

Chapter 4 Homework Answers

2023-02-01

Contents

Chapter 4: Longwave Radiation Spectrum	1
Exercise 4.1: Methane	1
Part (a)	1
Part (b)	2
Part (c)	4
Part (d)	6
Exercise 4.3: Water vapor	6
Part (a)	6
Part (b)	8
Part (c)	9

Chapter 4: Longwave Radiation Spectrum

Exercise 4.1: Methane

Methane has a current concentration of 1.7 ppm in the atmosphere and is doubling at a faster rate than CO₂.

Part (a)

Would an additional 10 ppm of methane in the atmosphere have a larger or smaller impact on the outgoing IR flux than an additional 10 ppm of CO₂ at current concentrations?

Answer: I ran MODTRAN three times.

- One run was a baseline, which used the current concentrations of CO₂ and CH₄.
- Then I ran MODTRAN with the CO₂ concentration increased by 10 ppm.
- Finally, I ran it a third time with the baseline value for CO₂, but with CH₄ increased by 10 ppm.

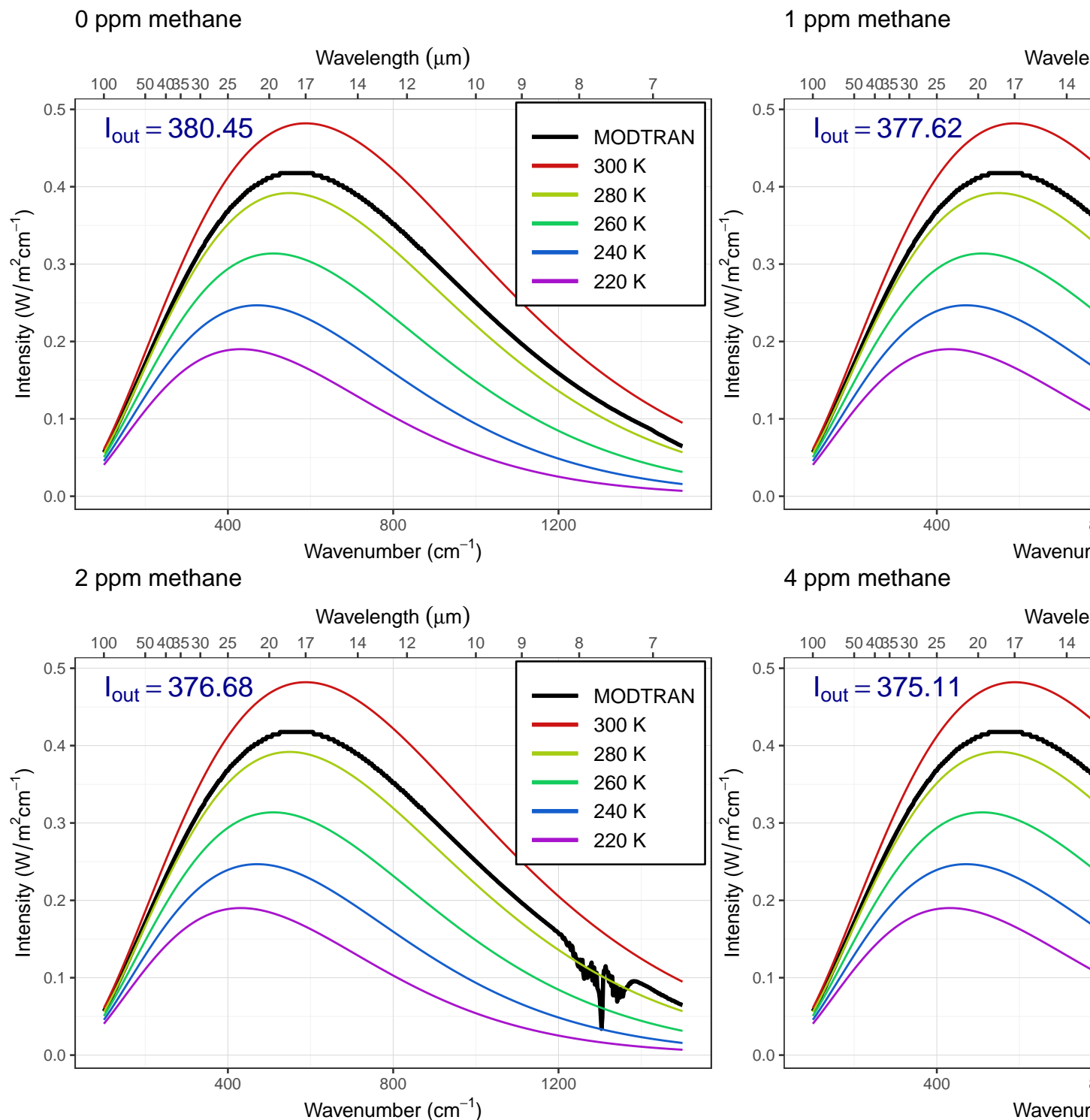
For the baseline run, the intensity of outgoing longwave light was 299. Watts per square meter. Increasing CO₂ by 10 ppm decreased the outgoing longwave light by 0.1 W/m², to 298. and increasing CH₄ by 10 ppm decreased the outgoing longwave light by 3.1 W/m² to 296.. The change in I_{out} for methane is is around 25. times as much as for CO₂.

