,k)*e_vec(2,k); ...
137             e_vec(1,k)*e_vec(3,k); e_vec(1,k)*e_vec(4,k); ...
138             e_vec(2,k)^2; e_vec(2,k)*e_vec(3,k); ...
139             e_vec(2,k)*e_vec(4,k); e_vec(3,k)^2; ...
140             e_vec(3,k)*e_vec(4,k); e_vec(4,k)^2];
141     rhoEK = [e_k_plus_1(1,k); e_k_plus_1(2,k); e_k_plus_1(3,k); ...
142             e_k_plus_1(4,k); e_k_plus_1(1,k)^2; ...
143             e_k_plus_1(1,k)*e_k_plus_1(2,k); ...
144             e_k_plus_1(1,k)*e_k_plus_1(3,k); ...
145             e_k_plus_1(1,k)*e_k_plus_1(4,k); ...
146             e_k_plus_1(2,k)^2; ...
147                 e_k_plus_1(2,k)*e_k_plus_1(3,k); ...
148                 e_k_plus_1(2,k)*e_k_plus_1(4,k); ...
149                 e_k_plus_1(3,k)^2; ...
150                 e_k_plus_1(3,k)*e_k_plus_1(4,k); e_k_plus_1(4,k)^2];
151
152     % State penalizing function in the continuous cost function
153     % Qbar = @(e) e'*Q_Mat*e;
154     % State penalizing function in the discretized cost function
155     % Q = @(e) Qbar(e)*tau;
156     V(k,:) = (e_vec(:,k)'*Q_Mat*e_vec(:,k)*tau) + ...
157             uNew'*R*uNew + WcLast'*rhoEK;
158     Lambda(k,:) = rhoE';
159
160     end
161 end
162
163 % Verify the least square solution exists for the critic's weights
164 % If the error data is consistent or there is no error, this will not
165 % hold, so set the weights to what they were initially before the
166 % simulation
167 if det(Lambda'*Lambda) == 0
168     weights = wcInit;
169     break;
170 end;
171
172 % Calulcate least squares solution of critic's weights — EQ 20
173 WcNew = (Lambda'*Lambda)^(-1)*Lambda'*V;
174 % Make sure the weights did not diverge
175 % If the weights diverged, set the weights to what they were ...
176     % initially
177 % before the simulation
178 if isnan(WcNew)
179     weights = wcInit;
180     break;
181 % Check for convergence of the critic weights
182 elseif norm(WcNew - WcLast) < EpsilonWcritic
183     weights = WcNew;
184     break;
185

```

```
179 % If we reach the last iteration of the loop, just use the last ...
180 % weights
181 elseif (i == (outerLoopMax-1))
182     weights = WcNew;
183 % If all else fails, just set the weights to the initial weights
184 else
185     weights = wcInit;
186 end
187 % If the weights did not converge, do another iteration of the loop
188 WcLast = WcNew;
189 end
190 % Use the weights to determine the P matrix
191 P_Mat = [weights(5) weights(6) weights(7) weights(8);
192           weights(6) weights(9) weights(10) weights(11);
193           weights(7) weights(10) weights(12) weights(13);
194           weights(8) weights(11) weights(13) weights(14)];
195
196 % Find the state-feedback gain EQ
197 K = 0.5*(R_Mat^-1)*B'*P_Mat;
198 end
```

Appendix F

Tutorials

F.1 USB Connection

1. Verify QuaRC is installed on computer
2. Install QFLEX 2 USB into Quanser Aero as seen in Figure F.1
3. Open Simulink model
4. Connect Quanser Aero to computer via the included USB adapter cable
5. Set simulation mode to external
6. Run MATLAB initialization code for motion controller
7. Click "Build Model" button
8. Click "Connect To Target" button
9. Click "Run" button



Figure F.1: Quanser Aero with QFLEX 2 USB panel installed

F.2 Raspberry Pi Implementation

1. Make sure software add ons are installed on MATLAB
 - (a) MATLAB Support Package for Raspberry Pi Hardware
 - (b) Simulink Support Package for Raspberry Pi Hardware
2. Install QFLEX 2 Embedded into Quanser Aero as seen in Figure F.2
3. Assuming Raspberry PI is not connected to network, establish a serial connection to the Raspberry PI
 - (a) Plug SD card into Linux computer and enable serial connectivity
