

EDIPack2: interoperable Lanczos-based exact diagonalization solver for generic quantum impurity problems.

Abstract

Keywords: Exact diagonalization, Quantum Impurity models, Strongly correlated electrons, Dynamical Mean-Field Theory

PROGRAM SUMMARY

Program Title: EDIPack2

Licensing provisions: GPLv3

Programming language: Fortran, Python

Classification: 6.5, 7.4, 20

Required dependencies: CMake ($\geq 3.0.0$), Scifortran, MPI

Nature of problem: .

Solution method: .

1. Introduction and Motivation

A few words about the motivations who led us to develop this software, possible applications and advantages:

- * flexibility: can address generic cases including multi-orbital, superconducting or spin-non-conserving regimes

- * zero and low finite temperatures

- * direct access to (well approximated) analytic dynamical functions

- * direct access to impurity Fock space quantities

bla bla bla

2. Structure and derived software

EDIPack2 is a modular library which contains three principal structures. At the core is the exact diagonalization solver: EDIPack2 . Next there is a `EDIPack2ineq` which extends application to the case of multiple inequivalent impurity problems. Finally, there we provide a Fortran-C interface, which enables development of additional API or inter-operability with external libraries.

- **EDIPack2.** This constitutes the building block of the whole software. This part implement the with the Lanczos-based solver for generic quantum impurity systems encoding different symmetries, i.e. quantum number conservations and apt to solve multi-orbital problems, also in presence of coupling to local phonons. The EDIPack2 solver has a hierarchical and modular structure: different sections of the library communicate through a shared memory layer. The top module of the library is `EDIPACK2` which, once loaded, enables access to the Fortran API in terms of suitable procedures to initialize, execute and finalize the solver or to retrieve internal quantities while making opaque to the user the internal structure of the library. A detailed presentation of the library can be found in Sec.4.

- **EDIPack2ineq.** This part of the software, leveraging on the object oriented concepts available in modern Fortran, aims to extend the EDIPack2 library to the case of multiple inequivalent and independent impurity problems. This is particularly useful while using EDIPack2 as a solver for DMFT in presence of unit cells with inequivalent atoms, for systems with somehow broken translational symmetry (e.g. heterostructures, large supercells, etc.).
- **EDIPack2 C-bindings.** EDIPack2 includes a single module implementing a Fortran-C interface of the main library procedures. The module is developed around the implicit `ISO_C_BINDING` capabilities of the most recent Fortran distributions, which enable to translate Fortran procedures directly to C. In order to overcome all the difficulties related to the internal structure of the library, we interfaced all and just the procedures and the variables exposed to the user. This module aims to foster interoperability of EDIPack2 with different third party softwares as well as to support development of additional API.
- **EDIPy2.** This is a simple Python module which provides Python API to the EDIPack2 Fortran library. This interface is built around the Python support to C-types, which allows to import the dynamic C-binding library generated upon building EDIPack2. The module contains a specific class, whose methods mirrors through duck-typing all the available procedures of EDIPack2 as well as it gives access to relevant shared control variables.
- **EDIPack2Triqs.** This is a thin interface layer from EDIPack2 to Triqs, built around the Python API of the EDIPack2 library. The exact diagonalization solver is encapsulated in a dedicated class, containing the necessary methods to initialize and run a single instance of the solver. The interface also includes a specific class encompassing the effective discretized bath structure as well as their optimization methods.

3. Installation

The installation of EDIPack2 is available through CMake which ensures multi-platforms compability and dependencies resolution. The software builds into two distinct libraries: `libedipack.a` and `libedipack_cbinding.so`. The former, alongside the generated Fortran modules files, wraps the EDIPack2 software. The latter enables interoperability through bindings to the C language.

3.1. Dependencies

Although EDIPack2 is as much self-contained as possible its development hinges on two external libraries.

- **SciFortran:** an open-source Fortran library to support mathematical and scientific software development.
- **MPI (optional):** a distributed memory parallel communication layer with support to modern Fortran compiler.

SciFortran provides a solid development platform enabling access to many algorithms and functions, including standard linear algebra operations and high-performance Lanczos based algorithms. This greatly reduces code clutter and development time. The use of distributed memory parallel environment, although optional, is required to access scalable parallel diagonalization algorithms which speed up calculations for large dimensional systems.