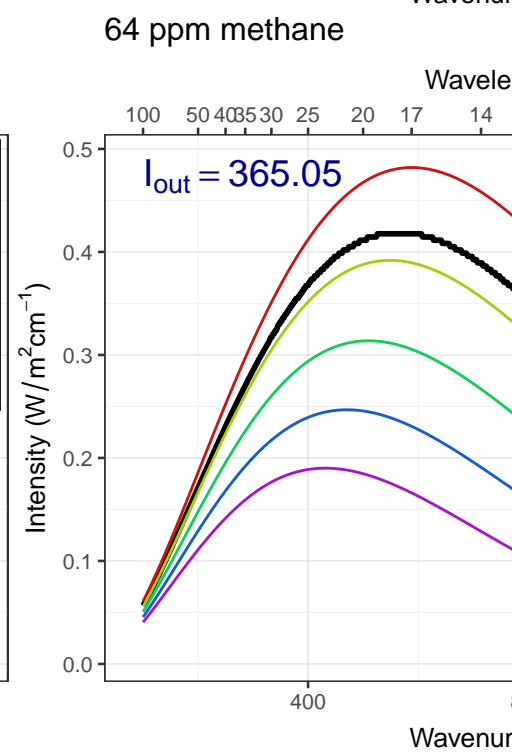
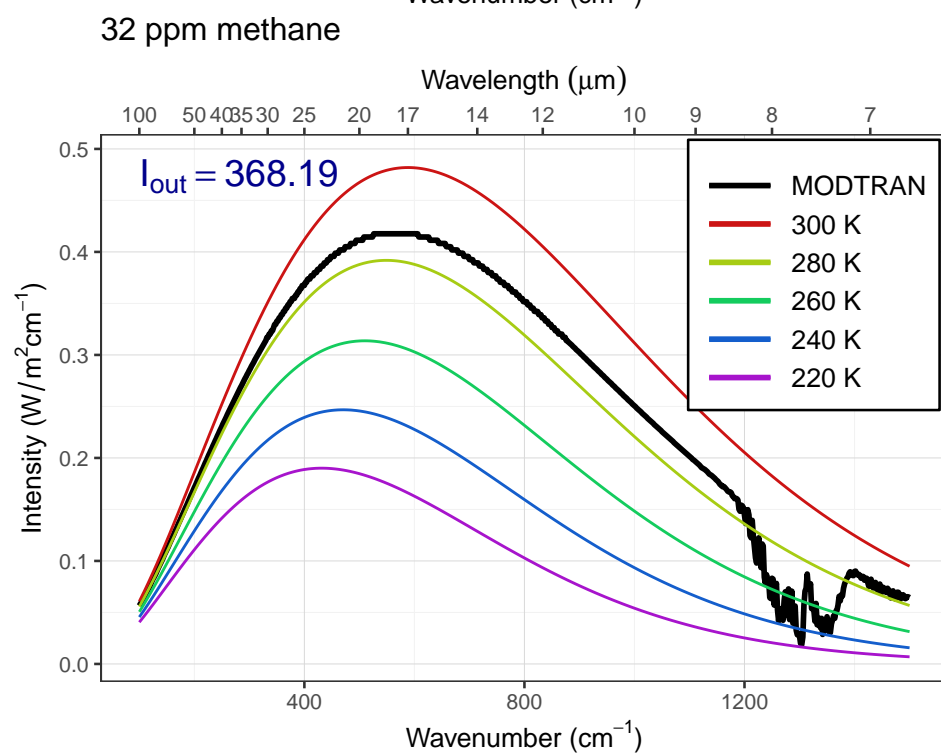
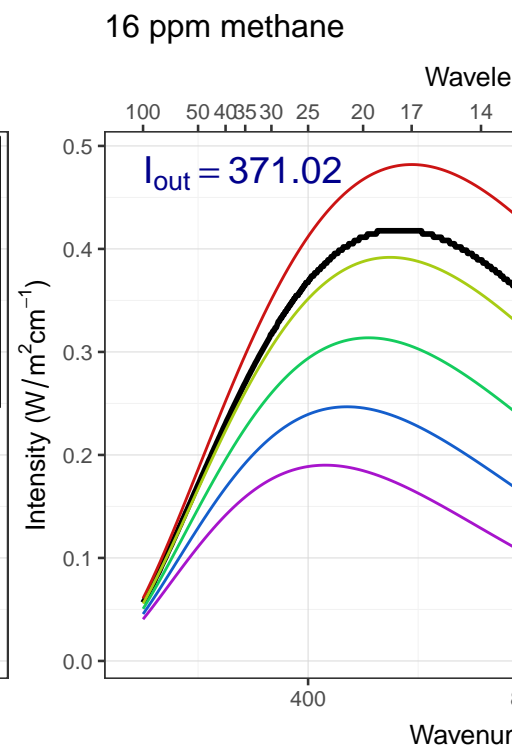
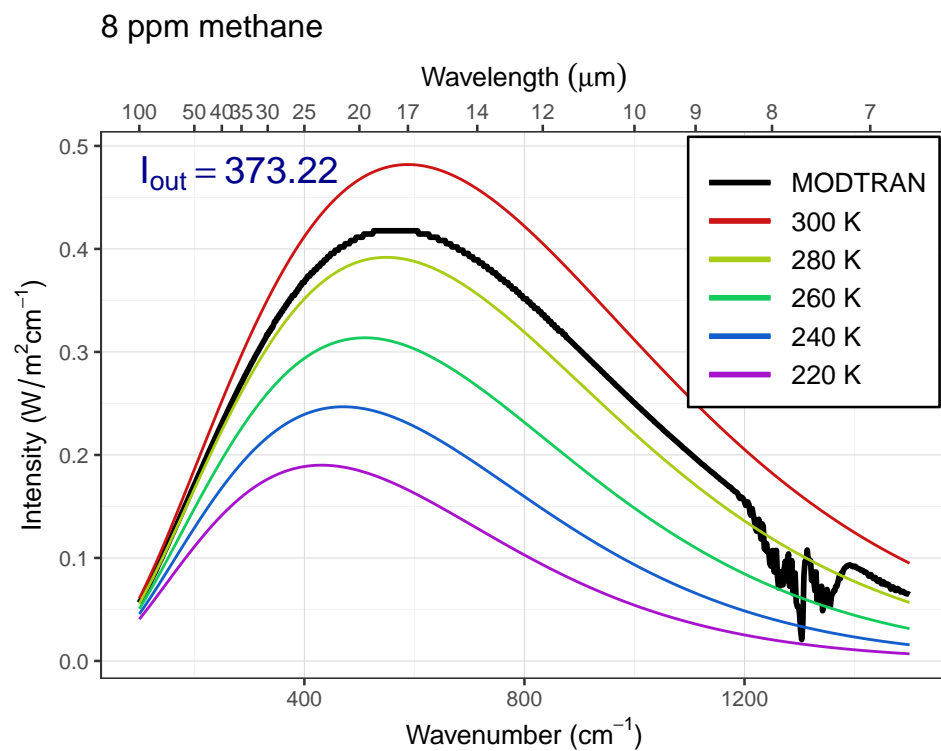
The difference is because absorption for CO₂ is strongly saturated, but the absorption for CH₄ is not saturated. Another way to think about this is that a 10 ppm increase in CO₂ increases the amount of CO₂ by 2.% and a 10 ppm increase in CH₄ increases the amount of CH₄ by 590.%.

