Applied Machine Learning - Feature Engineering and Preprocessing

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Load Packages



```
library(tidymodels)
                                                        tidymodels 0.0.2 —
## — Attaching packages
## ✓ broom
                               ✓ purrr
               0.5.0.9001
                                           0.2.5.9000
## ✓ dials
               0.0.2

✓ recipes 0.1.4.9000

## ✓ dplyr
               0.8.0.9000
                               ✓ rsample 0.0.3
## ✓ infer
               0.4.0

✓ tibble

                                           1.4.99.9006
                               ✓ yardstick 0.0.2
## ✓ parsnip 0.0.1
## — Conflicts -
                                                  tidymodels_conflicts() —
## * purrr::discard()
                            masks scales::discard()
## * rsample::fill()
                            masks tidyr::fill()
## * dplyr::filter()
                            masks stats::filter()
## * dplyr::group_rows()
                            masks kableExtra::group_rows()
## * dplyr::lag()
                            masks stats::lag()
## * purrr::lift()
                            masks caret::lift()
## * yardstick::precision() masks caret::precision()
## * yardstick::recall()
                            masks caret::recall()
## * recipes::step()
                            masks stats::step()
```

Load Ames Housing Data

```
# Previously...
library(AmesHousing)
ames <- make_ames() %>%
  dplyr::select(-matches("Qu"))

set.seed(4595)
data_split <- initial_split(ames, strata = "Sale_Price")

ames_train <- training(data_split)
ames_test <- testing(data_split)
set.seed(2453)
cv_splits <- vfold_cv(ames_train, v = 10, strata = "Sale_Price")</pre>
```

Preprocessing and Feature Engineering

This part mostly concerns what we can do to our variables to make the models more effective.

This is mostly related to the predictors. Operations that we might use are:

- transformations of individual predictors or groups of variables
- alternate encodings of a variable
- elimination of predictors (unsupervised)

In statistics, this is generally called *preprocessing* the data. As usual, the computer science side of modeling has a much flashier name: *feature engineering*.

Reasons for Modifying the Data

- Some models (*K*-NN, SVMs, PLS, neural networks) require that the predictor variables have the same units. **Centering** and **scaling** the predictors can be used for this purpose.
- Other models are very sensitive to correlations between the predictors and filters or PCA signal extraction can improve the model.
- As we'll see in an example, changing the scale of the predictors using a **transformation** can lead to a big improvement.
- In other cases, the data can be **encoded** in a way that maximizes its effect on the model.

 Representing the date as the day of the week can be very effective for modeling public transportation data.
- Many models cannot cope with missing data so **imputation** strategies might be necessary.
- Development of new *features* that represent something important to the outcome (e.g. compute distances to public transportation, university buildings, public schools, etc.)

Preprocessing Categorical Predictors

Dummy Variables

One common procedure for modeling is to create numeric representations of categorical data. This is usually done via *dummy variables*: a set of binary 0/1 variables for different levels of an R factor.

For example, the Ames housing data contains a predictor called Alley with levels: 'Gravel', 'No_Alley_Access', 'Paved'.

Most dummy variable procedures would make *two* numeric variables from this predictor that are 1 when the observation has that level, and 0 otherwise.

Data	Dummy Variables	
	No_Alley_Access	Paved
Gravel	0	0
No_Alley_Access	1	0
Paved	0	1

Dummy Variables

If there are C levels of the factor, only C-1 dummy variables are created since the last can be inferred from the others. There are different contrast schemes for creating the new variables.

For ordered factors, polynomial contrasts are used. See this blog post for more details.

How do you create them in R?

The formula method does this for you¹. Otherwise, the traditional method is to use model.matrix() to create a matrix. However, there are some caveats to this that can make things difficult.

We'll show another method for making them shortly.

