PT-100 Hardware Assignment

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This chapter illustrates the use of the least squares method in finding the voltage across the PT-100 RTD (Resistance Temperature Detector) as a function of temperature.

I. Training Data

The training data gathered by the PT-100 to train the Arduino is shown in Table 0.

Temperature (°C)	**Voltage (V)**
24.4	4.58
31.0	4.59
37.8	4.60
42.5	4.61
51	4.62
62.8	4.63
72.5	4.64
89.6	6.66

TABLE 0
Training data.

The C++ source file

```
pt100/codes/data.cpp
```

was used along with *platformio* to drive the Arduino. The effective schematic circuit diagram is shown in Figure 0.

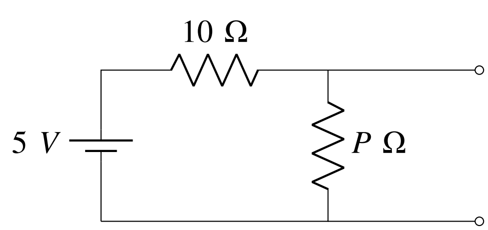

Fig. 0. Schematic Circuit Diagram to Measure the Output of PT-100 (P).

II. Model

For the PT-100, we use the Callendar-Van Dusen equation

$$V(T) = V(0)\left(1 + AT + BT^2\right) \tag{1}$$

$$\implies c = \mathbf{n}^\top \mathbf{x} \tag{2}$$

where

$$c = V(T), \ \mathbf{n} = V(0)\begin{pmatrix} 1 \\ A \\ B \end{pmatrix}, \ \mathbf{x} = \begin{pmatrix} 1 \\ T \\ T^2 \end{pmatrix} \tag{3}$$

For multiple points, (2) becomes

$$\mathbf{X}^\top \mathbf{n} = \mathbf{C} \tag{4}$$

where

$$\mathbf{X} = \begin{pmatrix} 1 & 1 & \dots & 1 \\ T_1 & T_2 & \dots & T_n \\ T_1^2 & T_2^2 & \dots & T_n^2 \end{pmatrix} \tag{5}$$

$$\mathbf{C} = \begin{pmatrix} V(T_1) \\ V(T_2) \\ \vdots \\ V(T_n) \end{pmatrix} \tag{6}$$

and $\mathbf{n}$ is the unknown.

III. Solution

We approximate $\mathbf{n}$ by using the least sqaures method. The Python code `codes/lsq.py` solves for $\mathbf{n}$. The calculated value of $\mathbf{n}$ is

$$\mathbf{n} = \begin{pmatrix} 1.6547 \\ 3.199 \times 10^{-3} \\ -3.9599 \times 10^{-6} \end{pmatrix} \tag{7}$$

The approximation is shown in Fig. 0.

Thus, the approximate model is given by

$$\begin{aligned} V(T) = 1.6547 &+ \left(3.199 \times 10^{-3}\right) T \\ &- \left(3.9599 \times 10^{-6}\right) T^2 \end{aligned} \tag{8}$$

Notice in (8) that the coefficient of T^2 is negative, and hence the governing function is strictly concave. Hence, we cannot use gradient descent methods to solve this problem.

IV. Validation

The validation dataset is shown in Table 0. The results of the validation are shown in Fig. 0.

Temperature (°C)	**Voltage (V)**
32.8	4.59
47.9	4.61
83.9	4.64
97.5	4.66

TABLE 0
Validation data.