Part (b)

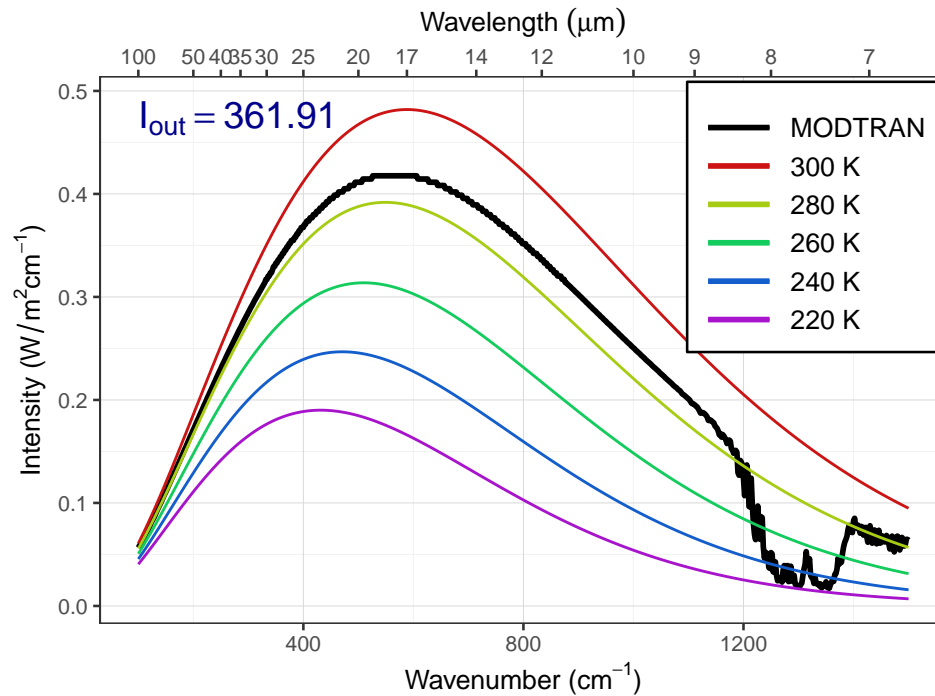
Where in the spectrum does methane absorb? What concentration does it take to begin to saturate the absorption in this band? Explain what you are looking at to judge when the gas is saturated.

Answer: The plots below show the MODTRAN spectrum with all gases set to zero except methane. Methane absorbs most strongly around 1300 wavenumbers.





128 ppm methane



As we increase the methane concentration, the big spike around 1300 wavenumbers gets bigger until it bottoms out on the purple line. This happens somewhere around 8, 16, or 32 ppm, so any of those answers would be correct. But the spectrum is complicated and so is its saturation, so other answers are plausible if they are supported by sound reasoning.

