Math Document Template

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Abstract—This is a document explaining a question about the concept of multiplying two complex numbers using matrices.

Download all python codes from

svn co https://github.com/chakki1234/summer -2020/trunk/linearalg/codes

and latex-tikz codes from

svn co https://github.com/chakki1234/summer -2020/trunk/linearalg/figs

1 Problem

Find
$$\begin{pmatrix} -\sqrt{3} \\ \sqrt{2} \end{pmatrix} \begin{pmatrix} 2\sqrt{3} \\ -1 \end{pmatrix}$$

2 Solution

A complex number $\binom{a}{b}$ can be represented as 2 x 2 matrix:

$$\begin{pmatrix} a & -b \\ b & a \end{pmatrix} \tag{2.0.1}$$

1) Multiplying the given matrices after converting them to a 2 x 2 matrix:

$$\begin{pmatrix} -\sqrt{3} & -\sqrt{2} \\ \sqrt{2} & -\sqrt{3} \end{pmatrix} \begin{pmatrix} 2\sqrt{3} & 1 \\ -1 & 2\sqrt{3} \end{pmatrix}$$
 (2.0.2)

$$\begin{pmatrix} -\sqrt{3} & -\sqrt{2} \\ \sqrt{2} & -\sqrt{3} \end{pmatrix} \begin{pmatrix} 2\sqrt{3} & 1 \\ -1 & 2\sqrt{3} \end{pmatrix}$$
 (2.0.2)
$$\begin{pmatrix} \sqrt{2} - 6 & -\sqrt{3} - 2\sqrt{6} \\ \sqrt{3} + 2\sqrt{6} & \sqrt{2} - 6 \end{pmatrix}$$
 (2.0.3)

(2.0.4)

2) Matrix 2.0.3 can be represented as a vector:

$$\therefore \begin{pmatrix} \sqrt{2} - 6 \\ \sqrt{3} + 2\sqrt{6} \end{pmatrix} \tag{2.0.5}$$

3) Python code to multiply two complex numbers: codes/line ex/complex ex/complex ex.py