# **Ecotoxicology is not normal.**

A comparison of statistical approaches for analysis of count and proportion data in ecotoxicology.

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## **Supplement 2 - Worked R examples**

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## 1 Count data example

## 1.1 Introduction

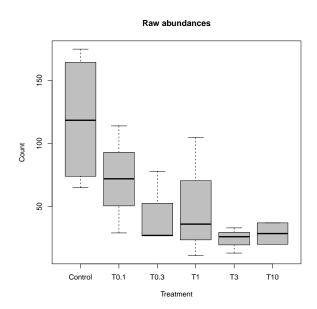
In this example we will analyse data from (Brock et al., 2015). The data are count of mayfly larvae in Macroinvertebrate Artificial Substrate Samplers in 18 mesocosms at one sampling day. There are 5 treatments and one control group.

First, we load the data, bring it to the long format and remove NA values.

```
df <- read.table(header = TRUE,</pre>
                   text = 'Control
                                     T0.1 T0.3
                                                      T3
                                                           T10
                                                  T1
                             175 29
                                      27
                                          36
                                               26
                                                   20
                                 114 78
                                                   37
                             65
                                          11
                                               13
                             154 72
                                      27
                                          105 33
                                                   NA
                                          NA
                                                   NA')
                             83
                                 NA
                                      NA
                                              NA
require(reshape2)
dfm <- melt(df, value.name = 'abu', variable.name = 'treatment')</pre>
dfm <- dfm[!is.na(dfm['abu']), ]</pre>
head(dfm)
##
     treatment abu
## 1
       Control 175
## 2
       Control 65
## 3
       Control 154
## 4
       Control 83
## 5
           T0.1 29
           TO.1 114
## 6
```

This results in a table with two columns - one indicating the treatment and one with the measured abundances.

Let's have a first look at the data:



We clearly see a treatment related response. Moreover, we may note that variances are increasing with increasing abundances.

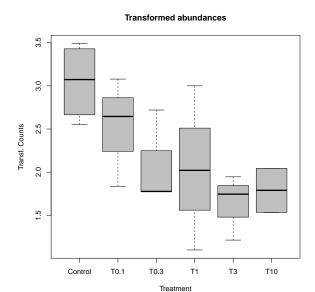
## 1.2 Assuming a normal distribution of transformed abundances

#### 1.2.1 Data transformation

Next we transform the data using a  $\ln(Ax + 1)$  transformation. A is chosen so that the term Ax equals two for the lowest non-zero abundance. We add these transformed abundances as extra column to our table.

```
A <- 2 / min(dfm$abu[dfm$abu != 0])
## [1] 0.1818182
dfm$abu_t <- log(A * dfm$abu + 1)</pre>
head(dfm)
##
     treatment abu
                       abu_t
## 1
       Control 175 3.490983
       Control 65 2.550865
       Control 154 3.367296
## 3
## 4
       Control
                83 2.778254
## 5
          T0.1 29 1.836211
## 6
          T0.1 114 3.078568
```

It looks like the transformation does a good job in equalizing the variances:



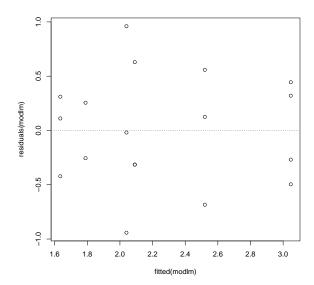
## 1.2.2 Model fitting

The model from eqn. 2 can be easily fitted using the lm() function:

```
modlm <- lm(abu_t ~ treatment, data = dfm)</pre>
```

The residuals vs. fitted values diagnostic plot show no problematic pattern, though it might be difficult to decide with such a small sample size

```
plot(residuals(modlm) ~ fitted(modlm))
abline(h = 0, lty = 'dotted')
```