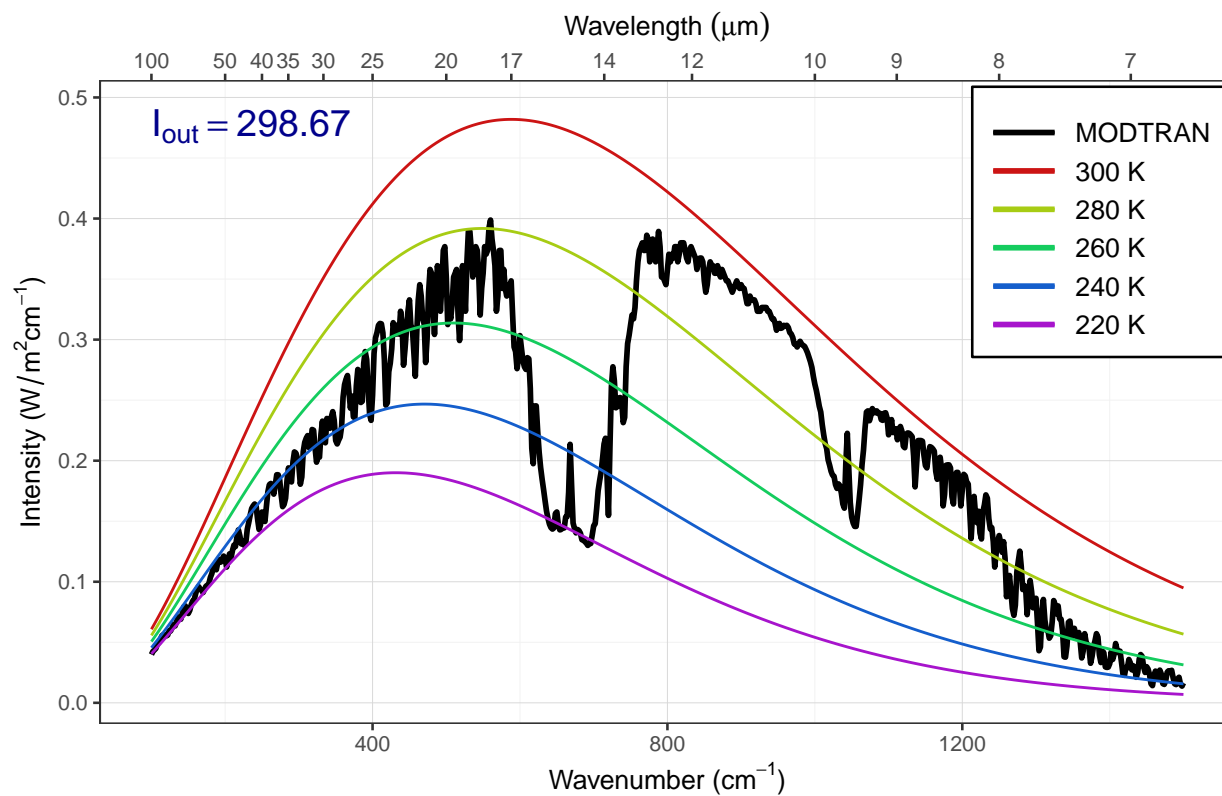
Part (c)

Would a doubling of methane have as great an impact on the heat balance as a doubling of CO₂?

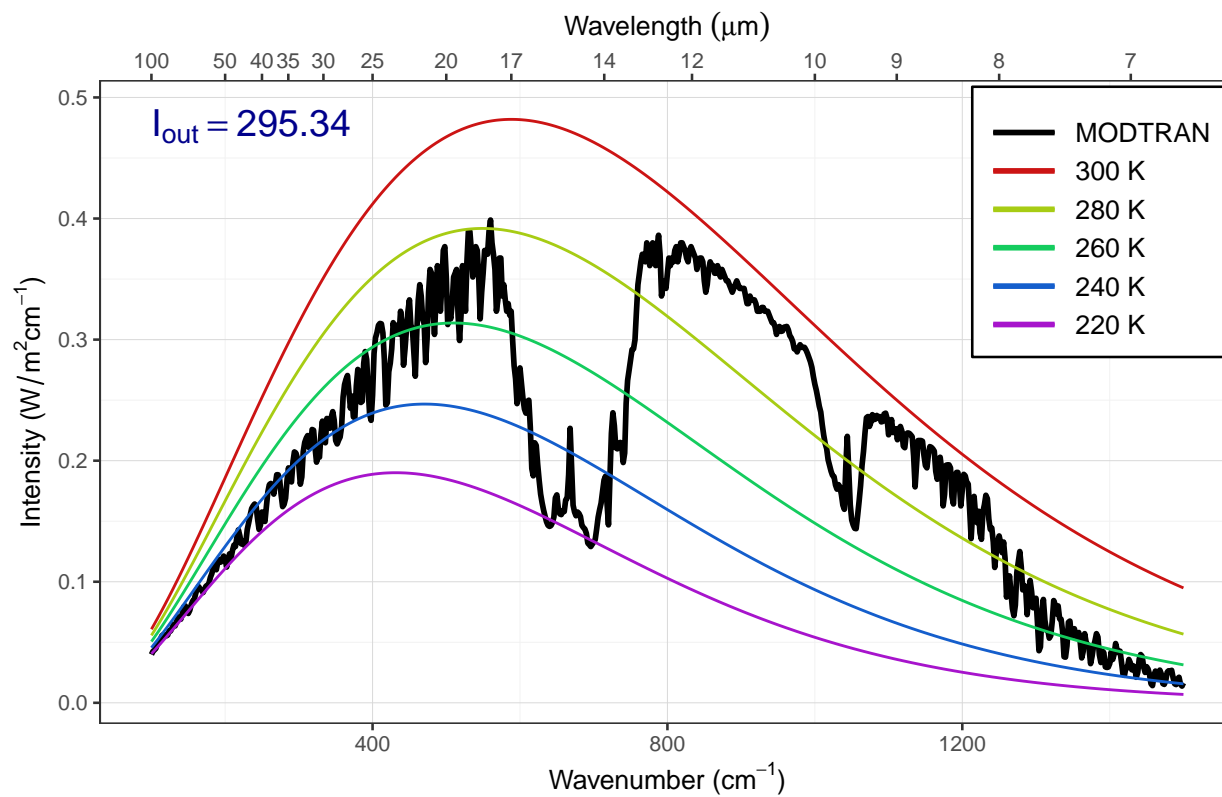
Answer: The baseline value for I_{out} is 299. W/m². If we double CO₂, it drops to 295. W/m², a decrease of 3. W/m², and if we double CH₄, it drops to 298. W/m², a decrease of 0.9 W/m². Doubling CO₂ has the larger effect because there is a lot more CO₂ in the atmosphere and that is more important than how saturated its absorption is.

