

**ECE 364: Programming Methods for Machine Learning,  
Spring 2025  
Midterm 1 Sample**

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- **You will have 75 minutes (1.25 hours) to solve all the problems. Most have multiple parts.** Don't spend too much time on questions you don't understand and focus on answering as much as you can!
  - ***BUDGET YOUR TIME WISELY***. I highly recommend working on the questions you know first and the questions you need to think about second.
  - *No* resources are allowed for use during the exam except a multi-page cheatsheet and scratch paper on the back of the exam. **Do not tear out the cheatsheet or the scratch paper!** It messes with the auto-scanner.
  - You should write your answers *completely* in the space given for the question. We will not grade parts of any answer written outside of the designated space.
  - Please *use a dark-colored pen* unless you are *absolutely* sure your pencil writing is forceful enough to be legible when scanned. We reserve the right to take off points if we have difficulty reading the uploaded document.
  - Unless otherwise stated, assume  $P \neq NP$ .
  - Assume that whenever the word "reduction" is used, we mean a (not necessarily polynomial-time) *mapping/many-one* reduction.
  - You can only refer to the cheat sheet content as a black box.
  - **Don't cheat.** If we catch you, you will get an F in the course.
  - **Good luck!**
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Name: \_\_\_\_\_

NetID: \_\_\_\_\_

Date: \_\_\_\_\_

## 1. Tensor manipulations

(4 points)

For each of the code segments, answer the following questions.

```
(a) import torch
2   a = torch.tensor([[0,1,2,3],[4,5,6,7],[8,9,10,11]])
3   b = a[3::2, ::5]
4   d = a>4
5   c = a[d]
```

i. (1 point) What will be the shape of  $b$ ?

ii. (1 point) What does  $c$  contain?

```
(b) import torch
2   a = torch.tensor([[0,1,2,3],[4,5,6,7],[8,9,10,11]])
3   e = a.view([6,-1])
4   f = torch.tensor([0,1,0])
5   l = a.multiply_(f.unsqueeze(-1))
```

i. (1 point) What does  $e$  contain?

ii. (1 point) What does  $a$  contain?

Total for Question 1: 8

## 2. Striding along

(1 point)

Consider the following code segment:

```
1 import torch
2 a = torch.arange(1000).view(10,10,10)
3 b = ?
```

Slice up  $a$  in a way that will cause  $b$  to have a separate data space from  $a$ .

## 3. Matrix Calculus

(1 point)

Given:

$$f(x) = x^T A^T A x$$

where  $x \in \mathbb{R}^n$ ,  $A \in \mathbb{R}^{n \times n}$

Find the solution to the following partial derivative:

$$\frac{\partial f}{\partial x} =$$

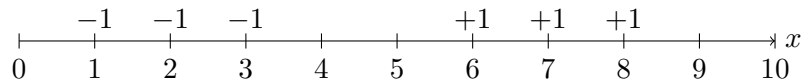
You must explain why your answer is correct for full credit.

#### 4. Support Vector Machines

(1 point)

Support vectors are the critical data points in an SVM that lie closest to the decision boundary. They determine both the optimal separating boundary and the margin width between classes. Removing these points from the training set would shift the boundary, potentially altering the classification results.

Consider a SVM that separates the following 1D points into two classes ( $-1$  and  $+1$ ) along the real number line:



With points:

- **Class  $-1$ :** 1, 2, 3
- **Class  $+1$ :** 6, 7, 8

- (a) (1 point) **Drawing the Boundary:** Sketch the decision boundary for an SVM on the provided number line. Choose the decision boundary that maximizes the margin and minimizes the loss. Additionally, sketch the margin boundaries for each class (these are the lines that pass through the closest data points from each class, positioned half a margin away from the decision boundary). Label each line clearly. You should draw a total of three lines. Include the approximate equation for each line.
- (b) (1 point) **Identifying Support Vectors:** For each class ( $-1$  and  $+1$ ) in the provided data, identify the support vectors and list them below.
- (c) (1 point) **Margin Calculation:** Calculate the margin (total width between class boundary lines) for your decision boundary.

5. **Linear Classification**

(1 point)

Let  $g$  be the logical **OR** function, defined on the feature space  $\{+1, -1\}^2$ , which maps:

- $g(+1, +1) = +1$
- $g(-1, +1) = +1$
- $g(+1, -1) = +1$
- $g(-1, -1) = -1$ .