The summary() gives the estimated parameters with standard errors and Wald t tests:

```
summary(modlm)
##
## Call:
## lm(formula = abu_t ~ treatment, data = dfm)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
##
   -0.94133 -0.31454
                      0.04576
                               0.31813
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
##
  (Intercept)
                   3.0468
                               0.2970
                                       10.260 2.71e-07 ***
## treatmentT0.1
                  -0.5267
                               0.4536
                                       -1.161
                                               0.26814
## treatmentT0.3 -0.9558
                               0.4536
                                       -2.107
                                               0.05682 .
                  -1.0069
                               0.4536
                                       -2.220
                                               0.04646 *
## treatmentT1
## treatmentT3
                  -1.4121
                               0.4536
                                       -3.113
                                               0.00897 **
                               0.5144
                                       -2.445
                                               0.03089 *
## treatmentT10
                  -1.2575
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 0.5939 on 12 degrees of freedom
## Multiple R-squared: 0.5167,Adjusted R-squared: 0.3154
## F-statistic: 2.566 on 5 and 12 DF, p-value: 0.08406
```

## 1.2.3 Inference on general treatment effect

Or, if you want to have the ANOVA table with an F-test:

```
## Df Sum Sq Mean Sq F value Pr(>F)

## treatment 5 4.526 0.9052 2.566 0.0841 .

## Residuals 12 4.233 0.3528

## ---

## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

From this output we might infer that we cannot detect any treatment effect (F = 2.566, p = 0.084).

#### 1.2.4 Inference on LOEC

Let's move on to the LOEC determination. This can be easily done using the multcomp package (Hothorn et al., 2008):

Here we perform a one-sided (alternative = 'less') using Dunnett contrasts of treatment (mcp(treatment='Dunnett')). Moreover, we adjust for multiple testing using Holm's method (test = adjusted('holm')):

```
require(multcomp)
summary(glht(modlm, linfct = mcp(treatment = 'Dunnett'), alternative = 'less'),
        test = adjusted('holm'))
##
##
    Simultaneous Tests for General Linear Hypotheses
##
## Multiple Comparisons of Means: Dunnett Contrasts
##
##
## Fit: lm(formula = abu_t ~ treatment, data = dfm)
##
## Linear Hypotheses:
                      Estimate Std. Error t value Pr(<t)
## T0.1 - Control >= 0 -0.5267
                                  0.4536 -1.161 0.1341
## T0.3 - Control >= 0 -0.9558
                                   0.4536 -2.107 0.0697 .
## T1 - Control >= 0
                                   0.4536 -2.220 0.0697 .
                       -1.0069
## T3 - Control >= 0
                       -1.4121
                                   0.4536 -3.113 0.0224 *
## T10 - Control >= 0
                                   0.5144 -2.445 0.0618 .
                       -1.2575
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## (Adjusted p values reported -- holm method)
```

Here only treatment 3 mg/L shows a statistically significant from control and is the determined LOEC. The column 'Estimate' gives the estimated difference in means between treatments and control and 'Std. Error' the standard errors of these estimated parameters.

To determine the LOEC we could also use a Williams type contrast (Bretz et al., 2010).

Here I use a step-up Williams contrast. First we need to define a contrast matrix (see also ?contrMat()):

Then we supply this contrast matrix to glht():

```
summary(glht(modlm, linfct = mcp(treatment = CM),
             alternative = 'less'),
        test = adjusted('holm'))
##
##
     Simultaneous Tests for General Linear Hypotheses
##
## Multiple Comparisons of Means: User-defined Contrasts
##
##
## Fit: lm(formula = abu_t ~ treatment, data = dfm)
##
## Linear Hypotheses:
           Estimate Std. Error t value Pr(<t)
##
## C 1 >= 0 -0.5267 0.4536 -1.161 0.1341
## C 2 \ge 0 -0.7413
                        0.3834 -1.934 0.0771 .
## C 3 >= 0 -0.8298
                       0.3569 -2.325 0.0576 .
## C 4 >= 0 -0.9754
                        0.3429 -2.845 0.0295 *
## C 5 >= 0 -1.0157
                        0.3367 -3.016 0.0268 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## (Adjusted p values reported -- holm method)
```

This indicates a LOEC at 3 mg/L.

If we do not adjust for multiple testing (test = adjusted('none')), we end up with the same NOEC (0.1 mg/L) as Brock et al. (2015):

