Math Document Template

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Abstract—This is a document explaining a question about the concept of finding the roots of a quadratic equation.

Download all python codes from

svn co https://github.com/chakki1234/summer -2020/trunk/linearalg/codes

and latex-tikz codes from

svn co https://github.com/chakki1234/summer -2020/trunk/linearalg/figs

1 Problem

Verify whether 2 and 0 are zeroes of the polynomial $x^2 - 2x$.

2 Construction

2.1. Draw Fig. 2.1.

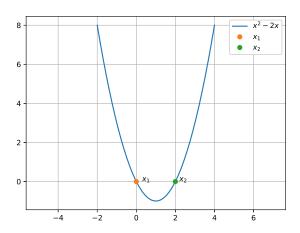


Fig. 2.1: $x^2 - 2x$ generated using python

Solution: The following Python code generates Fig. 2.1

codes/conics.py

3 Solution

Solution: $p(x, y) = Ax^2 + Bxy + Cy^2 + Dx + Ey + F$ can be represented as follow in the vector form:

$$x^{T} \begin{pmatrix} A & \frac{B}{2} \\ \frac{B}{2} & C \end{pmatrix} x + \begin{pmatrix} D & E \end{pmatrix} x + F = 0$$
 (1.1)

The given equation can be represented as follows in the vector form:

$$x^{T} \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} x + \begin{pmatrix} -2 & 0 \end{pmatrix} x + 0 = 0 \tag{1.2}$$

To find the roots y = 0:

$$X^2 - 2x = 0 ag{1.3}$$

$$x(x-2) = 0 (1.4)$$

$$x = 0, 2$$
 (1.5)