Given a linear classifier  $h(x) = \text{sign}(\mathbf{w} \cdot \mathbf{x} + b)$ , where  $\mathbf{w} \in \mathbb{R}^{1 \times 2}$ ,  $\mathbf{x} \in \mathbb{R}^{2 \times 1}$ , and  $b \in \mathbb{R}^{1 \times 1}$ , give a valid  $(\mathbf{w}, b)$  pair that matches the ground truth  $g$ . Let  $\text{sign}(z) = +1$  for  $z \geq 0$  and  $-1$  otherwise. Give your solution and show that it is valid.

## 6. Gradient Descent

(15 points)

Consider the following function

$$f(x, y) = \frac{1}{1 + e^{x-y}}$$

(a) Determine the gradient  $\nabla f(x, y)$ .

(b) Let the starting point for gradient descent at  $k = 0$  be  $(x^{(0)}, y^{(0)}) = (0, 0)$  and the step size be  $\alpha = 4$ . Apply gradient descent to obtain the values of  $x$  and  $y$  iterations  $k = 1$  and 2.

## 7. Dataloaders and Optimizers

(20 points)

- (a) Consider a dataset of type `torch.utils.data.Dataset` named `my_dataset`. We want to create two separate dataloaders for the training and validation sets of the dataset. Each batch must have 64 examples. The validation set is created by randomly selecting 512 examples from the dataset, and the remaining examples are used for training. Complete the below function to implement the dataloaders.

```
1 # Even though you should not need to import anything else, feel
2 # free to do so.
3 import random
4 import torch.utils.data import DataLoader, SubsetRandomSampler
5
6 def split_dataset(my_dataset):
7     # complete this function
8     train_loader = None
9     val_loader = None
10    return train_loader, val_loader
```

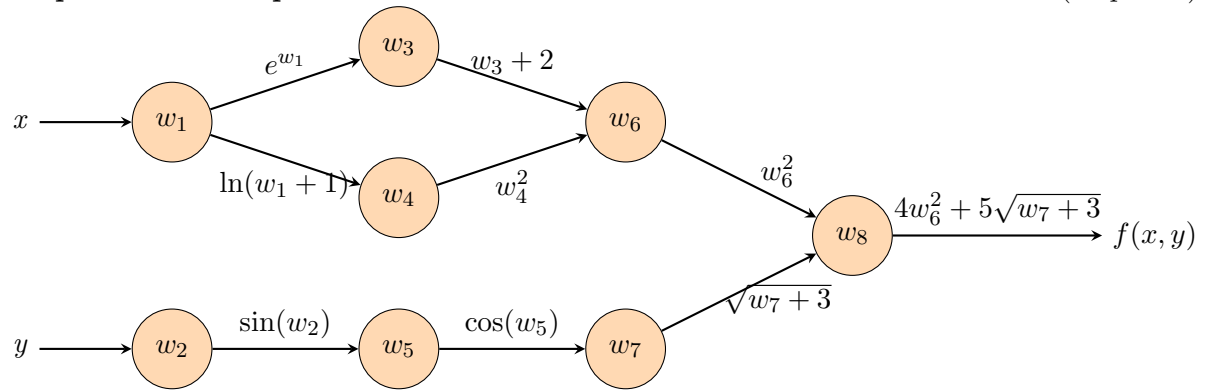
- (b) We aim to train `Model` using `SimpleDataset`. The dataloaders provide a dictionary containing the input and target, where the input has a shape of  $B \times M$  and the target has a shape of  $N$ . The `Model` expects an input of shape  $B \times M$  and produces an output of shape  $B$ . Here,  $B$  and  $M$  correspond to the batch size and the number of features, respectively. We will optimize the model using stochastic gradient descent (SGD) with a learning rate of 0.01 and a momentum of 0.9 and will use mean squared error loss. Complete the following code snippet.

```
1 import torch
2 from lib.model import Model
3 from lib.data import SimpleDataset
4
5 model = Model()
6 dataset = SimpleDataset()
7 train_loader, _ = split_dataset(dataset)
8 criterion = # Complete this
9 optim = # Complete this
10
11 for epoch in range(10):
12     for batch in train_loader:
13         inp, tgt = batch["input"], batch["target"]
14         # Complete this
```



## 8. Computational Graph

(15 points)



(a) Determine the function  $f(x, y)$  represented by the above computational graph.

(b) Compute the partial derivatives of each successor node with respect to its predecessors.

(c) Compute the adjoints at each node  $\bar{w}_i = \frac{\partial f}{\partial w_i}$ .