```
summary(glht(modlm, linfct = mcp(treatment = CM),
           alternative = 'less'),
       test = adjusted('none'))
##
##
    Simultaneous Tests for General Linear Hypotheses
##
## Multiple Comparisons of Means: User-defined Contrasts
##
##
## Fit: lm(formula = abu_t ~ treatment, data = dfm)
##
## Linear Hypotheses:
          Estimate Std. Error t value Pr(<t)
## C 1 \geq 0 -0.5267 0.4536 -1.161 0.13407
## C 4 \ge 0 -0.9754
                     0.3429 -2.845 0.00739 **
## C 5 >= 0 -1.0157
                      0.3367 -3.016 0.00537 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Adjusted p values reported -- none method)
```

Note, this multiple contrast test is different from the original Williams test (Williams, 1972) used by (Brock et al., 2015), because of different variance estimators (Bretz, 1999).

## 1.3 Assuming a Poisson distribution of abundances

#### 1.3.1 Model fitting

We are dealing with count data, so a Poisson GLM might be a good choice. GLMs can be fitted using the glm() function and here we fit the model from eqn. 3:

```
modpois <- glm(abu ~ treatment, data = dfm, family = poisson(link = 'log'))</pre>
```

Here family = poisson(link = 'log') specifies that we want to fit a poisson model using a log link between response and predictors.

The summary gives the estimated parameters, standard errors and Wald Z tests:

```
(sum_pois <- summary(modpois))

##

## Call:

## glm(formula = abu ~ treatment, family = poisson(link = "log"),

## data = dfm)

##

## Deviance Residuals:

## Min    1Q    Median    3Q    Max

## -6.7625    -2.7621    -0.8219    2.7172    6.6602</pre>
```

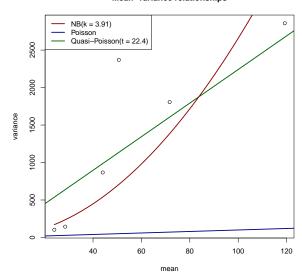
```
##
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
              4.78122 0.04579 104.423 < 2e-16 ***
## treatmentT0.1 -0.50920
                         0.08214 -6.199 5.69e-10 ***
-0.85595 0.09314 -9.190 < 2e-16 ***
## treatmentT1
## treatmentT3
               -1.60317
                         0.12643 -12.680 < 2e-16 ***
## treatmentT10 -1.43132
                       0.14014 -10.213 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
##
##
      Null deviance: 604.79 on 17 degrees of freedom
## Residual deviance: 273.77 on 12 degrees of freedom
## AIC: 387.63
##
## Number of Fisher Scoring iterations: 5
```

But is a poisson distribution appropriate here? A property of the poisson distribution is that its variance is equal to the mean. A simple diagnostic would be to plot group variances vs. group means:

```
require(plyr)
# mean and variance per treatment
musd <- ddply(dfm, .(treatment), summarise,</pre>
              mu = mean(abu),
              var = var(abu)
musd
##
     treatment
                      m11
      Control 119.25000 2857.583
## 1
## 2
         T0.1 71.66667 1806.333
## 3
          T0.3 44.00000 867.000
## 4
            T1 50.66667 2370.333
## 5
            T3 24.00000 103.000
## 6
           T10 28.50000 144.500
# plot mean vs var
plot(var ~ mu, data = musd,
     xlab = 'mean', ylab = 'variance', main = 'Mean-variance relationships')
# poisson
abline(a = 0, b = 1, col = 'darkblue', lwd = 2)
# quasi-Poisson
abline(a = 0, b = 22.41, col = 'darkgreen', lwd = 2)
# negative binomial
curve(x + (x^2 / 3.91), from = 24, to = 119.25, add = TRUE,
      col = 'darkred', lwd = 2)
legend('topleft',
       legend = c('NB(k = 3.91)', 'Poisson', 'Quasi-Poisson(t = 22.4)'),
```