You can see this if you look at the plots below. Notice that the effect of doubling CO₂ isn't to make the big CO₂ absorption feature get deeper, but to make it wider. You can see this if you compare the baseline to the doubled CO₂ spectrum where the spectrum crosses the 240 K blackbody curve near 600 cm⁻¹ and around 750 cm⁻¹. Compare this to the very small change in the methane spike near 1300 cm⁻¹ (you have to look very carefully at the doubled methane spectrum to notice this).

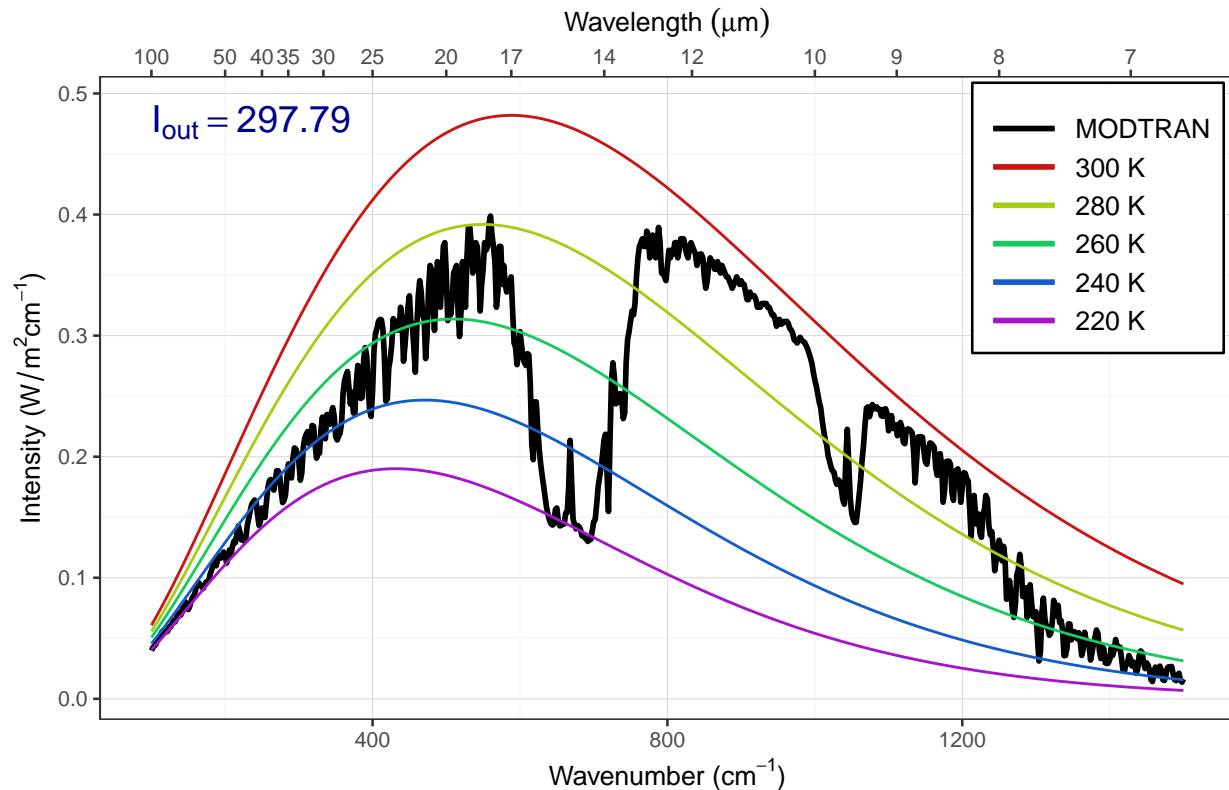
Baseline spectrum



Doubled CO2



Doubled CH₄



Part (d)

What is the “equivalent CO₂” of doubling atmospheric methane? That is to say, how many ppm of CO₂ would lead to the same change in outgoing IR radiation energy flux as doubling methane? What is the ratio of ppm CO₂ change to ppm methane change?

