## **Ecotoxicology is not normal.**

How the use of proper statistical models can increase statistical power in ecotoxicological experiments.

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## 1 Supplement 1 - Additional Figures / Tables

## 1.1 Count data simulations

Table 1: Count data simulations - Proportion of models converged. N = sample sizes,  $\mu_C$  = mean abundance in control, LM = Linear model after transformation,  $GLM_{nb}$  = negative binomial model,  $GLM_{qp}$  = quasi-Poisson model.

N	$\mu_C$	LM	$GLM_{nb}$	$GLM_{qp}$
3.00	2.00	1.00	0.30	1.00
3.00	4.00	1.00	0.51	1.00
3.00	8.00	1.00	0.72	1.00
3.00	16.00	1.00	0.93	1.00
3.00	32.00	1.00	0.98	1.00
3.00	64.00	1.00	1.00	1.00
3.00	128.00	1.00	1.00	1.00
6.00	2.00	1.00	0.57	1.00
6.00	4.00	1.00	0.87	1.00
6.00	8.00	1.00	0.97	1.00
6.00	16.00	1.00	1.00	1.00
6.00	32.00	1.00	1.00	1.00
6.00	64.00	1.00	1.00	1.00
6.00	128.00	1.00	1.00	1.00
9.00	2.00	1.00	0.82	1.00
9.00	4.00	1.00	0.98	1.00
9.00	8.00	1.00	0.99	1.00
9.00	16.00	1.00	1.00	1.00
9.00	32.00	1.00	1.00	1.00
9.00	64.00	1.00	1.00	1.00
9.00	128.00	1.00	1.00	1.00
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Table 2: Count data simulations - Power to detect a global treatment effect. N = sample sizes,  $\mu_C$  = mean abundance in control, LM = Linear model after transformation,  $GLM_{nb}$  = negative binomial model,  $GLM_{qp}$  = quasi-Poisson model,  $GLM_{pb}$  = negative binomial model with parametric boostrap, np = pairwise Wilcoxon.

N	$\mu_C$	LM	$GLM_{nb}$	$GLM_{qp}$	$GLM_{pb}$	np
3.00	2.00	0.14	0.17	0.19	0.07	0.09
3.00	4.00	0.13	0.18	0.20	0.08	0.05
3.00	8.00	0.21	0.38	0.24	0.19	0.12
3.00	16.00	0.28	0.45	0.32	0.26	0.18
3.00	32.00	0.33	0.54	0.45	0.36	0.18
3.00	64.00	0.30	0.57	0.35	0.37	0.14
3.00	128.00	0.25	0.57	0.35	0.32	0.13
6.00	2.00	0.30	0.33	0.33	0.21	0.27
6.00	4.00	0.36	0.45	0.43	0.33	0.26
6.00	8.00	0.44	0.65	0.59	0.53	0.44
6.00	16.00	0.58	0.78	0.72	0.65	0.49
6.00	32.00	0.59	0.82	0.71	0.67	0.51
6.00	64.00	0.65	0.74	0.73	0.68	0.63
6.00	128.00	0.80	0.91	0.85	0.84	0.70
9.00	2.00	0.34	0.30	0.35	0.27	0.30
9.00	4.00	0.54	0.65	0.65	0.61	0.47
9.00	8.00	0.56	0.74	0.73	0.67	0.58
9.00	16.00	0.80	0.89	0.90	0.88	0.79
9.00	32.00	0.88	0.93	0.92	0.91	0.89
9.00	64.00	0.90	0.94	0.95	0.93	0.91
9.00	128.00	0.91	0.95	0.93	0.94	0.91

Table 3: Count data simulations - Power to detect LOEC. N = sample sizes,  $\mu_C$  = mean abundance in control, LM = Linear model after transformation,  $GLM_{nb}$  = negative binomial model,  $GLM_{qp}$  = quasi-Poisson model, np = Kruskal-Wallis test.

N	$\mu_C$	LM	$GLM_{nb}$	$GLM_{qp}$	np
3.00	2.00	0.08	0.00	0.00	0.00
3.00	4.00	0.11	0.14	0.11	0.00
3.00	8.00	0.14	0.29	0.18	0.00
3.00	16.00	0.15	0.34	0.18	0.00
3.00	32.00	0.18	0.33	0.21	0.00
3.00	64.00	0.15	0.32	0.21	0.00
3.00	128.00	0.18	0.35	0.26	0.00
6.00	2.00	0.19	0.16	0.11	0.02
6.00	4.00	0.25	0.26	0.20	0.07
6.00	8.00	0.25	0.34	0.26	0.11
6.00	16.00	0.33	0.48	0.42	0.16
6.00	32.00	0.31	0.47	0.37	0.16
6.00	64.00	0.40	0.47	0.42	0.16
6.00	128.00	0.54	0.66	0.59	0.25
9.00	2.00	0.19	0.13	0.14	0.03
9.00	4.00	0.30	0.38	0.28	0.10
9.00	8.00	0.35	0.52	0.43	0.23
9.00	16.00	0.53	0.64	0.60	0.36
9.00	32.00	0.65	0.75	0.70	0.50
9.00	64.00	0.55	0.64	0.66	0.40
9.00	128.00	0.61	0.73	0.68	0.40

Table 4: Count data simulations - Type 1 error to detect a global treatment effect. N = sample sizes,  $\mu_C$  = mean abundance in control, LM = Linear model after transformation,  $GLM_{nb}$  = negative binomial model,  $GLM_{qp}$  = quasi-Poisson model,  $GLM_{pb}$  = negative binomial model with parametric boostrap, np = Kruskal-Wallis test.