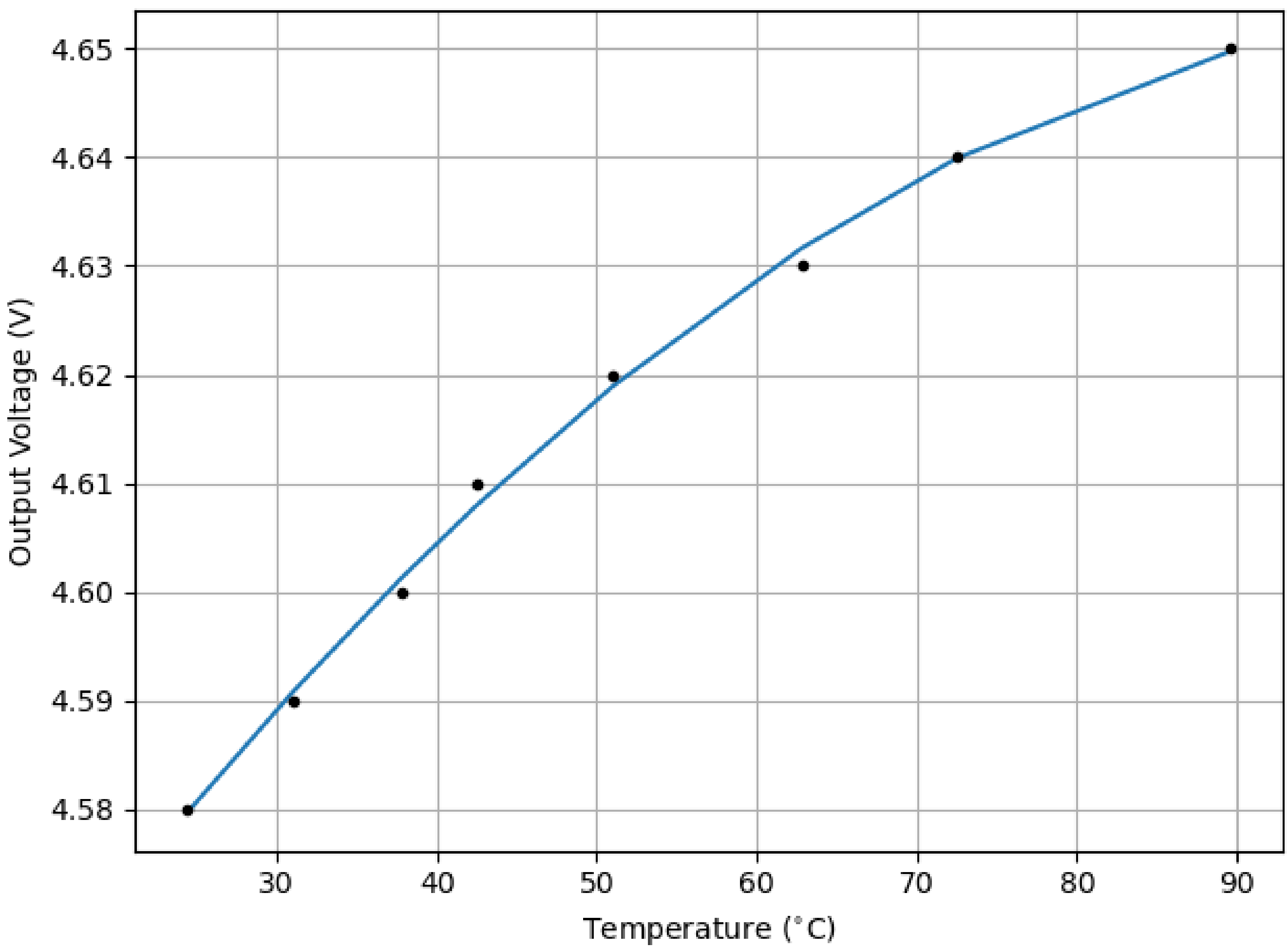

Fig. 0. Training the model.

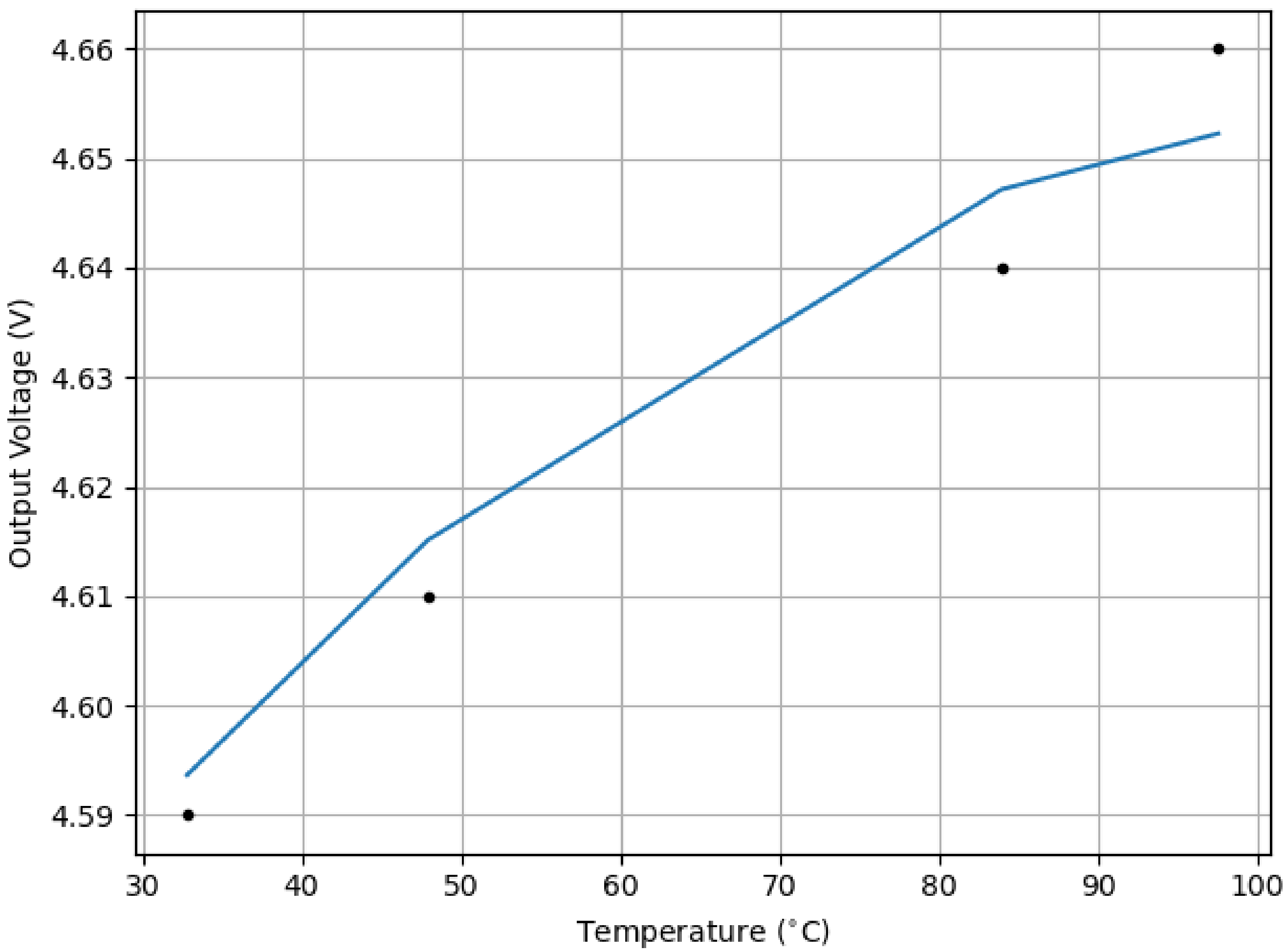

Fig. 0. Validating the model.