

Math Document Template

C ANISH

Abstract—This is a document explaining a question about the concept of vector addition.

Download all python codes from

```
svn co https://github.com/chakki1234/summer
-2020/trunk/linearalg/codes
```

and latex-tikz codes from

```
svn co https://github.com/chakki1234/summer
-2020/trunk/linearalg/figs
```

1 PROBLEM

A motorboat is racing towards north at 25 km/h and the water current in that region is 10 km/h in the direction of 60° east of south. Find the resultant velocity of the boat.

2 CONSTRUCTION

2.1. Draw Fig. 2.1.

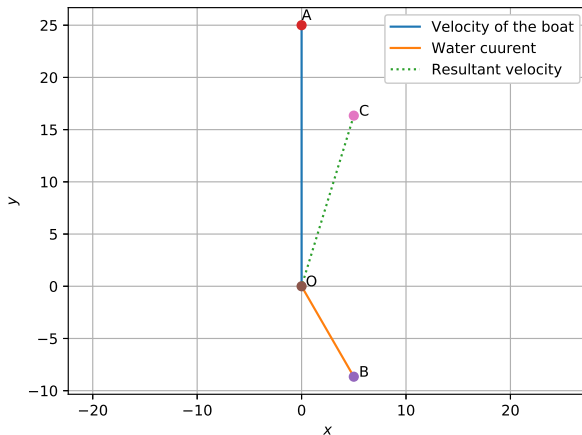


Fig. 2.1: Vectorial representation of velocities generated using python

Solution: The following Python code generates Fig. 2.1

```
codes/motion_plane.py
```

3 SOLUTION

Solution: Let **A** denote the velocity of the boat and **B** denote the water current and **C** represent the resultant velocity.

$$\mathbf{A} = \begin{pmatrix} 0 \\ 25 \end{pmatrix} \quad (1.1)$$

$$\mathbf{B} = \begin{pmatrix} 5 \\ -8.67 \end{pmatrix} \quad (1.2)$$

$$\mathbf{C} = \mathbf{A} + \mathbf{B} \quad (1.3)$$

$$\mathbf{C} = \begin{pmatrix} 5 \\ 16.34 \end{pmatrix} \quad (1.4)$$

Magnitude of the resultant velocity:

$$\|\mathbf{C}\| = 17.08 \quad (1.5)$$

Direction of resultant velocity:

$$\cos \theta = \frac{(\mathbf{A})^T (\mathbf{C})}{\|\mathbf{A}\| \|\mathbf{C}\|} \quad (1.6)$$

$$\theta = 17.01^\circ \quad (1.7)$$

\therefore The resultant velocity is 17.08 km/h at an angle of 17.01° east of north.