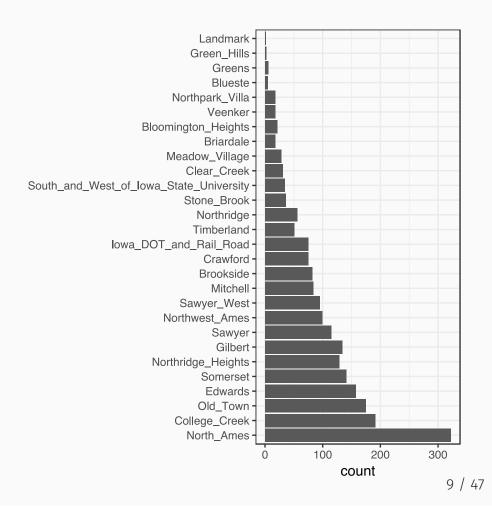
[1] Almost always at least. Tree- and rule-based model functions do not. Examples are randomforest::randomForest, ranger::ranger, rpart::rpart, C50::C5.0, Cubist::cubist, klaR::NaiveBayes and others.

Infrequent Levels in Categorical Factors

One issue is: what happens when there are very few values of a level?

Consider the Ames training set and the Neighborhood variable.

If these data are resampled, what would happen to Landmark and similar locations when dummy variables are created?



Infrequent Levels in Categorical Factors

A zero-variance predictor that has only a single value (zero) would be the result.

Many models (e.g. linear/logistic regression, etc.) would find this numerically problematic and issue a warning and NA values for that coefficient. Trees and similar models would not notice.

There are two main approaches to dealing with this:

- Run a filter on the training set predictors prior to running the model and remove the zero-variance predictors.
- Recode the factor so that infrequently occurring predictors (and possibly new values) are pooled into an "other" category.

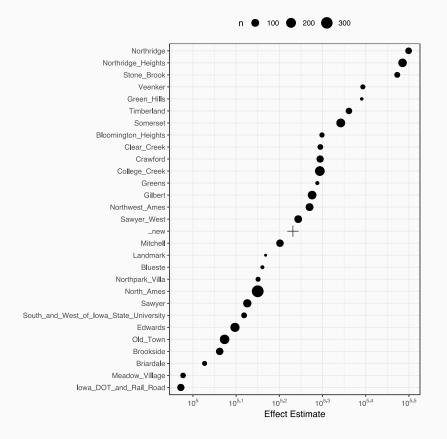
However, model.matrix() and the formula method are incapable of doing either of these.

Other Approaches

A few other approaches that might help here:

- effect or likelihood encodings of categorical predictors estimate the mean effect of the outcome for every factor level in the predictor. These estimates are used in place of the factor levels. Shrinkage/regularization can improve these approaches.
- entity embeddings use a neural network to create features that capture the relationships between the categories and the outcome.

An add-on to recipes called embed can be used for these encodings.



Recipes



Recipes are an alternative method for creating the data frame of predictors for a model.

They allow for a sequence of *steps* that define how data should be handled.

Recall the previous part where we used the formula log10(Sale_Price) ~ Longitude + Latitude? These steps are:

- Assign Sale_Price to be the outcome
- Assign Longitude and Latitude as predictors
- Log transform the outcome

To start using a recipe, these steps can be done using

```
mod_rec <- recipe(Sale_Price ~ Longitude + Latitude, data = ames_train) %>%
  step_log(Sale_Price, base = 10)
```

This creates the recipe for data processing (but does not execute it yet)

Recipes and Categorical Predictors



To deal with the dummy variable issue, we can expand the recipe with more steps:

```
mod_rec <- recipe(
    Sale_Price ~ Longitude + Latitude + Neighborhood,
    data = ames_train
) %>%
    step_log(Sale_Price, base = 10) %>%

# Lump factor levels that occur in
# <= 5% of data as "other"
    step_other(Neighborhood, threshold = 0.05) %>%

# Create dummy variables for _any_ factor variables
    step_dummy(all_nominal())
```

```
mod_rec

## Data Recipe
##

## Inputs:
##

## role #variables
## outcome    1
## predictor    3
##

## Operations:
##

## Log transformation on Sale_Price
## Collapsing factor levels for Neighborhood
## Dummy variables from all_nominal()
```

Note that we can use standard dplyr selectors as well as some new ones based on the data type (all_nominal()) or by their role in the analysis (all_predictors()).

