

# **Ecotoxicology is not normal.**

**A comparison of statistical approaches for analysis of count and proportion data in ecotoxicology.**

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## **Supplement 1 - Additional Figures / Tables**

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## **1 Count data simulations**

## **2 Binomial data simulations**

Table 1: Count data simulations - Proportion of models converged. N = sample sizes,  $\mu_C$  = mean abundance in control, LM = Linear model after transformation,  $GLM_{nb}$  = negative binomial model,  $GLM_{qp}$  = quasi-Poisson model,  $GLM_p$  = Poisson model

N	$\mu_C$	LM	$GLM_{nb}$	$GLM_{qp}$	$GLM_p$
3.00	2.00	1.00	0.33	1.00	1.00
3.00	4.00	1.00	0.53	1.00	1.00
3.00	8.00	1.00	0.79	1.00	1.00
3.00	16.00	1.00	0.94	1.00	1.00
3.00	32.00	1.00	0.99	1.00	1.00
3.00	64.00	1.00	1.00	1.00	1.00
3.00	128.00	1.00	1.00	1.00	1.00
6.00	2.00	1.00	0.63	1.00	1.00
6.00	4.00	1.00	0.85	1.00	1.00
6.00	8.00	1.00	0.98	1.00	1.00
6.00	16.00	1.00	1.00	1.00	1.00
6.00	32.00	1.00	1.00	1.00	1.00
6.00	64.00	1.00	1.00	1.00	1.00
6.00	128.00	1.00	1.00	1.00	1.00
9.00	2.00	1.00	0.76	1.00	1.00
9.00	4.00	1.00	0.95	1.00	1.00
9.00	8.00	1.00	1.00	1.00	1.00
9.00	16.00	1.00	1.00	1.00	1.00
9.00	32.00	1.00	1.00	1.00	1.00
9.00	64.00	1.00	1.00	1.00	1.00
9.00	128.00	1.00	1.00	1.00	1.00

Table 2: Count data simulations - Power to detect a treatment effect. N = sample sizes,  $\mu_C$  = mean abundance in control, LM = Linear model after transformation,  $GLM_{nb}$  = negative binomial model,  $GLM_{qp}$  = quasi-Poisson model,  $GLM_p$  = Poisson model, np = pairwise Wilcoxon test.

N	$\mu_C$	LM	$GLM_{nb}$	$GLM_{qp}$	$GLM_p$	np	NA
3.00	2.00	0.13	0.17	0.17	0.08	0.36	0.04
3.00	4.00	0.14	0.18	0.17	0.10	0.54	0.06
3.00	8.00	0.19	0.36	0.24	0.21	0.78	0.09
3.00	16.00	0.23	0.49	0.33	0.29	0.95	0.14
3.00	32.00	0.31	0.57	0.38	0.35	0.99	0.16
3.00	64.00	0.32	0.58	0.38	0.34	1.00	0.18
3.00	128.00	0.35	0.61	0.42	0.37	1.00	0.19
6.00	2.00	0.26	0.30	0.29	0.22	0.49	0.21
6.00	4.00	0.36	0.48	0.44	0.40	0.78	0.32
6.00	8.00	0.48	0.64	0.57	0.53	0.94	0.44
6.00	16.00	0.59	0.76	0.70	0.65	0.99	0.54
6.00	32.00	0.68	0.82	0.76	0.73	1.00	0.63
6.00	64.00	0.72	0.85	0.80	0.77	1.00	0.64
6.00	128.00	0.73	0.84	0.80	0.76	1.00	0.63
9.00	2.00	0.34	0.40	0.42	0.35	0.64	0.31
9.00	4.00	0.56	0.69	0.66	0.63	0.91	0.54
9.00	8.00	0.70	0.82	0.79	0.76	0.98	0.68
9.00	16.00	0.81	0.91	0.89	0.88	1.00	0.79
9.00	32.00	0.89	0.95	0.94	0.92	1.00	0.87
9.00	64.00	0.92	0.96	0.95	0.95	1.00	0.89
9.00	128.00	0.94	0.97	0.96	0.95	1.00	0.91

Table 3: Count data simulations - Power to detect LOEC. N = sample sizes,  $\mu_C$  = mean abundance in control, LM = Linear model after transformation,  $GLM_{nb}$  = negative binomial model,  $GLM_{qp}$  = quasi-Poisson model,  $GLM_p$  = Poisson model, np = pairwise Wilcoxon test.