Answer: When we double CH₄, I_{out} is 297.8 W/m². We need to adjust CO₂ to produce the same I_{out} with the default value of 1.7 ppm CH₄. After some trial and error, this turns out to be about 480 ppm, which has $I_{out} = 297.8$. The ratio of ΔCO_2 to ΔCH_4 is $80/1.7 = 47$.

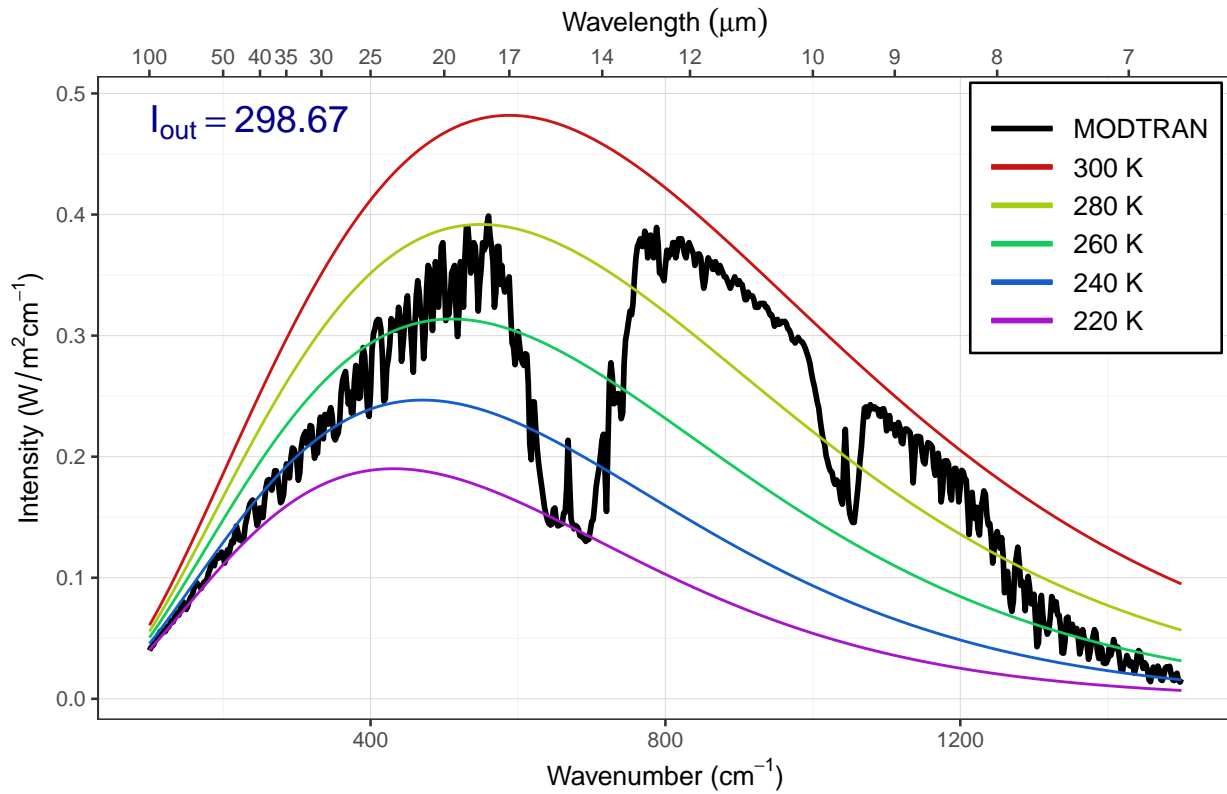
Exercise 4.3: Water vapor

Our theory of climate presumes that an increase in the temperature at ground level will lead to an increase in the outgoing IR energy flux at the top of the atmosphere.