Using Recipes



```
recipe --> prepare --> bake/juice

(define) --> (estimate) --> (apply)
```

Preparing the Recipe



Now that we have a preprocessing specification, let's run it on the training set to prepare the recipe:

```
mod_rec_trained <- prep(mod_rec, training = ames_train, verbose = TRUE)

## oper 1 step log [training]

## oper 2 step other [training]

## oper 3 step dummy [training]

## The retained training set is ~ 0.19 Mb in memory.</pre>
```

Here, the "training" is to determine which levels to lump together and to enumerate the factor levels of the Neighborhood variable.

An unused option, retain = TRUE, that keeps the processed version of the training set around so we don't have to recompute it.

Preparing the Recipe

mod_rec_trained

Getting the Values



Once the recipe is prepared, it can be applied to any data set using bake():

```
ames_test_dummies <- bake(mod_rec_trained, new_data = ames_test)
names(ames_test_dummies)

## [1] "Sale_Price" "Longitude" "Latitude"

## [4] "Neighborhood_College_Creek" "Neighborhood_Old_Town" "Neighborhood_Edwards"

## [7] "Neighborhood_Somerset" "Neighborhood_Northridge_Heights" "Neighborhood_Gilbert"

## [10] "Neighborhood_Sawyer" "Neighborhood_other"</pre>
```

If retain = TRUE, the training set does not need to be "rebaked". The juice() function can return the processed version of the training data.

Selectors can be used with bake() to only extract relevant columns and the default is everything().

How Data Are Used



Note that we have:

```
recipe(..., data = data_set)
prep(..., training = data_set)
bake(..., new_data = data_set)
```

In the first case, data is used by the recipe function only to determine the column names and types (e.g. factor, numeric, etc). A small subset can be passed via head or slice.

For prep, the training argument should have all of the data used to estimate parameters and other quantities.

For bake, new_data is the data that the pre-processing should be applied to.

Hands-On: Zero-Variance Filter

Instead of using step_other(), take 10 minutes and research how to eliminate any zero-variance predictors using the recipe reference site.

Re-run the recipe with this step.

What were the results?

Do you prefer either of these approaches to the other?

Principal Component Analysis

A Bivariate Example

The plot on the right shows two predictors from a real *test* set where the objective is to predict the two classes.

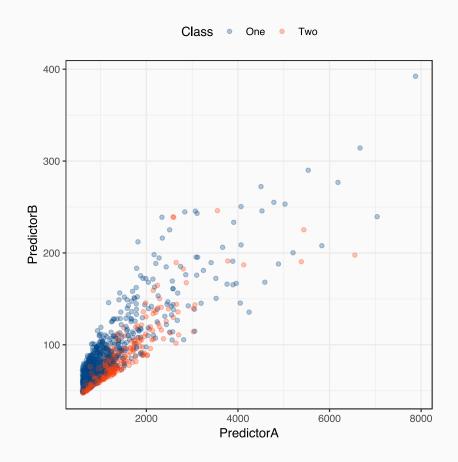
The predictors are strongly correlated and each has a rightskewed distribution.

There appears to be some class separation but only in the bivariate plot; the individual predictors show poor discrimination of the classes.

Some models might be sensitive to highly correlated and/or skewed predictors.

Is there something that we can do to make the predictors easier for the model to use?

Any ideas?



A Bivariate Example

We might start by estimating transformations of the predictors to resolve the skewness.

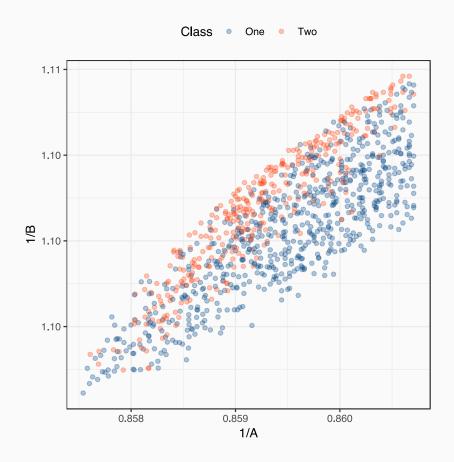
The Box-Cox transformation is a family of transformations originally designed for the outcomes of models. We can use it here for the predictors.

It uses the data to estimate a wide variety of transformations including the inverse, log, sqrt, and polynomial functions.

Using each factor in isolation, both predictors were determined to need inverse transformations (approximately).

