

Chap 3. Magnetic Aspect

- Circuit theory / Field theory

3.1 전자기장 요약

- Maxwell Equation :

$$\nabla \cdot \mathbf{B} = 0; \quad \oiint_S \mathbf{B} \cdot d\mathbf{S} = 0$$

$$\nabla \times \mathbf{H} = \mathbf{J}; \quad \oint_c \mathbf{H} \cdot d\mathbf{l} = I$$

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}; \quad \oint_c \mathbf{E} \cdot d\mathbf{l} = -\iint_S \frac{\partial \mathbf{B}}{\partial t} \cdot d\mathbf{S}$$

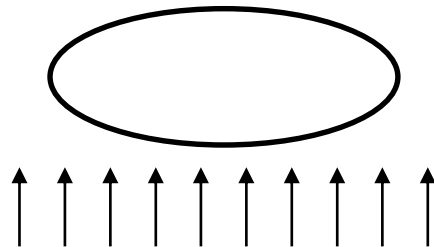
- Current Continuity :

$$\nabla \cdot \mathbf{J} = 0; \quad \oiint_S \mathbf{J} \cdot d\mathbf{S} = 0$$

KVL / KCL

- Faraday's Law : $\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$

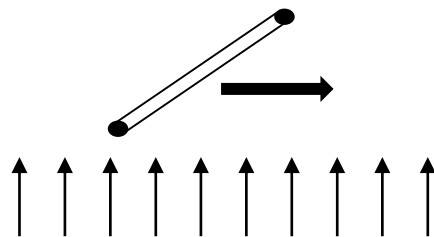
$$\oint_c \mathbf{E} \cdot d\mathbf{l} = -\iint_S \frac{\partial \mathbf{B}}{\partial t} \cdot d\mathbf{S}$$



$$e = -\frac{d\phi}{dt} \text{ or } -\frac{d\lambda}{dt}$$

$$\phi = \iint_S \mathbf{B} \cdot d\mathbf{S}$$

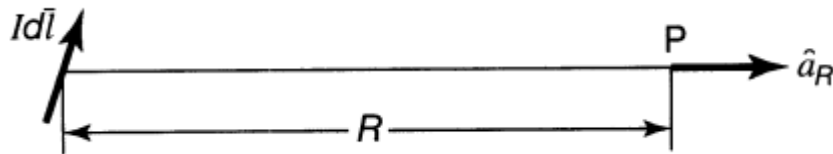
$$\lambda = N\phi$$



$$\begin{aligned} \text{Motional emf} &= \oint_c (\mathbf{U} \times \mathbf{B}) \cdot d\mathbf{l} \\ &= BlU \end{aligned}$$

3.2 자기장과 자력

• $I \rightarrow H \rightarrow F$



$$d\mathbf{H} = \frac{Id\mathbf{l} \times \hat{\mathbf{a}}_R}{4\pi R^2}$$

$$\mathbf{H} = \int \frac{Id\mathbf{l} \times \hat{\mathbf{a}}_R}{4\pi R^2}$$

$$d\mathbf{F} = Id\mathbf{l} \times \mathbf{B}$$

$$\mathbf{B} = \mu \mathbf{H}$$

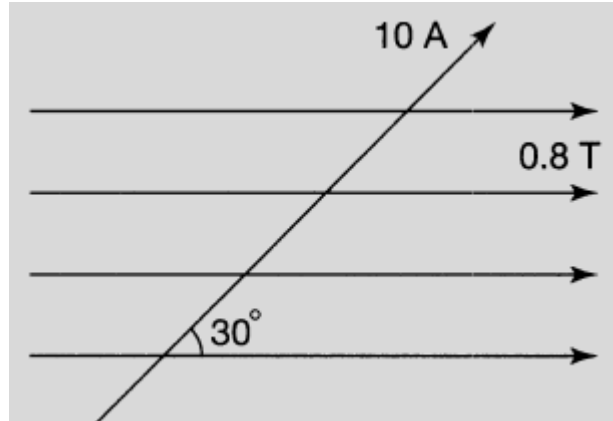
$$\mu_0 = 4 \times 10^{-7} \text{ H/m}$$

$$F = BIL$$

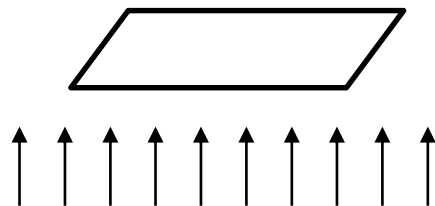
$$\phi = \int_S \mathbf{B} \cdot d\mathbf{S}$$

$$= \mathbf{B} \cdot \mathbf{S} = BS \cos \theta$$

< Ex 3.2.1 > $B=0.8\text{T}$, $L=2\text{m}$, $I=10\text{A}$, $\Theta=30^\circ \rightarrow F=?$



< Ex 3.2.2 > $B=0.5\text{T}$, $L=20\text{cm} \rightarrow \Phi=?$

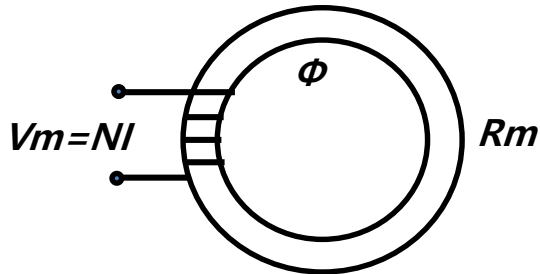


$$\phi = \int_S \mathbf{B} \cdot d\mathbf{S}$$

$$= \mathbf{B} \cdot \mathbf{S} = BS \cos \theta$$

3.3 기자력

- Magneto-Motive Force (mmf) / Electro-Motive Force (emf)

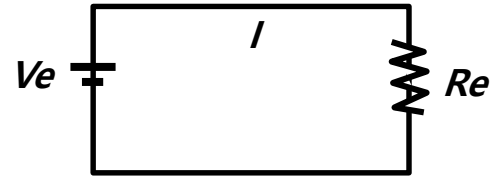


$$\text{mmf} = \oint \mathbf{H} \cdot d\mathbf{l} = IN$$

$$V_m = R_m \cdot \phi \quad \phi = \frac{F}{R}$$

$$R_m = \frac{L}{\mu S}$$

$$\text{mmf} = N \cdot I = H \cdot L = R_m \cdot \phi$$



$$\text{emf} = \int \mathbf{E} \cdot d\mathbf{l} = V_e$$

$$V_e = R_e \cdot I \quad I = \frac{V_e}{R_e}$$

$$R_e = \frac{L}{\sigma S}$$

<Ex 3.3.1>

N=500, for H=2kA/m

→ I=?

3.4 자성체

- Magnetic Materials :
 - Diamagnetic / Paramagnetic / Ferromagnetic , Super-paramagnetic / Ferrimagnetic
 - Magnetic Saturation (Linear / Nonlinear) , Magnetic Hysteresis
 - Isotropic / Anisotropic
 - Ferrofluidic (Magnetic Fluid)
 - Curie Temperature

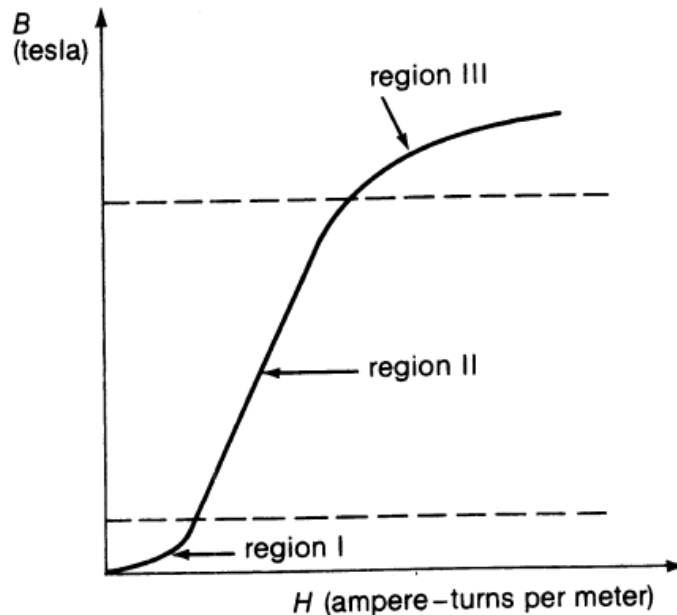
Trade Name	Saturation Flux Density (T)	Maximum Relative Permeability ($\times 10^3$)	Electrical Resistivity (ohm-meter $\times 10^{-6}$)	Curie Temperature ($^{\circ}\text{C}$)
Carpenter				
Silicon core iron	2-2.1	4-5	0.25-0.60	800
Electrical iron	2.15	2.2-5.5	0.10	760
430F solenoid quality	1.47	1.1-1.6	0.60	671
High-permeability 49	1.6	30-120	0.48	450
Hy mu 80	0.78	70-75	0.58	460
Hiperco 27	2.36	2.8	0.19	925
Silectron	1.97	10-20	0.50	732
2 V Permendur	2.30	8	0.40	932
Monimax	1.45	40-100	0.65	398
Deltamax	1.60	100-200	0.45	499
4-79 Molybdenum permalloy	0.80	100-400	0.55	454
Ferrite	0.22-0.45	0.16-10	$(0.1 \times 10^6) - (10 \times 10^6)$	135-500

- Permeability , Magnetic Saturation , B-H Curve :

- μ_{init} , μ_{max} , $\mu_{2.0}$
- DC curve / AC curve (60Hz)

$$\mathbf{B} = \mu \mathbf{H} \quad \mu = \mu_r \mu_0$$

$$\mu_0 = 4\pi \times 10^{-7} \text{ henry/meter} = 1.257 \times 10^{-6} \text{ H/m}$$



