



Challenging the Necessity of a Perfect Prior: Insights from a Replication and Robustness Study of NeRP

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2024.12.04

Background

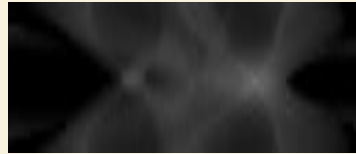
Computed Tomography (CT) Scans



How Do CT Scans Work?

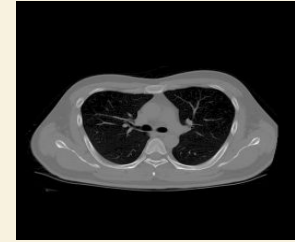


Scanning
with X-Rays



Multiple
2D Projections

Reconstruction



CT Scans

Essential for diagnosis
& treatment planning

Reconstruction

$$\mathbf{y} = \mathbf{A}\mathbf{x} + \mathbf{e}$$

Diagram illustrating the reconstruction equation $\mathbf{y} = \mathbf{A}\mathbf{x} + \mathbf{e}$:

- \mathbf{y} : Projection Signals (from device)
- \mathbf{A} : Radon Transform
- \mathbf{x} : Ground Truth CT Image
- \mathbf{e} : Acquisition Noise

Reconstruction Goal: Given \mathbf{y} , retrieve \mathbf{x}
(Approximate \mathbf{A}^{-1})

1000+ Projections are needed for **High-Quality Recon**

Issue

**1000+ Projections Per
Scan For High-Quality
Recon**

**Multiple Scans Needed
During Treatment**



**Frequent &
Prolonged Exposure
to Radiation**

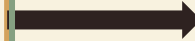
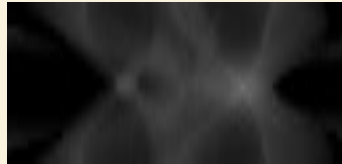
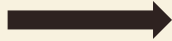
**Raised Risk
of Cancer
(to some extent)**

A Machine Learning Solution

Medical Imaging

Scan Acquisition

1000+ Projections



Reconstruction

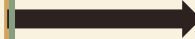
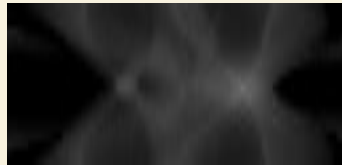
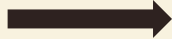
Traditional Imaging
Reconstruction



Medical Imaging + Deep Learning ?

Scan Acquisition

~~1000+~~ Projections
~20 Projections



Reconstruction

~~Traditional Imaging Reconstruction~~
Deep Learning Model



Fewer Projections → Reduced Radiation & Scanning Time

How to produce a high-quality reconstruction?

A Machine Learning Solution: NeRP^[1]

770

IEEE TRANSACTIONS ON NEURAL NETWORKS AND LEARNING SYSTEMS, VOL. 35, NO. 1, JANUARY 2024

NeRP: Implicit Neural Representation Learning With Prior Embedding for Sparsely Sampled Image Reconstruction

Liyue Shen^{ID}, *Student Member, IEEE*, John Pauly^{ID}, *Senior Member, IEEE*, and Lei Xing^{ID}

**Multi-Layer Perceptron
(MLP)**

Previous CT
for Pre-Training

[Sparsely Sampled] ~20 Projs
[Densely Sampled] 1000+ Projs

[1] Shen, L.; Pauly, J.; and Xing, L. 2022. NeRP: Implicit Neural Representation Learning With Prior Embedding for Sparsely Sampled Image Reconstruction. IEEE Transactions on Neural Networks and Learning Systems, 770–782.