The figure on the right shows the data after these transformations have been applied.

A logistic regression model shows a substantial improvement in classifying using the altered data.



More Recipe Steps



The package has a rich set of steps that can be used including transformations, filters, variable creation and removal, dimension reduction procedures, imputation, and others.

For example, in the previous bivariate data problem, the Box-Cox transformation was conducted using:

```
bivariate_rec <- recipe(Class ~ ., data = bivariate_data_train) %>%
    step_BoxCox(all_predictors())

bivariate_rec <- prep(bivariate_rec, training = bivariate_data_train, verbose = FALSE)
inverse_test_data <- bake(bivariate_rec, new_data = bivariate_data_test)</pre>
```

Correlated Predictors

In the Ames data, there are potential clusters of highly correlated variables:

- proxies for size: Lot_Area, Gr_Liv_Area, First_Flr_SF, Bsmt_Unf_SF, Full_Bath etc.
- Quality fields: Overall_Qual, Garage_Qual, Kitchen_Qual, Exter_Qual, etc.

It would be nice if we could combine/amalgamate the variables in these clusters into a single variable that represents them.

Another way of putting this is that we would like to create artificial features of the data that account for a certain amount of variation in the data.

There are a few different methods that can accomplish this; we will focus on principal component analysis (PCA) as a solution. Another, regularization, will be discussed later.

PCA Signal Extraction

Principal component analysis (PCA) is a multivariate statistical technique that can be used to create artificial new variables from an existing set.

The new variables are created to account for the most variation in the data. In this case, "variation" means correlation.

Conceptually, PCA determines which variables account for the most correlation in the data and creates a new variable that is a linear combination of all the predictors.

- This is called the first principal component (aka PC1).
- This linear combination emphasizes the variables that are the most correlated.

The information that PC #1 represents is then removed from the data.

The second PCA component is the linear combination that accounts for the most left-over correlation in the data (and so on).

PCA Signal Extraction

To recap:

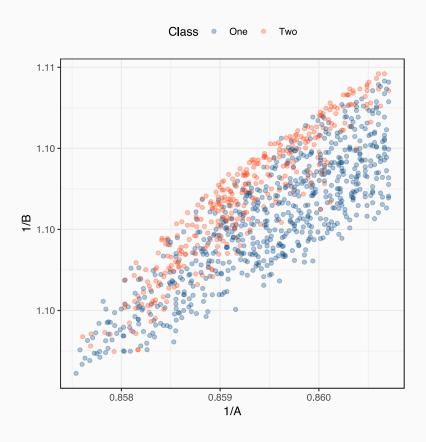
- The components account for as much as the variation in the original data as possible.
- Each component is uncorrelated with the others.
- The new variables are *linear combinations* of all of the input variables and are effectively unitless (It is generally a good idea to center and scale your predictors because of this).

For our purposes, we would use PCA on the predictors to:

- Reduce the number of variables exposed to the model (but this is not feature selection).
- Combat excessive correlations between the predictors (aka multicollinearity).

In this way, the procedure is often called *signal extraction* but this is poorly named since there is no guarantee that the new variables will have an association with the outcome.

Back to the Bivariate Example - Transformed Data



Back to the Bivariate Example - Recipes



We can build on our transformed data recipe and add normalization:

```
bivariate_pca <-
 recipe(Class ~ PredictorA + PredictorB, data = bivariate_data_train) %>%
 step_BoxCox(all_predictors()) %>%
 step_center(all_predictors()) %>%
 step_scale(all_predictors()) %>%
 step_pca(all_predictors()) %>%
 prep(training = bivariate_data_train, verbose = FALSE)
pca_test <- bake(bivariate_pca, new_data = bivariate_data_test)</pre>
# Put components axes on the same range
pca_rng <- extendrange(c(pca_test$PC1, pca_test$PC2))</pre>
ggplot(pca_test, aes(x = PC1, y = PC2, color = Class)) +
 geom_point(alpha = .2, cex = 1.5) +
 theme(legend.position = "top") +
 scale_colour_calc() +
 xlim(pca_rng) + ylim(pca_rng) +
 xlab("Principal Component 1") + ylab("Principal Component 2")
```