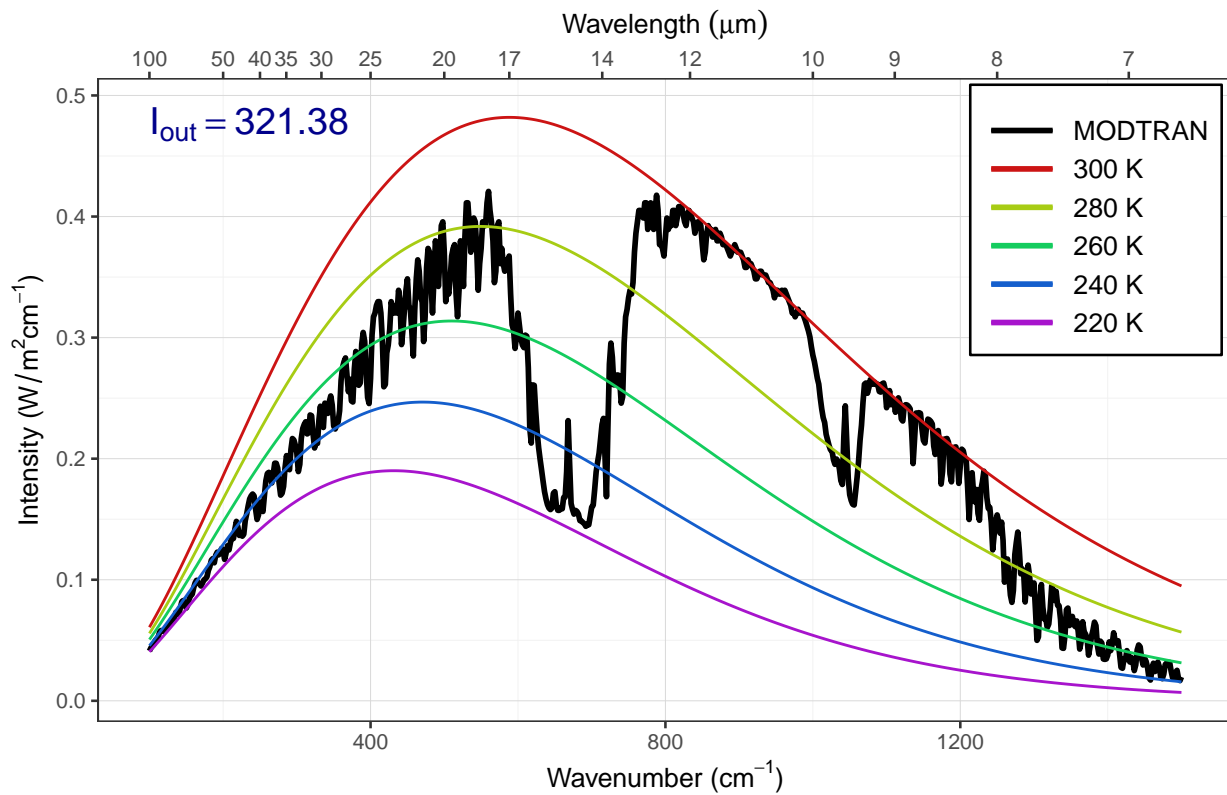
Part (a)

How much extra outgoing IR would you get by raising the temperature of the ground by 5°C? What effect does the ground temperature have on the shape of the outgoing IR spectrum and why?

Baseline spectrum



Ground temperature raised 5K

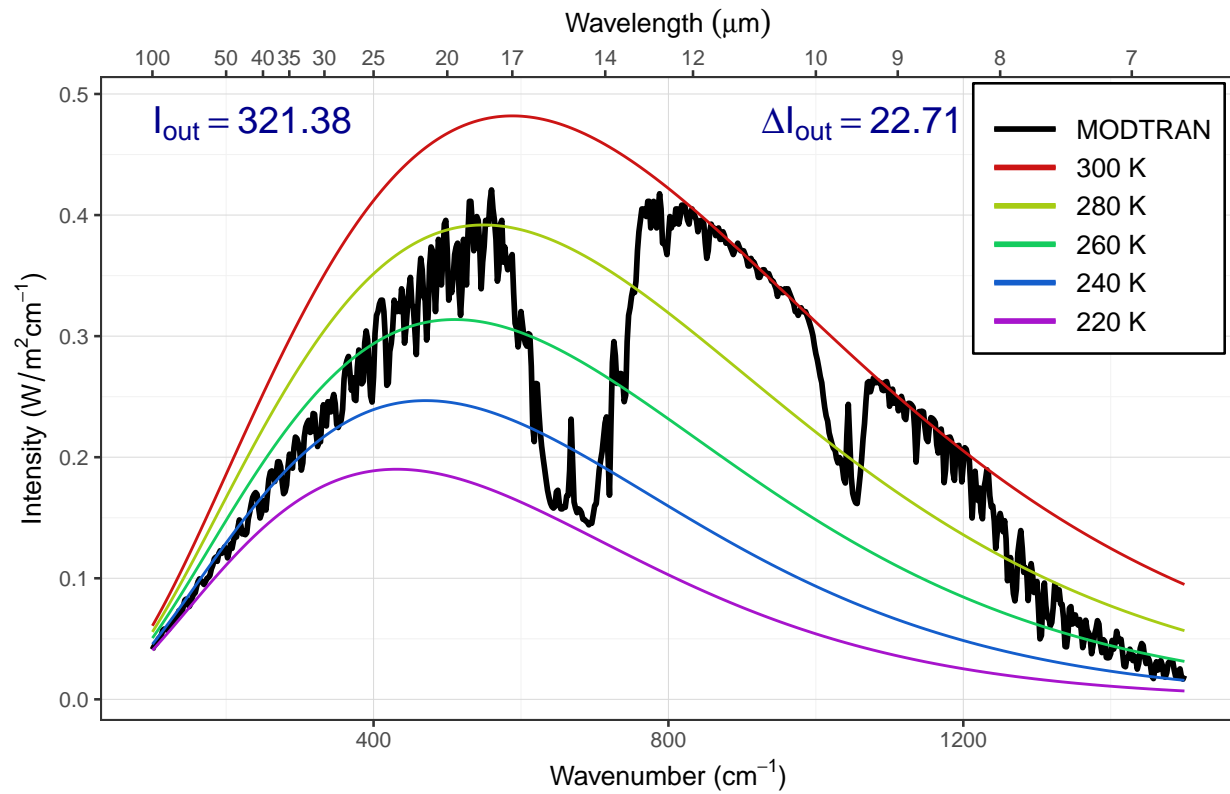


Answer: Raising the ground temperature raises the entire spectrum.