NeRP's Contributions & Significance

Novel method for sparsely sampled medical image reconstruction

**State-of-the-art
performance**

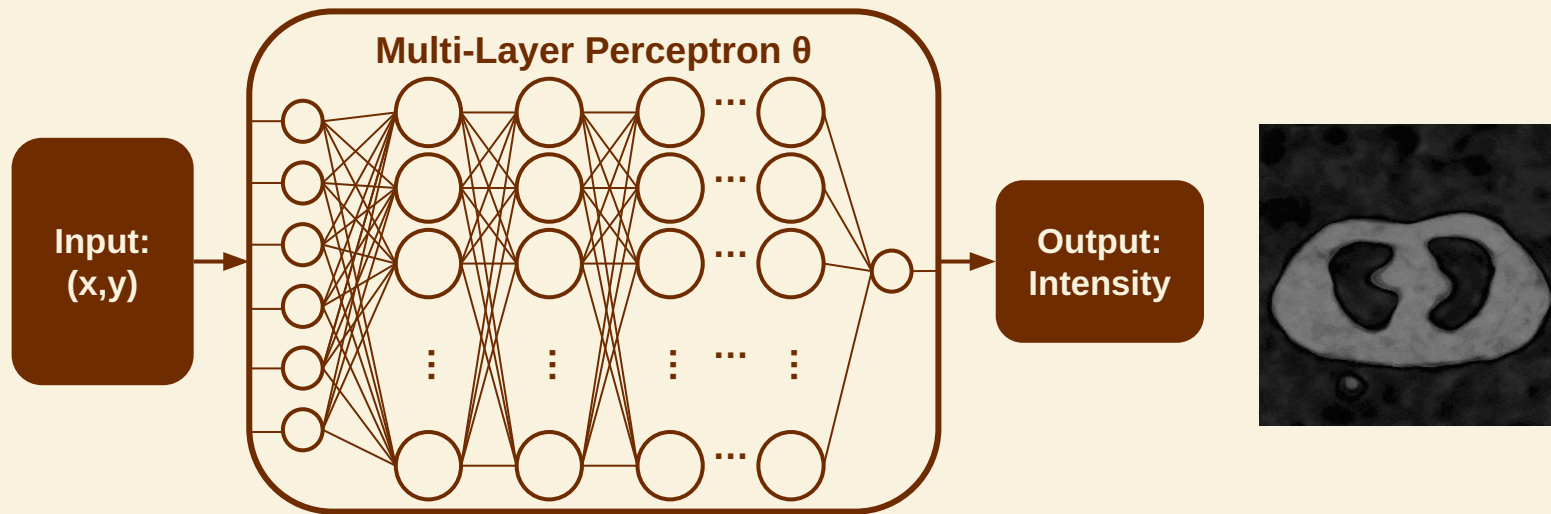
**Demonstrates the
importance of a prior
image for pre-training**

**Leverages a patient's prior
image for patient-specific
neural representation**

- Not reliant on large training datasets
 - More generalizable across diff imaging modalities & anatomical sites