 - (b) Insert SD card back into Raspberry Pi
 - (c) Connect serial cable to the Raspberry Pi, Pin 3 (black wire), Pin 4 (white wire), Pin 5 (green wire)
 - (d) Plug Raspberry Pi into computer
 - (e) Locate COM port for the connection
 - (f) Open Putty, select Serial connection, input COM number and 115200 as the speed
 - (g) Log into Raspberry Pi
 - (h) Configure network, type "sudo nano /etc/wpa_supplicant/wpa_supplicant.conf" and add network settings
4. Connect SPI wires to Raspberry PI. Pin 1 (white wire) on the embedded panel connects to +5V on the Pi. Pin 2 (yellow wire) connects to GPIO 10 on the Pi. Pin 3 (blue wire) connects to GPIO 9 on the Pi. Pin 4 (green wire) connects to GPIO 11 on the Pi. Pin 6 (purple wire) connects to GPIO 8 on the Pi. Pin 7 (Red wire) connects to ground on the Pi.
5. Connect Raspberry PI to QFLEX 2 Embedded
6. Right click on Simulink model
7. Open "Model Configuration Parameters"
8. Select "Hardware Implementation"
9. Set "Hardware Board" to "Raspberry Pi"
10. Under "Board Parameters" under "Groups" type in the IP address of the Raspberry PI, the username, and password
11. Under "Build options", set build action to "Build and run" and type in the file path that you want the model to be stored on the Raspberry PI

12. Set simulation mode to external
13. Run MATLAB initialization code for motion controller
14. Run MATLAB Raspberry PI/SPI initialization code [E.2](#)
15. Click "Deploy to Hardware" button
16. To stop program you must "kill" it
17. Open Putty, connect to your Raspberry PI, and log in
18. Type "ps -A" to view running programs and find the process number of your Simulink model
19. Type "sudo kill -9 #####" where ##### is your process number. This will kill the program
20. To run a file already on the Raspberry Pi use the command "sudo FILEPATH/FILE-NAME.elf", if file is in current directory use "sudo ./FILENAME.elf"
21. If the model runs to time infinity when started from the Raspberry Pi you can use Control-C to stop the model



Figure F.2: Quanser Aero with QFLEX 2 Embedded panel installed

F.3 Android Application

1. Make sure software add ons are installed on MATLAB, "Simulink Support Package for Android Devices"
2. Install Android Studio
3. Repeat steps from Appendix [F.2](#) to set up Raspberry Pi and push model to Raspberry Pi

4. From MATLAB open add on manager and click on the "Setup" gear next to the Android package
5. Verify Android Studio installed, Next
6. Verify Android SDK Tools installed
7. NOTE: The recent version of Android Studio removed one of their files that MATLAB needs to build android applications. Fixed by downloading and installing an older verision of Android Studio NDK bundle (December 2017) and copying over the missing folder into the file path that MATLAB was calling. This issue might be fixed in a newer version of Android Studio.
8. Click next
9. Follow intrustions on prompts to turn android on in developer mode
10. Turn on USB debugging
11. Install driver
12. Connect android to computer with USB cable
13. Allow USB debugging
14. Make sure both computer and android are on same network with internet access
15. Select device
16. Build and run Test App, App should close and delete itself after test is complete
17. Open simulink model's configuration parameters
18. Under "Hardware Implementation" set "Hardware Board" to "Android Device"
19. Build and deploy simulink model to android
20. Once APP is running, swtich network to same network as the Raspberry Pi
21. Execute code on Raspberry Pi
22. Control helicopter

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