N	$\mu_C$	LM	$GLM_{nb}$	$GLM_{qp}$	$GLM_p$	np
3.00	2.00	0.05	0.01	0.02	0.02	0.00
3.00	4.00	0.08	0.09	0.08	0.15	0.00
3.00	8.00	0.11	0.22	0.12	0.30	0.00
3.00	16.00	0.13	0.30	0.18	0.42	0.00
3.00	32.00	0.17	0.35	0.22	0.50	0.00
3.00	64.00	0.19	0.37	0.23	0.51	0.00
3.00	128.00	0.18	0.37	0.23	0.53	0.00
6.00	2.00	0.14	0.11	0.09	0.15	0.06
6.00	4.00	0.17	0.23	0.19	0.30	0.12
6.00	8.00	0.28	0.39	0.32	0.52	0.20
6.00	16.00	0.33	0.48	0.39	0.59	0.23
6.00	32.00	0.40	0.54	0.47	0.64	0.28
6.00	64.00	0.44	0.56	0.48	0.61	0.29
6.00	128.00	0.44	0.57	0.49	0.56	0.29
9.00	2.00	0.19	0.20	0.18	0.26	0.13
9.00	4.00	0.29	0.37	0.31	0.48	0.27
9.00	8.00	0.40	0.52	0.46	0.62	0.35
9.00	16.00	0.51	0.63	0.57	0.70	0.45
9.00	32.00	0.57	0.69	0.63	0.68	0.52
9.00	64.00	0.61	0.72	0.66	0.65	0.53
9.00	128.00	0.65	0.73	0.68	0.61	0.58

Table 4: Count data simulations - Type 1 error to detect a global treatment effect. N = sample sizes,  $\mu_C$  = mean abundance in control, LM = Linear model after transformation,  $GLM_{nb}$  = negative binomial model,  $GLM_{qp}$  = quasi-Poisson model,  $GLM_{pb}$  = negative binomial model with parametric bootstrap,  $GLM_p$  = Poisson model, np = Kruskal-Wallis test.

N	$\mu_C$	LM	$GLM_{nb}$	$GLM_{qp}$	$GLM_{pb}$	$GLM_p$	np
3.00	2.00	0.07	0.04	0.02	0.07	0.21	0.03
3.00	4.00	0.05	0.07	0.03	0.05	0.37	0.01
3.00	8.00	0.04	0.12	0.05	0.05	0.58	0.02
3.00	16.00	0.05	0.14	0.05	0.05	0.84	0.02
3.00	32.00	0.04	0.13	0.03	0.04	0.94	0.01
3.00	64.00	0.05	0.16	0.05	0.05	0.99	0.03
3.00	128.00	0.05	0.13	0.05	0.06	1.00	0.02
6.00	2.00	0.04	0.05	0.04	0.06	0.20	0.03
6.00	4.00	0.05	0.08	0.05	0.05	0.36	0.04
6.00	8.00	0.06	0.09	0.05	0.06	0.58	0.04
6.00	16.00	0.05	0.08	0.05	0.05	0.80	0.04
6.00	32.00	0.06	0.08	0.05	0.06	0.94	0.04
6.00	64.00	0.05	0.09	0.05	0.05	0.98	0.04
6.00	128.00	0.05	0.09	0.04	0.05	1.00	0.04
9.00	2.00	0.06	0.06	0.05	0.07	0.20	0.05
9.00	4.00	0.04	0.08	0.05	0.06	0.36	0.04
9.00	8.00	0.05	0.08	0.05	0.06	0.58	0.04
9.00	16.00	0.04	0.07	0.04	0.05	0.81	0.04
9.00	32.00	0.04	0.06	0.04	0.06	0.94	0.05
9.00	64.00	0.04	0.07	0.05	0.05	0.99	0.04
9.00	128.00	0.05	0.07	0.05	0.06	1.00	0.04

Table 5: Count data simulations - Type 1 error to detect LOEC. N = sample sizes,  $\mu_C$  = mean abundance in control, LM = Linear model after transformation,  $GLM_{nb}$  = negative binomial model,  $GLM_{qp}$  = quasi-Poisson model,  $GLM_p$  = Poisson model, np = pairwise Wilcoxon.