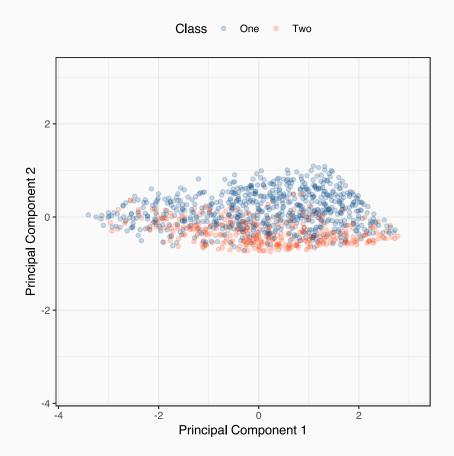
Back to the Bivariate Example

Recall that even after the Box-Cox transformation was applied to our previous example, there was still a high degree of correlation between the predictors.

After the transformation, the predictors were centered and scaled, then PCA was conducted. The plot on the right shows the results.

Since these two predictors are highly correlated, the first component captures 91.7% of the variation in the original data. However...

...recall that PCA does not guarantee that the components are associated with the outcome. In this example, the *least important* component has the association with the outcome.



Resampling and Preprocessing

It is important to realize that almost all preprocessing steps that involve estimation should be bundled inside of the resampling process so that the performance estimates are not biased.

- **Bad**: preprocess the data, resample the model
- **Good**: resample the preprocessing and modeling

Also:

- Avoid information leakage by having all operations in the modeling process occur only on the training set.
- Do not reestimate anything on the test set. For example, to center new data, the training set mean is used.

Interaction Effects

Interactions

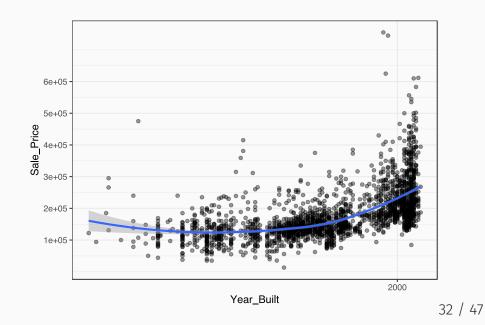


An **interaction** between two predictors indicates that the relationship between the predictors and the outcome cannot be describe using only one of the variables.

For example, let's look at the relationship between the price of a house and the year in which it was built. The relationship appears to be slightly nonlinear, possibly quadratic:

```
price_breaks <- (1:6)*(10^5)

ggplot(
    ames_train,
    aes(x = Year_Built, y = Sale_Price)
) +
    geom_point(alpha = 0.4) +
    scale_x_log10() +
    scale_y_continuous(
        breaks = price_breaks
) +
    geom_smooth(method = "loess")</pre>
```



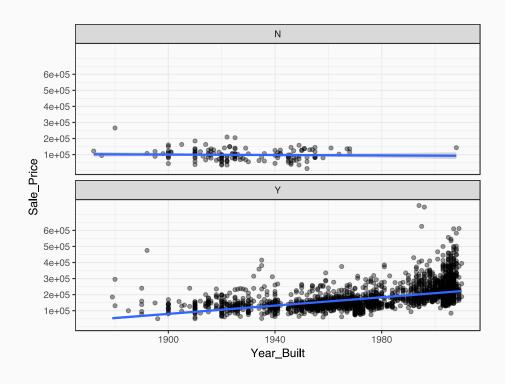
Interactions



However... what if we separate this trend based on whether the property has air conditioning (93.4% of the training set) or not (6.6%):

```
library(MASS) # to get robust linear regression model

ggplot(
    ames_train,
    aes(x = Year_Built,
        y = Sale_Price)
) +
    geom_point(alpha = 0.4) +
    scale_y_continuous(
        breaks = price_breaks
) +
    facet_wrap(~ Central_Air, nrow = 2) +
    geom_smooth(method = "rlm")
```



Interactions

It appears as though the relationship between the year built and the sale price is somewhat *different* for the two groups.