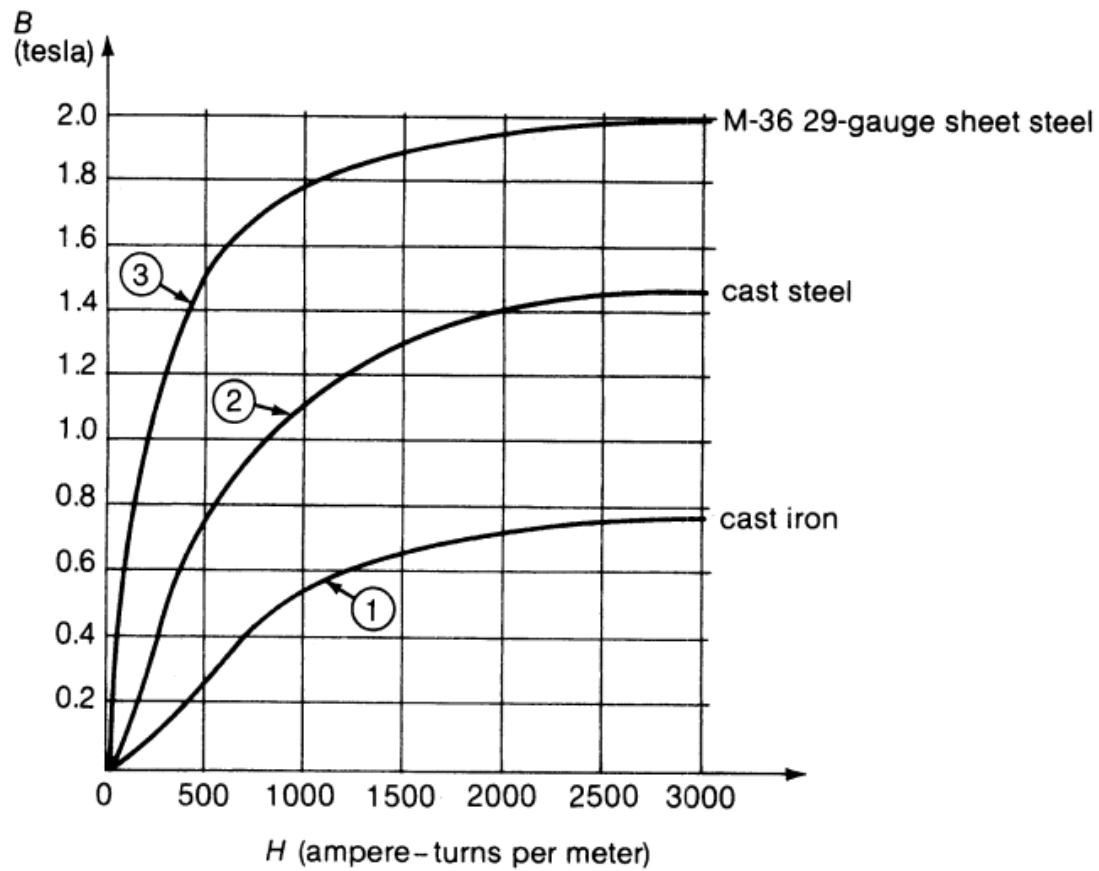
$$B = \frac{aH}{1 + bH}$$

$$B = \frac{a_0 + a_1H + a_2H^2 + \dots}{1 + b_1H + b_2H^2 + \dots}$$

$$H = [k_1 \exp(k_2B^2) + k_3] B$$

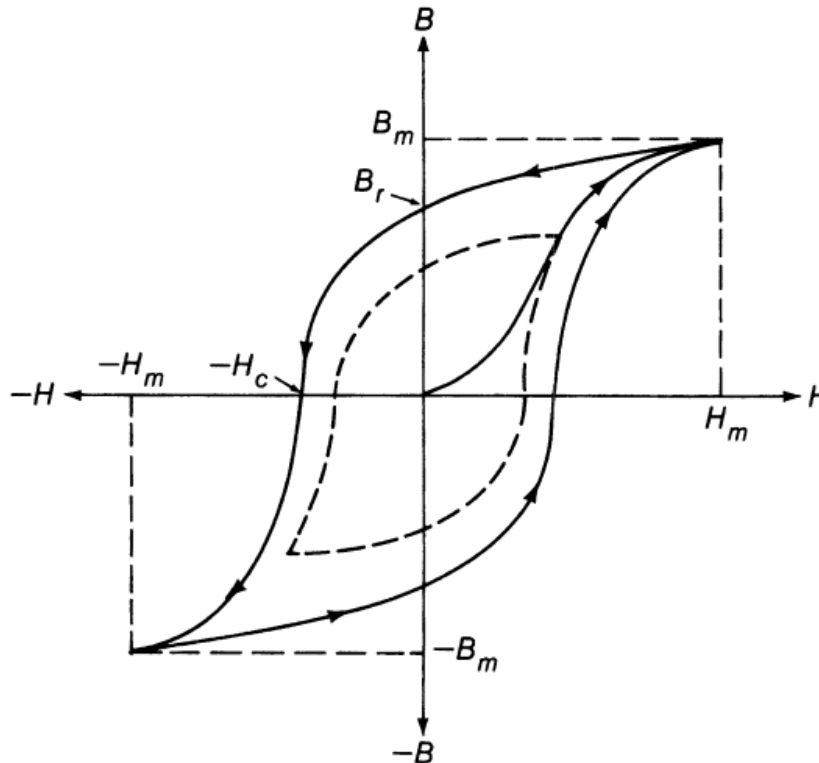
표 3.4.2 • 일부 물질의 투자율과 유형

Material	Classification	Relative Permeability, μ_r
Bismuth	diamagnetic	0.99983
Silver	diamagnetic	0.99998
Lead	diamagnetic	0.999983
Copper	diamagnetic	0.999991
Water	diamagnetic	0.999991
Vacuum	nonmagnetic	1
Air	paramagnetic	1.0000004
Aluminum	paramagnetic	1.00002
Palladium	paramagnetic	1.0008
2-81 Permalloy powder (2 Mo, 81 Ni, Iron)	super-paramagnetic	130
Cobalt	ferromagnetic	250
Nickel	ferromagnetic	600
Ferroxcube 3 (Mn-Zn-ferrite powder)	ferrimagnetic	1,500
Ferrites	ferrimagnetic	160~10,000
Mild steel (0.2 C)	ferromagnetic	2,000
Iron (0.2 impurity)	ferromagnetic	5,000
Silicon iron (4 Si)	ferromagnetic	7,000
78 Permalloy (78.5 Ni)	ferromagnetic	100,000
Mumetal (75 Ni, 5 Cu, 2 Cr)	ferromagnetic	100,000
Purified iron (0.05 impurity)	ferromagnetic	200,000
Superalloy (5 Mo, 79 Ni)	ferromagnetic	1,000,000

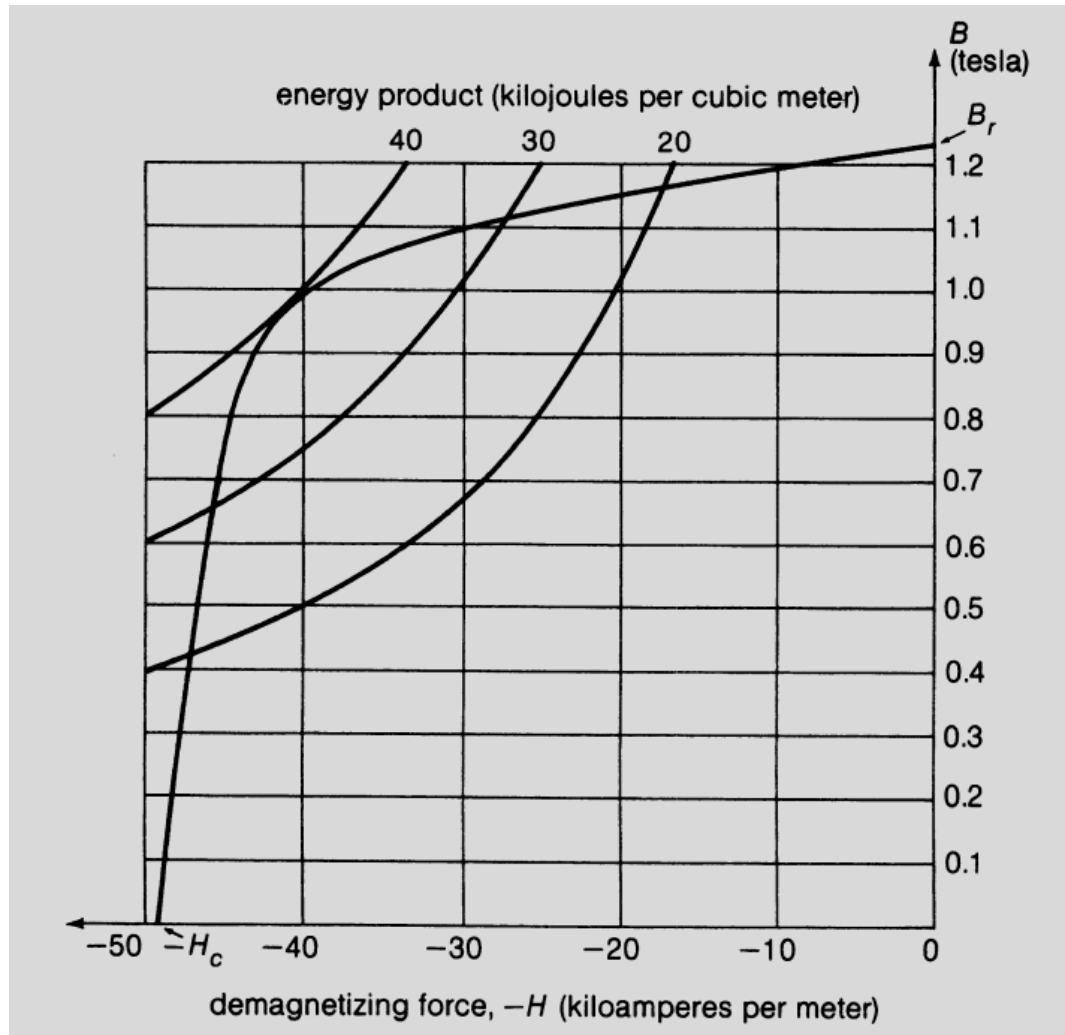


- **Magnetic Hysteresis Curve :**

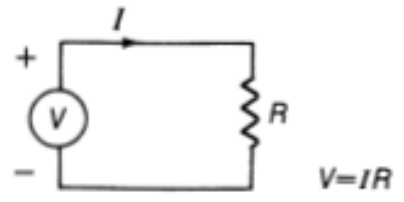
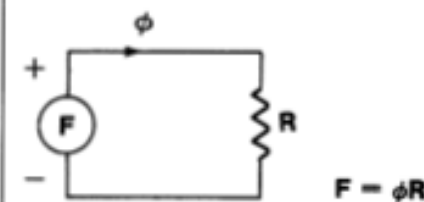
- B_s , B_r , H_c , S , S^*
- Major loop / Minor Loop / History dependent tracer
- Hysteresis Loss, Steinmetz
- Magnetic energy, Permanent Magnet



- Magnetization / Demagnetization
- Degaussing / Deperming



3.5 자기회로

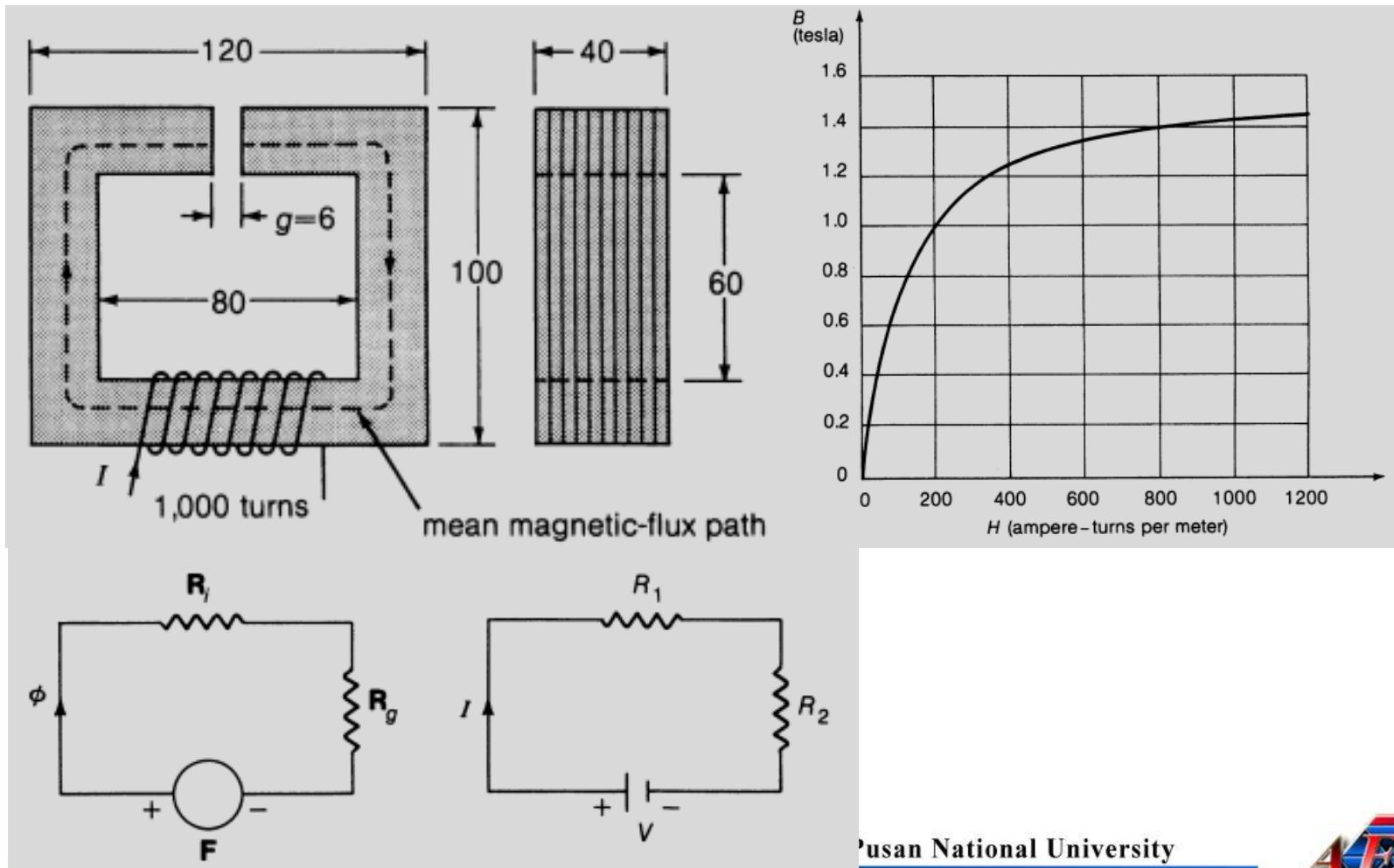
	Electric Circuit	Unit	Magnetic Circuit	Unit
Driving force	emf (V)	V	mmf (F)	At
Response	current (I)	A	flux (ϕ)	Wb
Impedance	resistance (R)	Ω	reluctance (R)	1/H
Equivalent circuit				
Field intensity relationship	$\oint \mathbf{E} \cdot d\mathbf{l} = V$	V	$\oint \mathbf{H} \cdot d\mathbf{l} = I$	A
Potential difference	$V = IR$	V	$\mathbf{F} = \phi \mathbf{R}$	At
Other relations	$J = \frac{I}{A} = \frac{V}{AR} = \frac{El}{A(\rho l/A)}$ $= \frac{E}{\rho} = \sigma E$ <p>or $E = \rho J = J/\sigma$, where J is the current density, ρ is the resistivity, and σ is the conductivity</p>	A/m^2 $\Omega \cdot \text{m}$ $1/(\Omega \cdot \text{m})$	$B = \frac{\phi}{A} = \frac{F}{AR} = \frac{Hl}{A(l/\mu A)}$ $= \mu H = H/\nu$ <p>or $H = B/\mu = \nu B$, where B is the flux density, μ is the permeability, and ν is the reluctivity</p>	T or Wb/m^2 H/m m/H
Admittance	conductance $G = 1/R$	S	permeance $\mathbf{P} = 1/\mathbf{R}$	H

$$N \cdot I = H \cdot L = R_m \cdot \Phi$$

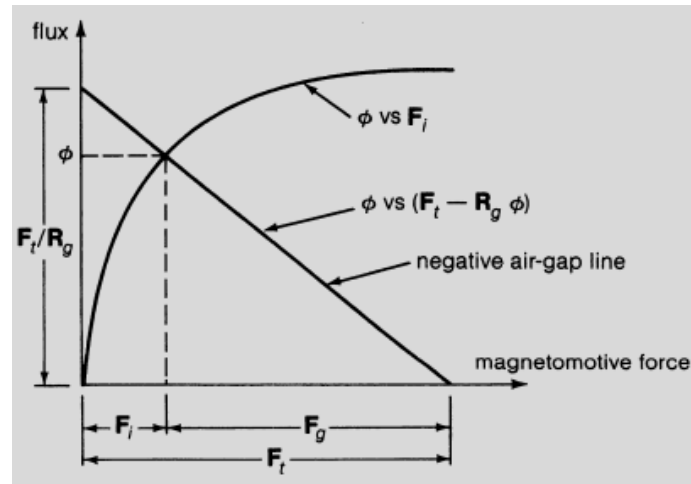
<Ex 3.5.1> $A=10\text{mm}^2$, $L=20\text{cm}$, $\mu_r=500 \rightarrow$ (a) $R_m=?$, (b) Φ , $B=?$