N	$\mu_C$	LM	$GLM_{nb}$	$GLM_{qp}$	$GLM_p$	np
3.00	2.00	0.05	0.02	0.02	0.02	0.00
3.00	4.00	0.04	0.08	0.04	0.14	0.00
3.00	8.00	0.05	0.11	0.06	0.24	0.00
3.00	16.00	0.03	0.11	0.04	0.36	0.00
3.00	32.00	0.04	0.15	0.05	0.55	0.00
3.00	64.00	0.05	0.16	0.06	0.61	0.00
3.00	128.00	0.04	0.13	0.05	0.68	0.00
6.00	2.00	0.04	0.04	0.02	0.07	0.02
6.00	4.00	0.03	0.06	0.03	0.15	0.02
6.00	8.00	0.04	0.08	0.05	0.26	0.03
6.00	16.00	0.04	0.08	0.05	0.37	0.03
6.00	32.00	0.04	0.08	0.04	0.52	0.03
6.00	64.00	0.05	0.10	0.05	0.61	0.04
6.00	128.00	0.04	0.08	0.04	0.66	0.05
9.00	2.00	0.03	0.05	0.04	0.08	0.03
9.00	4.00	0.04	0.06	0.05	0.15	0.04
9.00	8.00	0.04	0.05	0.04	0.27	0.04
9.00	16.00	0.04	0.07	0.04	0.38	0.03
9.00	32.00	0.03	0.05	0.04	0.49	0.03
9.00	64.00	0.04	0.06	0.04	0.61	0.04
9.00	128.00	0.04	0.06	0.04	0.67	0.04

Table 6: Binomial data simulations - Power to detect a global treatment effect. N = sample sizes,  $p_E$  = probability in effect treatments, LM = Linear model after transformation,  $GLM$  = binomial model, np = Kruskal-Wallis test.

N	$p_E$	LM	$GLM$	np
3.00	0.60	0.97	1.00	0.87
3.00	0.65	0.90	0.99	0.76
3.00	0.70	0.78	0.95	0.60
3.00	0.75	0.60	0.84	0.41
3.00	0.80	0.36	0.64	0.22
3.00	0.85	0.20	0.41	0.10
3.00	0.90	0.11	0.17	0.05
3.00	0.95	0.06	0.06	0.03
6.00	0.60	1.00	1.00	1.00
6.00	0.65	1.00	1.00	1.00
6.00	0.70	1.00	1.00	1.00
6.00	0.75	0.97	1.00	0.97
6.00	0.80	0.85	0.93	0.82
6.00	0.85	0.53	0.62	0.48
6.00	0.90	0.17	0.24	0.15
6.00	0.95	0.04	0.08	0.03
9.00	0.60	1.00	1.00	1.00
9.00	0.65	1.00	1.00	1.00
9.00	0.70	1.00	1.00	1.00
9.00	0.75	1.00	1.00	1.00
9.00	0.80	0.98	0.99	0.97
9.00	0.85	0.75	0.82	0.73
9.00	0.90	0.26	0.32	0.23
9.00	0.95	0.05	0.07	0.04



Table 7: Count data simulations - Power to detect LOEC. N = sample sizes,  $p_E$  = probability in effect treatments, LM = Linear model after transformation,  $GLM$  = binomial model, np = pairwise Wilcoxon.