- When there is no AC, the trend is perhaps flat or slightly decreasing.
- With AC, there is a linear increasing trend or is perhaps slightly quadratic with some outliers at the low end.

```
mod1 <- lm(log10(Sale_Price) ~ Year_Built + Central_Air, data = ames_train)
mod2 <- lm(log10(Sale_Price) ~ Year_Built + Central_Air + Year_Built:Central_Air, data = ames_train)
anova(mod1, mod2)</pre>
```

Interactions in Recipes



We first create the dummy variables for the qualitative predictor (central_Air) then use a formula to create the interaction using the : operator in an additional step:

```
recipe(Sale_Price ~ Year_Built + Central_Air, data = ames_train) %>%
  step_log(Sale_Price) %>%
  step_dummy(Central_Air) %>%
  step_interact(~ starts_with("Central_Air"):Year_Built) %>%
  prep(training = ames_train) %>%
  juice() %>%

# select a few rows with different values
  slice(153:157)
```

```
## # A tibble: 5 x 4
    Year_Built Sale_Price Central_Air_Y Central_Air_Y_x_Year_Built
                      <dbl>
                                     <dbl>
##
          <int>
                                                                  <dbl>
## 1
           1912
                      12.0
                                         1
                                                                   1912
## 2
           1930
                      10.9
                                         (-)
                                                                      (-)
                      11.8
## 3
           1900
                                         1
                                                                   1900
                       12.1
           1959
                                         1
                                                                   1959
                       11.6
                                                                      0
## 5
           1917
                                         0
```

Adding Recipes to our rsample Workflows

Linear Models Again



Let's add a few extra predictors and some preprocessing.

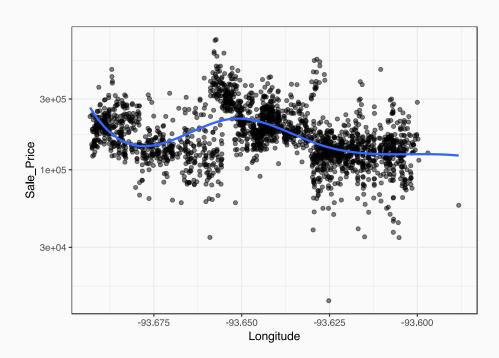
- Two numeric predictors are very skewed and could use a transformation (Lot_Area and Gr_Liv_Area).
- We'll add neighborhood in as well and a few other house features.
- The K-NN model suggests that the coordinates can be helpful but probably require a nonlinear representation. We can add these using *B-splines* with 5 degrees of freedom. To evaluate this, we will create two versions of the recipe to evaluate this hypothesis.

Longitude



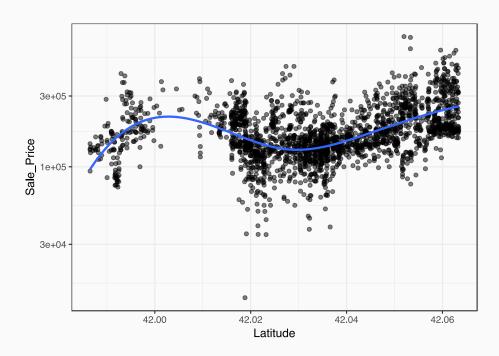
Splines add nonlinear versions of the predictor to a linear model to create smooth and flexible relationships between the predictor and outcome.

This "basis expansion" technique will be seen again in the regression section of the workshop.



Latitude





Preparing the Recipes



Our first step is the run prep() on the nonlin_terms recipe but using each of the analysis sets.

recipes has a function that is a wrapper around prep() that can be used to map over the split objects, prepping on the analysis set of each one:

```
cv_splits <- cv_splits %>%
  mutate(nonlin_terms = map(splits, prepper, recipe = nonlin_terms))
```

Fitting the Models







We can use code that is very similar to the previous section.

