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# **EE1200 - ELECTRIC CIRCUITS LAB**

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# 1 BAND-PASS FILTER USING SALLEN-KEY SECOND-ORDER FILTERS

## 1.1 AIM :

- To design and implement a band-pass filter using separate Sallen-Key Low Pass Filter ( LPF ) and High Pass Filter ( HPF ) .
- To analyze and compare the frequency response of LPF, HPF, and the final band-pass filter.
- To plot the magnitude response ( gain vs frequency ) of all the three filters.

## 1.2 APPARATUS REQUIRED :

- Breadboard
- Op-Amps
- Four resistors
- Four capacitors
- Oscilloscope
- Digital function generator
- DC Power supply
- Connecting wires

## 1.3 THEORY :

A bandpass filter allows signals within a specific frequency range (*passband*) to pass while attenuating frequencies outside this range. This can be achieved by cascading a high-pass filter (HPF) and low-pass filter (LPF), where:

- HPF sets the lower cutoff frequency ( $f_{low}$ )
- LPF sets the upper cutoff frequency ( $f_{high}$ )
- Bandwidth  $B = f_{high} - f_{low}$

The combined frequency response exhibits:

- -20 dB/decade roll-off below  $f_{low}$
- -20 dB/decade roll-off above  $f_{high}$
- Flat response between  $f_{low}$  and  $f_{high}$

For first-order filters, the transfer functions are:

$$H_{HP}(s) = \frac{sRC_{HP}}{1 + sRC_{HP}} \quad (1)$$

$$H_{LP}(s) = \frac{1}{1 + sRC_{LP}} \quad (2)$$

The combined bandpass transfer function becomes:

$$H_{BP}(s) = H_{HP}(s) \cdot H_{LP}(s) = \frac{sRC_{HP}}{(1 + sRC_{HP})(1 + sRC_{LP})} \quad (3)$$

The cutoff frequencies are determined by:

$$f_{low} = \frac{1}{2\pi R_{HP}C_{HP}} \quad (4)$$

$$f_{high} = \frac{1}{2\pi R_{LP}C_{LP}} \quad (5)$$

- Cascading order affects roll-off slope (-40 dB/decade for second-order)
- Component tolerance impacts actual cutoff frequencies
- Loading effects between stages may require buffer amplifiers [5][8]
- Quality factor  $Q = \frac{f_0}{B}$ , where  $f_0 = \sqrt{f_{low}f_{high}}$

The ideal bandpass response can be represented as:

$$|H(f)| = \begin{cases} 1 & \text{if } f_{low} \leq f \leq f_{high} \\ 0 & \text{otherwise} \end{cases} \quad (6)$$

A Sallen-key second order is an active filter topology made using operational amplifiers. It provides a Butterworth, Bessel or Chebyshev response based on component selection. The corresponding transfer function is given by -

$$H(s) = \frac{A}{s^2 + \frac{\omega_c}{Q}s + \omega_c^2} \quad (7)$$

$$\omega_c - \text{Cut-off frequency } Q - \text{Quality Factor} \quad (8)$$

## 1.4 CIRCUIT DESIGN :

The three types of filters are shown in Figure 1, Figure 2 and Figure 3

## 1.5 PROCEDURE :

- Connect the HPF circuit as shown in the circuit diagram.
- A sine wave input is given using the digital function generator. The input frequency is varied and the output voltage is measured.
- The gain value is recorded for different frequencies, and is plotted against frequency ( Bode Plot ).
- Repeat the same steps with LPF and Bandpass filters.

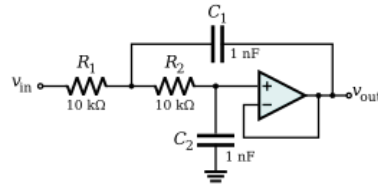


Figure 1: Low Pass Filter

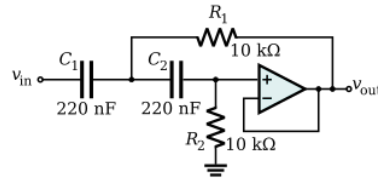


Figure 2: High Pass Filter

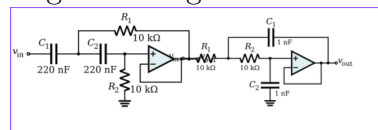


Figure 3: Band Pass Filter

## 1.6 OBSERVATION :

The frequency response of HPF, LPF and Bandpass filters can be seen in the figures attached.

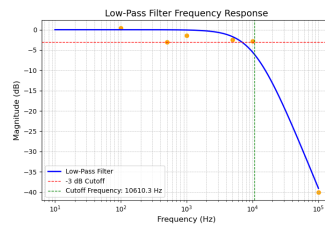


Figure 4: Mag vs Freq of Low Pass Filter

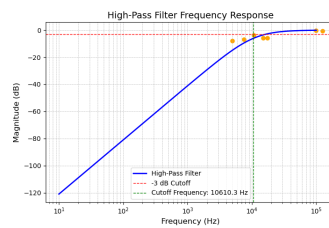


Figure 5: Mag vs Freq of High Pass Filter

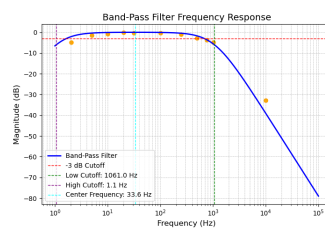


Figure 6: Mag vs Freq of Band Pass Filter

- **LOW PASS FILTER :**

$$R_1 = R_2 = 15k\Omega$$

$$C_1 = C_2 = 1nF$$

Experimental cutoff frequency =

Theoretical cutoff frequency = 10610.32 Hz

- **HIGH PASS FILTER :**

$$R_1 = R_2 = 15k\Omega$$

$$C_1 = C_2 = 1nF$$

Experimental cutoff frequency =

Theoretical cutoff frequency = 10610.32 Hz

- The bandpass filter is connected by cascading HPF and LPF, i.e., by connecting the  $v_{out}$  of LPF as  $v_{in}$  of HPF.

$$R_{LPF} = 15\Omega, R_{HPF} = 150\Omega$$

$$C_1 = C_2 = 1\mu F$$

The frequency range of BPF = 1 Hz - 1000 Hz

## 1.7 RESULT :

- Cut-off frequency for LPF of BPF = 1 Hz  
Cut-off frequency for HPF of BPF = 1 kHz
- Roll-off slope =
- Phase difference goes from 90° to 0°