NeRP Replication - Technical Details

NeRP Replication: 2-D CT Reconstruction



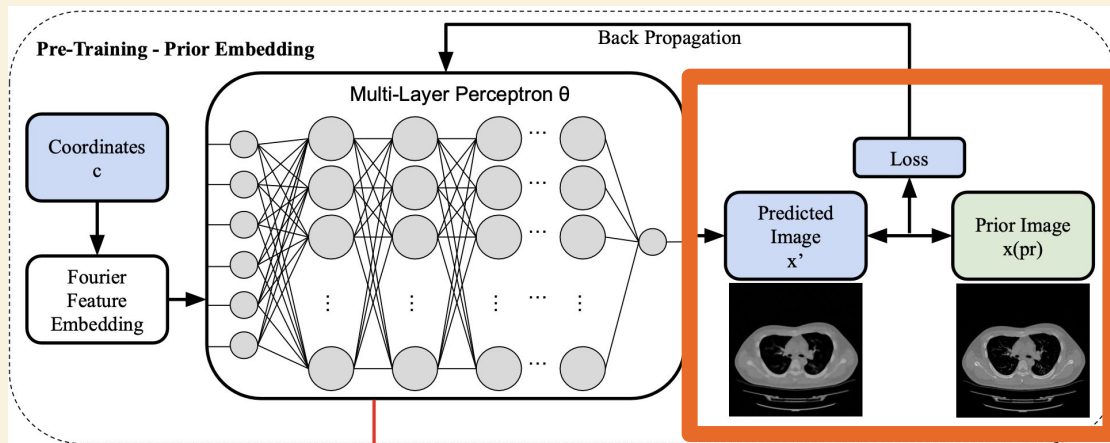
Technical Steps

Prior Embedding

MLP learns a **continuous function $M(\theta)$**

$M(\theta)$: maps the coordinates to intensity values of the **prior image**

Loss: between **CT Images**



Technical Steps

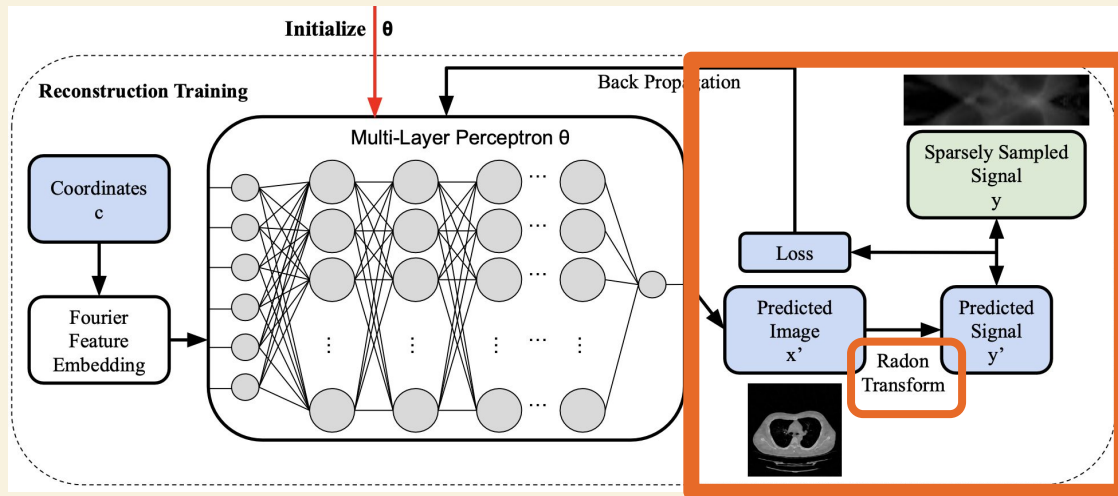
Prior
