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Matrix theory Assignment 1

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Abstract—This document explains the equation of the line passing through the point of intersection of the lines that has equal intercepts on the axes

Download all python codes from

https://github.com/pavanmanesh/EE5609/tree/master/codes

and latex-tikz codes from

https://github.com/pavanmanesh/EE5609

1 Problem

Find the equation of the line passing through the point of intersection of the lines

$$(4 7)\mathbf{x} = 3$$
$$(2 -3)\mathbf{x} = -1$$

that has equal intercepts on the axes

2 Solution

Constructing the augmented matrix

$$\begin{pmatrix} 4 & 7 & 3 \\ 2 & -3 & -1 \end{pmatrix}$$

Transforming the matrix into row-echelon form

$$\begin{pmatrix} 4 & 7 & 3 \\ 2 & -3 & -1 \end{pmatrix} \xrightarrow{R2 \leftarrow 2R2 - R1}$$

$$\begin{pmatrix} 4 & 7 & 3 \\ 0 & -13 & -5 \end{pmatrix} \xrightarrow{R2 \leftarrow -R2/13, R1 \leftarrow R1/4}$$

$$\begin{pmatrix} 1 & 7/4 & 3/4 \\ 0 & 1 & 5/13 \end{pmatrix} \xrightarrow{R1 \leftarrow R1 - 7/4R1/4}$$

$$\begin{pmatrix} 1 & 0 & 2/26 \\ 0 & 1 & 5/13 \end{pmatrix}$$

$$(2.0.1)$$

Thus, The point of intersection is at point (2/26, 5/13) i.e. (0.07, 0.38)

The equation of line in terms of vector notations can be written as

$$\mathbf{n}^T \mathbf{x} = b$$
 where $\mathbf{n} = \begin{pmatrix} n_{11} \\ n_{12} \end{pmatrix}$ (2.0.2)

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$$\begin{pmatrix} n_{11} & n_{12} \end{pmatrix} \mathbf{x} = b \tag{2.0.3}$$

Let the intercepts be $\binom{a}{0}$, $\binom{0}{b}$ respectively. As the required line passes through the point of intersection (2/26, 5/13) and the intercepts are equal, the intercepts can be written as: $\binom{6/13}{0}$ and $\binom{0}{6/13}$.

When the line passes through

$$(6/13 \quad 6/13)$$
 (2.0.4)

upon substitution we get,

$$\frac{6}{13}n_{11} = b \implies n_{11} = \frac{b}{6/13} \tag{2.0.5}$$

$$\frac{6}{13}n_{12} = b \implies n_{12} = \frac{b}{6/13} \tag{2.0.6}$$

Therefore, the equation of the line is

$$\left(\frac{b}{6/13} \quad \frac{b}{6/13}\right)\mathbf{x} = b \tag{2.0.7}$$

$$\implies \begin{pmatrix} 1 & 1 \end{pmatrix} \mathbf{x} = 6/13 \tag{2.0.8}$$

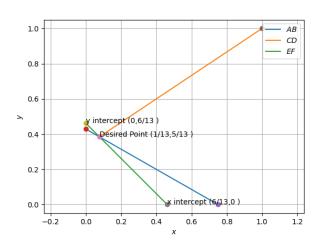


Fig. 0: The intercepts of the required line are equal