<Ex 3.5.2> USS 변압기, $\Phi \rightarrow NI?$

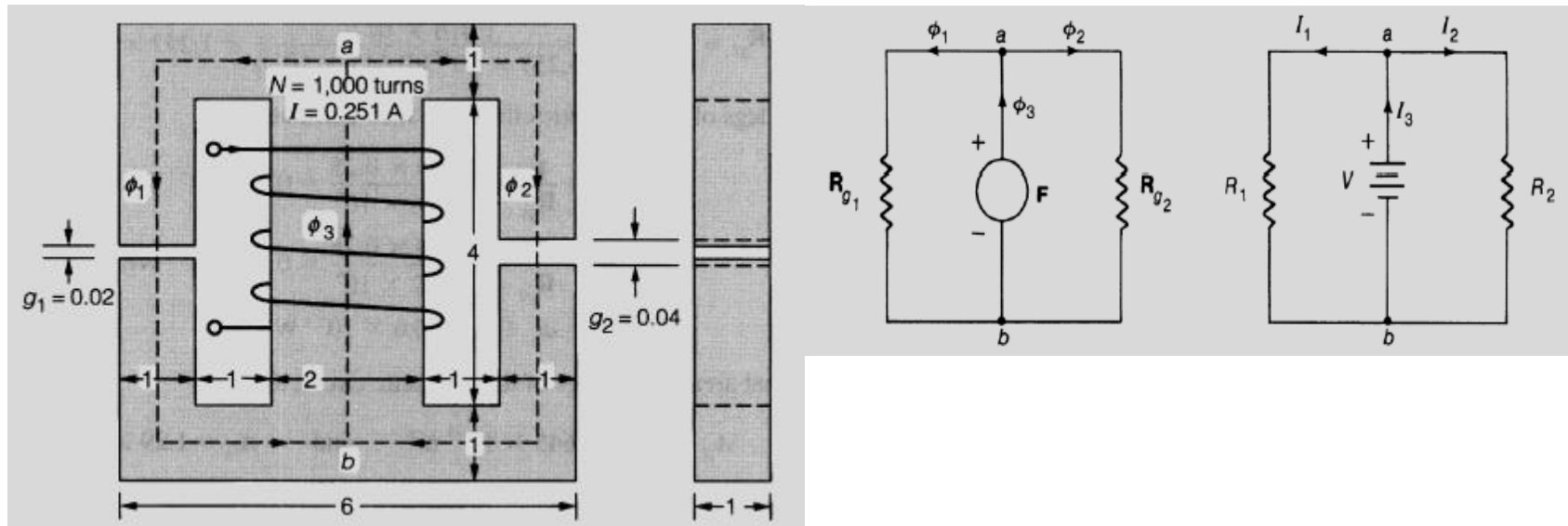
적층철 0.94, B_H curve, $\Phi = 1\text{mWb} \rightarrow I=??$



<Ex 3.5.3> Ex 3.5.2 : $NI \rightarrow \Phi$?



<Ex 3.5.4> 2개의 병렬공극 :



<Ex 3.5.5> Ex 3.5.4 : 철심 B-H curve : B in each leg = ?

<Problems>

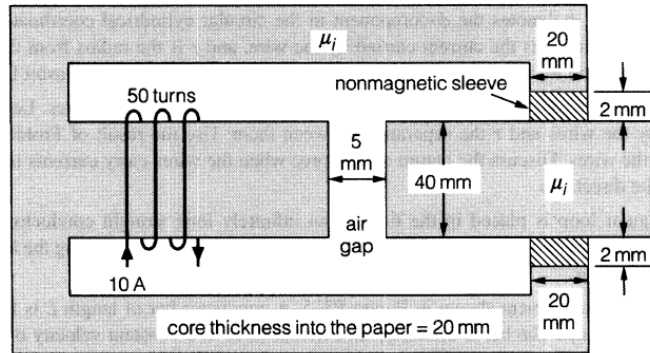


그림 P3-7

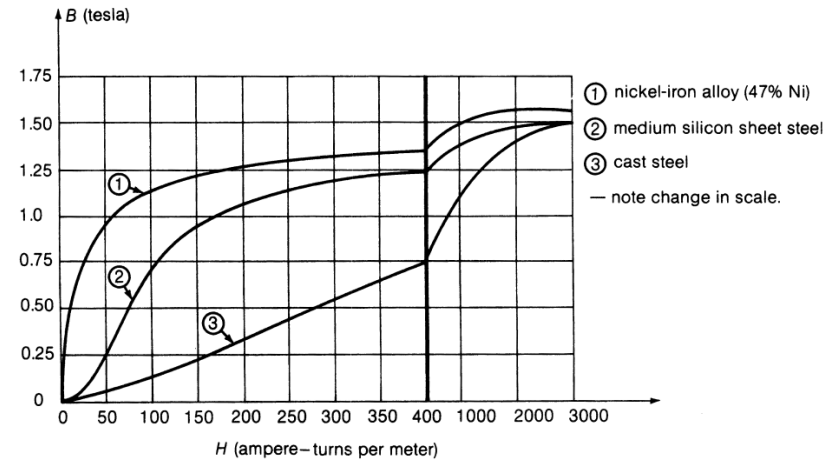
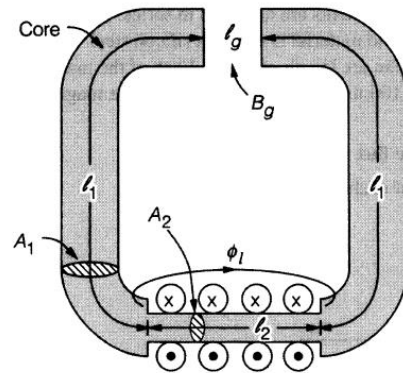
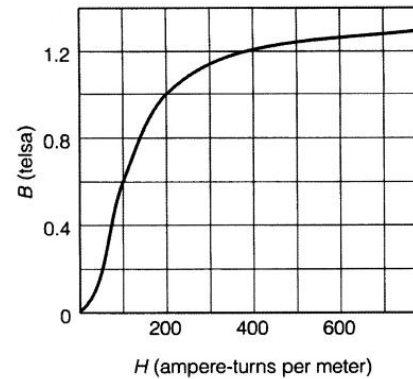


그림 P3-8



(a)



(b)

그림 P3-10

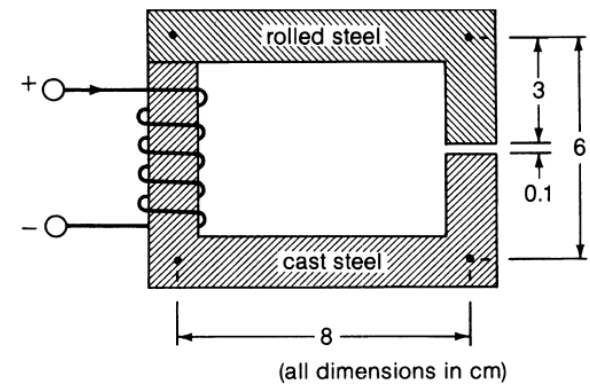


그림 P3-11

<Problems>

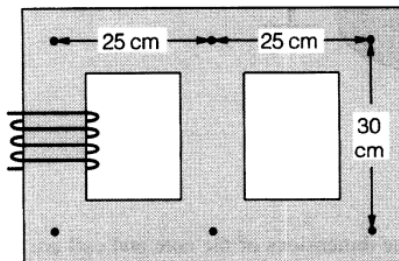


그림 P3-14

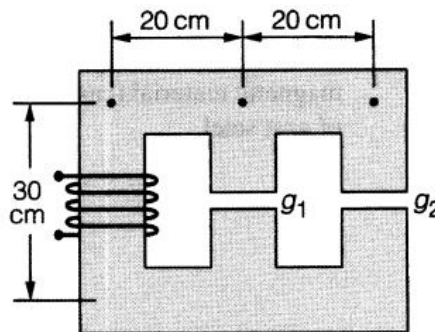


그림 P3-18

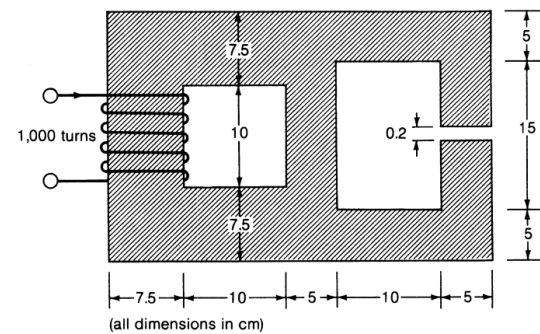


그림 P3-13

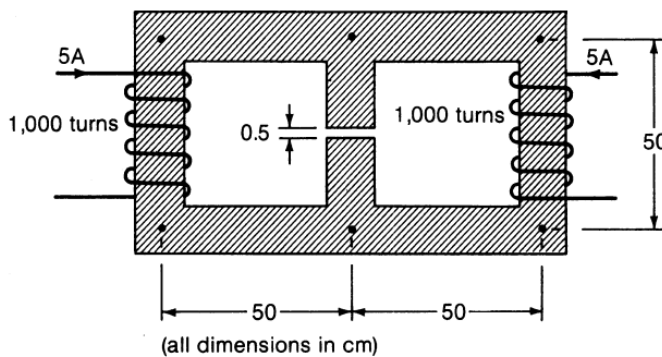


그림 P3-12

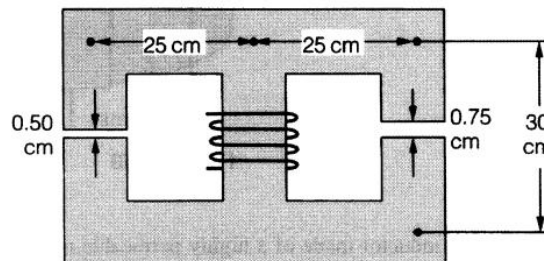


그림 P3-15

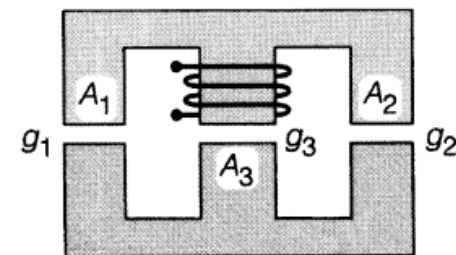


그림 P3-17

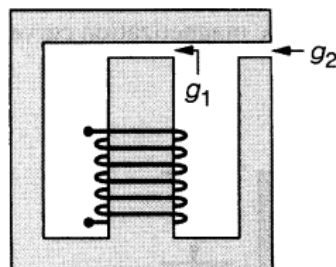


그림 P3-16

<Problems>

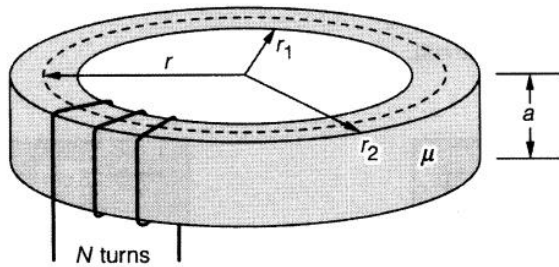


그림 P3-19

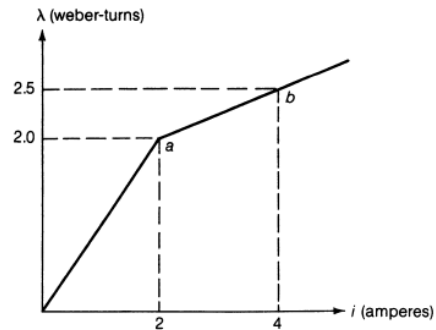


그림 P3-23

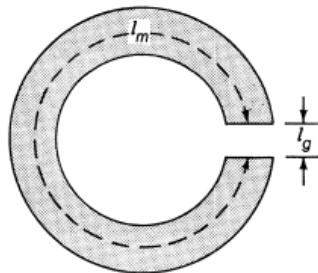
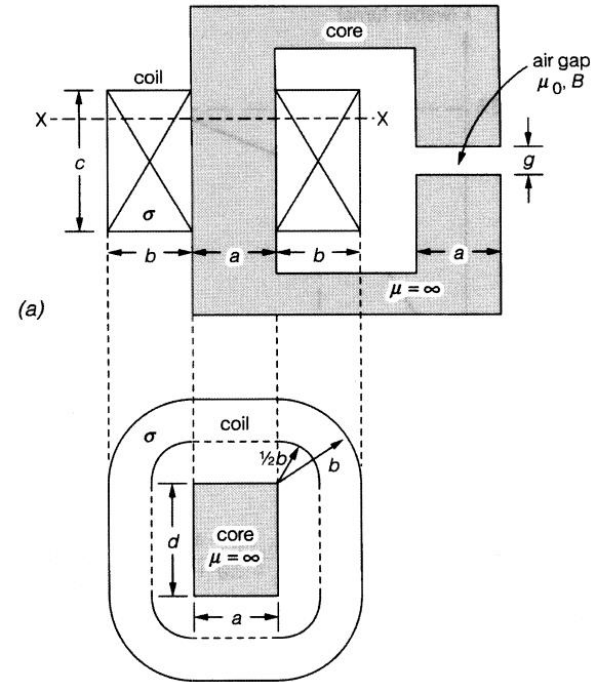