Embedding θ

Network
Training

MLP is initialized as $M(\theta)$

Fine-tuning with sparsely sampled projections to get $M(\theta')$

Loss: between **Projection Signals**



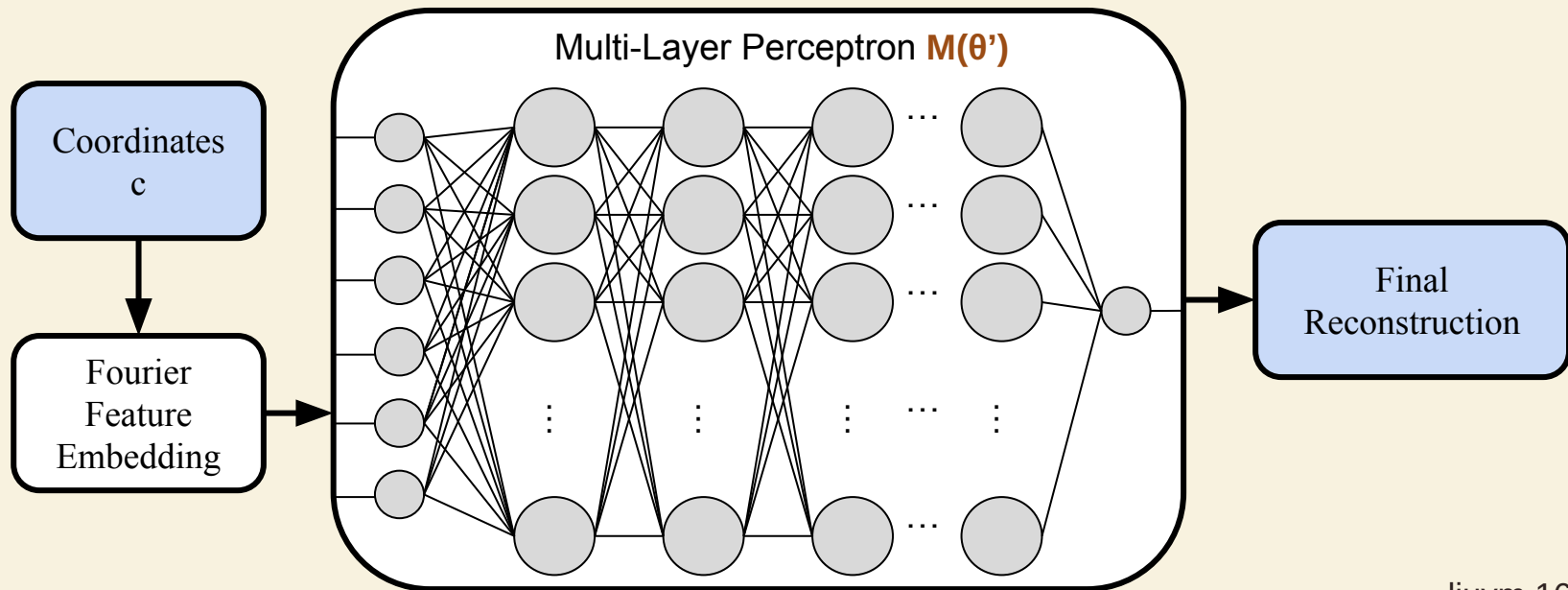
Technical Steps

Prior
Embedding θ

Network
Training θ'

Image
Inference

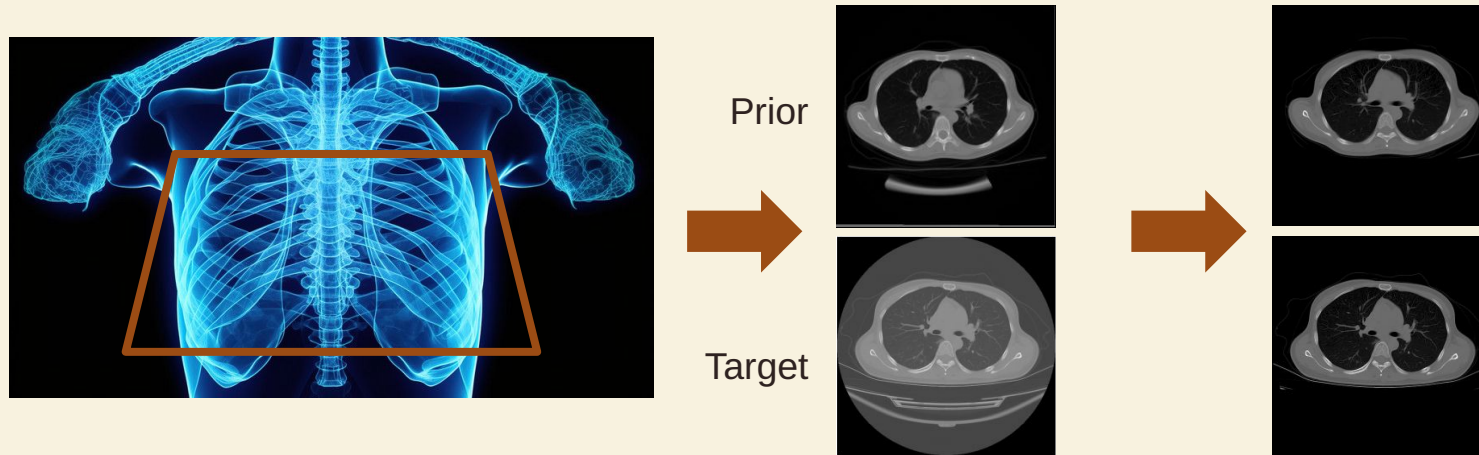
Trained MLP generates final image with $M(\theta')$