This code will use the recipe object to get the data. Since each analysis set is used to train the recipe, our previous use of retain = TRUE means that the processed version of the data is within the recipe. This can be returned via the juice() function.

```
spec_lm <- linear_reg() %>%
  set_engine("lm")

lm_fit_rec <- function(rec_obj, formula) {
  fit(spec_lm, formula, data = juice(rec_obj))
}</pre>
```

```
cv_splits <- cv_splits %>%
  mutate(models = map(
     nonlin_terms,
     lm_fit_rec,
     Sale_Price ~ .)
)
glance(cv_splits$models[[1]]$fit)
```

```
## # A tibble: 1 x 11
    r.squared adj.r.squared sigma statistic p.value
                                                                        BIC deviance df.residual
                                                       df logLik
                                                                    AIC
        <dbl>
                      <dbl> <dbl>
                                       <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
                                                                                  <dbl>
                                                                                              <int>
## 1
        0.803
                      0.801 0.0796
                                       319.
                                                       26 2211. -4368. -4217.
                                                                                  12.4
                                                                                              1951
```

Predicting the Assessment Set











This is a little more complex. We need three elements contained in our tibble:

- the split object (to get the assessment data)
- the recipe object (to process the data)
- the linear model (for predictions)

The function is not too bad:

```
assess_predictions <- function(split, recipe, model) {
  raw_assessment <- assessment(split)
  processed <- bake(recipe, new_data = raw_assessment)

model %>%
  predict(new_data = processed) %>%
  bind_cols(processed) %>%
  mutate(
    # Sale_Price is already logged by the recipe
    .resid = Sale_Price - .pred,
    # Save the original row number of the data
    .row = as.integer(split, data = "assessment")
  )
}
```

Predicting the Assessment Set



Since we have three inputs, we will use purrr::pmap() to walk along all three columns in the tibble.

```
cv_splits <- cv_splits %>%
  mutate(
    pred = pmap(
        list(
        split = splits,
        recipe = nonlin_terms,
        model = models
        ),
        assess_predictions
    )
)
```

We do get some warnings that the assessment data are outside the range of the analysis set values:

```
## Warning in bs(x = c(-93.6235954, -93.636372, -93.627536, -93.65332, ## -93.649447, : some 'x' values beyond boundary knots may cause ill-## conditioned bases
```

Predicting the Assessment Set



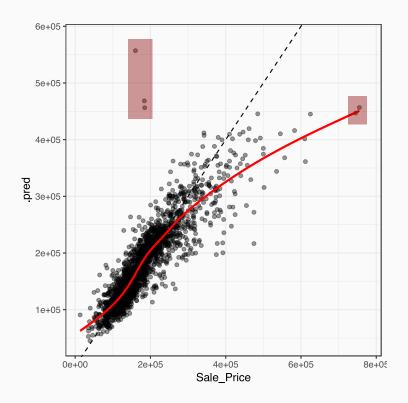
yardstick::metrics() will compute a small set of summary statistics for the model based on the type of outcome (e.g. regression, classification, etc).

```
# Compute the summary statistics
cv_splits %>%
  unnest(pred) %>%
  group_by(id) %>%
  metrics(truth = Sale_Price, estimate = .pred) %>%
  group_by(.metric) %>%
  summarise(
   resampled_estimate = mean(.estimate)
)
```

These results are better than our K-NN model but "the only way to be comfortable with your results is to never look at them".

Graphical Checks for Fit





• The code used for highlighting the points is slightly more complex

Graphical Checks for Fit

The current model is:

- Drastically *over*-predicting the price of three houses.
- Significantly under-predicting the price of a number of expensive houses.

We would we do next?

- 1. Try to understand the big residuals. Are these aberrant houses or does this have something to do with our model? Maybe those extrapolation warnings?
- 2. Find more predictors that differentiate the more expensive houses with the others.
- 3. Try a different model.

(I wrote this slide long before the next one)

About Those Five Houses

From Dmytro Perepolkin via GitHub/topepo/AmesHousing:

I did a little bit of research on Kaggle regarding those five houses (three "partial sale" houses in Edwards and two upscale in Northridge):

In fact all three of Edwards properties were sold within three months by the same company. The lots are located next to each other in Cochrane Pkwy Ames, IA. I guess the story was that developer was either in trouble or wanted to boost sales, so they were signing sales contracts on half-finished houses in a new development area at a deep discount. Those few houses are likely to have been built first out of the whole residential block that followed.

Two of the upscale houses in Northridge (sold at 745 and 755 thousand, respectively) are located next to each other. Houses are, of course, eyecandies (at least to my taste). They are outliers with regards to size in their own neighborhoods!

Sometimes it really pays off to be a forensic statistician.