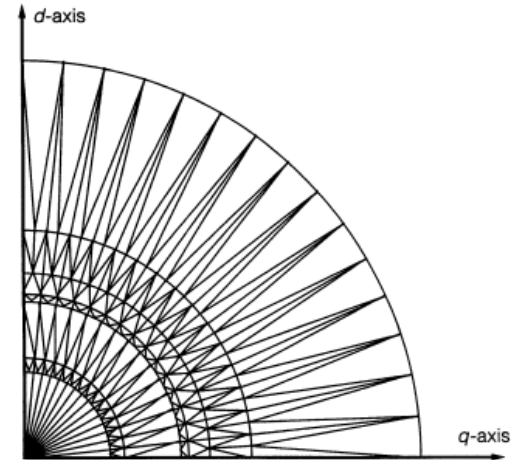
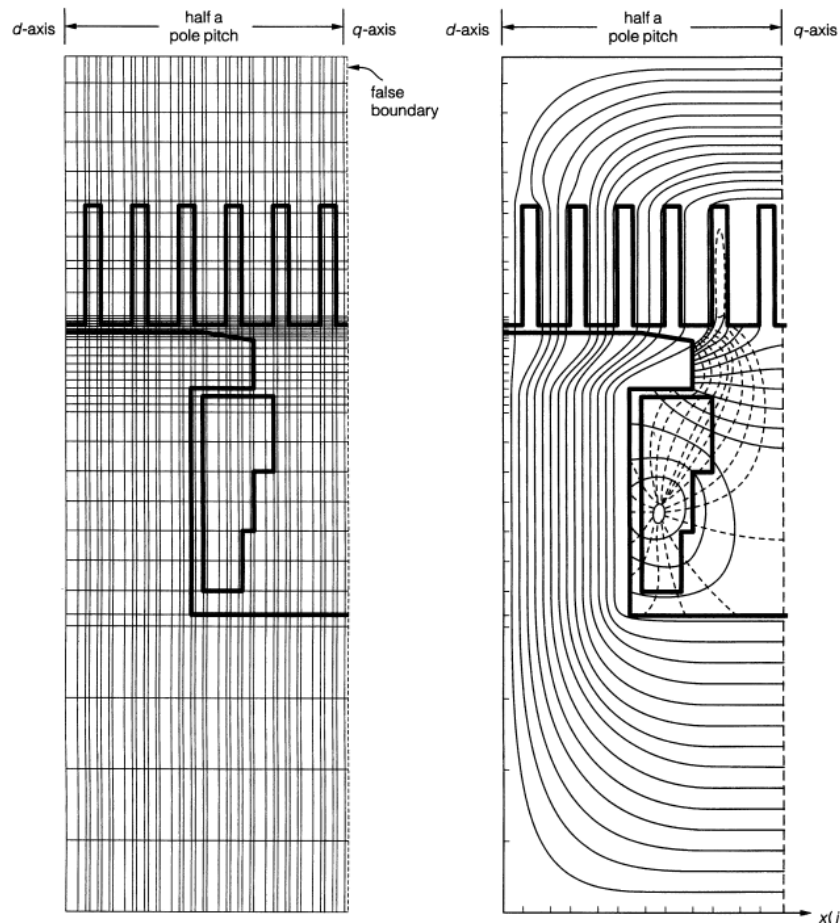
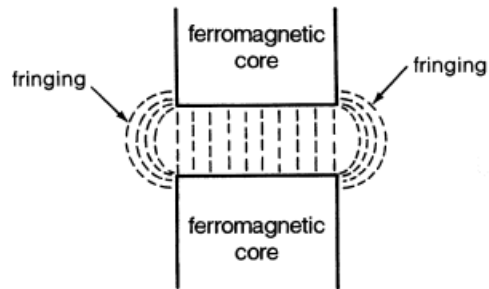
그림 P3-32



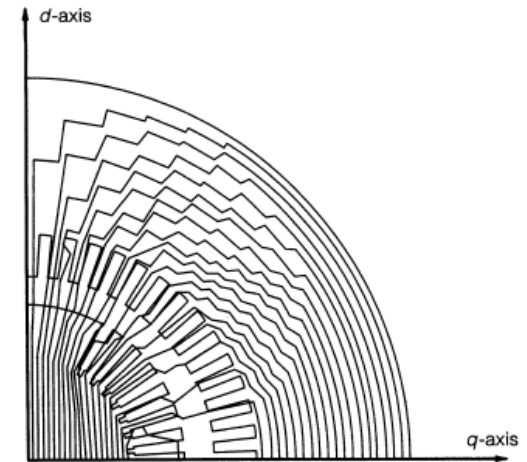
(b) Cross section at XX

그림 P3-20

- Fringing, Leakage :**

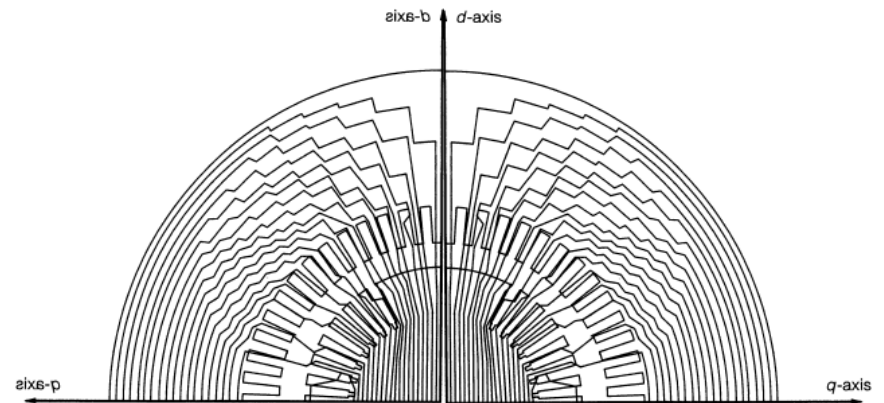
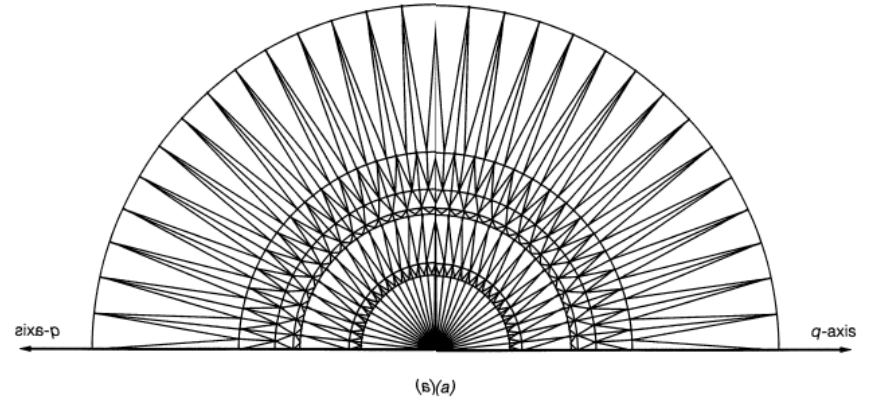
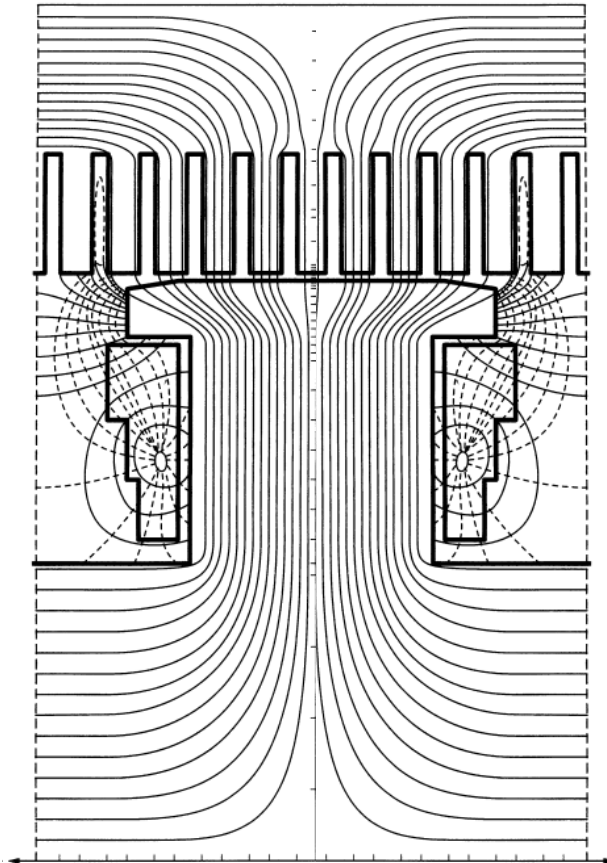


(a)



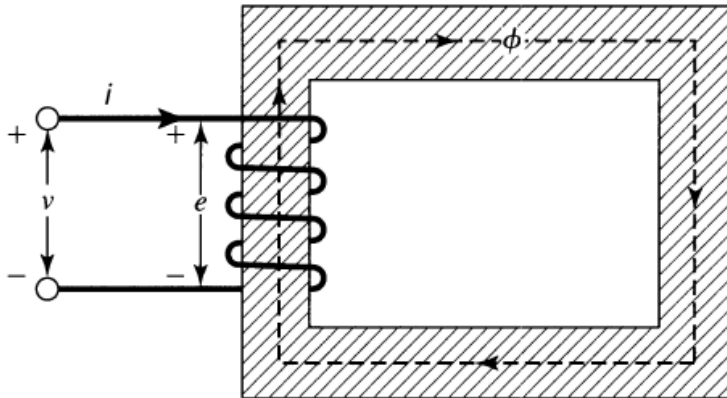
(b)

• $I \rightarrow H \rightarrow F$



3.6 AC 자기회로

- 유도기전력 :



$$N \cdot I = H \cdot L = R_m \cdot \Phi$$

$$i(t) = I_m \sin(\omega t)$$

$$\phi(t) = \frac{\text{mmf}}{R} = \frac{Ni(t)}{R} = \frac{NI_m \sin(\omega t)}{R} = \phi_m \sin(\omega t)$$

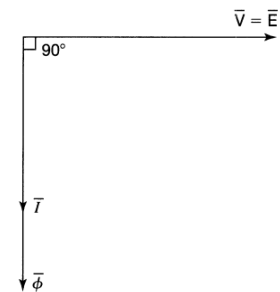
$$\phi_m = \frac{NI_m}{R}$$

$$\lambda(t) = N\phi(t) = N\phi_m \sin(\omega t)$$

$$e = \frac{d\lambda(t)}{dt} = \frac{d}{dt} (N\phi_m \sin(\omega t)) = \omega N\phi_m \cos(\omega t) = \underline{\omega N\phi_m \sin(\omega t + 90^\circ)} = Em \sin(\omega t + 90^\circ)$$

- 유도기전력, rms :

$$E = \frac{\omega N\phi_m}{\sqrt{2}} = \frac{2\pi f N\phi_m}{\sqrt{2}} = 4.44 N\phi_m f$$



- 철손(Iron Loss) = 히스테리시스 손실(Hysteresis Loss) + 와전류 손실(Eddy Current Loss)

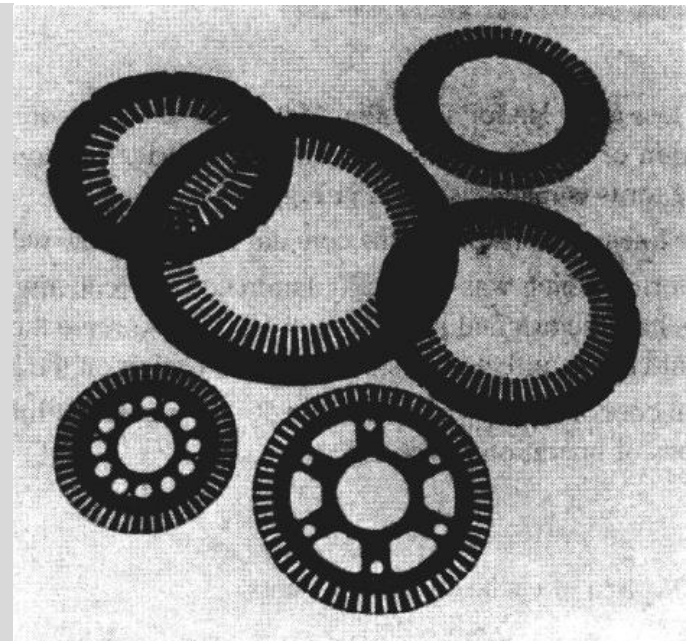
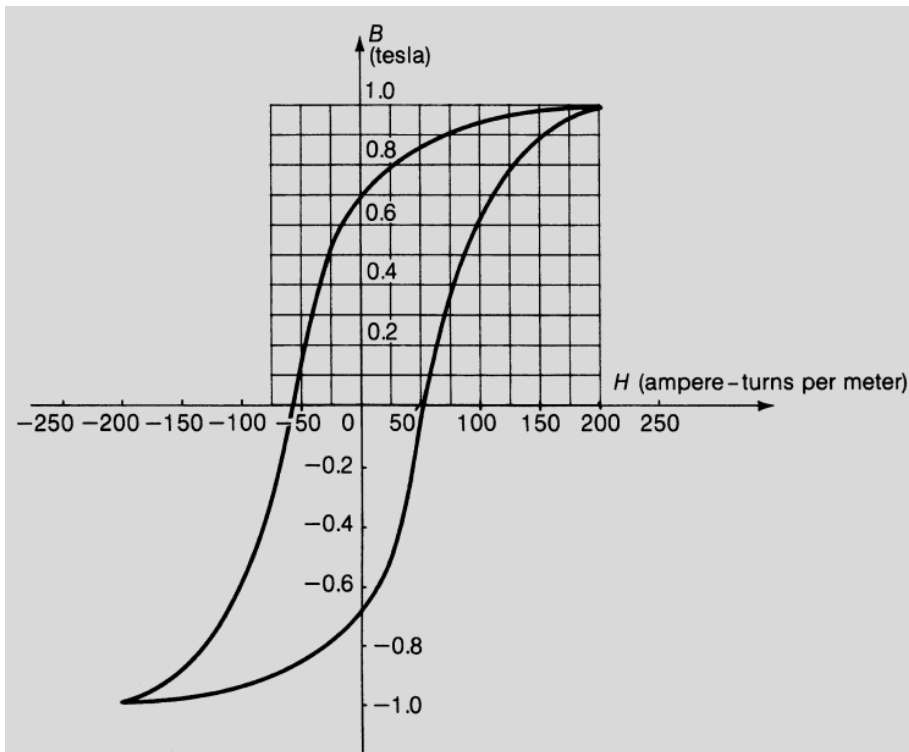
$$P_h \text{ per cycle} = \text{Vol} \oint H dB$$

$$P_h = k_h \cdot \text{Vol} \cdot f \cdot B_m^n$$

$$(\propto f \cdot B_m^n)$$

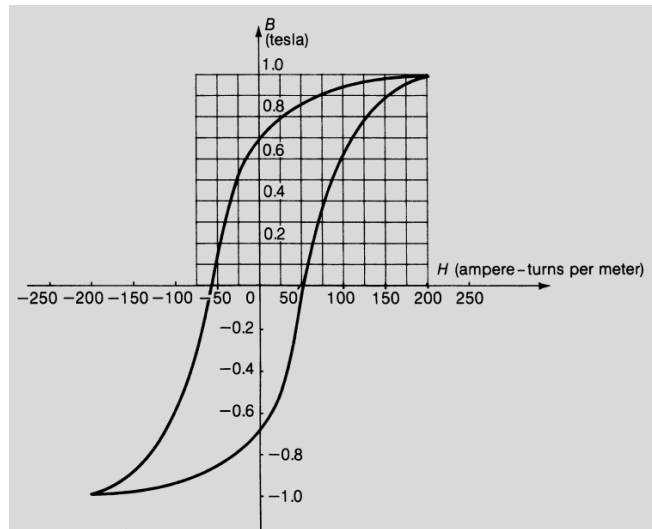
$$P_e = k_e \cdot \text{Vol} \cdot f^2 \cdot \tau^2 B_m^2$$

$$(\propto f^2 \cdot B_m^2)$$



<Ex 3.6.1> 사각단면 도넛 코어의 히스테리시스 손실 :