N	$\mu_C$	LM	$GLM_{nb}$	$GLM_{qp}$	$GLM_{pb}$	np
3.00	2.00	0.09	0.03	0.00	0.10	0.04
3.00	4.00	0.07	0.11	0.04	0.06	0.03
3.00	8.00	0.05	0.11	0.09	0.07	0.01
3.00	16.00	0.03	0.12	0.05	0.03	0.01
3.00	32.00	0.05	0.14	0.05	0.04	0.00
3.00	64.00	0.02	0.11	0.04	0.04	0.00
3.00	128.00	0.07	0.19	0.05	0.09	0.02
6.00	2.00	0.04	0.03	0.03	0.05	0.02
6.00	4.00	0.04	0.12	0.05	0.09	0.04
6.00	8.00	0.05	0.04	0.04	0.04	0.03
6.00	16.00	0.04	0.09	0.04	0.06	0.04
6.00	32.00	0.06	0.08	0.06	0.07	0.05
6.00	64.00	0.05	0.06	0.05	0.05	0.03
6.00	128.00	0.04	0.09	0.02	0.04	0.01
9.00	2.00	0.04	0.03	0.03	0.05	0.05
9.00	4.00	0.05	0.07	0.03	0.07	0.04
9.00	8.00	0.08	0.12	0.07	0.09	0.08
9.00	16.00	0.07	0.09	0.06	0.08	0.06
9.00	32.00	0.06	0.07	0.05	0.06	0.05
9.00	64.00	0.03	0.06	0.04	0.04	0.03
9.00	128.00	0.05	0.07	0.04	0.07	0.02

Table 5: Count data simulations - Type 1 error to detect LOEC. N = sample sizes,  $\mu_C$  = mean abundance in control, LM = Linear model after transformation,  $GLM_{nb}$  = negative binomial model,  $GLM_{qp}$  = quasi-Poisson model, np = pairwise Wilcoxon.

N	$\mu_C$	LM	$GLM_{nb}$	$GLM_{qp}$	np
3.00	2.00	0.06	0.03	0.02	0.00
3.00	4.00	0.10	0.14	0.10	0.00
3.00	8.00	0.04	0.08	0.05	0.00
3.00	16.00	0.01	0.12	0.02	0.00
3.00	32.00	0.04	0.16	0.03	0.00
3.00	64.00	0.01	0.14	0.03	0.00
3.00	128.00	0.08	0.14	0.11	0.00
6.00	2.00	0.05	0.05	0.05	0.00
6.00	4.00	0.10	0.15	0.09	0.02
6.00	8.00	0.04	0.07	0.03	0.02
6.00	16.00	0.04	0.08	0.04	0.02
6.00	32.00	0.06	0.10	0.06	0.05
6.00	64.00	0.06	0.07	0.05	0.07
6.00	128.00	0.04	0.12	0.06	0.05
9.00	2.00	0.04	0.06	0.04	0.03
9.00	4.00	0.05	0.05	0.05	0.04
9.00	8.00	0.09	0.11	0.09	0.09
9.00	16.00	0.04	0.04	0.01	0.02
9.00	32.00	0.08	0.09	0.07	0.03
9.00	64.00	0.05	0.10	0.04	0.05
9.00	128.00	0.05	0.11	0.05	0.03

## 1.2 Binomial data simulations

Table 6: Binomial data simulations - Power to detect a global treatment effect. N = sample sizes,  $p_E$  = probability in effect treatments, LM = Linear model after transformation, GLM = binomial model, np = Kruskal-Wallis test.

N	$p_E$	$_{ m LM}$	GLM	np
3.00	0.60	0.96	1.00	0.86
3.00	0.65	0.88	0.99	0.73
3.00	0.70	0.79	0.97	0.64
3.00	0.75	0.63	0.85	0.44
3.00	0.80	0.44	0.63	0.28
3.00	0.85	0.22	0.42	0.10
3.00	0.90	0.08	0.13	0.04
3.00	0.95	0.06	0.07	0.03
6.00	0.60	1.00	1.00	1.00
6.00	0.65	1.00	1.00	1.00
6.00	0.70	1.00	1.00	1.00
6.00	0.75	0.98	1.00	0.96
6.00	0.80	0.82	0.88	0.80
6.00	0.85	0.55	0.64	0.50
6.00	0.90	0.16	0.24	0.14
6.00	0.95	0.04	0.06	0.02
9.00	0.60	1.00	1.00	1.00
9.00	0.65	1.00	1.00	1.00
9.00	0.70	1.00	1.00	1.00
9.00	0.75	1.00	1.00	1.00
9.00	0.80	0.98	0.99	0.97
9.00	0.85	0.74	0.83	0.73
9.00	0.90	0.28	0.32	0.25
9.00	0.95	0.07	0.06	0.05

Table 7: Count data simulations - Power to detect LOEC. N = sample sizes,  $p_E$  = probability in effect treatments, LM = Linear model after transformation, GLM = binomial model, np = pairwise Wilcoxon.