N	$p_E$	LM	$GLM$	np
3.00	0.60	0.86	0.70	0.00
3.00	0.65	0.74	0.57	0.00
3.00	0.70	0.59	0.40	0.00
3.00	0.75	0.41	0.17	0.00
3.00	0.80	0.23	0.04	0.00
3.00	0.85	0.11	0.01	0.00
3.00	0.90	0.05	0.00	0.00
3.00	0.95	0.01	0.00	0.00
6.00	0.60	0.98	0.95	0.97
6.00	0.65	0.97	0.93	0.91
6.00	0.70	0.93	0.90	0.82
6.00	0.75	0.82	0.78	0.62
6.00	0.80	0.60	0.55	0.36
6.00	0.85	0.33	0.19	0.16
6.00	0.90	0.08	0.01	0.03
6.00	0.95	0.01	0.00	0.00
9.00	0.60	0.97	0.95	0.97
9.00	0.65	0.98	0.96	0.98
9.00	0.70	0.97	0.96	0.96
9.00	0.75	0.94	0.93	0.89
9.00	0.80	0.82	0.81	0.73
9.00	0.85	0.46	0.43	0.35
9.00	0.90	0.13	0.08	0.08
9.00	0.95	0.01	0.00	0.00

Table 8: Binomial data simulations - Type 1 error to detect a global treatment effect. N = sample sizes,  $p$  = probability, LM = Linear model after transformation,  $GLM$  = binomial model, np = Kruskal-Wallis test.

N	$p$	LM	$GLM$	np
3.00	0.60	0.05	0.06	0.02
3.00	0.65	0.06	0.06	0.02
3.00	0.70	0.04	0.05	0.02
3.00	0.75	0.06	0.05	0.02
3.00	0.80	0.05	0.07	0.02
3.00	0.85	0.06	0.07	0.02
3.00	0.90	0.05	0.08	0.01
3.00	0.95	0.06	0.07	0.02
6.00	0.60	0.06	0.06	0.04
6.00	0.65	0.04	0.05	0.03
6.00	0.70	0.04	0.05	0.04
6.00	0.75	0.05	0.05	0.03
6.00	0.80	0.06	0.06	0.04
6.00	0.85	0.04	0.06	0.04
6.00	0.90	0.06	0.06	0.04
6.00	0.95	0.05	0.08	0.03
9.00	0.60	0.05	0.05	0.04
9.00	0.65	0.06	0.06	0.05
9.00	0.70	0.06	0.05	0.05
9.00	0.75	0.05	0.05	0.05
9.00	0.80	0.06	0.07	0.06
9.00	0.85	0.04	0.05	0.04
9.00	0.90	0.06	0.07	0.05
9.00	0.95	0.06	0.06	0.04

Table 9: Binomial data simulations - Type 1 error to detect LOEC. N = sample sizes,  $p$  = probability, LM = Linear model after transformation, *GLM* = binomial model, np = pairwise Wilcoxon.

N	$p_E$	LM	<i>GLM</i>	np
3.00	0.60	0.03	0.03	0.00
3.00	0.65	0.04	0.03	0.00
3.00	0.70	0.04	0.03	0.00
3.00	0.75	0.04	0.03	0.00
3.00	0.80	0.03	0.01	0.00
3.00	0.85	0.04	0.01	0.00
3.00	0.90	0.03	0.00	0.00
3.00	0.95	0.05	0.00	0.00
6.00	0.60	0.05	0.06	0.02
6.00	0.65	0.03	0.04	0.01
6.00	0.70	0.05	0.04	0.02
6.00	0.75	0.03	0.03	0.02
6.00	0.80	0.04	0.04	0.01
6.00	0.85	0.03	0.02	0.01
6.00	0.90	0.05	0.01	0.01
6.00	0.95	0.05	0.00	0.01
9.00	0.60	0.04	0.04	0.04
9.00	0.65	0.04	0.03	0.04
9.00	0.70	0.05	0.04	0.05
9.00	0.75	0.03	0.04	0.02
9.00	0.80	0.04	0.04	0.03
9.00	0.85	0.04	0.03	0.03
9.00	0.90	0.04	0.03	0.03
9.00	0.95	0.05	0.00	0.01