- 모든 방향으로 코어의 크기가 2배씩 커졌을 때, 히스테리시스 손실은 어떻게 달라지는가?
- 코어의 적층 두께를 원래 두께의 반으로 줄였다. 축적 계수는 동일하게 1이라고 가정하면 이러한 변화가 히스테리시스 손실에는 어떤 영향을 주는가?
- 코어가 50 Hz에서 동작할 경우 히스테리시스 손실은 어떻게 변화하는지 계산하시오.



$$P_h = k_h \cdot \text{Vol} \cdot f \cdot B_m^n$$

$$b. \propto V$$

$$d. \propto f$$

<Ex 3.6.2> $f=50\text{Hz}$, $B=0.8\text{T}$ → 철손 1000W : $P_h=?$, $P_e=?$
 $f=75\text{Hz}$, // → 철손 1800W : $P_h=?$, $P_e=?$

$$P = af + bf^2, \quad P/f = a + bf, \quad a=?/b=? \quad , \quad P_h \text{ \& } P_e$$

3.7 에너지 저장

- Magnetic Energy, Energy Density :

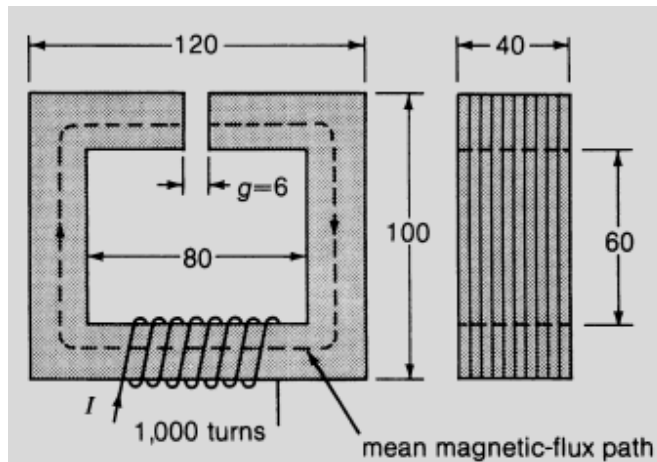
$$W_m = \frac{1}{2} \int_{\text{Vol}} \mathbf{B} \cdot \mathbf{H} dv$$

$$w_m = \frac{1}{2} \mathbf{B} \cdot \mathbf{H}$$

$$w_m = \frac{1}{2} BH = \frac{1}{2} \frac{B^2}{\mu} = \frac{1}{2} \frac{B^2}{\mu_r \mu_0}$$

- Air gap Energy : $W_{m \text{ air}} = \frac{1}{2} \left(\frac{B_g^2}{\mu_0} \right) \text{Vol} = \frac{1}{2} \mathbf{F} \Phi = \frac{1}{2} \mathbf{R} \Phi^2 = \frac{1}{2} i \lambda$

Ex3.5.2. :

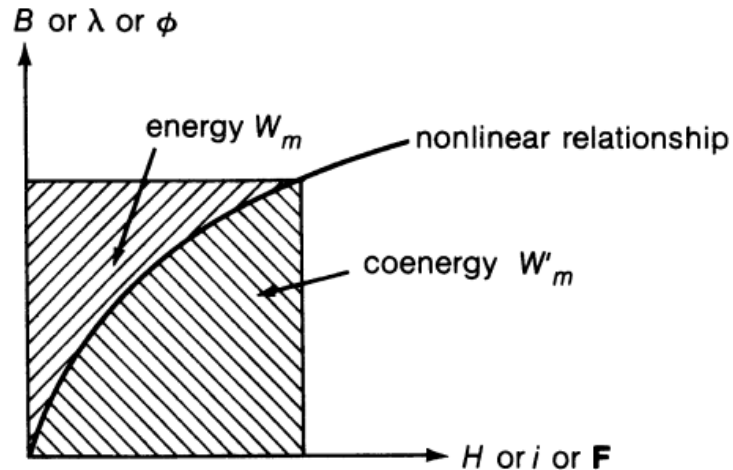


$$W_{m \text{ air}} = \frac{1}{2} \left(\frac{B_g^2}{\mu_0} \right) \text{Vol} = 1.995 \text{ J}$$

$$W_{\text{air}} = \frac{1}{2} F_{\text{gap}} \Phi = 1.995 \text{ J}$$

$$W_{\text{iron}} = \frac{1}{2} F_{\text{iron}} \Phi = 0.1 \text{ J (!!)}$$

- **Magnetizing Energy :**

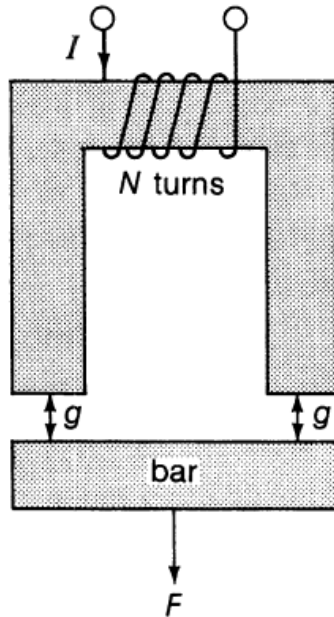


- **Magnetic Energy :** $W_m = \text{Vol} \int_0^B H dB = \int_0^\lambda i(\lambda) d\lambda = \int_0^\phi \mathbf{F}(\phi) d\phi$

- **Co-Energy :** $W'_m = \text{Vol} \int_0^H B dH = \int_0^i \lambda(i) di = \int_0^F \phi(\mathbf{F}) d\mathbf{F}$

$$W'_m + W_m = \text{Vol} \cdot BH = \lambda i = \phi \mathbf{F}$$

• Magnetic Force :



$$dW_m = \frac{1}{2} (\mathbf{B} \cdot \mathbf{H}) dv$$

$$dv = A dg$$

$$dW_m = \frac{1}{2} BH dv = \frac{1}{2} BHA dg = \frac{1}{2} \left(\frac{B^2}{\mu_0} \right) A dg$$

Definition : $dW = \mathbf{F} \cdot d\mathbf{l} = F dg$

$$dW_m = dW$$

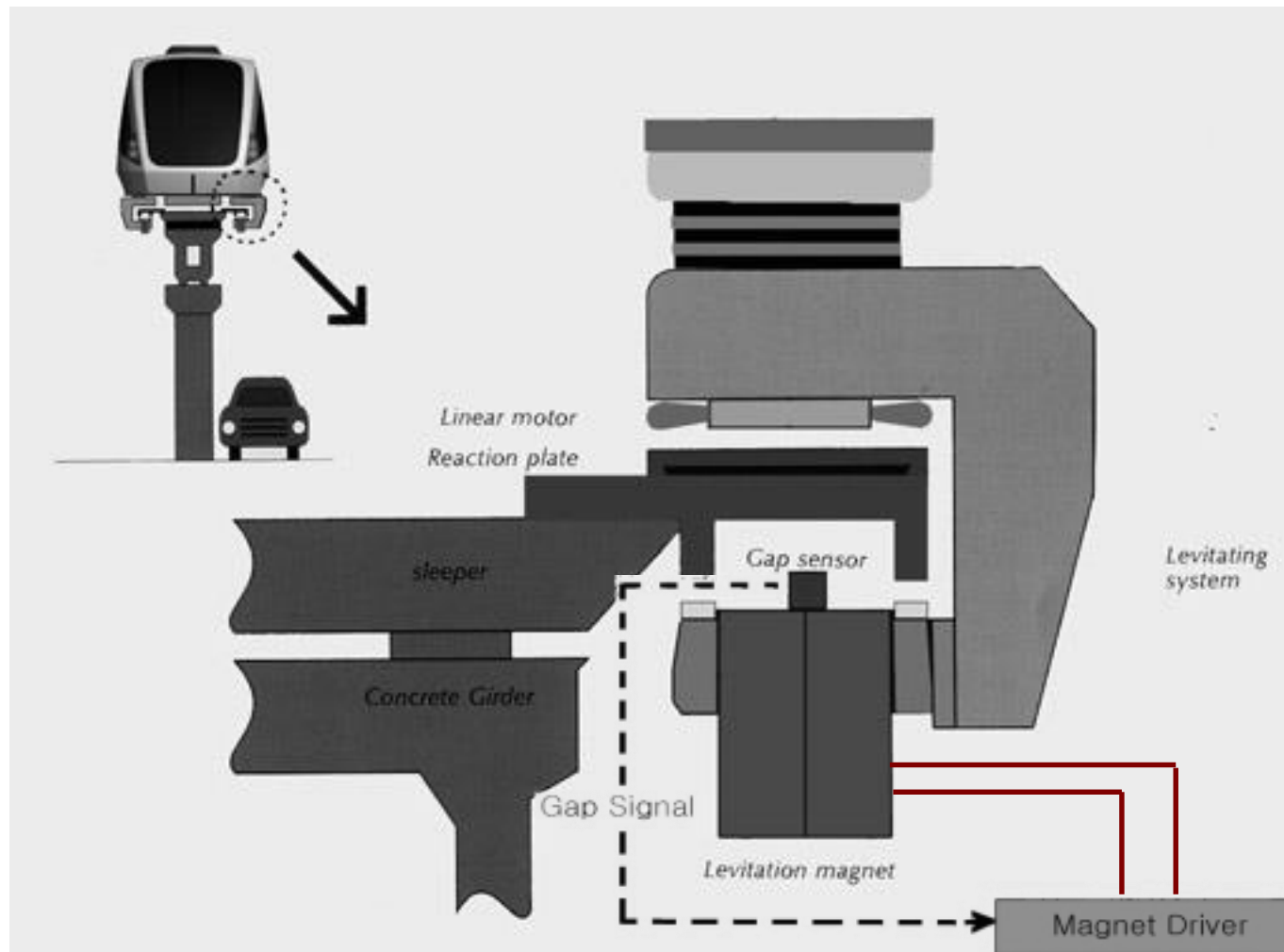
So, $\frac{1}{2} \left(\frac{B^2}{\mu_0} \right) A dg = F dg$

Which gives : $F = \frac{1}{2} \left(\frac{B^2}{\mu_0} \right) A$

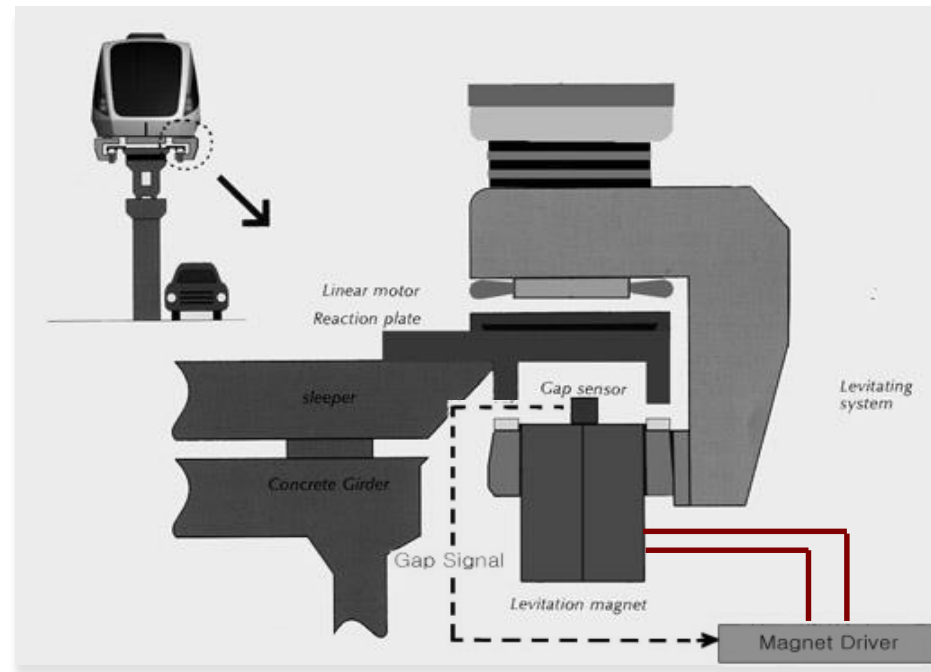
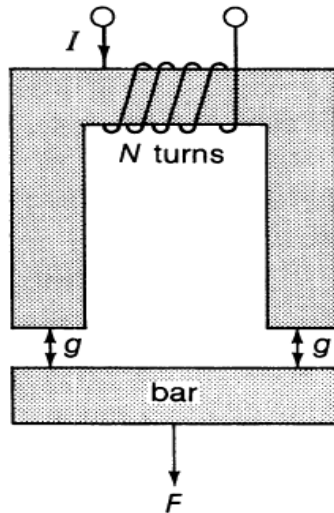
Total force on the bar : $F_{\text{total}} = 2 \left(\frac{1}{2} \right) \left(\frac{B^2}{\mu_0} \right) A = \left(\frac{B^2}{\mu_0} \right) A$