3.2. Build and Install

3.2.1. Source

The software can be installed from source as follows. The source can be retrieved directly from its GitHub repository, for instance using:

```
git clone https://github.com/edipack/EDIPack2.0 EDIPack2
```

Then, assuming to be in the software directory, a conventional out-of-source building is performed using two different compilations backends.

- **GNU Make**

This is the default CMake workflow:

```
mkdir build
cd build
cmake ..
make -j
make install
```

- **Ninja**

An alternative workflow employs the Ninja building backend with Fortran support. Ninja is generally faster and automatically supports multi-threaded building:

```
mkdir build
cd build
cmake -GNinja ..
ninja
ninja install
```

The CMake configurations can be further tuned using the following variables:

Option	Scope	Value
-DPREFIX	Install directory	~/opt/EDIPack2/TAG/PLAT/BRANCH
-DUSE_MPI	MPI support	True/ False
-DWITH_INEQ	Inequivalent impurities support	True /False
-DVERBOSE	Verbose CMake output	True /False
-DBUILD_TYPE	Compilation flags	RELEASE /TESTING/DEBUG/AGGRESSIVE

The default target builds and install either the main library and the C-binding. However, a specific building for each library is available specifying the required target. A recap message is printed at the end of the CMake configuration step.

3.2.2. Anaconda

As an alternative we provide for both Linux and OSX systems installation through Anaconda packages into a virtual environment containing Python (> 3.10).

The Conda package installation procedure reads:

```
conda create -n edipack
conda activate edipack
conda install -c conda-forge -c edipack edipack2
```

which installs a bundle of Scifor and EDIPack2 libraries together with specific **pkg-config** configurations files which can be used to retrieve compilation and linking flags.

3.3. OS Loading

In order to avoid possible conflicts or require administrative privileges, the building step results get installed by default in a user home directory, specified by the CMake variable `PREFIX`. In doing so, however, one misses the chance of automatic loading into the operative system.

We offer different strategies to perform this action:

1. A CMake generated configuration file for environment module which allows to load and unload the library at any time. This is preferred solution for HPC systems.
2. A CMake generated bash script to be sourced (once or permanently) in any shell session to add EDIpack2 library to the default environment.
3. A CMake generated pkg-config configuration file to be added in the pkg-config path itself.

An automatically generated recap message with all instructions is generated at the end of the installation procedure.

3.4. Python API

3.4.1. Build from source

EDIpy2, i.e. the Python API of EDIpack2, is available as a stand-alone module which depends on both EDIpack2 and SciFortran. The package can be obtained from the repository [EDIpy2](https://github.com/edipack/EDIpy2).

```
git clone https://github.com/edipack/EDIpy2 EDIpy2
cd EDIpy2
pip install .
```

In some more recent Python distribution the flag `--break-system-packages` might be required to complete installation or a virtual environment should be used instead.

3.4.2. Anaconda

As for EDIpack2, also the Python API in EDIpy2 are available through Anaconda packaging. In this case the resolution of the dependencies is taken care from Conda itself:

```
conda create -n edipack
conda activate edipack
conda install -c conda-forge -c edipack edipack2
```

3.5. TRIQS interface

A purely Python EDIpack2 to Triqs interface is available, leveraging on the C-bindings and Python API. The corresponding module depends on EDIpack2 (which ultimately depends on SciFortran) and Triqs. Assuming the two software are correctly installed in the OS, the EDIpack2Triqs interface is installed as follows:

```
git clone https://github.com/krivenko/edipack2triqs
cd edipack2triqs
pip install .
```

4. Implementation

Here we present an overview of the implementation of the different parts of the EDIpack2 library.

- 4.1. The quantum impurity problem*
- 4.2. The basis states*
- 4.3. Conserved quantum numbers*
- 4.4. Krylov based Diagonalization*
- 4.5. Dynamical correlation functions*
- 4.6. Observables*
- 4.7. Reduced impurity density matrix*
- 4.8. Bath parametrization*
- 4.9. Bath Optimization*
- 4.10. Input/Output*

5. Inequivalent impurities

6. C-bindings

7. Python API

8. Triqs interface

9. Usage

- 9.1. Bethe lattice DMFT (Fortran API)*
- 9.2. Attractive Hubbard model (Python API)*
- 9.3. Multi-orbital Hubbard (Triqs)*

10. Conclusions

Acknowledgements

References