```
col = c('darkred', 'darkblue', 'darkgreen'),
lty = c(1,1, 1),
lwd = c(2,2, 2))
```

#### Mean-variance relationships



I also added the assumed mean-variance relationships of the Poisson, quasi-Poisson and negative binomial models (see below). We clearly see that the variance increases much more than would be expected under the poisson distribution (the data is overdispersed). Moreover, we could check overdispersion from the summary: If the ratio of residual deviance to degrees of freedom is >1 the data is overdispersed.

```
sum_pois$deviance / sum_pois$df.residual
## [1] 22.81412
```

## 1.4 Apply quasi-Poisson to deal with overdispersion

The plot above suggests that the variance may increasing stronger than the mean and a quasi-Poisson or negative binomial model might be more appropriate for this data.

## 1.4.1 Model fitting

Fitting a quasi-Poisson model (eqn. 4) is straight forward:

```
modqpois <- glm(abu ~ treatment, data = dfm, family = 'quasipoisson')</pre>
```

The summary gives the estimated parameters:

```
summary(modqpois)

##

## Call:
## glm(formula = abu ~ treatment, family = "quasipoisson", data = dfm)
```

```
##
## Deviance Residuals:
      Min 1Q Median 3Q
                                        Max
## -6.7625 -2.7621 -0.8219 2.7172
                                      6.6602
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                4.7812 0.2168 22.058 4.43e-11 ***
## (Intercept)
## treatmentT0.1 -0.5092
                           0.3889 -1.309
                                           0.2149
## treatmentT0.3 -0.9970
                            0.4656 - 2.142
                                            0.0534 .
                -0.8560
                            0.4409 - 1.941
## treatmentT1
                                            0.0761 .
## treatmentT3
                -1.6032
                            0.5985 -2.679
                                            0.0201 *
                -1.4313
## treatmentT10
                            0.6634 - 2.157
                                            0.0519 .
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for quasipoisson family taken to be 22.41055)
##
##
      Null deviance: 604.79 on 17
                                   degrees of freedom
## Residual deviance: 273.77 on 12 degrees of freedom
## AIC: NA
##
## Number of Fisher Scoring iterations: 5
```

, with the dispersion parameter  $\Theta=22.41055$ . Note, that the parameter estimates are the same as from the Poisson model, only the standard errors are scaled/wider.

## 1.4.2 Inference on general treatment effect

An F-test can be performed using drop1():

Here we would reject that there is treatment effect (at alpha = 0.05).

#### 1.4.3 Inference on LOEC

The LOEC can be determined with multcomp:

```
##
##
    Simultaneous Tests for General Linear Hypotheses
##
## Multiple Comparisons of Means: Dunnett Contrasts
##
##
## Fit: glm(formula = abu ~ treatment, family = "quasipoisson", data = dfm)
##
## Linear Hypotheses:
                      Estimate Std. Error z value Pr(<z)
## T0.1 - Control >= 0 -0.5092   0.3889 -1.309 0.0952 .
## T0.3 - Control >= 0 -0.9970
                                 0.4656 -2.142 0.0619 .
## T1 - Control >= 0 -0.8560
                                 0.4409 -1.941 0.0619 .
## T3 - Control >= 0
                       -1.6032
                                 0.5985 -2.679 0.0185 *
## T10 - Control >= 0 -1.4313
                                  0.6634 -2.157 0.0619 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Adjusted p values reported -- holm method)
```

, which determines 3 mg/L as LOEC.

## 1.5 Assuming a negative binomial distribution of abundances

## 1.5.1 Model fitting

To fit a negative binomial GLM (eqn. 5) we could use glm.nb() from the MASS package (Venables and Ripley, 2002):

```
require(MASS)
modnb <- glm.nb(abu ~ treatment, data = dfm)</pre>
```

The estimated parameters:

```
summary(modnb)
##
## Call:
## glm.nb(formula = abu ~ treatment, data = dfm, init.theta = 3.905898474,
##
      link = log)
##
## Deviance Residuals:
      Min 1Q Median
                               3Q
                                       Max
## -2.2554 -0.8488 -0.3020 0.5954
                                  1.5899
##
## Coefficients:
##
               Estimate Std. Error z value Pr(>|z|)
## (Intercept)
              4.7812 0.2571 18.596 < 2e-16 ***
## treatmentT0.1 -0.5092
                          0.3951 -1.289 0.19746
## treatmentT0.3 -0.9970
                         0.3988 -2.500 0.01241 *
## treatmentT1 -0.8560 0.3975 -2.153 0.03130 *
## treatmentT3 -1.6032 0.4066 -3.943 8.05e-05 ***
```

```
## treatmentT10 -1.4313 0.4601 -3.111 0.00186 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
  (Dispersion parameter for Negative Binomial (3.9059) family taken to be 1)
##
##
      Null deviance: 39.057 on 17 degrees of freedom
## Residual deviance: 18.611 on 12 degrees of freedom
## AIC: 181.24
##
## Number of Fisher Scoring iterations: 1
##
##
##
                Theta: 3.91
##
            Std. Err.: 1.37
##
   2 x log-likelihood: -167.238
##
```

, with  $\kappa = 3.91$ .

## 1.5.2 Inference on general treatment effect (LR-test)

For an LR-Test we need to first fit a reduced model:

```
modnb.null <- glm.nb(abu ~ 1, data = dfm)</pre>
```

, so that the dispersion parameter  $\kappa$  is re-estimated for the reduced model. Then we can compare these two models with a LR-Test:

```
anova(modnb, modnb.null, test = 'Chisq')
## Likelihood ratio tests of Negative Binomial Models
##
## Response: abu
        Model
                theta Resid. df
                                   2 x log-lik.
                                                 Test
                                                        df LR stat.
            1 1.861577 17
                                      -181.2281
## 1
                                      -167.2383 1 vs 2 5 13.98985
## 2 treatment 3.905898
                            12
##
     Pr(Chi)
## 1
## 2 0.015674
```

, which suggests a treatment related effect on abundances.

#### 1.5.3 Inference on general treatment effect (parametric bootstrap)

To test the LR statistic using paramtric bootstrap, we use two custom functions:

The first function myPBrefdist generates a boostrap sample and return the LR statistic for this sample:

```
#' PB of LR statistic
#' @param m1 Full model
#' @param mO reduced model
#' @param data data used in the models
#' @return LR of boostrap
# generate reference distribution
myPBrefdist <- function(m1, m0, data){</pre>
  # simulate from null
  x0 <- simulate(m0)</pre>
  # refit with new data
  newdata0 <- data
  newdata0[ , as.character(formula(m0)[[2]])] <- x0</pre>
  m1r <- try(update(m1, .~., data = newdata0), silent = TRUE)</pre>
  mOr <- try(update(m0, .~., data = newdata0), silent = TRUE)</pre>
  # check convergence (otherwise return NA for LR)
  if(inherits(m0r, "try-error") | inherits(m1r, "try-error")){
    LR <- 'convergence error'
  } else {
    if(!is.null(m0r[['th.warn']]) | !is.null(m1r[['th.warn']])){
      LR <- 'convergence error'
    } else {
      LR \leftarrow -2 * (logLik(m0r) - logLik(m1r))
  return(LR)
```

The second one (myPBmodcomp) repeats myPBrefdist many time and returns a p-value:

```
#' generate LR distribution and return p value
#' @param m1 Full model
#' @param mO reduced model
#' @param data data used in m1 and m0
#' @param npb number of bootstrap samples
#' @return p-value of boostrapped LR values
myPBmodcomp <- function(m1, m0, data, npb){</pre>
  ## calculate reference distribution
  LR <- replicate(npb, myPBrefdist(m1 = m1, m0 = m0, data = data),
                   simplify = TRUE)
  LR <- as.numeric(LR)</pre>
  nconv_LR <- sum(!is.na(LR))</pre>
  ## original stats
  LRo \leftarrow c(-2 * (logLik(m0) - logLik(m1)))
  ## p-value from parametric bootstrap
  p.pb <- mean(c(LR, LRo) >= LRo, na.rm = TRUE)
  return(list(nconv_LR = nconv_LR, p.pb = p.pb))
```

Sounds complicated, but we can easily apply this to the negative binomial model using:

```
set.seed(1234)
myPBmodcomp(modnb, modnb.null, data = dfm, npb = 500)

## $nconv_LR
## [1] 499
##
## $p.pb
## [1] 0.042
```

Here, we specify to generate 500 bootstrap samples (npb = 500). Of these 500 samples, 499 converged (nconv\_LR) (one did not and throws some errors) and gives a p-value of 0.042.

#### 1.5.4 Inference on LOEC

This is similar to the other parametric models:

```
summary(glht(modnb, linfct = mcp(treatment = 'Dunnett'), alternative = 'less'),
        test = adjusted('holm'))
##
     Simultaneous Tests for General Linear Hypotheses
##
##
## Multiple Comparisons of Means: Dunnett Contrasts
##
##
## Fit: glm.nb(formula = abu ~ treatment, data = dfm, init.theta = 3.905898474,
       link = log)
##
##
## Linear Hypotheses:
##
                       Estimate Std. Error z value
                                                     Pr(\langle z)
## T0.1 - Control >= 0 -0.5092
                                    0.3951 -1.289 0.098731 .
## T0.3 - Control >= 0 -0.9970
                                    0.3988 -2.500 0.018615 *
## T1 - Control >= 0
                                    0.3975 -2.153 0.031300 *
                        -0.8560
## T3 - Control >= 0
                        -1.6032
                                    0.4066 -3.943 0.000201 ***
## T10 - Control >= 0
                        -1.4313
                                    0.4601 -3.111 0.003727 **
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## (Adjusted p values reported -- holm method)
```

which suggests a LOEC at the 0.3 mg/l treatment.

## 1.6 Non-parametric methods

#### 1.6.1 Kruskal-Wallis Test

We can use the Kruskal-Wallies test to check if there is a difference between treatments:

```
kruskal.test(abu ~ treatment, data = dfm)

##

##

Kruskal-Wallis rank sum test
##
```

```
## data: abu by treatment
## Kruskal-Wallis chi-squared = 8.219, df = 5, p-value = 0.1446
```

#### 1.6.2 Pairwise Wilcoxon test

To determine the LOEC we could use a Pairwise Wilcoxon test. The built-in pairwise.wilcox.test() compares by default all levels (Tukey-contrasts). We are only interested in a subset of these comparisons (Dunnett-contrast).

Therefore, we use a custom function, which is a wrapper around wilcox.exact() from the exactRankTests package:

```
#' pairwise wilcox.test with dunnett contrasrs
#' @param y numeric; vector of data values
#' @param g factor; grouping vector
#' @param dunnett logical; if TRUE dunnett contrast, otherwise Tukey-contrasts
#' @param padj character; method for p-adjustment, see ?p.adjust.
#' Oparam ... other arguments passed to wilcox.exact {exactRankTests}
pairwise_wilcox <- function(y, g, dunnett = TRUE, padj = 'holm', ...){</pre>
  if(!require(exactRankTests)){
    stop('Install exactRankTests package')
  tc <- t(combn(nlevels(g), 2))
  # take only dunnett comparisons
  if(dunnett){
    tc <- tc[tc[ , 1] == 1, ]
  pval <- numeric(nrow(tc))</pre>
  # use wilcox.exact (for tied data)
  for(i in seq_len(nrow(tc))){
    pval[i] <- wilcox.exact(y[as.numeric(g) == tc[i, 2]],</pre>
                             y[as.numeric(g) == tc[i, 1]], exact = TRUE,
                             ...)$p.value
  # adjust p-values
  pval <- p.adjust(pval, padj)</pre>
  names(pval) = paste(levels(g)[tc[,1]], levels(g)[tc[,2]], sep = ' vs. ')
  return(pval)
```

Here, we use one-sided Dunnett contrasts and adjust p-values using Holm's method:

This indicates no treatment effect at no level of concentration.

## 2 Binomial data example

#### 2.1 Introduction

Here we will show how to analyse binomial data (x out of n). Data is provided in Newman (2012) (example 5.1, page 223) and EPA (2002). Ten fathead minnow ( $Pimephales\ promelas$ ) larvals were exposed to sodium pentachlorophenol (NaPCP) and proportions of the total number alive at the end of the exposure reported.

First we load the data:

```
df <- read.table(header = TRUE, text = 'conc A B C D</pre>
0 1 1 0.9 0.9
32 0.8 0.8 1 0.8
64 0.9 1 1 1
128 0.9 0.9 0.8 1
256 0.7 0.9 1 0.5
512 0.4 0.3 0.4 0.2')
df
##
            A B
                    С
     conc
## 1
       0 1.0 1.0 0.9 0.9
      32 0.8 0.8 1.0 0.8
## 3
     64 0.9 1.0 1.0 1.0
## 4 128 0.9 0.9 0.8 1.0
## 5 256 0.7 0.9 1.0 0.5
## 6 512 0.4 0.3 0.4 0.2
```

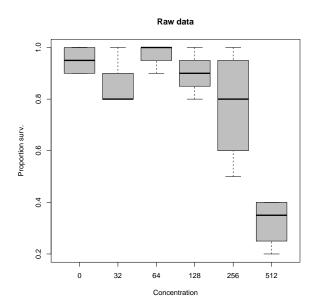
The we do some house-keeping, reformat the data and convert concentration to a factor:

```
require(reshape2)
# wide to long
dfm <- melt(df, id.vars = 'conc', value.name = 'y', variable.name = 'tank')
# conc as factor
dfm$conc <- factor(dfm$conc)</pre>
```

So after data cleaning the data looks like

```
head(dfm)
##
     conc tank
## 1
        0
             A 1.0
## 2
       32
             A 0.8
             A 0.9
## 3
     64
## 4
     128
             A 0.9
## 5 256
             A 0.7
## 6 512
             A 0.4
```

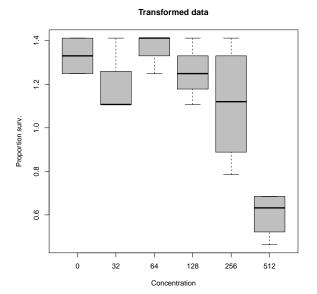
Let's have a first look at the data:



This plot indicates a strong effect at the highest concentration.

## 2.2 Assuming a normal distribution of transformed proportions

First, we arcsine transform (eqn. 6) the proportions:



Then, like in the count data example we fit the model using lm():

```
modlm <- lm(y_asin ~ conc, data = dfm)</pre>
```

The summary gives the estimated parameters:

```
summary(modlm)
##
## Call:
## lm(formula = y_asin ~ conc, data = dfm)
##
## Residuals:
##
       Min
                 1Q
                     Median
                                   3Q
                                           Max
##
  -0.32401 -0.08149 -0.00527 0.08150
                                       0.30261
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
                          0.07693
                                   17.295 1.16e-12 ***
## (Intercept) 1.33053
## conc32
              -0.14717
                          0.10880
                                   -1.353
                                            0.1929
## conc64
               0.04074
                          0.10880
                                    0.374
                                             0.7124
## conc128
              -0.07622
                          0.10880
                                   -0.701
                                             0.4925
## conc256
              -0.22113
                          0.10880
                                   -2.032
                                             0.0571 .
## conc512
              -0.72735
                          0.10880
                                   -6.685 2.86e-06 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1539 on 18 degrees of freedom
## Multiple R-squared: 0.7871, Adjusted R-squared: 0.7279
## F-statistic: 13.31 on 5 and 18 DF, p-value: 1.612e-05
```

The F-test suggests a treatment related effect:

```
drop1(modlm, test = 'F')

## Single term deletions

##

## Model:

## y_asin ~ conc

## Df Sum of Sq RSS AIC F value Pr(>F)

## <none> 0.42613 -84.746

## conc 5 1.5753 2.00142 -57.621 13.308 1.612e-05 ***

## ---

## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

And the LOEC is at the highest concentration:

```
summary(glht(modlm, linfct = mcp(conc = 'Dunnett'), alternative = 'less'),
       test = adjusted('holm'))
##
##
     Simultaneous Tests for General Linear Hypotheses
##
## Multiple Comparisons of Means: Dunnett Contrasts
##
##
## Fit: lm(formula = y_asin ~ conc, data = dfm)
## Linear Hypotheses:
##
               Estimate Std. Error t value
                                             Pr(<t)
## 32 - 0 \ge 0 -0.14717 0.10880 -1.353
                                              0.289
## 64 - 0 >= 0 0.04074
                          0.10880 0.374
                                              0.644
## 128 - 0 >= 0 -0.07622
                          0.10880 - 0.701
                                              0.493
## 256 - 0 \ge 0 -0.22113   0.10880   -2.032
                                              0.114
## 512 - 0 >= 0 -0.72735
                           0.10880 -6.685 7.14e-06 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Adjusted p values reported -- holm method)
```

## 2.3 Assuming a binomial distribution

The binomial model with a logit link (eqn. 7) between predictors and response can be fitted using the glm() function:

Here the weights arguments, indicates how many fish where exposed in each treatment (N=10, eqn .7).

The summary gives the estimated parameters:

```
summary(modglm)
##
## Call:
## glm(formula = y ~ conc, family = binomial(link = "logit"), data = dfm,
     weights = rep(10, nrow(dfm)))
##
## Deviance Residuals:
     Min 1Q Median
                              3Q
                                      Max
## -1.8980 -0.5723 0.0000 0.7869
                                   2.2578
##
## Coefficients:
            Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) 2.9444 0.7255 4.059 4.94e-05 ***
## conc32 -1.2098
                       0.8499 -1.423 0.1546
## conc64
              0.7191
                       1.2458 0.577 0.5638
             -0.7472
## conc128
                       0.8967 -0.833 0.4047
             ## conc256
                       0.8002 -4.593 4.37e-06 ***
## conc512
             -3.6753
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
     Null deviance: 88.672 on 23 degrees of freedom
## Residual deviance: 23.889 on 18 degrees of freedom
## AIC: 72.862
##
## Number of Fisher Scoring iterations: 5
```

To perform a LR-test we can used the drop1() function:

```
drop1(modglm, test = 'Chisq')

## Single term deletions

##

## Model:

## y ~ conc

## Df Deviance AIC LRT Pr(>Chi)

## <none> 23.889 72.862

## conc 5 88.672 127.645 64.783 1.243e-12 ***

## ---

## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Also with the binomial model the LOEC is at the highest concentration:

```
## Multiple Comparisons of Means: Dunnett Contrasts
##
##
## Fit: glm(formula = y ~ conc, family = binomial(link = "logit"), data = dfm,
       weights = rep(10, nrow(dfm)))
##
##
## Linear Hypotheses:
                Estimate Std. Error z value
                                               Pr(\langle z)
## 32 - 0 >= 0
                -1.2098
                             0.8499
                                    -1.423
                                               0.2319
## 64 - 0 >= 0
                 0.7191
                                      0.577
                             1.2458
                                               0.7181
## 128 - 0 >= 0 -0.7472
                             0.8967
                                     -0.833
                                               0.4047
## 256 - 0 >= 0 -1.7077
                             0.8183
                                     -2.087
                                               0.0738
## 512 - 0 >= 0 -3.6753
                             0.8002 -4.593 1.09e-05 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## (Adjusted p values reported -- holm method)
```

## References

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