<Ex 3.7.1> Iron ring : $L=10$ m, $A=20\text{cm}^2$, $N=100$, $B=0.8\text{T}$ $\rightarrow W=0.102$ J

• 자기 부상 열차



• Magnetic Force :



$$dW_m = \frac{1}{2} (\mathbf{B} \cdot \mathbf{H}) dv = \frac{1}{2} BH dv = \frac{1}{2} BHA dg = \frac{1}{2} \left(\frac{B^2}{\mu_0} \right) A dg$$

$$dW = \mathbf{F} \cdot d\mathbf{l} = F dg$$

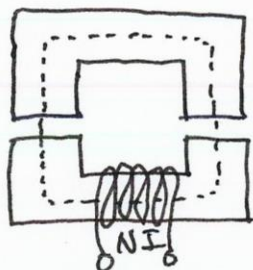
$$\frac{1}{2} \left(\frac{B^2}{\mu_0} \right) A dg = F dg$$

$$F = \frac{1}{2} \left(\frac{B^2}{\mu_0} \right) A$$

Total force on the bar : $F_{\text{total}} = 2 \left(\frac{1}{2} \right) \left(\frac{B^2}{\mu_0} \right) A = \left(\frac{B^2}{\mu_0} \right) A$

<Ex 3.7.1> Iron ring : L=10 m, A=20cm², N=100, B=0.8T → W=0.102 J

@ 자기 부상열차의 부상력 (Lifting Force)



$$\int \vec{H} \cdot d\vec{l} = NI$$

$$H_c l_c + H_g l_g = NI$$

$$NI = \frac{B_c}{\mu_c} \cdot l_c + \frac{B_g}{\mu_0} \cdot l_g \approx B_g \left(\frac{l_c}{\mu_c} + \frac{l_g}{\mu_0} \right) \quad (\because B_g \approx B_c)$$

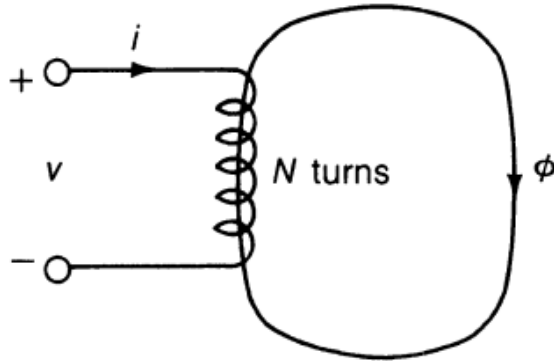
$$\therefore B_g = \frac{NI}{\frac{l_c}{\mu_r \mu_0} + \frac{l_g}{\mu_0}} = \frac{\mu_r \mu_0 \cdot NI}{l_c + \mu_r \cdot l_g}$$

$$\text{Force } F = \int \frac{B^2}{2\mu_0} \cdot dS \approx \frac{B_g^2}{2\mu_0} \cdot S$$

$$= \frac{S}{2\mu_0} \cdot \left(\frac{\mu_r \mu_0 \cdot NI}{l_c + \mu_r \cdot l_g} \right)^2 = \frac{\mu_0 S}{2} \cdot \left(\frac{\mu_r \cdot NI}{l_c + \mu_r l_g} \right)^2$$

3.8 AC excitation & L

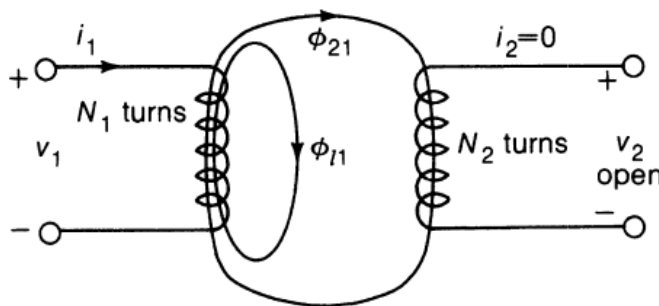
- $I \rightarrow \Phi \rightarrow$ self Induction L :



$$L = \frac{\lambda}{i} = \frac{N\phi}{i} = \frac{N^2}{\mathbf{R}} = N^2\mathbf{P}$$

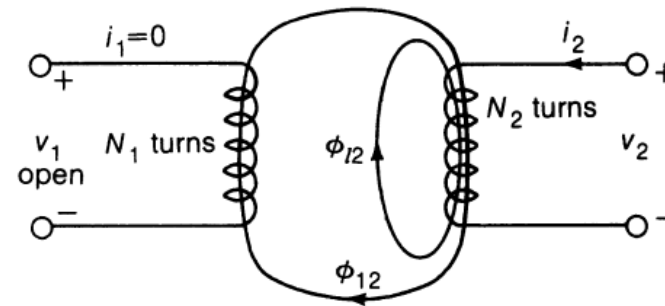
$$W_m = \frac{1}{2}i\lambda = \frac{Li^2}{2}$$

- $I \rightarrow \Phi \rightarrow$ mutual Induction M :



$$L_{11} = \frac{\lambda_{11}}{i_1}$$

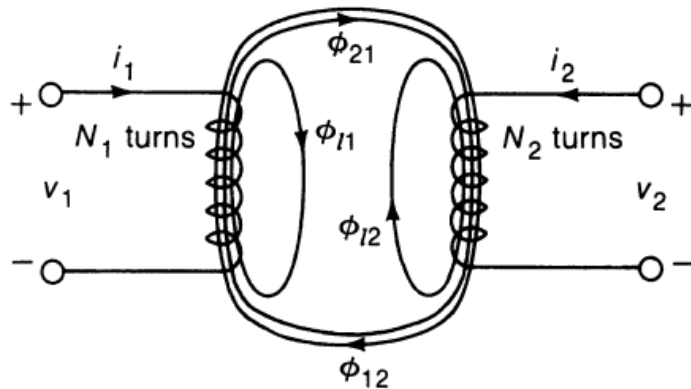
$$L_{21} = \frac{\lambda_{21}}{i_1}$$



$$L_{12} = \frac{\lambda_{12}}{i_2}$$

$$L_{22} = \frac{\lambda_{22}}{i_2}$$

$$\bullet \quad I \rightarrow \Phi \rightarrow L/M \rightarrow v :$$



$$\bullet \quad \text{Leakage flux : } \phi_{l1} = \phi_{11} - \phi_{21}$$

$$\phi_{l2} = \phi_{22} - \phi_{12}$$

$$\bullet \quad \text{결합계수 : } k = \sqrt{k_1 k_2}, \quad k_1 = \phi_{21} / \phi_{11} \\ (0 \sim 1) \quad k_2 = \phi_{12} / \phi_{22}$$

$$\bullet \quad \text{mutual Induction M :}$$

$$M = L_{12} = L_{21} = k \sqrt{L_{11} L_{22}}$$

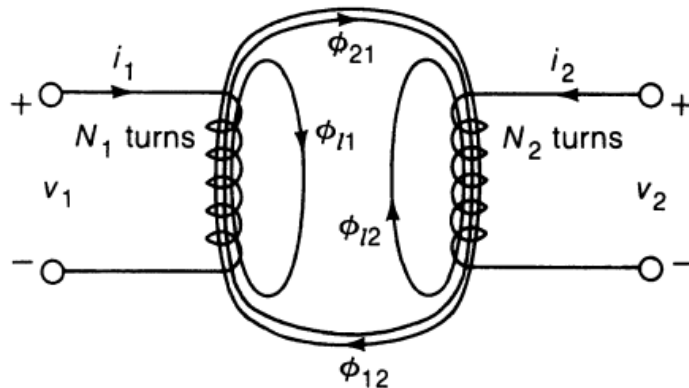
$$\bullet \quad \text{Energy , Inductance :}$$

$$W_m = \frac{i_1 \lambda_1}{2} + \frac{i_2 \lambda_2}{2}$$

$$W_m = \frac{1}{2} L_{11} i_1^2 + M i_1 i_2 + \frac{1}{2} L_{22} i_2^2$$

$$\bullet \quad \text{If non-linear : } \lambda_1 = f_1(i_1, i_2) \\ \lambda_2 = f_2(i_1, i_2)$$

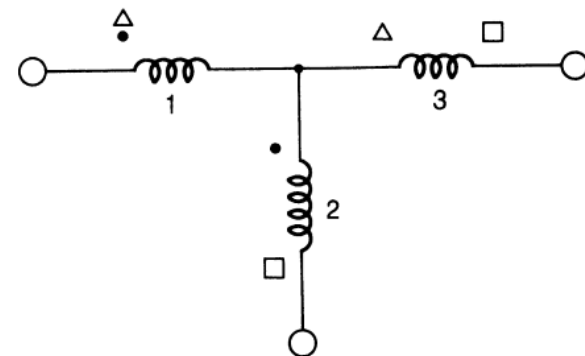
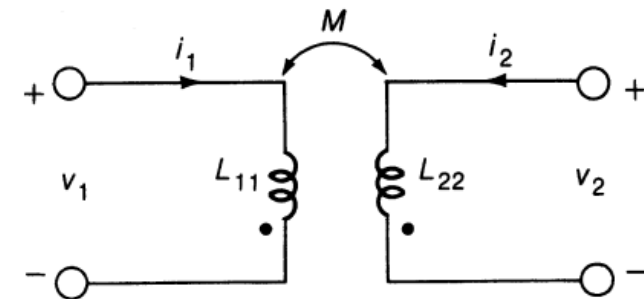
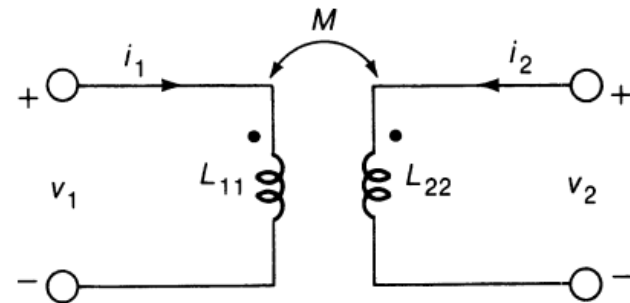
$$\bullet \quad \text{If multi : } W_m = \sum_{j=1}^n \sum_{k=1}^n \frac{1}{2} L_{jk} i_j i_k$$



$$v_1 = \frac{d\lambda_1}{dt} = L_{11} \frac{di_1}{dt} + M \frac{di_2}{dt}$$

$$v_2 = \frac{d\lambda_2}{dt} = M \frac{di_1}{dt} + L_{22} \frac{di_2}{dt}$$

$$W_m = \frac{1}{2} L_{11} i_1^2 + M i_1 i_2 + \frac{1}{2} L_{22} i_2^2$$



• Equivalent circuit :

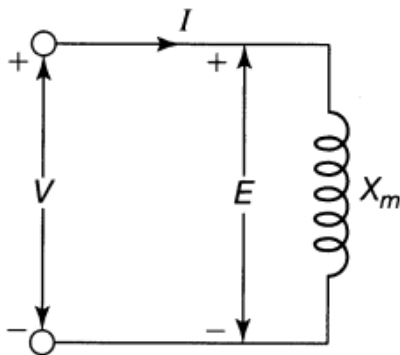
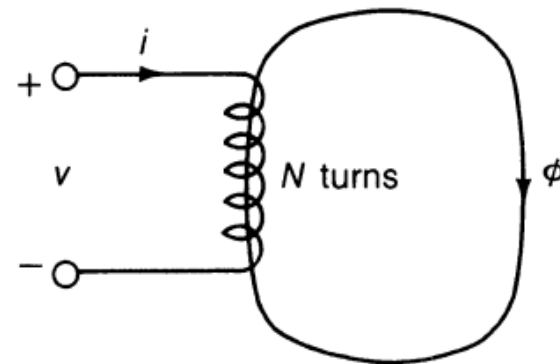
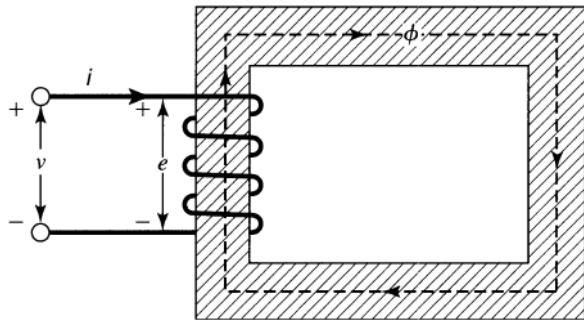


그림 3.8.5 • AC 여자 코일의 등가회로.

$$X_m = \frac{E}{I} = \omega L_m$$

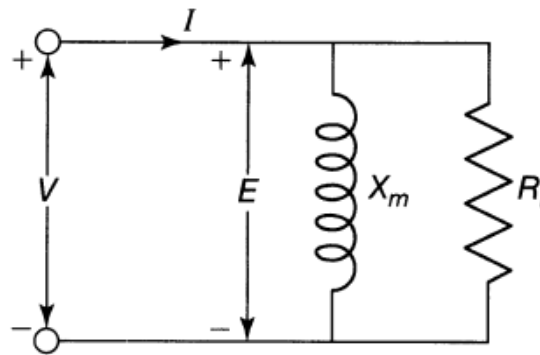


그림 3.8.6 • 철손이 있는 AC 여자 코일의 등가회로.