	N	$p_E$	$_{ m LM}$	GLM	np
	3.00	0.60	0.82	0.71	0.00
	3.00	0.65	0.75	0.58	0.00
	3.00	0.70	0.61	0.43	0.00
	3.00	0.75	0.45	0.23	0.00
	3.00	0.80	0.28	0.11	0.00
	3.00	0.85	0.12	0.03	0.00
	3.00	0.90	0.04	0.01	0.00
	3.00	0.95	0.01	0.00	0.00
	6.00	0.60	1.00	0.95	0.98
	6.00	0.65	0.99	0.95	0.95
	6.00	0.70	0.94	0.92	0.83
	6.00	0.75	0.78	0.76	0.59
	6.00	0.80	0.52	0.51	0.32
	6.00	0.85	0.30	0.22	0.13
	6.00	0.90	0.10	0.04	0.03
	6.00	0.95	0.00	0.00	0.00
	9.00	0.60	1.00	0.98	0.98
	9.00	0.65	1.00	0.99	0.97
	9.00	0.70	0.99	0.96	0.95
	9.00	0.75	0.95	0.97	0.92
	9.00	0.80	0.80	0.81	0.72
	9.00	0.85	0.42	0.50	0.34
	9.00	0.90	0.16	0.14	0.08
_	9.00	0.95	0.02	0.01	0.00

Table 8: Binomial data simulations - Type 1 error to detect a global treatment effect. N = sample sizes, p = probability, LM = Linear model after transformation, GLM = binomial model, np = Kruskal-Wallis test.

N	p	LM	GLM	np
3.00	0.60	0.03	0.03	0.02
3.00	0.65	0.04	0.06	0.01
3.00	0.70	0.05	0.04	0.00
3.00	0.75	0.05	0.06	0.01
3.00	0.80	0.06	0.06	0.01
3.00	0.85	0.06	0.06	0.02
3.00	0.90	0.06	0.09	0.02
3.00	0.95	0.04	0.04	0.02
6.00	0.60	0.07	0.08	0.06
6.00	0.65	0.04	0.05	0.04
6.00	0.70	0.04	0.06	0.04
6.00	0.75	0.04	0.06	0.04
6.00	0.80	0.05	0.06	0.03
6.00	0.85	0.04	0.05	0.03
6.00	0.90	0.06	0.08	0.04
6.00	0.95	0.04	0.08	0.03
9.00	0.60	0.05	0.04	0.04
9.00	0.65	0.06	0.04	0.04
9.00	0.70	0.08	0.06	0.07
9.00	0.75	0.04	0.04	0.03
9.00	0.80	0.03	0.02	0.02
9.00	0.85	0.03	0.02	0.02
9.00	0.90	0.04	0.05	0.02
9.00	0.95	0.05	0.07	0.04

Table 9: Binomial data simulations - Type 1 error to detect LOEC. N = sample sizes, p = probability, LM = Linear model after transformation, GLM = binomial model, np = pairwise Wilcoxon.

N	$p_E$	LM	GLM	np
3.00	0.60	0.03	0.04	0.00
3.00	0.65	0.04	0.04	0.00
3.00	0.70	0.05	0.04	0.00
3.00	0.75	0.05	0.02	0.00
3.00	0.80	0.08	0.06	0.00
3.00	0.85	0.06	0.04	0.00
3.00	0.90	0.07	0.00	0.00
3.00	0.95	0.06	0.00	0.00
6.00	0.60	0.06	0.04	0.01
6.00	0.65	0.02	0.04	0.02
6.00	0.70	0.05	0.05	0.02
6.00	0.75	0.05	0.06	0.04
6.00	0.80	0.03	0.04	0.02
6.00	0.85	0.06	0.04	0.02
6.00	0.90	0.05	0.03	0.02
6.00	0.95	0.04	0.00	0.01
9.00	0.60	0.07	0.06	0.04
9.00	0.65	0.04	0.03	0.02
9.00	0.70	0.06	0.06	0.05
9.00	0.75	0.06	0.07	0.04
9.00	0.80	0.03	0.03	0.01
9.00	0.85	0.05	0.04	0.02
9.00	0.90	0.02	0.03	0.02
9.00	0.95	0.04	0.01	0.01