NeRP Replication - Data & Result

Replication: Dataset & Pre-Processing

- 3D Chest CT scans from 'CT Images in Covid 19'[2]
 - Each patient has **2 scans** obtained several days apart
- 2D slices preprocessed for experiments
 - Clipping & Normalization; Alignment; Device Bed Masking



Replication: Evaluation Metrics

Peak Signal-to-Noise Ratio (**PSNR**):

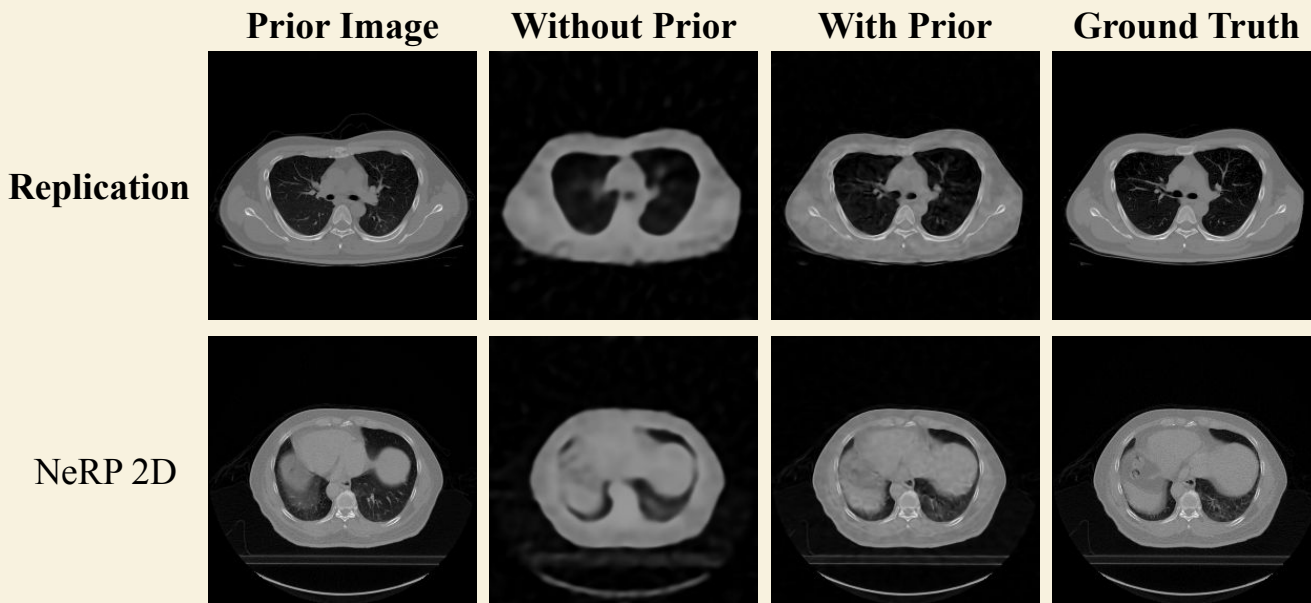
- Comparing maximum signal power to noise
- Higher Value → Better

Structural Similarity Index Measure (**SSIM**):

- Evaluating luminance, contrast, and structural similarity
- SSIM of 1.0 → Perfect

Replication Results

	With Prior PSNR/SSIM	Without Prior PSNR/SSIM
Replication	30.42/0.734	28.61/0.623
NeRP 2D	34.87/0.886	27.08/0.660