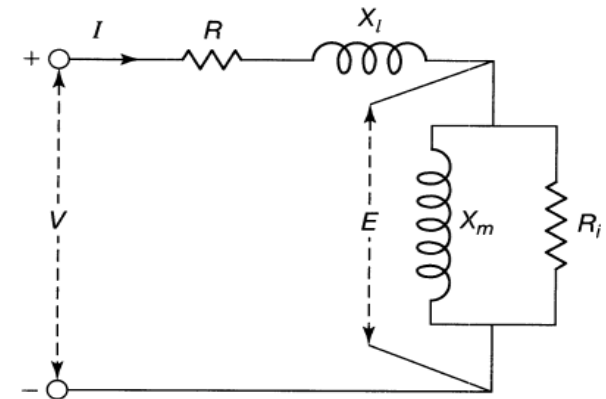
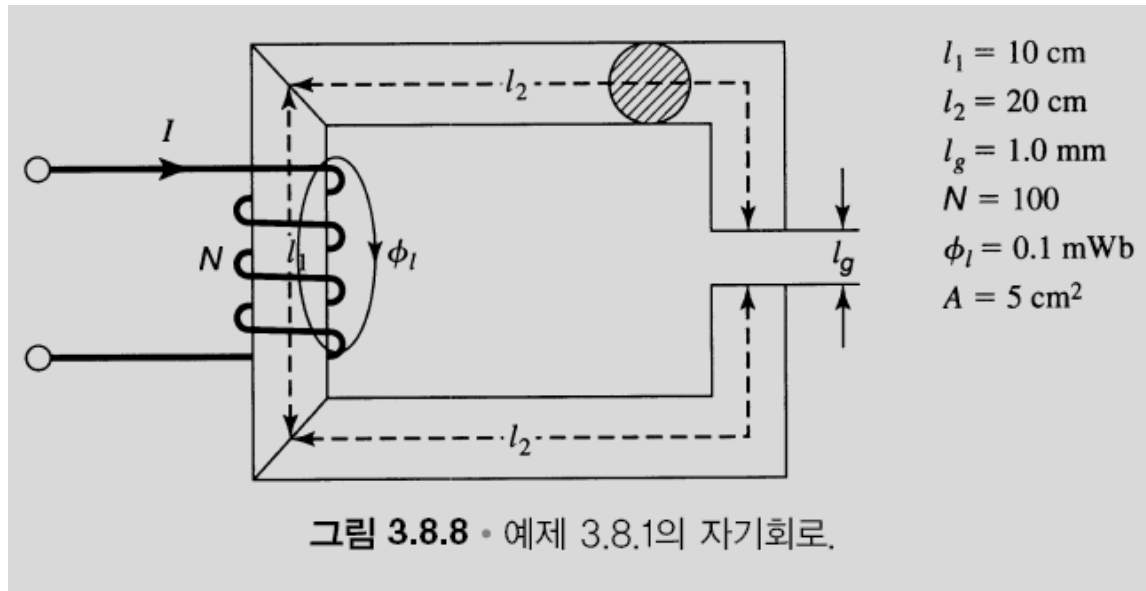


그림 3.8.7 • AC 여자 코일의 전체 등가회로.

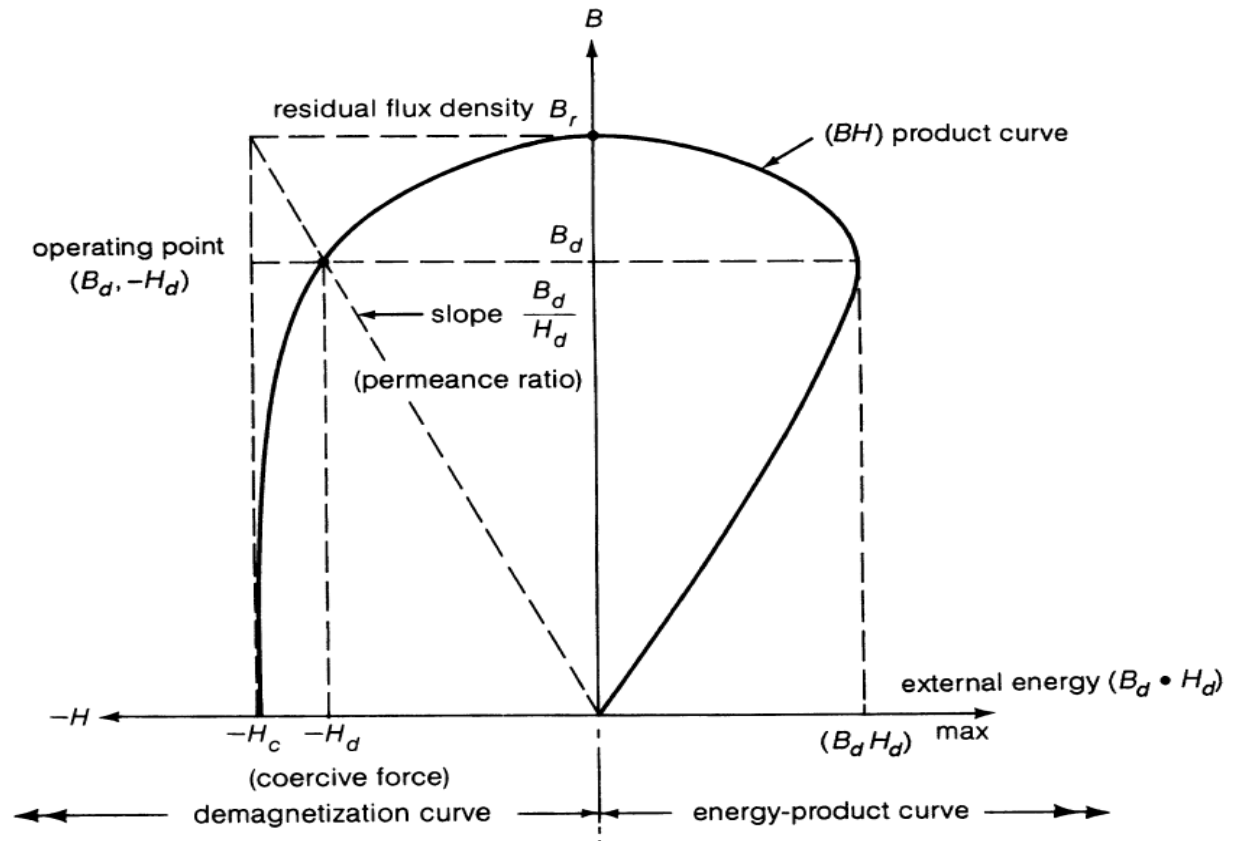
- R
- X_l
- X_m
- R_i

<Ex 3.8.1> Cast Steel, B-H curve, $B=1.1\text{T} \rightarrow I, L_s, LI$

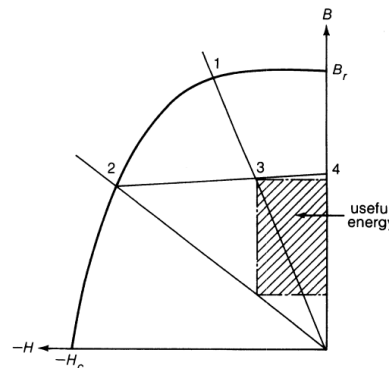


3.9 영구자석 응용

- Permanent Magnet : Iron base magnet, Ferrite, AlNiCo, Rare Earth Magnet(NdFeB, SmCo)
- Magnetizing, Demagnetizing
- Hysteresis Characteristics, Energy Product

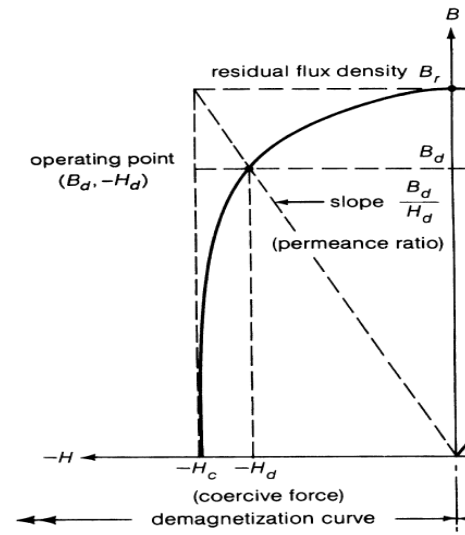
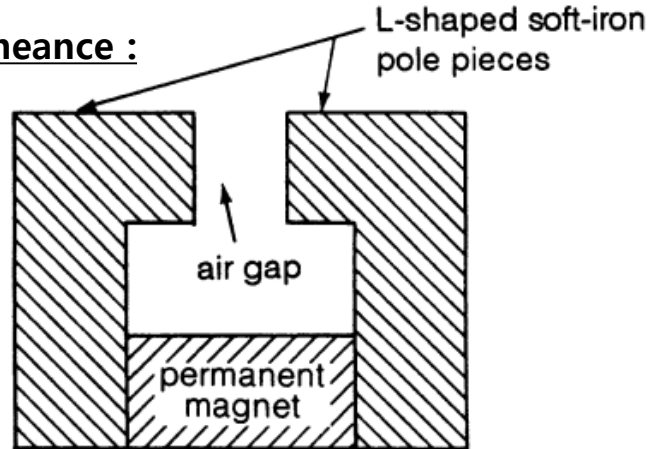


- Magnetizing , Demagnetizing
- Permeance , Load line, B_g
- Major loop , Minor loop ,
- Recoil line , Recoil Permeability



Material (Trade name)		Residual Flux Density B_r (T)	Coercive Force H_c (kA/m)	Maximum Energy product (kJ/m ³)	Average Recoil Permeability (H/m $\times 10^{-6}$)
Cast alnico	5	1.28	51	44	2.1
	5-7	1.34	58	60	1.9
	6	1.05	62	31	5.0
Sintered alnico	5	1.09	49	31	2.0
	6	0.94	64	23	5.0
Cunife		0.55	42	11	1.7
Indox	1	0.22	145	8	1.15
	2	0.29	193	14	1.15
	3	0.335	187	21	1.1
	4	0.255	183	12	1.1
Rare-earth-cobalt	18	0.87	637	143	1.05
Incor	16	0.81	629	127	1.05
36% Cobalt steel		1.04	18	8	10

- How many B ?
- Magnetic Permeance :



$$N \cdot I = H \cdot L = R_m \cdot \Phi$$

$$\sum HL = 0$$

$$(B_d, -H_d)$$

$$H_m = -H_d$$

$$H_d l_m = H_g l_g$$

- f : 철심의 자기저항 보정계수 (1.1~1.5)

$$H_d l_m = f H_g l_g = f B_g l_g / \mu_0$$

$$l_m = \frac{f B_g l_g}{\mu_0 H_d}$$

- F : 누설계수 (1.2~60)

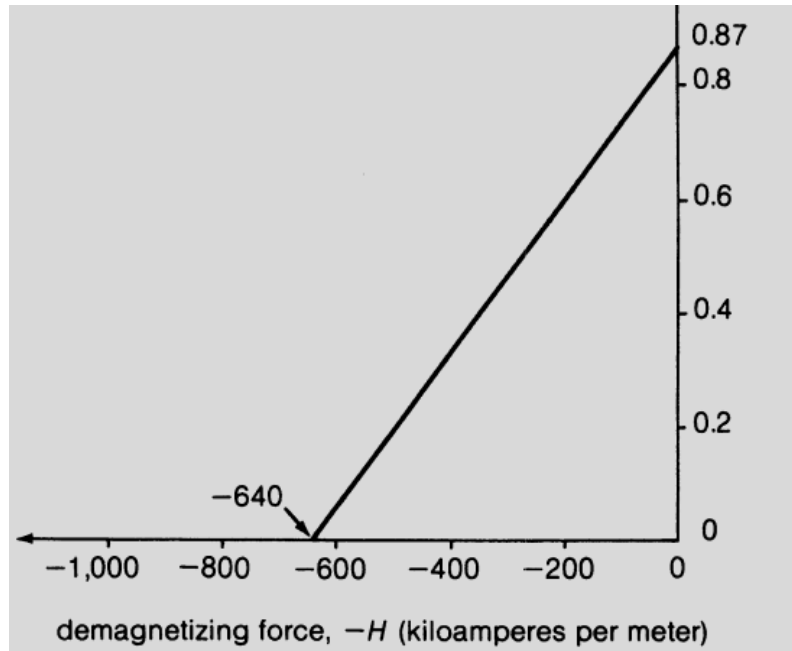
$$\Phi = B_d A_m = F B_g A_g$$

$$A_m = \frac{F B_g A_g}{B_d}$$

$$V_m = A_m l_m = \frac{f F B_g^2 V_g}{\mu_0 B_d H_d}$$

$$P_c = \frac{B_d}{H_d} = \frac{F}{f} \cdot \frac{l_m}{A_m} \cdot \frac{A_g}{l_g} \cdot \mu_0$$