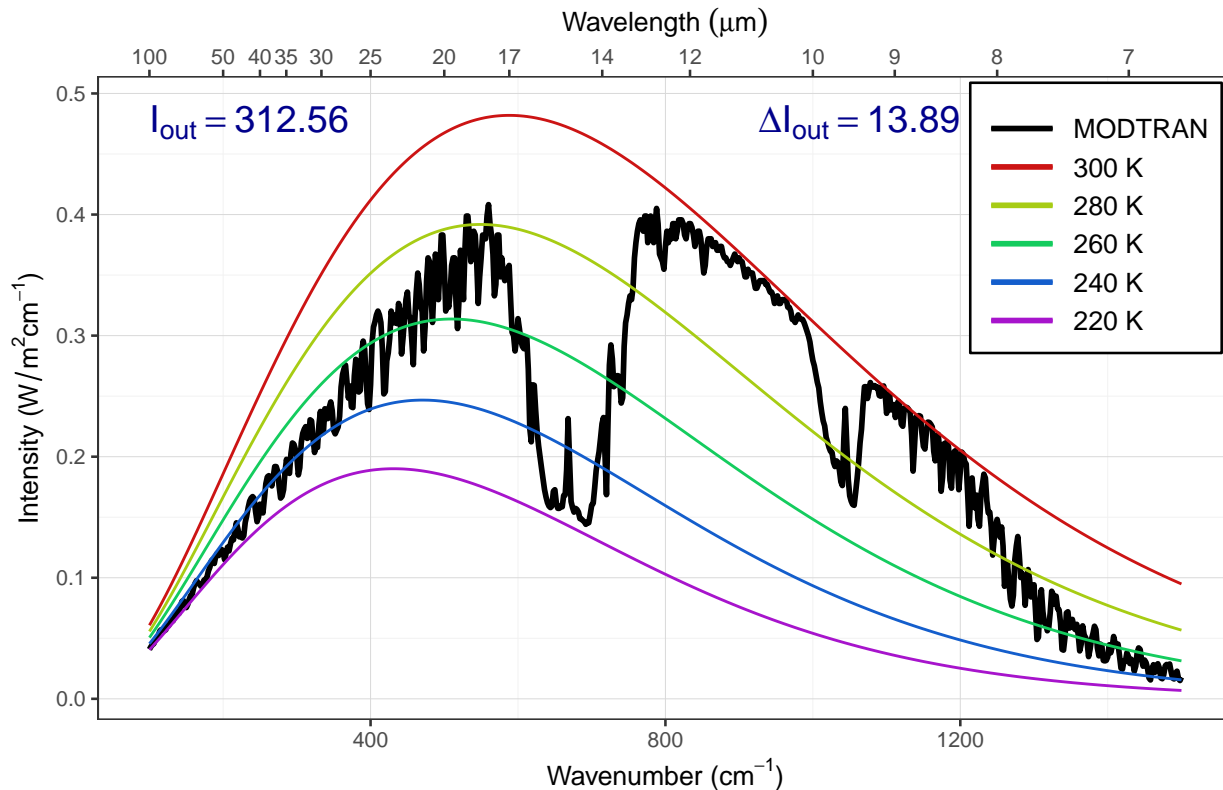
Part (b)

More water can evaporate into warm air than into cool air. Change the model settings to hold the water vapor at constant relative humidity rather than constant vapor pressure (the default), calculate the change in outgoing IR energy flux for a 5°C temperature increase. Is it higher or lower? Does water vapor make the Earth more sensitive to CO₂ increases or less sensitive?

Constant vapor pressure



Constant relative humidity



Answer: Raising the surface temperature has a bigger effect on I_{out} when water vapor pressure is fixed than when relative humidity is fixed. This means that compensating for a change in CO_2 would require a bigger change in temperature with fixed relative humidity, so the climate is more sensitive to changes in CO_2 when relative humidity is fixed.

Part (c)

Now see this effect in another way.

- Starting from the default base case, record the total outgoing IR flux.
- Now double CO_2 . The temperature in the model stays the same (that's how the model is written), but the outgoing IR flux goes down.
- Using constant water vapor pressure, adjust the temperature offset until you get the original IR flux back again. Record the change in temperature.
- Now repeat the exercise, but holding the relative humidity fixed instead of the water vapor pressure.
- The ratio of the warming when you hold relative humidity fixed to the warming when you hold water vapor pressure fixed is the feedback factor for water vapor. What is it?

Answer: In the baseline case, $I_{\text{out}} = 298.7 \text{ W/m}^2$. When we double CO_2 with constant water vapor pressure, I_{out} drops to 295.3 W/m^2 and we have to raise the ground temperature by 0.76 K to bring I_{out} back to 298.7 W/m^2 .

When we double CO_2 with constant water relative humidity, I_{out} drops to 295.3 W/m^2 and we have to raise the ground temperature by 1.2 K to bring I_{out} back to 298.7 W/m^2 .

The feedback factor is the ratio of the temperature change with relative humidity fixed to the temperature change with vapor pressure fixed: $f = 1.2 \text{ K} / 0.76 \text{ K} = 1.6$.

Notice that there is no difference between holding vapor pressure constant and holding relative humidity constant until the temperature changes.