Extension - Idea & Results

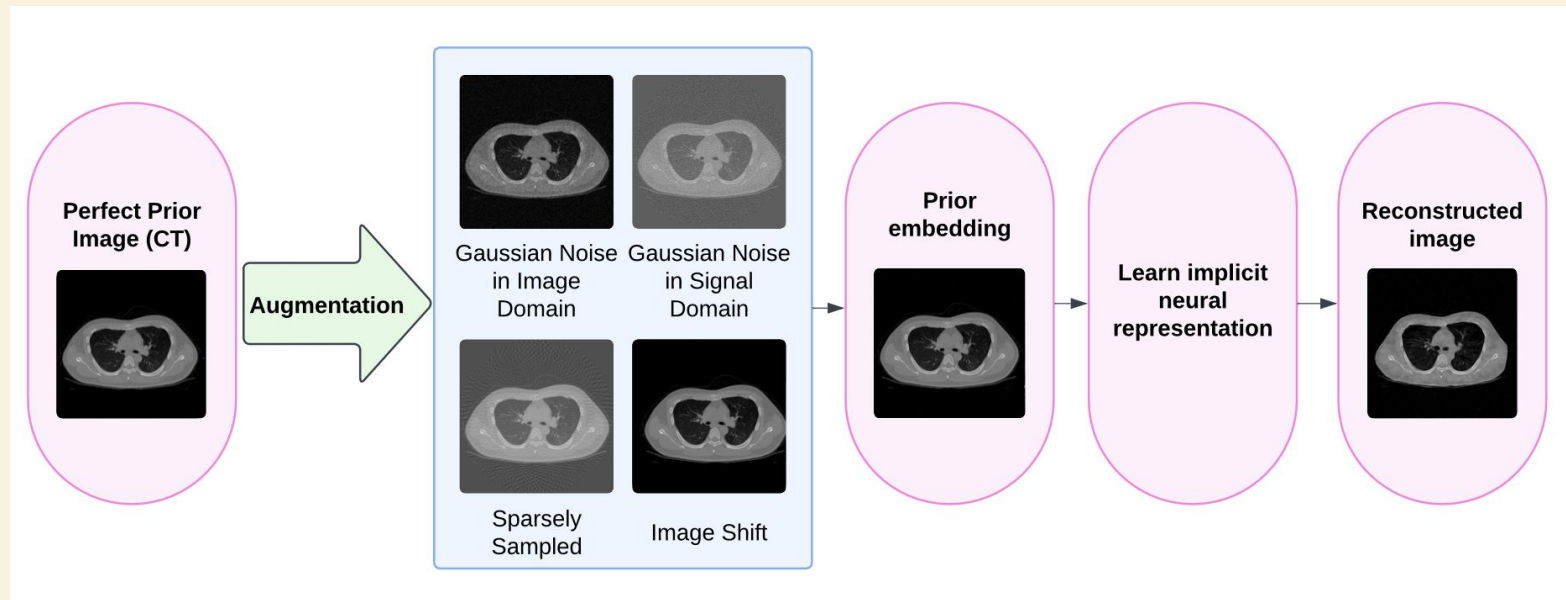
Research Problem (Extension)

Our Observation:

NeRP was only tested with a **perfect (high quality) prior** and **no prior**

How does a **reduction** in the **quality** of prior images impact a model's ability to implicitly learn a **neural representation** to perform image reconstruction?

Extension Pipeline



Extension Results

- Most noise types do not have much impact on reconstruction quality.

Prior Type	PSNR(dB)	SSIM
Perfect Prior	30.89	0.821
Gaussian Noise (Image Domain)	30.80	0.819
Gaussian Noise (Signal Domain)	31.13	0.819
Sparse Sampling	31.32	0.848

Table 2: Results of 2D CT reconstruction with priors altered with different noises; Noisy priors have a PSNR \approx 40dB.