<Ex 3.9.1> 영구자석 크기결정 : $B=0.5T \rightarrow A_m=?$, $L_m=?$



<Ex 3.9.2> 영구자석 크기결정 : 도넛모양의 AlNiCo, for $BH_{max} \rightarrow L_g=?$

<Problems>

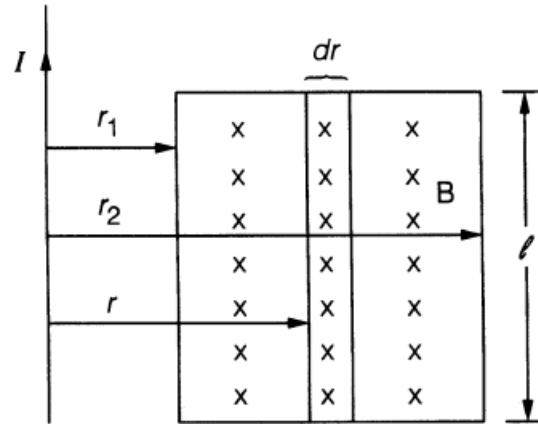


그림 P3-4

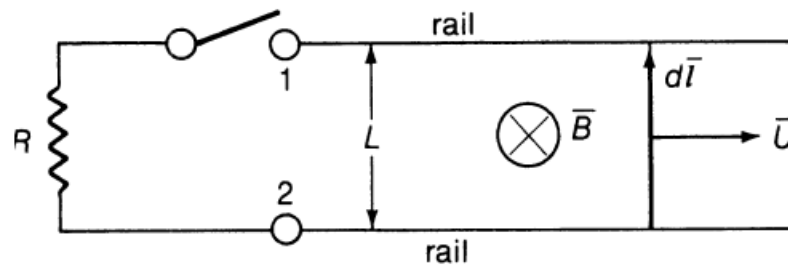


그림 P3-5

<Problems>

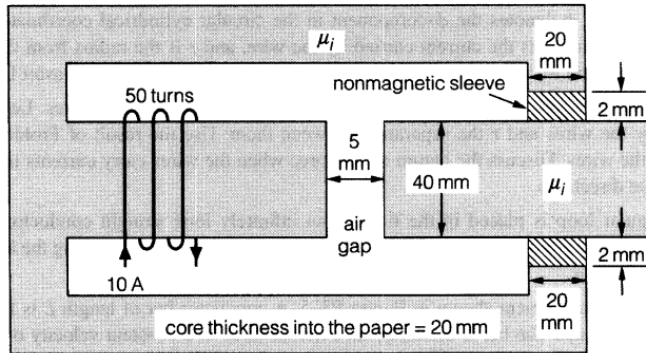


그림 P3-7

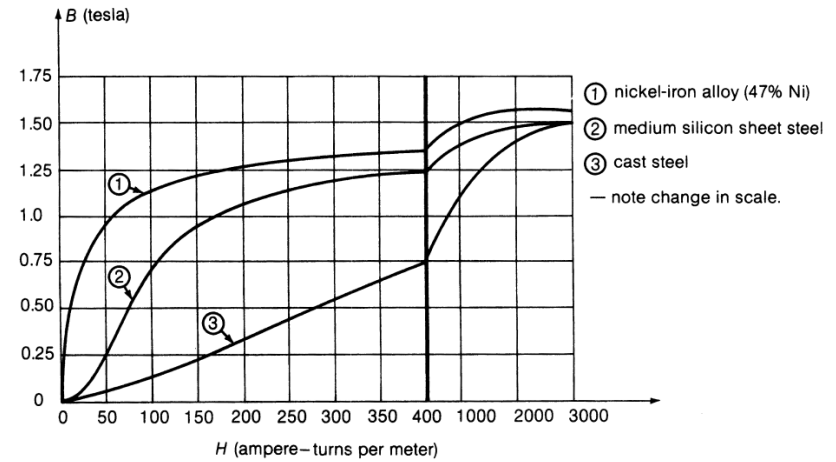
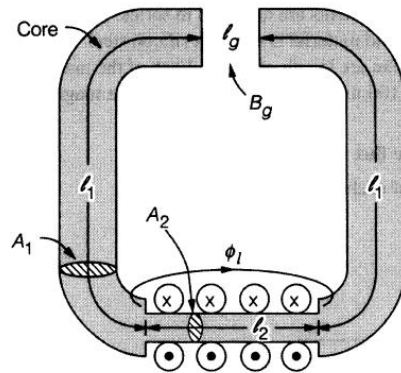
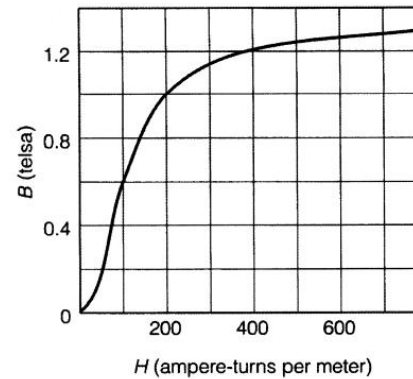


그림 P3-8



(a)



(b)

그림 P3-10

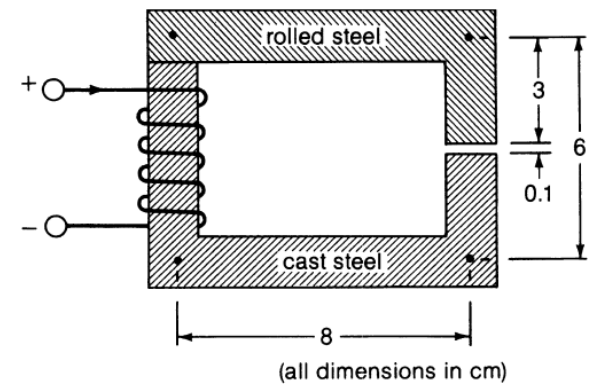


그림 P3-11

<Problems>

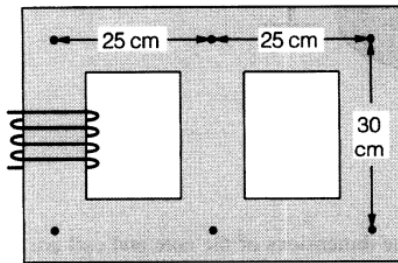


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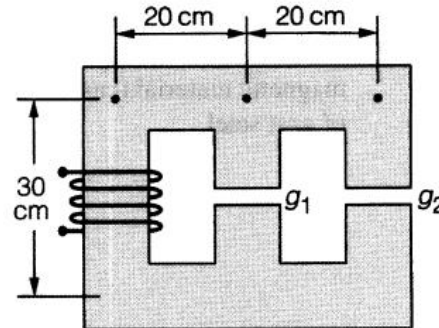


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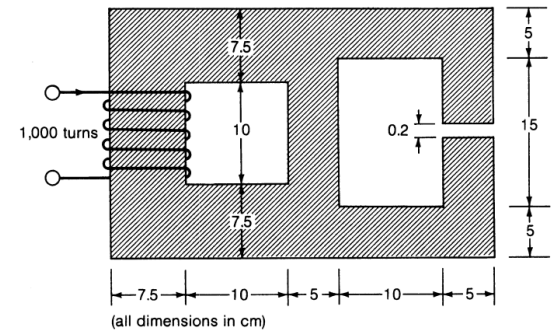


그림 P3-13

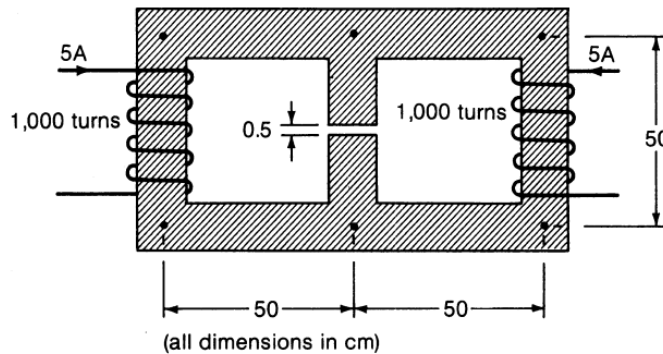


그림 P3-12

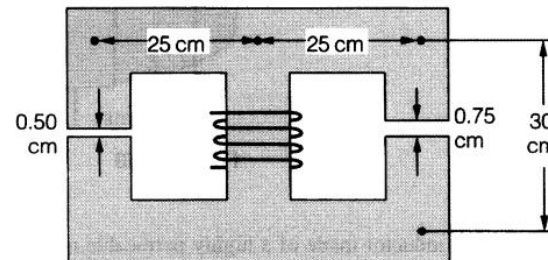


그림 P3-15

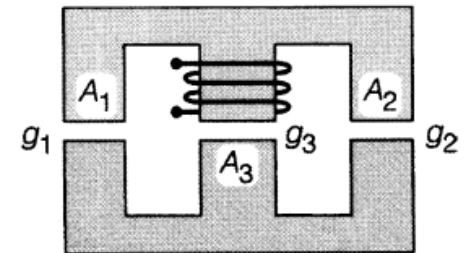


그림 P3-17

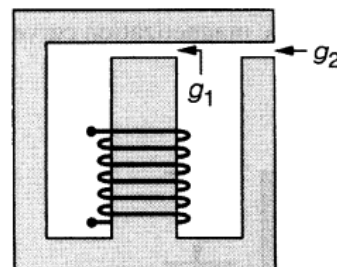


그림 P3-16

<Problems>

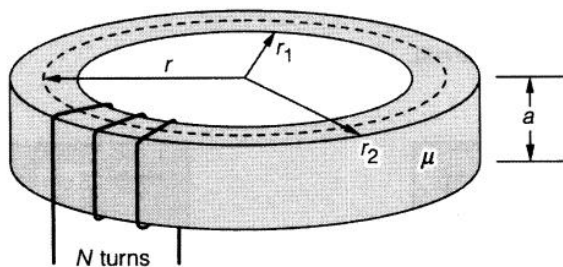


그림 P3-19

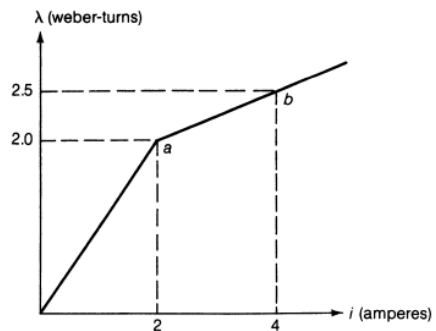


그림 P3-23

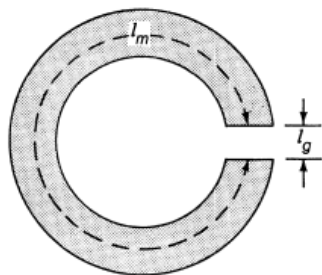
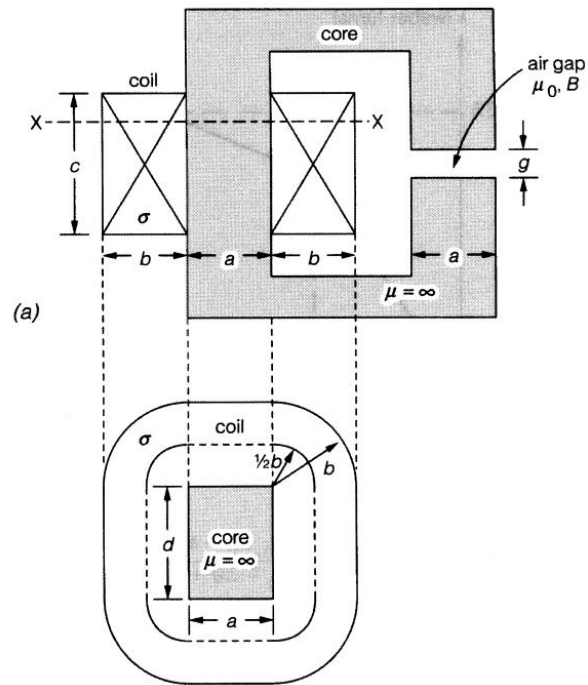


그림 P3-32



(b) Cross section at XX

그림 P3-20

<Problems>

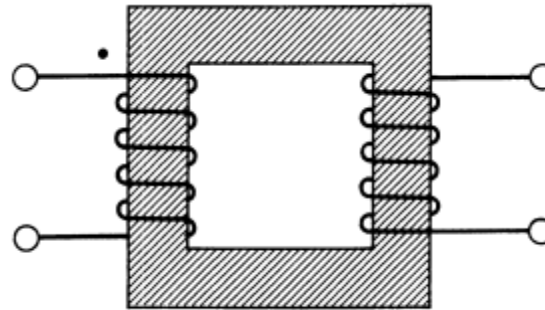


그림 P3-27

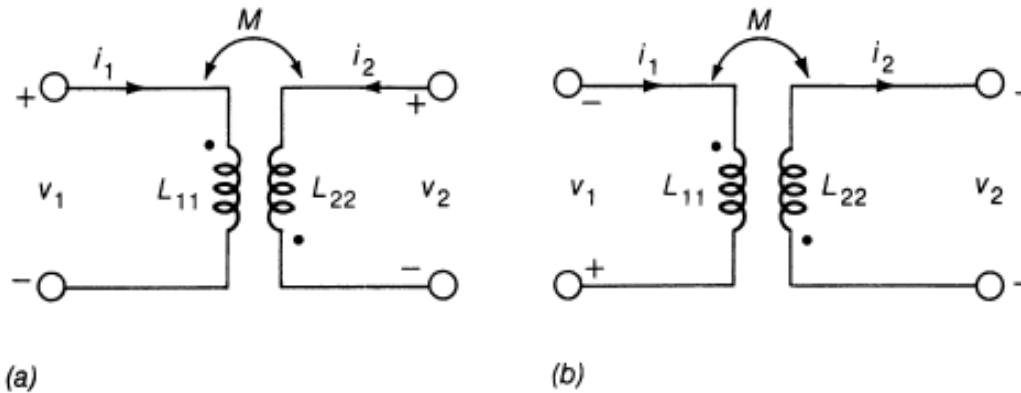


그림 P3-28