Extension Results

Ground Truth

Reconstruction



with Perfect Prior



with Noisy Prior
(Gaussian Signal)



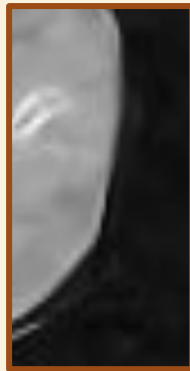
Extension Results: Shifting

- Shifting resulted in degraded reconstruction performance
- Larger shifts led to ghosting artifacts

X-Shift(pixel)	PSNR(dB)	SSIM
0	30.89	0.821
5	30.67	0.826
10	29.41	0.735
20	28.74	0.668

Reconstruction

5-pixel prior
shift



10-pixel prior
shift



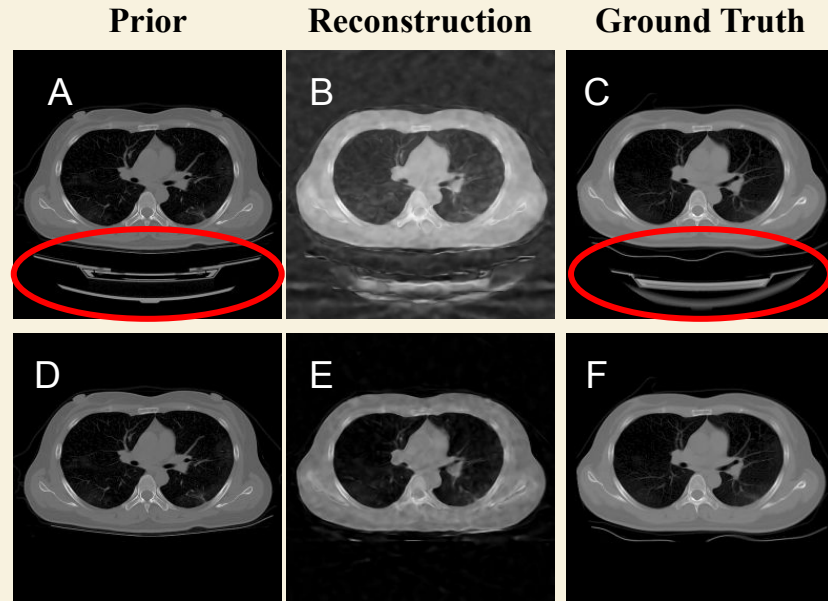
20-pixel prior
shift



Discussion

Accidental Discovery: Device Bed Inconsistency

- Initially getting poor results for a specific patient
- Prior and target images were taken on **different device bed shapes**



Key Extension Findings

NeRP is robust to most types of noise

⇒ produces high-quality reconstructions with noisy priors

- Noise in images and signal domain has minimal effect on reconstruction
- Spatial misalignment from shifting and device beds have a larger effect
 - Need for consistent patient positioning
 - Keep the device consistent in applications

Societal Impact



Robustness to Noisy Priors

Expands NeRP's potential application in clinical settings.



Guidance for Effective Applications

Spatial alignment and device consistency needed for optimal deployment.



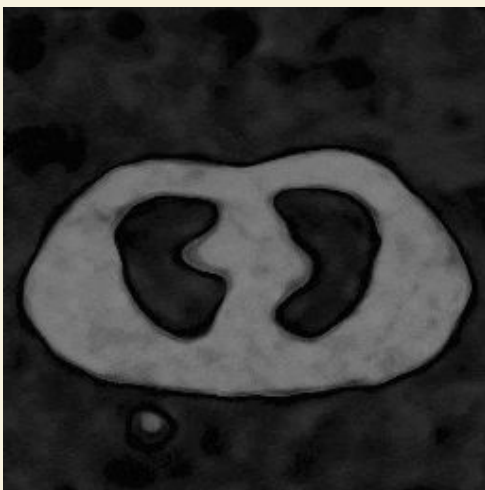
Step Towards Efficient CT Reconstruction

Reduces scanning time and radiation exposure.



Broad Implication

Opens new opportunities for effective imaging solutions in healthcare.



Thanks!

Have any questions?

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